Two-scale multi-model ensemble:
Is a hybrid ensemble of opportunity telling us more?

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Abstract

In this study we introduce a hybrid ensemble consisting of air quality models operating at both the global and regional scale. The work is motivated by the fact that these different types of models treat specific portions of the atmospheric spectrum with different levels of detail and it is hypothesized that their combination can generate an ensemble that performs better than mono-scale ensembles. A detailed analysis of the hybrid ensemble is carried out in the attempt to investigate this hypothesis and determine the real benefit it produces compared to ensembles constructed from only global scale or only regional scale models. The study utilizes 13 regional and 7 global models participating in the HTAP2/AQMEII3 activity and focuses on surface ozone concentrations over Europe for the year 2010. Observations from 405 monitoring rural stations are used for the evaluation of the ensemble performance. The analysis first compares the modelled and measured power spectra of all models and then assesses the properties of the mono-scale ensembles, particularly their level of redundancy, in order to inform the process of constructing the hybrid ensemble. This study has been conducted in the attempt to identify that the improvements obtained by the hybrid ensemble relative to the mono-scale ensembles can be attributed to its hybrid nature. The improvements are visible in a slight increase of the diversity and a marked improvement of the accuracy. The results show that the optimal set is constructed from an equal number of global and regional models at only 15% of the stations. This implies that for the majority of the cases the regional scale set of models governs the ensemble. However given high degree of redundancy that characterises the regional scale models, no further improvement could be expected in the ensemble performance by adding yet more regional models to it. Therefore the improvement obtained with the hybrid set can confidently be attributed to the different nature of the global models. The study strongly reaffirms the importance of an in-depth inspection of any ensemble of opportunity in order to extract the maximum amount of information and to have full control over the data used in the construction of the ensemble.
1. Introduction

It has been widely demonstrated (e.g. Potempsky and Galmarini, 2009) that when multiple model results are distilled to retain only original and independent contributions (Solazzo et al. 2012) and thereafter statistically combined in what is usually called an ensemble, one obtains results that are systematically superior to the performance of the individual models and therefore can provide more accurate and robust assessments or predictions.

An additional advantage of using an ensemble treatment resides in the fact that the multiplicity of the results also quantifies the spread of the model solutions, which provides useful information for the subsequent use of the model predictions for planning purposes or more generically decision-making as it is a measure of the variability of the options, scenarios or simply predictions.

When using ensembles in the realm of air quality modeling and atmospheric dispersion, the general tendency is to combine results of models that belong to the same category. Especially when referring to ensembles of opportunity (e.g. Galmarini et al. 2004; Tebaldi and Knutti al. (2007); Potempsky and Galmarini, 2009, Solazzo et al. 2012; Solazzo and Galmarini, 2015), which combine results from different models applied to the same case study, it is customary to consider as members those obtained from a homogeneous group of models. In particular, the scale at which models operate seems to be a discriminant in all such studies that have been performed to date. Therefore, meso-, regional-, and global-scale model results are grouped in ensembles according to their scale of pertinence. In air quality studies, this has been the case for example in Fiore et al. (2009), Solazzo et al. (2012), Kioutsioukis and Galmarini (2014), and Kioutsioukis et al (2016). Colette et al. (2012) analyzed as part of an analysis of the exposure in Europe, results from an ensemble of opportunity of a total of 6 models, 3 of which were global and 3 regional. The focus however was not the analysis of the contribution of neither the hybrid character of the group to the ensemble result nor the role of redundancy and reducibility of the set, but more obtaining a robust assessment of the 2030 air quality in Europe. A potential benefit of the mixed ensemble was spelled out there
but never verified in line with the opportunity character of the grouping. Therefore there is no record in the literature of a study of an ensemble of models working at different scales.

When developing a model, the scale selection is deeply rooted in the approach to atmospheric modeling and it finds a theoretical justification in the alleged scale-separation shown in the energy spectrum of dynamic variables such as horizontal or vertical wind velocities (Van der Hoven, 1957). Although it is now well accepted that the assumed scale separation does not have general validity, (e.g. Galmarini et al. 1999, Pielke, 2013) and especially not for scalars (e.g. Galmarini et al., 2000; Michelutti et al., 1999; Jonker et al., 1999; Jonker et al., 2004), it has become a convenient theoretical justification for the development of numerical models at specific scales and to address the challenge that the computational solution of the fundamental equation is imposing. Numerical constraints, in fact, oblige us to identify the portion of the energy spectrum to be explicitly resolved by the model. Larger domains imply larger grid spacing for practical constraints on the number of grid points where the equations are to be solved. Larger domains on the one hand allow us to move the resolved scales up in the atmospheric spectrum but at the same time the coarser resolution leads to the loss of detail in the treatment of sub-grid processes which are represented by parameterizations. Thus, for example, a model that has the entire globe as simulation domain will have to use a horizontal grid spacing of 25 to 100 km and therefore approximate (parameterize) the large number of important processes occurring below those grid sizes. Conversely and under normal conditions, a regional scale model that works with a horizontal grid spacing of approximately 12-15 km will resolve explicitly the dynamics and transport that occurs at scales larger than that distance but will not be able to extend the computational domain to the hemispheric or the global scale. The scale separation hypothesis states that the energy peak of boundary layer processes is isolated from the rest of the spectrum, thus justifying their parameterization in a global model. The same principle holds for a regional scale model. However, in the case of a regional scale model, all the processes with scales falling in between 12-15 km and a global-scale model grid-spacing (25-100 km) are resolved explicitly.
Although models are developed according to specific scales, nothing prevents us from combining them in an across-scale ensemble. What may appear to be just another attempt to combine model results for the sake of further and diversely populating an ensemble, has in fact a more rigorous motivation. Models working at different scales represent with different degrees of accuracy and precision different portions of the atmospheric spectrum and therefore processes. Our working hypothesis is therefore that by combining global and regional scale models into an ensemble, there is a high probability that they would complement each other across scales and consequently provide an improved ensemble performance compared to single scale ensembles.

Since in this study we are dealing with chemical transport models (CTM) we should also consider that chemical mechanisms span across a wide range of time scales. This could also constitute an element of diversity for these two groups of the models although the time resolutions for regional and global scale models are comparable. One could argue that in regional domains in particular, regional models essentially represent in detail the chemistry over a timescale of 10-days which then gets advected out and “reset”. For example, differing representations of organic nitrate lifetimes and how long they sequester NO\textsubscript{x} in the system, impacts large scale O\textsubscript{3}. Thus the difference in chemical mechanisms related to longer-lived species and multi-day chemistry could also introduce diversity and be another reason for exploring such an “across-scale ensemble”.

Apparent ancillary elements that could also improve the ensemble results are for example the differences in emission inventories or in general sources of primary information, whose accuracy and precision cannot be guaranteed a priori or evaluated and that could contribute to the development of additional probable solutions.

As presented in the past, the diversity of modeling approaches is the element that favors a better ensemble product (Kioutsioukis and Galmarini, 2014; Kioutsioukis et
al., 2016). In this sense the combination of model results that focus on different scales and that account in a different form for the chemical mechanism has the potential to increase the value of an ensemble to which we will refer from now on as the hybrid ensemble.

The focus in this paper will therefore be on the analysis of the behavior of a hybrid ensemble. The variable considered is the ozone concentration measured and modeled for the year 2010 over the European continent. The analysis takes advantage of the unique opportunity offered by the HTAP2/AQMEII3 activity which brought together global and regional scale models to work on the same case study with a high level of coordination (Galmarini et al., 2017) as far as the input data are concerned.

In section 2, the observations and model results used in the analysis are presented in detail. In Section 3 the model results are characterized in the phase space to clearly establish whether the two scale groups do indeed account for different portions of the energy spectrum in a distinctly different way. Prior to analyzing the performance of the different ensembles, in Section 4 we evaluate the individual models against the measurements using conventional statistics as well as the newly developed error apportionment analysis presented by Solazzo and Galmarini (2016). Section 5 and 6 are dedicated to the analysis of the individual scale ensembles and the hybrid ensemble. Section 7 is dedicated to the comparison hybrid ensemble and single scale ensemble performance. The conclusions are discussed in section 8.

2. The models used and the case study

The set of models results considered and analyzed in this work are those that contributed to the HTAP2 and AQMEII3 modeling initiatives described in Galmarini et al. (2017).

HTAP2 is the second phase of the modeling activities of the Task Force on Hemispheric Transport of Air Pollutants (TF-HTAP) during which a community of
global scale CTMs performed a large number of simulations with the primary goal of investigating the transcontinental exchange of atmospheric pollutants (Dentener et al., 2010; Fiore et al. 2009). AQMEII3 is the third phase of the Air Quality Model Evaluation International Initiative (AQMEII, Rao et al. 2011) which brings together a community of European (EU) and North American (NA) regional scale modelers to work on coordinated case studies over EU and NA. For this third phase, the regional scale air quality modeling activity has been performed within HTAP2 framework. The coordination between HTAP2 and AQMEII3, as detailed in Galmarini et al. (2017), relates to the use of HTAP2 global model results as boundary conditions to the regional scale models and the use of the same anthropogenic emission inventory (Janssens-Maenhout et al., 2015) by both communities. The list of regional and global scale models analyzed in this work is presented in Tables 1 and 2 respectively. The simulations are for the year 2010 and the regional scale models were all initiated and received boundary conditions from the same global chemistry transport model C-IFS (Flemming et al., 2015). C-IFS is also one of the global models that are part of the global model ensemble. Different meteorological drivers are used by the models as presented in the table thus adding an additional level of diversity to the groups, which is beneficial for any ensemble treatment. The two sets of models have been extensively evaluated (Solazzo et al. 2017; Solazzo and Galmarini, 2016; Jonson et al., 2018; Galmarini et al. 2018).

The analysis presented here focuses exclusively on ozone over the EU continent for which the largest abundance of models for the two groups is available and for which case we can take advantage from the fact that the models’ performance has been analyzed with respect to other species elsewhere (Im et al., 2017). In the figures and tables resulting from our analysis, we shall not identify the individual models used since our goal is the identification of possible advantages in using hybrid ensembles rather than evaluating individual model results.

Hourly modeled concentrations of ozone were extracted by the modeling groups at European routine and non-routine sampling locations presented in Figure 1S of the supplemental material. Details on the networks used can be found in Solazzo et al.
(2012), Im et al. (2015), and Solazzo et al. (2017). Surface data were provided by the European Monitoring and Evaluation Programme (EMEP; http://www.emep.int/) and the European Air Quality Database, AirBase (http://acm.eionet.europa.eu/databases/airbase). For the purposes of comparing the ensemble performance with observations, only rural stations with data completeness greater than 75% for the entire year and elevation above ground lower than 1000 m have been included in the analysis. The total number of valid time series used is 405. Only rural stations have been selected as the capture more background signal than local effects. Including urban and suburban stations in the analysis would penalise global model, which won’t be able to capture local effects on ozone.

3. Preliminary analysis of the two groups of models

3.1 Spectral analysis of the global and regional model time series of ozone concentrations

One year of one-hour resolution ozone data allows us to produce detailed spectra from the two groups of models and the measured concentrations. In Figures 1, the individual power spectra of ozone (plotted against the period in days for easier interpretation) from global and regional models are compared with the spectrum of the measured ozone. The time series of the rural monitoring stations have been averaged prior to producing the spectra. In all subsequent results the measured time series should be interpreted as ensemble averages of all available rural monitoring stations.

Since ozone is a scalar quantity, its spectrum grows monotonically in log-log scale as expected (e.g. Galmarini et al., 2000), showing a distinct peak around a period of 24 hours, corresponding to the daily boundary layer evolution and photochemical production of ozone. This peak is captured well by the two groups of model. The global set tends to slightly underestimate the energy associated with this period with only a single model that overestimates it. The regional scale models are evenly distributed around the spectrum of the measured time series. The two groups
behave remarkably similarly at scales smaller than the daily peak. The majority of the models overestimate the energy but capture the slope of the measured spectrum. As expected, the spectra of the global models are more scattered but yet very well behaved. A weak second peak is visible between 30 and 50 days, which could be easily attributed to the synoptic variability. Solazzo and Galmarini (2016) demonstrated that it could indeed be connected to meteorology and/or removal by dry deposition. Moving up the period scale, after the daily peak, all regional scale model spectra are below the observed spectra a behavior that continues apart from a few exceptions up until the 60-70 day period range. Out of seven global models however, only 3 under- or over-estimate the energy in this period-range while the rest matches the observed spectrum. At 70-80 days a new peak appears in the observed time series, corresponding to the seasonal variability. Only one global model captures the observed time series, three models seem to anticipate it at smaller periods and even in the regional scale group there is a variety of behaviors including a monotonic increase of the energy throughout this period range. Beyond the 100-day period the ozone energy spectrum grows monotonically, which the global model group matches the power line very closely whereas the regional scale group shows a more erratic behavior.

This first test is important to assess the fundamental differences between the two sets of models with respect to the characteristics of the signal, the periodicities present in the latter and the ability to reproduce the power or the variance of the measured signal at the various frequencies (periods). In addition, it can give us an idea of the level of complementarity that exists between the two groups of models in the representation of the measured power spectrum. As clearly evident from Figure 1, both groups of models show an internal coherence in the representation of the power spectra. A remarkable result is the capacity of global models to represent the high frequency part of the ozone spectrum with an accuracy that is comparable with regional models. We can expect a complementarity in the behavior of the two groups in the large-scale energy range, which should be regulating the long-range transport and background values. The global models have a better representation of that portion of the spectrum than the regional one.
3.2 Group performance and error apportionment

A characterization of model performance for the individual members of the two groups beyond the information provided in Galmarini et al. (2018), Solazzo et al. (2017), and Jonson et al. (2018) is also appropriate at this stage.

The Taylor diagrams presented in Figures 2 provide an overview of the individual model performance across the year of reference. All model results underwent un-biasing (subtract the annual mean bias from the predicted hourly values, which produces a shift of the annual time series up or down by Mean Bias). We notice that the global models show a more scattered behaviour compared to the regional scale models, with performance distributed across a wider range of standard deviation values. Among the global scale models we find a clear outlier (model 5) whereas the rest tend to group in a rather narrow range of standard deviation values and correlations. Among the regional scale models we can also identify an outlier specifically model 9. The average RMSE values over all stations ranges from 22.4 to 25.9 ugm$^{-3}$ for the global models and 21 to 24.7 ugm$^{-3}$ for the regional models and are thus comparable. Global models overestimate the observed standard deviation while regional scale models with the exception of model 9 are evenly distributed across the observed values. The correlation coefficient is comparable for the two groups of models.

Figure 3 presents two classical skill scores for categorical events also applied by Kioutsoukis et al. (2016), namely the probability of detection (POD) and false alarm rate (FAR). The former represents the proportion of occurrences (e.g. events exceeding a threshold value) that were correctly identified, whereas the latter is the proportion of non-occurrences that were incorrectly identified as happening. In other words they measure true and false positives. In this case the scores are calculated on the basis of the individual model performances at each station. POD and FAR plots are presented as probabilities above breakdowns for different threshold values, where the abundance of the observed data per concentration
range is also given as histogram. A binned analysis of the RMSE demonstrates that

global models achieve lower RMSE at concentrations above 100ug/m³; the opposite

is true for concentrations below this threshold. This partially explain the facts of

Figure 3.

At the same time the global models also have a higher percentage of false positives

as can be gleaned from the FAR index. This analysis is important to establish the
capacity of the models to simulate extreme values.

Using the methodology proposed by Galmarini et al. (2013), in Figure 4 we present

the decomposition of the model errors according to specific time scales. In this

figure, the individual model errors are shown as decomposed in the diurnal (<6h),

inter-diurnal (6h-1d), synoptic (1-10d), and long-term (>10d) time scales and the

residual. The decomposition is performed using a Kolmogorov-Zurbenko filter (Rao

and Zurbenko, 1997) applied to the Mean Squared Error (MSE) calculated from each

model and the observed ozone time series. Such analysis can be very revealing as it

identifies the scale and therefore the processes that are mainly responsible for the

deviation of the model results from the measurements as well as possible

persistence of errors at specific scales.

The figure reveals that most of the error is contained in the long term and diurnal
time scales. For regional-scale models, this is in agreement with the findings of

Solazzo and Galmarini (2016) and Solazzo et al. (2017). The same behaviour is also

found in the group of global models. What is remarkable is the similarity of the error

values at the diurnal time scale across the two groups. This suggests that the
difference in spatial resolution between the two sets of models does not seem to

influence the error at the scale at which atmospheric boundary layer dynamics and
daily emissions of ozone precursors are the dominant processes. Apart from few

exceptions (model 13 and 17 in the regional scale group and model 5 and 1 in the

global scale group), all other models have very comparable errors at that scale. A

comparable error across the two groups is found at the synoptic scale although this

is less surprising because this scale is explicitly resolved by the models in both groups

and strongly depends on the quality of the meteorological driver used. Since both
global and regional models employ assimilation of meteorological observations, they
are able to represent the synoptic scale comparably and are less dependent on
parameterizations employed. The long-term components have the largest error and
also show the most variability across models. Remarkably, the regional-scale models
seem to show smaller long-term error values than the global models although the
former show highly variable model-to-model errors. The strong dependence of the
long-term error on boundary conditions, (specifically lateral boundary conditions for
regional scale models and long range transport in the case of a global model, upper
air stratospheric intrusions and surface emission of ozone precursors and direct
ozone deposition) appears to influence the global scale group concentrations more
than the regional scale, though one should consider that almost all regional scale
models used boundary conditions from the same global model which nevertheless
does not have the smallest long-term error component of the error.

A useful pre-characterization of an ensemble can be obtained by the construction of
the Talagrand diagram (Talagrand et al. 1997). It is achieved by binning the range
from the minimum to the maximum modelled concentrations with as many bins as
the number of ensemble members plus one. The bins are then filled with observed
values based accordingly. For example, if an observed value is lower than the lowest
model value, it is assigned to the first bin, if it falls between the lowest and second-
lowest model value, it is assigned to the second bin, and so on. If it exceeds the
highest model value, it is assigned to the last bin. Figures 5 shows the Talagrand
diagrams for the global and regional and the regional+global set of models. The
figures reveal the tendency of the global model ensemble to be over-dispersed as
indicated by the accumulation of most of the observed data at the centre of
histogram and relatively few observations falling into the more extreme modelled
bins. The regional scale model ensemble shows a flat diagram which is an indication
of good group performance. A flat Talagrand diagram is an indication of the fact that
the group members equally cover (by proportion) all the observed range of values
and the group variability does not show an excess or deficiency in the number of
predictions in a specific range of observed values.
The first result obtained for a combined set of model results is shown in the third panel of Figure 6, which presents the Talagrand diagram for the combination of the two groups of models. Note that the number of bins (x-axis) has increased corresponding to the new total number of models considered plus 1 (i.e. 7 global models plus 13 regional models plus 1). The diagram for the combined group of models qualitatively constitutes an improvement compared to those of the individual group ensembles. The combination of the bell shaped diagram of the global set with the relatively flat shape of the regional set produces a new distribution within the range of modelled values of the observation showing a flat region between bins 5 and 18 and an under prediction region between bins 1 and 5 and 19 and 21, which now account for lower and higher values respectively compared to the same bins of the global and regional sets.

4. Analysis of the ensembles and building the hybrid one

4.1 Ensemble analysis per scale group

Prior to analyzing the performance of the hybrid multi-model ensemble (mme_GR), let us concentrate on the individual ensembles (mme_R and mme_G) of the two groups for the sake of having an extra term of comparison beyond the measured concentrations against which to compare mme_GR. In this study, we would also like to build upon the research performed in other multi-model ensembles over the years and rather than calculating only the classical model average or median ensemble (mme) we shall also calculate three ensembles based on the findings from Potempski and Galmarini (2009), Riccio et al. (2012), Solazzo et al. (2012); Solazzo et al. (2013); Galmarini et al. (2013), and Kioutsioukis and Galmarini (2014). We shall therefore refer to mmeS (Solazzo et al., 2012) as the ensemble made by the optimal subset of models that produce the minimum RMSE; kzFO (Galmarini et al., 2013) as the ensemble produced by filtering measurements and all model results using the Kolmogorov-Zurbenko decomposition presented earlier and recombining the four components that best compare with the observed components into a new model set; and the optimally weighted combination mmeW (Potempski and Galmarini, 2009, Kioutsioukis and Galmarini, 2014, Kioutsioukis et al., 2016).
Figures 6 shows the effect of the various ensemble treatments for the two groups of models separately and presented as Taylor diagram. The correlation has increased and narrowed between 0.90 and 0.95 for both groups. As expected, the best ensemble treatment of the two individual groups is mmeW which in the case of the global models is comparable to mmeS and in the case of the regional scale models is farther apart from mmeS. The fact that the optimal partition of the error in terms of accuracy and diversity in an equal weighted sub-ensemble (mmeS) and the analytical optimization of the error in a weighted full-ensemble (mmeW) are comparable for the global models implies that this group better replicates the behavior of an independent and identically distributed (i.i.d., represented by the square in all pannels) ensemble around the true state set (on average). The range of improvement of the RMSE is comparable for the two groups of models.

Of the entire set of ensemble treatments proposed, mmeS is the only one that works with an identified subset of elements. The elements chosen in this context are those that minimize a specific metric (e.g. RMSE). The combination of all possible permutations of a pre-defined subset and for all possible subsets allows us to identify the subgroup of models that performs best (Solazzo et al. 2012). This group is the one that best reduces the redundancies and optimizes the complementarity of the model results (Kioutsioukis and Galmarini, 2014). Other methods have been devised to determine the optimal number of models (Bretherton et al., 1999; Riccio et al. 2012) that are equally effective as the one used here, though they do not allow identifying the members of the subset. Beyond the use of the mmeS for the current analysis, given the diversity in the number of models comprising the two ensembles we have calculated the effective numbers of models (Bretherton et al., 1999) for the regional and global sets in the attempt to verify whether the effective numbers were close for the two sets. Figure 7 shows the $N_{\text{eff}}$ obtained for the global set and the regional set. At over two third of the stations, the mmeS used 3-4 global models and 3-5 regional models. In other words, roughly half of the global models (3-4 out of 7) produce the best result when constructing the mmeS globally while in the case of the regional scale models less than half (3-5 out of 13) of all models are required.
Figure 7 also provides the frequency of contribution of the individual models to the mmeS thus confirming the dominance of 3 global and 4 regional models determined with the $N_{\text{eff}}$ analysis. What is presented in Figure 7 is the analysis for the aggregated set of model results at all available monitoring points. We also would like to determine the spatial variability of this result, i.e. to answer the question whether $N_{\text{eff}}$ is uniform throughout the domain or whether there are sub regions that require more or less models to construct mmeS.

In order to have a more objective assessment of the result presented in Figure 7 we introduce a metric which samples only the diversity of the model results (see section 4.3). Following Pennel and Reichler (2011) and Solazzo et al. (2013) we introduce the metric $d_m$ defined for $M$ models at location $i$ as:

$$ d_{m,i} = e_{m,i}^* - R_{m,mme} mme_i^* $$

where

$$ mme_i = \frac{1}{M} \sum_{m=1}^{M} e_{m,i} $$

$$ e_{m,i} = \frac{\text{mod}_{m,i} - \text{obs}_i}{\sigma_{\text{obs}}} $$

and the * version of $e_{m,i}$ and $mme_i$ is obtained by normalizing them with $\sigma_e$ and $\sigma_{mme_i}$ respectively. $R_{m,mme}$ is the correlation between the individual and average model results. Therefore only the uncorrelated portion of the individual result is retained in $d$ as measure of the diversity whereas the correlated portion is filtered out. Applying this metric, the model results have been decomposed by means of the Kolmogorov-Zurbenko filter described earlier and $N_{\text{eff}}$ has been calculated across the domain for the most relevant components LT, SY, and DU. Figure 2S presents the results for the two groups of models. For the long-term component, $N_{\text{eff}}$ results shown in Figure 7 are largely confirmed with an overall spatial homogeneity of $N_{\text{eff}}$. The global model set appears to require a larger number of models than the average in critical areas like Northern Italy where the resolution would be insufficient to capture the inhomogeneity of the concentration field due to the complex terrain in
that region (similarly in the western part of the domain). At the synoptic scale, the regional scale models require slightly more models on average than the numbers presented in Figure 7 and in some portions of the domain almost all available models are required. The number of required models increases even further at the diurnal scale. In the case of the global set, the average $N_{\text{eff}}$ is the same across these two scales and more models are required in the Po valley (Italy) at the synoptic scale and western Poland at the diurnal scale.

4.2 Building the hybrid ensemble

Given the fact that there is redundancy in the two groups of models and a disparity exists in the overall and effective number of models in the two groups, a strategy has to be devised so that no pre-determined weight is assigned to one of the two groups thus masking the potential outcome of this study or creating false results. This goal is accomplished by applying the following strategy.

We want to compare three equally populated ensembles of just global, just regional, and mixed global and regional models. We will therefore reduce the ensemble of regional-scale models and include extra models in the ensemble of global models beyond the effective number calculated in Figures 7 and 25 so that the joint ensemble will not be too small. In order to accomplish this, we select the global models contributing most to the global ensemble beyond those identified by $N_{\text{eff}}$. We begin by assuming that six is a reasonably abundant ensemble (as also indicated by the effective number of regional scale models) and as such the single-scale ensembles will be based on six members. Taking advantage of the various techniques developed to build an ensemble presented earlier we define the following sets:

- (mme_GR) hybrid ensemble of rank 6 (ensemble of 6 members) composed of the best three global models and the best three regional models
- (mme_G) global ensemble of best six global models
- (mme_R) regional ensemble of best six regional models
Among them, the mmeS_GR is the only ensemble product that allows unbalanced contributions from global and regional models.

### 4.3 Comparing the single scale multi-model ensembles with the hybrid one

The comparison of the ensemble performances will be restricted to the months of June -August when the photochemical production of ozone is at its maximum and the number of exceedances is expected to peak throughout the continent. The results of the comparison of the mme, mmeS and mmeW for the regional (_R), global (_G) and hybrid cases (_GR) are shown in Figures 8. The elements common to the three panels are:

- The hybrid ensemble of rank 6 composed of the three best global models and the three best regional models (mme_GR) when compared to mme_G (best six global models) and mme_R (best six regional models) does not show improved performance, rather its skill is inferior to both mme_G and mme_R.
- For the other two kinds of ensemble treatments (mmeS and mmeW), the combination of global and regional models produces some improvement compared to just the global or regional ensembles in terms of correlation coefficients, standard deviations and RMSE.

The partition of global and regional models in mmeS (Figure 9) shows that the contribution of regional models is more frequent. Specifically, at two thirds of the stations, the optimum hybrid ensemble of rank 6 consists of one or two global
models and five or four regional models, respectively. At only 15% of the stations, mmeS consists of an equal number of global and regional models. The maximum number of global models in the mmeS_GR ensemble is four, achieved at roughly 1% of the stations. Conversely, at around 10% of the stations the hybrid ensemble utilized only regional models. The second panel of Figure 9 also gives the regional distribution of the number of Global models contributing to the hybrid ensemble clearly indicating a deficiency in the northeastern part of the domain.

In Figures 10, POD and FAR show a net improvement over the mmeW_G results when the hybrid ensemble is considered, with a minimum in false positives and a maximum in true positives that closely match the mmeW_R results.

The real improvement of the hybrid ensemble with respect to the single scale model ensembles becomes evident when analyzing Figure 11. The pannels in the figure are the collective representation of three of the most important characteristics of an ensemble as proposed by Kioutsioukis and Galmarini (2014), i.e. diversity, accuracy and error. On the x and y axes respectively “diversity” and “accuracy” are presented. The former represents the average square deviation of the single models from the mean of the models, whereas the latter is the square of the average deviation of the individual model results from the observed value. As presented by Krogh and Vedelsby (1995), the difference of the diversity and accuracy defines the quadratic deviation of the ensemble average from the observed value. From the definition it follows that in order for the ensemble result to be closer to the observed value one has to find the right trade off between accuracy and diversity (A-D). A mere increase in diversity does not guarantee a minimization of the ensemble error since it might produce a reduction in the accuracy. What one hopes to obtain is the right combination of models that provides the maximum accuracy and maximum diversity. In the plots of Figure 11, the optimal condition is achieved when the model results concentrate in the upper left quadrant of the plot toward the (x=100/(Number of Models),y=1) point. In the plot, the accuracy parameter is presented as deviation from the best model performance. The dots represent the estimate of the two parameters at every location where measurements are
available. The colour scale is based on the RMSE. The two upper panels give the A-D mapping for the mme_R and mme_G ensembles; the lower two panels give the map for the hybrid ensembles, i.e. mme_GR + mmeS_GR. The difference in nature of the two ensembles is clear from the two panels. Ensemble mme_G is more diverse and accurate than mme_R (x values: 69 in G and 66 for R, y: 0.75 in G, 0.66 in R). The combination of the two produces a decrease in the two parameters (GLO+REG (mme6)). However, if the models are selected as in mmeS, both accuracy and diversity increase (GLO+REG (mmeS6)). The real advantage of the combination is visible in a slight increase of the diversity as compared to mme_GR and a marked improvement of the accuracy from 0.71 to 0.81. The error decreases from a median value of 17.9 to 15.6 and from an Inter Quartile Range of 5.1 to 3.8.

In Figures 12 the spectra of the ensembles are presented. For the just global, just regional-scale ensembles and the rank 6 hybrid ensemble, the spectra of mme, mmeS, mmeW and kFO are shown in the figure. Figure 12 also shows the spectra of the four ensembles, mme_R6, mme_G6, mme_GR6 and mmeS_GR6 for which the largest six contributors from the regional models, the six global, and three regional plus three global models were used. From the picture we see that regardless of the treatment, the ensemble data capture the ozone power spectrum with no notable deviation from the measured spectrum. It is important to note that an ensemble treatment is a purely statistical treatment that does not consider any physics constraints. The deficiencies that were originally present in the individual model spectra are still present in the ensemble results, particularly the large power deficit in the range from 0.8 days to 100 days. The mme_GR spectrum appears to produce a slight improvement toward filling this energy gap, but the change is very small.

5. Discussion and conclusions. How much is the improvement attributable to the hybrid character of the ensemble?

The analysis presented above gives us clear indications that the combination of the two sets of models analysed produces an improvement in the ensemble performance. In particular, the hybrid ensemble appears to be superior to any single-scale ensemble in the optimum setting. For example, given six global, six regional and three global and three regional ensembles, the optimization always
favours the hybrid ensemble. This was repeated for all examined cases: the annual hourly records, the JJA hourly records and the annual daily maximum records.

- The improvement is in the range 1-5% compared to single scale optimum ensembles
- POD/FAR show a remarkable improvement, with a steep increase in the largest POD values, though comparable to the other for the hybrid ensemble and comparatively smallest values of FAR across the concentration ranges.

Some important considerations need to be made at this point. It is difficult to find quantitative evidence for the fact that the hybrid ensemble improvement can be unequivocally attributed to the multi-scale nature of the ensemble. We have no evidence, nor guarantee, that the same kind of improvement could be reached by adding more regional-scale models to the regional-scale ensemble, or more global models to the global-scale ensemble. However, what is a clear conclusion is that the regional-scale ensemble is characterised by a higher level of redundancy in the members than the global ensemble, since less than half of the members produced the optimal ensemble, and that the use of the three best members from the regional-scale ensemble and three best global-scale models produces an improvement in the ensemble performance. This last argument suggests that the addition of more model results of the same “nature” would just contribute to further increase the level of redundancy, while on the other hand, the improvement obtained could indeed be attributed to the different “nature” of the global-scale models compared to the regional-scale models.

Therefore, considering:

- the large number of regional scale models and the spectrum of diversity in their nature (only a small number of the same models were used by multiple groups and there was an abundance of models developed independently from one another);
- the relatively smaller number of global model results compared to the regional models and also their different nature;
the fact that the two groups of models used the same emission inventories
and all the regional scale models used boundary conditions from the same
global model;

one could attribute the improvement of the mmeS_GR ensemble performance to
the difference in nature of the two groups and a complementary contribution of the
two toward an improved result.

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Figure Captions

Figure 1S: Spatial distribution of the 405 rural monitoring stations where ozone model results where produced and observations were available.

Figure 1: Power spectrum of observed ozone (thick line) obtained from the average one year time series across all measuring locations and of global models and regional models.

Figure 2: Taylor diagram of Global models and regional models.

Figure 3: Cumulated Probability of detection (POD) and False alarm rate (FAR) for Global and regional models at various ozone concentration threshold.

Figure 4: Distribution of the Mean Square Error (MSE) across the models of the two communities and the scales in which the signal has been decomposed (LT, long term; SY synoptic; DU diurnal; ID inter diurnal; see text for definition).

Figure 5: Talagrand diagrams of Global models, Regional models and the Global + Regional set of model results.

Figure 6: Taylor diagram of the four ensemble treatments considered in the text obtained from the global and regional models.

Figure 7: Effective number (N_{eff}) of models calculated according to Bretherton et al. (1999) for the two groups of models; and frequency of contribution of each model to the mmeS.
Figure 2S: Number of effective models for the two groups obtained at all monitoring locations considered thus giving the spatial structure of the ensemble size and for three of the four components in which the modelled time series have been decomposed, namely: LT, SY and DU.

Figure 8: Comparison of the performance of three ensemble treatments (mme, mmeS and mmeW) for three groupings of models (regional _R, global _G, and mixed global and regional _GR)

Figure 9: Contribution of Global models to mmeS_GR and its spatial representation

Figure 10: POD and FAR for the best performing ensemble treatment (mmeW) and for three ensemble grouping (regional _R, global _G, and mixed global and regional _RG)

Figure 11: Representation of the accuracy (y-axis) vs diversity (x-axis) and RMSE for the ensemble of the most present 6 global and regional models respectively (top row) and a hybrid ensemble calculated with mme and mmeS ensemble methods (bottom row). For reference, the square represents the ideal point corresponding to an independent and identically distributed models (i.i.d ensemble). If the models are i.i.d. then all eigenvalues are equal, each explains 1/N of the variance and therefore for 6 models the point is at (0.16; 1).

Figure 12: Spectra behaviour of the ensemble treatments: full global ensemble (top); full regional ensemble (middle); mme of 6 most frequently present global and regional models and the hybrid ensemble calculated with mme and mmeS ensemble methods (bottom)
<table>
<thead>
<tr>
<th>Operated by</th>
<th>Modelling system</th>
<th>Horizontal grid</th>
<th>Vertical grid</th>
<th>Global meteo data provider</th>
<th>Gaseous chemistry module</th>
</tr>
</thead>
<tbody>
<tr>
<td>Finnish Meteorological Institute (working with 2 versions)</td>
<td>ECMWF-SILAM_H, SILAM_M</td>
<td>0.25 x 0.25 deg (lat/lon)</td>
<td>12 uneven layers up to 13km. First layer ~30m</td>
<td>ECMWF (nudging within the PBL)</td>
<td>CBM-IV</td>
</tr>
<tr>
<td>Netherlands Organization for Applied Scientific Research</td>
<td>ECMWF-L-EUROS</td>
<td>0.5 x 0.25 deg (lat/lon)</td>
<td>Surface layer (~25m depth), mixing layer, 2 reservoir layers up to 3.5km.</td>
<td>Direct interpolation from ECMWF</td>
<td>CBM-IV</td>
</tr>
<tr>
<td>University of L’Aquila</td>
<td>WRF-WRF/Chem1</td>
<td>23 km</td>
<td>33 levels up to 50hPa. 12 layers below 1km. First layer ~12m</td>
<td>ECMWF (nudging above the PBL)</td>
<td>RACM-ESRL</td>
</tr>
<tr>
<td>University of Murcia</td>
<td>WRF-WRF/Chem2</td>
<td>23 x 23 km²</td>
<td>33 levels, from ~24m to 50hPa</td>
<td>ECMWF (nudging above the PBL)</td>
<td>RAM2</td>
</tr>
<tr>
<td>Ricerca Sistema Energetica</td>
<td>WRF-CAMx</td>
<td>23 x 23 km²</td>
<td>14 layers up to 8km. First layer ~25m.</td>
<td>ECMWF (nudging within the PBL)</td>
<td>CB05</td>
</tr>
<tr>
<td>University of Aarhus</td>
<td>WRF-DEHM</td>
<td>50 x 50 km²</td>
<td>29 layers up to 100hPa.</td>
<td>ECMWF (no nudging within the PBL)</td>
<td>Brandt et al. (2012)</td>
</tr>
<tr>
<td>Istanbul Technical University</td>
<td>WRF-CMAQ1</td>
<td>30 x 30 km²</td>
<td>24 layers up to 10hPa.</td>
<td>NCEP (nudging within PBL)</td>
<td>CB05</td>
</tr>
<tr>
<td>Kings College</td>
<td>WRF-CMAQ4</td>
<td>15 x 15 km²</td>
<td>23 layers up to 100hPa. 7 layers below 1km. First layer ~14m</td>
<td>NCEP (Nudging within the PBL)</td>
<td>CB05</td>
</tr>
<tr>
<td>Ricardo E&amp;E</td>
<td>WRF-CMAQ2</td>
<td>30 x 30 km²</td>
<td>23 VL up to 100hPa. 7 layers &lt; 1km. 1st ~0–15m</td>
<td>NCEP (nudging above the PBL)</td>
<td>CB05-TUCL</td>
</tr>
<tr>
<td>Helmholtz-Zentrum Geesthacht</td>
<td>CCLM-CMAQ</td>
<td>24 x 24 km²</td>
<td>30 VL from ~40m to 50hPa</td>
<td>NCEP (spectral nudging above f. troposphere)</td>
<td>CB05-TUCL</td>
</tr>
<tr>
<td>University of Hertfordshire</td>
<td>WRF-CMAQ3</td>
<td>18 x 18 km²</td>
<td>25 VL from ~20m to ~18km</td>
<td>ECMWF (nudging above PBL)</td>
<td>CB05-TUCL</td>
</tr>
<tr>
<td>INERIS/Ciemat</td>
<td>ECMWF-Chimere_H, Chimere_M</td>
<td>0.25 x 0.25 deg</td>
<td>9 VL up to 500hPa. 1st ~0–20m</td>
<td>Direct interpolation from ECMWF</td>
<td>MELCHIO2</td>
</tr>
</tbody>
</table>

**TABLE 1. Participating Regional Modelling Systems and Key Features. The dark shaded cells contain information on models that worked over the NA domain the others on the EU one.**
TABLE 2. PARTICIPATING GLOBAL MODELLING SYSTEMS AND KEY FEATURES.

<table>
<thead>
<tr>
<th>Operated by</th>
<th>Modelling system</th>
<th>Horizontal grid (km x km or “lat x lon”)</th>
<th>Vertical grid</th>
<th>Global meteo data provider</th>
<th>Gaseous chemistry module</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>NAGOYA, JAMSTEC, NIES</td>
<td>CHASER_rel</td>
<td>2.8 x 2.8°</td>
<td>32 VL up to 40 km</td>
<td>ECMWF (nudging above PBL)</td>
<td>Sudo et al. (2002)</td>
<td>Sudo et al. (2002), Watanabe et al. (2011)</td>
</tr>
<tr>
<td>NAGOYA, JAMSTEC, NIES</td>
<td>CHASER_1106</td>
<td>1.3 x 1.3°</td>
<td>32 VL up to 40 km</td>
<td>ECMWF (nudging above PBL)</td>
<td>Sudo et al. (2002)</td>
<td>Sudo et al. (2002), Watanabe et al. (2011)</td>
</tr>
<tr>
<td>ECMWF</td>
<td>C-IFS</td>
<td>ca. 80 km</td>
<td>60 VL from surface to 0.1 hPa – lowest level 15 m</td>
<td>JS</td>
<td>CB05</td>
<td>Hemming et al. 2015</td>
</tr>
<tr>
<td>MetNo</td>
<td>EMEP_rv4.8</td>
<td>0.5° x 0.5°</td>
<td>20 uneven layers up to 100 hPa. First layer ~ 50 m</td>
<td>ECMWF IFS dedicated model run</td>
<td>EMEP</td>
<td>Simpson et al. 2012, <a href="http://emep.int/msec/msec_publications.html">http://emep.int/msec/msec_publications.html</a></td>
</tr>
<tr>
<td>Univ. Tennessee</td>
<td>H-CMAQ</td>
<td>108 km x 108 km</td>
<td>44 layers up to 50 hPa</td>
<td>WRF</td>
<td>CB05</td>
<td>Xing et al. (2015)</td>
</tr>
<tr>
<td>Univ.Col. Boulder</td>
<td>GEOSCHEM-ADJOINT</td>
<td>2° x 2.5°</td>
<td>47 levels up to 0.066 hPa (bottom of the last grid)</td>
<td>GEOS-5</td>
<td>GEOS-Chem</td>
<td>Henze et al. (2007)</td>
</tr>
<tr>
<td>US-EPA</td>
<td>H-CMAQ*</td>
<td>108km x 108km</td>
<td>44 lev to 50 hPa</td>
<td>WRF nudged with NCEP/NCAR</td>
<td>CB05/UCCL</td>
<td>Mathur et al. (2017)</td>
</tr>
</tbody>
</table>

*H-CMAQ is strictly a hemispheric model but for the purposes of this analysis is expected to behave the same as global models over the EU domain, therefore, for the rest of the paper we will refer to it as “global models”.

29
Figure 1
Figure 2
Figure 4
Figure 5

- **GLOBAL**
  - Frequency vs. Observation bin

- **REGIONAL**
  - Frequency vs. Observation bin

- **GLOBAL+REGIONAL**
  - Frequency vs. Observation bin
Figure 6
Figure 7
Figure 8
Figure 9
Figure 11
Figure 12

GLOBAL ENSEMBLE ESTIMATORS (obs in black)

REGIONAL ENSEMBLE ESTIMATORS (obs in black)

ENSEMBLE ESTIMATORS of RANK 6 (obs in black)