We thank Maarten Krol and an anonymous referee for their comments and suggestions.

Reviewer 1 Maarten Krol

This is an interesting approach that has the aim to get OH information from CH4 satellite retrievals. The paper presents an OSSE and is generally positive about the possibilities to get this information. After reading the paper I am much less optimistic and the annotated manuscript contains my comments and suggestions. Some main points are summarised below.

First of all, the overly optimistic summary "We find that the satellite observations can constrain the global tropospheric OH concentrations with a precision better than 1% and an accuracy of about 3% for SWIR and 7% for TIR." relies very much on the OSSE set-up. This statement is based on the results of our OSSE analysis. We now change the text to emphasize that the purpose of OSSE is assess the potential of the method. The above text is modified to “we find that the satellite observations of methane have the potential to constrain …”. We now also remind readers in several places (abstract, method, and conclusion) that error specifications in our OSSE are idealized and can result in over-optimistic estimation.

I like the fact that the authors took the effort to run the inversion with various different OH distributions, because this highlights the problem: we are far from sure what the OH distribution is, and how OH varies in time. While for the emissions a grid-optimisation is performed, OH is optimised as only 1 parameter. This hides the fact that you assume knowledge of the distribution. I acknowledge that the inversion uses a (slightly) different OH distribution, as well as perturbations to the meteorology. However, these differences are poorly quantify. It would help
to show the impact of different OH/meteorology on forward CH4 column simulations (see comments in the manuscript). I think it is appropriate to tone down the conclusions considerably and to acknowledge that the result is sensitive to the set-up of the OSSE. An optimisation of the 3D distribution of OH together with an emission scaling would give totally different results I guess.

The argument behind this assumption is that we have certainty about the broad global-scale signature of OH distribution (high OH in tropics and shift seasonally with solar radiation), which determines the global distribution of methane loss, although the details of OH seasonal and spatial distribution is more uncertain. “An optimisation of the 3D distribution of OH together with an emission scaling”, the counter-example suggested by the reviewer, is against this prior knowledge and the fact that emission distribution is more heterogeneous and more uncertain on a large spatial scale. In Section 4, we quantify the uncertainty resulting from this assumption with different OH distributions from ACCMIP, which represents a sufficiently large spread of OH distributions (they are not only slightly different). We also add a new figure (Figure 11) to better understand which aspect of the OH distribution affects the inversion most, providing insight on how to improve the method with better design of the state vector. Following the reviewer’s suggestions, we now quantify and visualize the effect of different meteorological fields on CH4 column simulations in a new figure (Section 2.1 and Figure 3).

Second, the authors claim that "GEOS-Chem relates linearly x to y". This is true for emissions, but not for OH. In that sense the analysis might be flawed, although I believe that non-linearities are small. Nevertheless this should be corrected and a work-around for the non-linearities should be found.
Thanks for pointing out this issue. We now state the linearity assumption and the reasoning in Section 2.3: “The inverse problem presented here is not strictly linear because the loss rate depends on the methane concentration. However, a quasi-linearity can be assumed, as the range of variability of methane concentrations is sufficiently small.”

Third, figure 6 appears wrong to me since lifetime and emissions should be negatively correlated (I guess OH is analysed in the plots).

Thanks for pointing out the error! We correct the figure and the corresponding text.

Also the authors should try to find a work-around for determining the regularisation parameter gamma. I understand that the massive amount of observations in the cost-function has to be de-weighted, but in practical application the "true" emissions are not available and the methods breakdown. Chi-square statistics or another form of regularisation are possible alternatives.

We add a panel to Figure 5 (formerly Figure 4) to show the L-curve for determining the regularization parameter independent of “truth” information.

Minor
Page 2 Line 28-29 There is substantial uncertainty in the inter-annual variability derived using MCF, and now it is presented as the "benchmark".

We change the sentence to avoid the impression that MCF is the benchmark “Compared to estimates from the methylchloroform proxy, global tropospheric chemistry models tend to predict higher OH concentrations (Voulgarakis et al., 2013; Naik et al., 2013), smaller inter-
annual variability (Holmes et al., 2013; Murray et al., 2013), and larger long-term trends (Holmes et al., 2013).

Page 3 Line 12 “Evasion of MCF from the ocean” has never been substantiated. Use “possible evasion from …”

We change the sentence to “… possible evasion from the ocean may complicate interpretation”.

Page 3 Line 29 Maasakkers et al. 2018 has not been published.

We would like to cite Maasakkers et al. (2018) because we inherit much of the methodology from Maasakkers et al. (2018). We expect the paper be submitted to ACP in September. We will ask the editor, if necessary, to recommend a hold on our paper until Maasakkers et al. (2018) appears on ACPD.

Page 4 Line 14 TROPOMI is NOT a candidate mission, it is reality. CrIS also.

We change “candidate satellite instruments” to “TROPOMI and CrIS”.

Page 5 Line 13 Unclear: the global methane lifetime is in the state (= optimized) while the distribution of OH is varied. But these are coupled?

We only optimize the global methane lifetime but assume the 3-D seasonal and spatial distribution in the prior is correct. They are not coupled in our setup. We now state this in Section 2.1 “… the magnitude (global mean concentration expressed as global tropospheric methane lifetime) and the distribution (seasonal and spatial variations) of the OH field are decoupled and only the former is optimized.”
It would be good here to quantify the differences by running the model forward with identical emissions and OH, but different meteo-drivers.

We add Figure 3, which shows the difference between simulated monthly mean methane column with identical emissions and OH but different meteorological fields. We also report the statistics (RMSE) that quantifies the difference in simulated daily methane columns (Section 2.1).

But this does not solve the "bias" problem in general. Adding random noise is fine, but a more interesting test would be to included biases, which are known to occur for satellite observations (e.g. due to aerosol, cirrus, etc.).

We now add a line to state this limitation of the idealized error specification in our OSSE here and also in the abstract and conclusion. Specifying these error in an OSSE in a realistic way is nontrivial. We believe it is better to assess the impact of these error sources with actual data in future work.

Are observations considered independent? (e.g. diagonal $S_{O}$)

Yes. We now state this limitation of the idealized error specification. We also point out in Section 2.3 that neglecting correlations in the model transport error is the major reason that a small regularization parameter is required in our setup.

This is a bit strange: there is adjoint GEOS-Chem available? Or is full-chemistry simulated (including feedback?). More worrying: the relation between lifetime and $y$ is not linear. Using linear assumptions would invalidate the results.
Our simulation does not include full chemistry. With our method, the Jacobian matrix can be pre-computed, which allows us to conduct inversions of varied perturbed “true” atmosphere with little additional computational expense, as well as a full characterization of posterior error covariance matrix. This cannot be easily done with adjoint. As mentioned in response to major comments, we now add text in Section 2.3 to state the rationale for the linearity assumption.

Page 7 Line 29 In general applications, this truth is not available, so this sounds as a rather hand-waving procedure. The results imply an increase in observational weight of a factor 20. An alternative metric for overfitting is the chi-squared approach, and overfitting would introduce significant noise in the posterior emissions. We add a panel to Figure 5 (formerly Figure 4) to show the L-curve for determining the regularization parameter independent of “truth” information.

Page 8 Line 2 The information provided is very limited. In terms of OH it would be good to report also the total emissions (since more emissions would logically correspond to more OH). We now report in the text that “…all three satellite observing systems retrieve global total methane emissions within 5% of the “true” value…”

Page 8 Line 9 I also wonder here what is the role of the (wrong) linearity assumption We now add text in Section 2.3 to state the rationale of linearity assumption.

Page 8 Line 14 “correlation should be negative”

Thanks. We make the corrections.
Page 8 Line 16 “TIR are incapable of resolving the spatial distribution of emission rates” Figure 5 not informative in this respect.

I remove this sentence and reference to Figure 5 here. The paragraph is rewritten for clarification.

Page 8 Line 20 “become less consequential” unclear what you want to say here.

We rewrite the paragraph for clarification.

Page 8 Line 33 Refer to Rigby

We now cite Rigby et al. (2017).

Page 9 Line 18 “These results are somewhat counterintuitive. Apparently the system is very sensitive to combination of TIR observations and OH distribution. Why? More analysis is required here. From the annual average zonal mean OH fields CESM, GISS and CICERO do not stick out as anomalous.”

Additional analysis shows that these outliers are associated errors in N/S OH ratio in the DJF months. We add a new figure (Figure 11) and discuss in Section 4.

Page 10 Line 2 I find it a bit suspect that the "combined" SWIR + TIR system is left out of the analysis. For sure, it seems that the (vertical) distribution of OH plays a dominant role in retrieving information for CH4 TIR and/or SWIR observations.

The SWIR+TIR results are added in the figure.
Page 10 line 16 I understand that transport is different, but somehow you have to quantify how this impacts the calculated CH4 fields. Also an analysis without meteorological perturbations would help the interpretation.

We add Figure 3 as well as a RMSE statistic showing the difference in simulated methane fields solely resulting from difference in meteorological fields.

Page 10 Line 19 “…with a precision better than 1%…” This statement attracts attention, but does not reflect the overall impression I get. By optimizing emissions on a grid and OH as one scaling factor you more or less "force" this result, by trusting the model-calculated OH distribution. Indeed sensitivity analyses show much poorer performance when the OH distribution is perturbed. One might ask: why not optimizing OH is 3D/monthly?

We now remind readers that the precision estimation from our OSSE is over-optimistic because idealized error specification. The fixed OH distribution issue that reviewers raise here is extensively discussed and quantified in Section 4. This error, which is considerably larger than 1% as the reviewer noted, is attributed as accuracy (rather than precision discussed in this sentence) because they behave like systematic biases. The full statement of uncertainty including both precision and accuracy is given in the last paragraph of Section 5.

Page 10 Line 30 Quite a positive assessment of figure 10. My estimate would be that the error is ~10%.

We now modify the statement to “…retrieved within ~ 10% of the “true” value.”
Reviewer 2

This paper uses OSSEs to test whether satellite CH4 measurements (SWIR and TIR) can be used to constrain gridded CH4 emissions and global/hemispheric mean OH simultaneously. The paper is well written and within the scope of ACP. I have a few suggestions below.

Major comments:

The key argument here is that gridded CH4 emissions and global/hemispheric [OH] can be constrained independently. To assist such an argument, the paper uses a few sensitivity tests using a global scaling of CH4 emissions and/or [OH]. The argument would be much more robust if additional tests perturbing the spatial/temporal distribution of gridded CH4 emissions can be done.

We did not use a global scaling of CH4 emissions and/or [OH] in our test. Instead, in the prior and “true” simulations, the spatial/temporal distributions of OH fields and methane emissions are different (see Figure 2 and Section 2.1). Particularly, the prior gridded methane emissions are from a compilation of bottom-up emission inventory including EDGAR v4.3.2+ WetCHARTs (see Table 1), while the “true” gridded emissions from an inversion study using the GOSAT record. Therefore, they differ both in the global total emission and their distribution. We now change the text in method description and footnote in Table 1 to avoid confusion.
MERRA-2 and GEOS-FP are used in both “true” and prior simulations. The two met fields are similar in model setups and assimilation system. Thus the effect of transport errors (e.g., in horizontal advection) is largely not taken into account in the OSSE, which may mean an underestimate of the error in the inversion. Although the native resolutions of MERRA-2 and GEOS-FP are different, the GEOS-Chem simulations here are done on a low resolution (4x5), lower than the native resolutions, thus the effect of resolution difference (that would lead to differences in transport) is not in effect here. These caveats should be better discussed. Is it possible to compare the met fields (e.g., wind fields) to ECMWF or other assimilated fields, to better discuss the transport errors? The horizontal transport errors are particularly important here, because the loss of methane mostly occurs in the tropics but methane emissions can be from anywhere.

We understand the reviewer’s concern. Unfortunately, currently our model (GEOS-Chem) can only run with GEOS-FP and MERRA-2. We now mention this limitation in Section 2.1. For readers to better evaluate the difference between GEOS-FP and MERRA-2, we add Figure 3 to demonstrate the difference in monthly methane columns resulting from the difference in these two meteorological fields (with identical emissions and OH). The differences in daily methane columns are also quantified in terms of RMSE (Section 2.1).

In Sect. 2.3, please show the equation linking x to y. This will much improve the understanding of the inversion theoretical basis.

We add the equation \( \mathbf{y} = \mathbf{Kx} + \mathbf{c} \) in the text.
Ignoring the off-diagonal component of a priori error covariance matrix (SA) is a concern, and the choice should be better justified. Errors in gridded CH4 emissions are obviously correlated. Also, it is no surprise that errors in [OH] (from v11 simulations) and errors in CH4 emissions (that drive v11 simulations) may be correlated to some extent.

To address these questions, we add the following text in Section 2.3: “This assumes no spatial error correlation in the prior emissions on the 4°×5° grid, which is likely adequate for anthropogenic emissions because of the fine spatial variability of different source types (Maasakkers et al., 2016) but may not be adequate for wetlands emissions (Bloom et al., 2017). Prior emission errors can only be roughly characterized in any case.”

We also add in Section 2.1: “These OH distributions are generated from GEOS-Chem full chemistry simulations with specified methane fields based on observations, and thus are independent of the prior emissions used in the inversion” (which are from bottom-up emission inventory).

We also discuss in Section 2.3 the linkage between these assumptions and the usage of a regularization parameter: “The need for a regularization parameter γ in equation (4) is because of uncertainty in the specifications of $S_O$ and $S_A$, and notably the assumption that these matrices are diagonal.”

The use of gamma in Eqs. 4-7 changes the weight of a priori versus observation in determining the a posteriori, and is essentially an adjustment of the errors in a priori (SA) versus observation (SO). The very low value of gamma chosen here (0.05) means that SO is scaled up by a factor of
20, assuming SA is not changed, which is a concern. An extensive explanation (beyond the argument about overfitting) is needed. Could this scaling be a reflection of how the off-diagonal components of error covariance matrices (in SA and/or SO) are treated?

We now explain the reason in Section 2.3. The small $\gamma$ results mainly from unable to specifying off-diagonal elements of $S_O$, particularly the correlations in the model transport error. This is supported by a test we performed where inversion with perfect knowledge of meteorology (i.e., both prior and “true” simulations are driven by the same meteorological field) achieves best performance with $\gamma = 1$.

Specific comments:

P2, L23, the tropospheric OH-induced lifetime is 6.3 yr in Prather et al.

We change the number from $6.9 \pm 0.4$ years to $6.3 \pm 0.4$ years.

P4, L27, the “fraternal twin” problem is reduced here, not avoided. For example, see my major comments on transport.

We change the word “avoid” to “reduce” as suggested.

P5, L20-21. The “true” lifetime here appears to be shorter than Prather et al. (10.2 yr) or the multi-model average in Naik et al. (9.7 yr). Please indicate this difference.

We now indicate this difference in Section 2 when we introduce our definition of tropospheric methane lifetime (equation (1)).

P5, L34, please see my major comment. MERRA-2 and GEOS-FP cannot be regarded as two independent met fields.
See response above to the major comment.

P6, L19-20, please indicate that you assume the errors to be random, which may not be realistic.
We now add a sentence acknowledging this limitation.

P6, L31, are there particular reasons to exclude ice-covered land, which may contain anthropogenic emissions (e.g., from industries and pipe lines) and/or natural sources (e.g., from seeping).
We change it to “The state vector … includes annual methane emission rates … over land (excluding Antarctica)”.

P7, L1, “linearly” is not correct.
We make the correction and add more clarification in the text.

P7, L8-9, the statement that model transport error correlation can be ignored needs better explanations.
We remove this sentence now. Also see response above to major comments.

P7, 9-10, here the a priori error in gridded CH4 emissions is assumed independent from the error in [OH]. Please justify this argument. I suspect that these two errors are correlated, because the model global [OH] are simulated with inputted CH4 emissions.
We now explain in Section 2.1 that “These OH distributions are generated from GEOS-Chem full chemistry simulations with specified methane fields based on observations, and thus are independent of the prior emissions used in the inversion.”

P8, L17, TIR is more sensitive to the upper troposphere, which means limited capability of retrieving [OH] (as shown in Figure 5). Please revise the sentence.

We now rewrite the paragraph for clarity.

P8, L22-34, as mentioned before, additional tests on the spatial distribution of priori gridded CH4 emissions would be necessary for a robust test of the interdependency between inversed gridded CH4 emissions and inversed [OH].

P11, L4-5, see my last comment on testing the importance of a priori gridded CH4 emissions. See response above to major comments. We change the text mentioned here to clarify what we did.
Monitoring Global Tropospheric OH Concentrations using Satellite Observations of Atmospheric Methane

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Abstract. The hydroxyl radical (OH) is the main tropospheric oxidant and is the largest main sink for atmospheric methane. The global abundance of OH has been monitored for the past decades using atmospheric methyl chloroform (CH\textsubscript{3}CCl\textsubscript{3}) as a proxy. This approach is becoming ineffective as atmospheric CH\textsubscript{3}CCl\textsubscript{3} concentrations decline. Here we propose that satellite observations of atmospheric methane in the shortwave infrared (SWIR) and thermal infrared (TIR) can provide an effective replacement alternative method for monitoring global OH concentrations. The premise is that the atmospheric signature of the methane sink from oxidation by OH is distinct from that of methane emissions. We evaluate this method in an observing system simulation experiment (OSSE) framework using synthetic SWIR and TIR satellite observations representative of the TROPOMI and CrIS instruments, respectively. The synthetic observations are interpreted with a Bayesian inverse analysis optimizing both gridded methane emissions and global OH concentrations. The optimization is done analytically to provide complete error accounting, including error correlations between posterior emissions and OH concentrations. The potential bias caused by prior errors in the 3-D seasonal OH distribution is examined using OH fields from 12 different models in the ACCMIP archive, including errors in meteorological fields and in OH distributions. We find that the satellite observations of methane can have the potential to constrain the global tropospheric OH concentrations with a precision better than 1% and an accuracy of about 3% for SWIR and 7% for TIR. The inversion can successfully separate the effects of perturbations to methane emissions and to OH concentrations to the methane budget and its trend. We also show that satellite methane observations can constrain the interhemispheric differences in OH concentrations can also be successfully retrieved. Error estimates may be overoptimistic because of the idealized treatment of errors inherent in the OSSE approach. The availability of TROPOMI and CrIS data will soon provide an opportunity to test the method with actual observations.

The main limitation to the accuracy is uncertainty in the spatial and seasonal distribution of OH.
1 Introduction

The hydroxyl radical (OH) is the main oxidant in the troposphere, responsible for the oxidation of a wide range of gases including nitrogen oxides ($\text{NO}_x \equiv \text{NO} + \text{NO}_2$), sulfur dioxide ($\text{SO}_2$), carbon monoxide (CO), methane, and other volatile organic compounds (VOCs). Subsequent reactions can lead to the formation of tropospheric ozone, strong acids, and organic aerosol. Monitoring of global tropospheric OH concentrations and its trends is a central problem in atmospheric chemistry. Here we show that satellite observations of atmospheric methane could can provide a powerful vehicle for this purpose.

The chemistry controlling tropospheric OH concentrations is complex (Levy, 1971; Logan et al., 1981). The primary source for OH is photolysis of ozone in the presence of water vapor. OH then reacts with CO and VOCs on a time scale of ~1 s to produce peroxo radicals, which can be converted back to OH by reaction with NO. This cycling of radicals is terminated by conversion to non-radical forms, principally peroxides. The dependences of OH concentrations on natural and anthropogenic emissions of $\text{NO}_x$, CO, and VOCs, as well as on UV radiation and humidity, are complicated and poorly established (Holmes et al., 2013; Murray et al., 2013; Monks et al., 2015).

OH concentrations are highly variable spatially and temporally, making it nearly impossible to infer global mean OH concentration from sparse direct measurements, which are difficult by themselves because of the low concentrations (~$10^6$ molecules cm$^{-3}$). Singh (1977) and Lovelock (1977) first pointed out the possibility of estimating the global mean OH concentration through atmospheric measurements of methyl chloroform ($\text{CH}_3\text{CCl}_3$), an industrial solvent. The industrial production of methyl chloroform is well known, and essentially all of this production is eventually released to the atmosphere, where it mixes globally in the troposphere and is removed by oxidation by OH. From measurements of atmospheric methyl chloroform and knowledge of the source, one deduces by mass balance a methyl chloroform lifetime against oxidation by tropospheric OH of 6.9 ± 0.4 years (Prather et al., 2012), providing a proxy for the global mean tropospheric OH concentration. The method became more accurate after the global ban on methyl chloroform production under the Montreal Protocol in the 1990s, as the source could then be assumed close to zero (Montzka et al., 2011).

Estimates of annual and decadal OH variability can be obtained from the long-term methyl chloroform record (Prinn et al., 2001; Krol and Lelieveld, 2003; Bousquet et al., 2005; Montzka et al., 2011). Compared to estimates from the methylchloroform proxy, global tropospheric chemistry models tend to overestimate predict higher the OH concentrations (Voulgarakis et al., 2013; Naik et al., 2013), smaller inter-annual variability (Holmes et al., 2013; Murray et al., 2013), and larger long-term trends (Holmes et al., 2013) -- inferred from the methyl chloroform proxy by ~ 15% (Voulgarakis et al., 2013; Naik et al., 2013) and have little success in reproducing inter-annual variability and long-term trends (Holmes et al., 2013; Murray et al., 2013).
Understanding the factors controlling OH concentrations and its trends is particularly important for interpretation of methane trends. Methane is the second most important anthropogenic greenhouse gas after CO₂ and contributes to about a quarter of the climate warming experienced today from pre-industrial times to present (Myhre et al., 2013). About 90% of atmospheric methane is lost by reaction with tropospheric OH (Kirschke et al., 2013). Atmospheric methane rose by 1-2% a⁻¹ in the 1970s and 1980s, stopped growing in the late 1990s, and resumed a steady growth of 0.3-0.7% a⁻¹ since 2006 (Rigby et al., 2008; Dlugokencky et al., 2009; Hartmann et al., 2013). Interpretation of these trends has generally focused on changing emissions (Rice et al., 2016; Hausmann et al., 2016; Nisbet et al., 2016; Schaefer et al., 2016), but recent studies have suggested that the growth over the past decade could be contributed by a decline in global OH concentration (Turner et al., 2017; Rigby et al., 2017). On the other hand, the trend in atmospheric CO over the past decade suggests an increase in global OH concentrations (Gaibert et al., 2017).

Inferring OH trends from methyl chloroform will become more difficult in the future as concentrations approach the detection limit (Liang et al., 2017) and possible evasion from the ocean may complicate interpretation (Wennberg et al., 2004). Finding an alternative proxy for tropospheric OH is viewed as a pressing problem in the atmospheric chemistry community (Lelieveld et al., 2006). Huang and Prinn (2002) pointed out that the major limitation to hydrochlorofluorocarbons and hydrofluorocarbons as the alternative proxies is the lack of accurate estimates of global emission inventories. To alleviate this difficulty, Liang et al. (2017) proposed to use the inter-hemispheric gradients of a suite of these compounds to jointly retrieve global emissions and tropospheric OH, but their approach may be limited by the sparsity of the surface observation network.

Here we propose that satellite methane observations could provide a reliable proxy for global tropospheric OH, using inverse analyses that optimize OH concentrations from the satellite data alongside with methane emission rates. Satellite measures methane in the shortwave infrared (SWIR, at 1.65 μm and 2.3 μm) by solar backscatter, and in the thermal infrared (TIR, around 7.6 μm) by terrestrial emission (Jacob et al., 2016). SWIR measurements are sensitive to the full column of methane but are mainly restricted to land, while TIR measurements are most sensitive to the middle/upper troposphere and operate over both land and ocean (Worden et al., 2015). A number of studies have used SWIR observations from the SCIAMACHY and GOSAT satellite instruments to infer methane emissions through inverse analyses. Most of these studies have assumed OH to be known (Bergamaschi et al., 2009; Spahni et al., 2011; Bergamaschi et al., 2013; Fraser et al., 2013; Monteil et al., 2013; Fraser et al., 2014; Houweling et al., 2014; Alexe et al., 2015; Pandey et al., 2015; Turner et al., 2015), while a few have optimized methane emissions together with OH concentrations using methyl chloroform measurements (Cressot et al., 2014; Cressot et al., 2016). Maasakkers et al. (2018) used six years of GOSAT data (2010-2015) to constrain methane emissions and their trends together with global OH trends.
TIR observations are of marginal value for inversion of methane emissions because they are insensitive to the boundary layer (Wecht et al., 2012) but they could provide complementary information for constraining OH. The methane sink from oxidation by OH has a distinct atmospheric signature peaking in the tropical troposphere, distributed zonally, and shifting seasonally with the UV flux (Figure 1). The expected availability in the coming years of new high-density satellite data from TROPOMI in the SWIR (Hu et al., 2018) and CrIS in the TIR (Gambacorta et al., 2016) motivates the assessment of the potential of these data to provide a continuous means for monitoring global tropospheric OH concentrations.

2 Observing System Simulation Experiment

We conduct an observing system simulation experiment (OSSE) to examine the feasibility of inferring global tropospheric OH concentrations by inversion of satellite observations of atmospheric methane, focusing on the potential of TROPOMI (SWIR) and CrIS as representative of SWIR and TIR observations respectively (TIR). The OSSE approach allows us to examine the ability of the observations to separately constrain methane emissions and OH, and to investigate the effects of errors in inversion parameters.

Figure 2 describes the structure of the OSSE. We use a chemical transport model (GEOS-Chem CTM) (Maasakkers et al., 2018) to generate a “true” global 3-D time-dependent distribution of methane concentrations, given a “true” state defined by known 2-D monthly methane emissions and 3-D monthly OH concentrations. The “true” methane concentration field is sampled following the specifications of candidate target satellite instruments TROPOMI and CrIS to generate synthetic observations. We then use these synthetic observations in an inverse analysis system, with an independent CTM simulation and deliberately incorrect prior estimates of emissions and OH concentrations, to assess the capability of the observing system to retrieve the “true” state. See Brasseur and Jacob (2017) for further discussion of the OSSE approach.

The mean tropospheric OH concentration is often defined in terms of the lifetime of a long-lived gas (Prather and Spivakovsky, 1990), and in our case the natural metric is the lifetime of a well-mixed tropospheric methane tracer against oxidation by tropospheric OH:

\[
\tau_{CH_4}^{OH} = \frac{\int_{troposphere} n_a \, dv}{\int_{troposphere} k(T)[OH]n_a \, dv}
\]

where \( n_a \) is air number density, \( v \) is volume, and \( k(T) = 2.45 \times 10^{-12} e^{-1775/T} \) cm\(^3\) molec\(^{-1}\) s\(^{-1}\) is the temperature-dependent oxidation rate constant (Burkholder et al., 2015). We will also examine interhemispheric differences in OH by integrating over the northern and southern hemisphere separately (\( \tau_{CH_4}^{OH, NH} \) and \( \tau_{CH_4}^{OH, SH} \)). An advantage of using equation (1) as metric for OH is that it is independent of the atmospheric distribution of methane. Note that the integration in the numerator of equation (1) is over the troposphere, therefore \( \tau_{CH_4}^{OH} \) defined in equation (1) is shorter than the lifetime of total atmospheric methane against oxidation by tropospheric OH (e.g., Prather et al., 2012).
2.1 Model simulation

We use the GEOS-Chem CTM to simulate atmospheric methane concentrations in the “true” atmosphere and to serve as the forward model for the inversion, with different meteorological fields and OH distributions to avoid the “fraternal twin” problem (Table 1). GEOS-Chem solves the continuity equation for atmospheric methane as

\[ \frac{\partial n}{\partial t} = - \nabla \cdot (n \mathbf{u}) + E - k(T)n[\text{OH}] - \text{minor sinks} \]  

(2)

where \( n \) is the methane number density, \( \mathbf{u} \) is the wind vector, \( E \) is the emission field, and \( k(T) \) is the rate constant for reaction with OH. Minor sinks include other tropospheric sinks (reaction with the Cl atom and soil uptake) and stratospheric sinks specified as 2-D loss rate constants. The transport term \(- \nabla \cdot (n \mathbf{u})\) includes not only advection by grid-resolved winds but also parameterized subgrid convection and boundary layer mixing. The methane simulation with GEOS-Chem v11 is as described by Maasakkers et al. (2018), which builds on the previous work of Wecht et al. (2014) and Turner et al. (2015).

The GEOS-Chem simulation is conducted on a 4°x5° horizontal grid and 47 vertical layers (~30 layers in the troposphere). The simulation is for year 2015 with a half-year spin-up starting from June 2014 to establish methane gradients driven by synoptic-scale transport (Turner et al., 2015). We vary the state vector elements (i.e., gridded methane emission rates and global tropospheric methane OH lifetime) between the “true” simulation and the inversion, to assess the ability of the inversion to improve estimations of these elements. To include the effect of errors in model parameters that are not optimized in the inversion, we also vary in the inversion the model meteorological fields (for the same meteorological year) and the monthly 3-D distribution of OH. It should be noted that in this setup the magnitude (global mean concentration expressed as global tropospheric methane lifetime) and the distribution (seasonal and spatial variations) of OH are decoupled and only the former is optimized.

Table 1 summarizes the OSSE conditions. The “true” emissions on the 4°x5° grid are the posterior values taken from the inversion of GOSAT data optimization of methane emissions by Maasakkers et al. (2018). The prior emissions used in the inversion are specified following Maasakkers et al. (2018) including anthropogenic emissions from (global EDGAR v4.3.2 global emission inventory (European Commission, 2017) replaced with Sheng et al. (2017) in Mexico and Canada for the oil and gas sector and with Maasakkers et al. (2016) in the US), wetland emissions from WetCHARTs v1.0 from Bloom et al. (2017), and other sources (biomass burning, termite, and geological and geothermal seeps). The “true” global OH concentration as expressed by \( \tau_{\text{OH}} \) is 8.6 years with spatial/seasonal OH distribution from GEOS-Chem v5, while the prior estimate is 7.5 years with distribution from GEOS-Chem v11. The difference between the “truth” and the prior for \( \tau_{\text{OH}} \) is comparable to the difference between a recent observation-based analysis (11.2 ± 1.3 years) (Prather et al., 2012) and the mean values from current models (9.7 ± 1.5 years) (Naik et al., 2013; Voulgarakis et al., 2013). These OH distributions are generated from GEOS-Chem full chemistry simulations with specified methane fields based on observations, and thus are
The OH distributions in GEOS-Chem v5 and v11 are significantly different due to many updates between these versions for lightning, isoprene chemistry, halogen chemistry, and emissions (Hu et al., 2017). In Section 4, we will consider even larger differences in OH distributions using the ACCMIP model ensemble (Naik et al., 2013).

GEOS-Chem simulations can be conducted with either of two different meteorological data sets produced by the NASA Global Modeling and Assimilation Office (GMAO): Meteorological fields used to produce the “true” methane concentrations are the operational Goddard Earth Observing System Forward Processing (GEOS-FP) product (Lucchesi, 2017) from the NASA Global Modeling and Assimilation Office (GMAO). Meteorological fields used in the forward model for the inversion are—and the Modern-Era Retrospective analysis for Research and Applications, Version 2 (MERRA-2) (Gelaro et al., 2017). Here we use the GEOS-FP data for 2015 to produce the “true” methane concentrations, and the MERRA-2 data also for 2015 in the forward model for the inversion. Although GEOS-FP and MERRA-2 have commonalities, they also produced by GMAO. GEOS-FP and MERRA-2 differ in grid resolution (cubed-sphere c720 for GEOS-FP and c360 for MERRA-2), model physics (in particular convection), and level of data assimilation. This allows us to introduce some model transport error in the OSSE. The root-mean-squared difference in daily methane tropospheric column mixing ratios between the two simulations driven by GEOS-FP and MERRA-2 (with identical emissions and OH fields) is ~ 2 ppbv. Comparison of monthly mean columns between the two simulations shows patterns of differences on regional and hemispheric scales (Figure 3), introducing a systematic component of inversion error.

2.2 Synthetic observations

Synthetic observations sample the “true” methane fields following the configurations of the satellite instrument—with instrument noise added (Figure 2). Here we consider the TROPOMI instrument for SWIR and the CrIS instrument for TIR. For SWIR, the sampling is at local time 13:30 over land; and for TIR, at both 13:30 and 1:30, and over land and ocean. The retrieval success rate (ratio between the number of successful retrievals and the number of attempted retrievals) is taken to be 3% for SWIR (Hu et al., 2016) and 60% for TIR (Xiong et al., 2008) because SWIR observations require cloud-free pixels whereas TIR has tolerance for fractional cloud cover. The retrievals are for the dry air column mixing ratio \( X \) [ppb] after applying typical averaging kernels to describe vertical sensitivity (Figure 3). Gaussian random noise is added to the individual retrievals to simulate the instrument error, with a standard deviation of 0.6% for SWIR TROPOMI (Butz et al., 2012) and 2% for TIR CrIS (Gambacorta et al., 2016). To account for model biases in simulation of stratospheric methane (Patra et al., 2011) and following the recommendation of Saad et al. (2016), we replace the concentrations above 200 hPa by the 2-D seasonal climatology from ACE-FTS satellite observations (Koo et al., 2017), both in the synthetic observations and in the forward model. Our test shows that the biases in stratospheric methane concentrations resulting from different meteorological fields (MERRA-2 for the forward model and GEOS-FP for the “true” atmosphere) can lead to substantial
biases in posterior estimates of $r_{\text{OH}}$—particularly for satellite observing systems involving TIR observations. This problem is solved by imposition of the ACE-FTS stratospheric methane field.

The synthetic observations are sampled on the GEOS-Chem 4°×5° grid for the purpose of the inversion. This means that successful retrievals from individual pixels are averaged over 4°×5° grid cells and the noise is random and thus reduced by the square root of the number of successful retrievals ($N_{i,t}$) within grid cell $i$ at time $t$. The noise will be greater if there are systematic errors in the retrievals. $N_{i,t}$ is determined as the ratio between the grid cell area ($A_{[i]}$) and the pixel area ($a$), weighted by the local cloud-free fraction ($1 - f_{i,t}$) taken from the “true” GEOS-FP meteorological fields:

$$N_{i,t} = \left[ c \times \frac{A_{i} \times (1 - f_{i,t})}{a} \right]$$

The global scaling factor $c$ enforces the designed retrieval success rate (3% for SWIR and 60% for TIR). For $a$, we use the nadir resolution of SWIR TROPOMI ($7 \times 7$ km$^2$) and TIR CrIS ($14 \times 14$ km$^2$). The brackets [] represent the rounding function.

### 2.3 Inversion

We use the synthetic observations (assembled in an observation vector $y$) together with the prior estimates ($x_b$) and error covariance matrices for the prior ($S_b$) and observations ($S_o$) (Figure 2) to find the analytic solution to the inverse problem. The state vector ($x$) that we seek to optimize includes annual methane emission rates on a 4°×5° grid cells-over for ice-free land–(excluding Antarctica) (1009 elements) plus either 1 or 2 elements representing the global or hemispheric methane inverse lifetimes (loss frequency).

The inverse problem presented here is not strictly linear because the loss rate depends on the methane concentration. However, a quasi-linearity can be assumed, as the range of variability of methane concentrations is sufficiently small. GEOS-Chem can be described for the purpose of the inversion by its Jacobian matrix $K = \partial y / \partial x$, which relates linearly $x$ to $y$ and through $y = Kx + c$ ($c$ is an initialization constant) can therefore be described for the purpose of the inversion by its Jacobian matrix $K = \partial y / \partial x$. We compute explicitly this Jacobian matrix by perturbing the individual terms of $x$ and calculating the resulting changes in $y$ with GEOS-Chem.

The observation error covariance matrix $S_o$ is specified as a diagonal matrix summing the instrument and forward model error variances. The instrument error is computed as described in Section 2.2. The forward model error variance is derived with the residual error method (Heald et al., 2004). We assume no model transport error correlations (which would introduce off-diagonal terms in $S_o$) can be ignored for daily or twice daily sampling on a 4°×5° grid—the GEOS-Chem model transport error correlations can be assumed to be negligible for this sampling rate. The prior error covariance matrix $S_A$ is also specified as a diagonal matrix, assuming 50% error standard deviation for
gridded emission rates as in Maasakkers et al. (2018), and 10% error standard deviation for the methane inverse lifetime (Naik et al., 2013). Again this assumes no spatial error correlation in the prior emissions on the 4°×5° grid, which is likely adequate for anthropogenic emissions because of the fine spatial variability of different source types (Maasakkers et al., 2016) but may not be adequate for wetlands emissions (Bloom et al., 2017). Prior emission errors can only be roughly characterized in any case.

The Bayesian cost function for the inverse problem (Brasseur and Jacob, 2017) is

\[ J(x) = (x - x_A)^T S_A^{-1}(x - x_A) + \gamma (y - Kx)^T S_0^{-1}(y - Kx) \]

where \( \gamma \) is an adjustable regularization parameter to prevent overfitting to the observations (see below). Analytic solution to the \( J(x) \) minimization problem (\( \frac{dJ}{dx} = 0 \)) yields the posterior estimate \( \hat{x} \):

\[ \hat{x} = x_A + G(y - Kx_A) \]

where \( G \) is the gain matrix given by

\[ G = (\gamma K^T S_0^{-1} K + S_A^{-1})^{-1} \gamma K^T S_0^{-1} \]

The solution also provides a closed form of the posterior error covariance matrix (\( \tilde{S} \)):

\[ \tilde{S} = (\gamma K^T S_0^{-1} K + S_A^{-1})^{-1} \]

The diagonal elements of \( \tilde{S} \) represents the error variances of the posterior estimates \( \hat{x} \).

The need for a regularization parameter \( \gamma \) in equation (4) is because of uncertainty in the specifications of \( S_0 \) and \( S_A \), and notably the assumption that these matrices are diagonal, may lead to overfitting when the cost function in equation (4) is minimized with \( \gamma = 1 \) in a Standard Bayesian optimization, by minimizing the cost function in equation (4) with \( \gamma = 1 \) assumes that the observations are independent and identically distributed (IID condition) but this is generally not the case and can result in overfitting. Here we determine based on the L-curve plot (Hansen, 2000) that optimal \( \gamma \) is should be in the range of 0.01-0.1 (left panel of Figure 5). We also show This range of values also choose an optimal value for \( \gamma \) based on the ability of the inversion to achieve the best match agreement of the inversion with the “true” emissions in this range as evaluated with the root mean square error (RMSE) (right panel of Figure 5). We use \( \gamma = 0.05 \) in the subsequent analysis. The small \( \gamma \) value mainly results from neglecting the correlations in the model transport errors; a sensitivity test in which both prior and “true” simulations are driven by MERRA-2 meteorology shows best performance with \( \gamma = 1 \) for the metrics of Figure 45.

3 Joint Optimization of Global \( \tau_{CH_4}^{FH} \) and Methane Emission Rates
Figure 5-6 shows the ability of the three different satellite observing systems considered here (SWIR, TIR, and SWIR+TIR) to jointly constrain gridded emission rates and $\tau_{CH_4}^{OH}$. The ability to constrain the spatial distribution of emissions is measured by the RMSE on the 4°×5° grid. Although all three satellite observing systems retrieve global total methane emissions within 5% of the “true” value (not shown), the inversions with SWIR observations are able to resolve the distribution of constrain methane emissions (low RMSE) but while the one with only TIR observations is not (high RMSE). This is consistent with the low sensitivity of TIR to the lower troposphere (Figure 3), where most of the information on spatially resolved emissions is contained. On the other hand, both SWIR and TIR are able to retrieve $\tau_{CH_4}^{OH}$ within 3% of the “true” value.

Analysis of the posterior error covariance matrix ($\mathbf{S}$) shows that the error standard deviations $\sigma_p$ on the posterior estimate of $\tau_{CH_4}^{OH}$ are 0.75%, 0.46%, and 0.39% for SWIR, TIR, and SWIR+TIR satellite observing systems, respectively, for a one-year inversion (Table 2). $\mathbf{S}$ tends to be overoptimistic as a measure of posterior error because it assumes no systematic error in model parameters affecting the accuracy of the inversion (Brasseur and Jacob, 2017). Below we will explore the effect of errors in the global OH distribution as a limitation on accuracy.

A central question is the ability of the inversion to independently constrain $\tau_{CH_4}^{OH}$ global OH concentrations and total emissions. The error covariance between the two can be computed from $\mathbf{S}$ (See Appendix for the method) and is visualized in Figure 67. For SWIR, the significant negative correlation ($r = -0.78$) implies some aliasing between corrections to OH concentration and emissions: nevertheless, the posterior error on $\tau_{CH_4}^{OH}$ is greatly decreased relative to its 10% prior value. Error correlation is much less ($r = -0.47$) with the TIR observing system and the error on $\tau_{CH_4}^{OH}$ is further decreased. TIR observations are more effective than SWIR for independently constraining global emissions and OH concentrations because they provide better global coverage (higher retrieval success rate) including over the oceans. TIR observations can constrain global total emissions although they are incapable of resolving the spatial distribution of emission rates (Figure 5), and this provides a basis for successful inversion of $\tau_{CH_4}^{OH}$. The combined SWIR+TIR system results in smallest confidence ellipses (Figure 6) has the lowest posterior errors for among the three satellite observing systems, suggesting that combining SWIR and TIR observations improves the ability to jointly constrain OH concentration and emissions. It should be noted that because SWIR+TIR achieves smaller errors in both $\tau_{CH_4}^{OH}$ and global total emission (probable solutions of $\tau_{CH_4}^{OH}$ and total even though the error correlation with global emissions lie in a smaller subspace), the error correlation ($r = -0.57$) also become less consequential than the SWIR or is greater than for TIR-only case.

To go further than the error correlation analysis, we used the OSSE environment to directly test whether perturbations to OH concentrations and global emissions can be retrieved independently. We perturbed the emission rates and/or OH concentrations in three additional simulations for the “true” atmosphere. In the first case we increased global emissions by
10\%, in the second case we decreased global OH concentration by 5\%, and in the third case we combined both perturbations.

Figure 7–8 shows that the posterior estimations all correctly identify the percentage changes in global total emissions and/or OH concentration, within 2\% from the “true” changes, in all three tests. This result provides evidence that further demonstrates the potential for satellite observations of methane to independently constrain global methane emissions and OH concentrations. Our method has good ability to resolve the aliasing effect between emissions and OH on the global scale. Among all three satellite observing systems, inferred OH percentage changes with SWIR+TIR observations are closest to the “true” changes for all three cases, demonstrating that combining SWIR and TIR observations improves the ability to separate changes in OH from changes in emissions, consistent with the analysis of posterior error covariance matrices (Figure 6). The results shown in Figure 7–8 suggest that satellite observations of methane should be able to detect trends in OH separately from trends in methane emissions, which has important implications for attribution of trends in methane observations (Turner et al., 2017; Rigby et al., 2017).

4 Impact of Errors in Prior OH Distributions

In our method, global OH abundance (i.e., global methane inverse lifetime) is represented by a single state vector element \( \tau_{\text{CH}_4}^{\text{OH}} \). The seasonal and spatial distribution of OH is a forward model parameter that the inversion does not seek to optimize. Errors in the prior OH distribution may therefore result in errors in the posterior estimate of \( \tau_{\text{CH}_4}^{\text{OH}} \), which may not be fully captured by \( \mathbf{S} \). To test the impact of this uncertainty source, we use alternative “true” OH distributions from the 11 models that participated in the ACCMIP intercomparison (Naik et al., 2013), replacing the OH distribution from GEOS-Chem v5. The ACCMIP archive includes present-day (the 2000s) 3-D monthly mean OH concentrations from the different models and was retrieved/downloaded from http://badc.nerc.ac.uk/ (See Lamarque et al. (2013) for model descriptions). The ACCMIP models differ greatly in both global OH abundance and distribution (Figure 8). To focus on errors in OH distributions, we applied a global scaling factor to each model to impose a methane lifetime \( \tau_{\text{CH}_4}^{\text{OH}} \) of 8.6 years, same as in our baseline “true” atmosphere. To avoid complicating influence from errors in the meteorological field, we do not vary the meteorological field (i.e. MERRA-2) between the “true” simulation and the inversion in this test of the sensitivity to the OH distribution.

Figure 9–10 shows the posterior estimation of \( \tau_{\text{CH}_4}^{\text{OH}} \) resulting from the 12 different “true” OH distributions (all with the same “true” \( \tau_{\text{CH}_4}^{\text{OH}} \)). For all three satellite observing systems, the median posterior \( \tau_{\text{CH}_4}^{\text{OH}} \) is within 2\% of the “true” \( \tau_{\text{CH}_4}^{\text{OH}} \). But some model OH distributions (CESM, GISS, and CICERO) result in large errors when using TIR observations even though they do not seem anomalous in Figure 8. Further inspection indicates that the errors are due to large anomalies in hemispheric \( \tau_{\text{CH}_4}^{\text{OH}} \) ratios in boreal winter (Figure 11), when the effect of emissions and OH on atmospheric methane is most differentiated. Errors in posterior \( \tau_{\text{CH}_4}^{\text{OH}} \) are smaller for SWIR only and this is because SWIR draws its information on emissions from regional patterns in concentrations, rather than the larger-scale patterns in TIR. We determine the relative accuracy due to the
uncertainty in the OH distribution (σa) as the ratio of the half interquartile range to the “true” τCH4. This results in σa of 2.6%, 6.9%, and 6.0% for SWIR, TIR, and SWIR+TIR (Table 2). Our results suggest that satellite observing systems involving TIR measurements are likely more susceptible to errors in the OH distribution for τCH4 estimations.

We also applied these different “true” OH distributions to the OSSE test of Figure 7-8 perturbing emissions and/or OH to evaluate the impact of errors in OH distribution on detecting and separating changes in global τCH4 and emissions. The spread in inferred changes in OH is almost negligible for all the observing systems considered (Figure 7-8), indicating that the errors resulting from imperfect OH distribution in a single-year inversion are systematic. An important implication is that these errors from imperfect OH distribution (Figure 9) may not impair the ability to detect long-term inter-annual trends in OH concentrations, as long as the inter-annual variability in the OH distribution is relatively small. We therefore present them in Table 2 as a statement of accuracy.

The above results suggest that we may improve the estimation of τCH4 if the inversion is able to retrieve information on the OH distribution from the satellite methane observations. For this purpose, we tried to optimize separately the mean OH concentrations in the northern and southern hemisphere, expressed as τCH4NH and τCH4SH. In general, the inversion is able to resolve the interhemispheric OH ratio (τCH4NH/τCH4SH) for the range of OH distributions from the different global models using both SWIR and TIR satellite observing systems (Figure 10). However, the improvement in the estimate of the global OH concentration τCH4 (computed as harmonic mean of τCH4NH and τCH4SH) is insignificant in most cases (not shown), indicating that errors in other factors in OH distributions (e.g., vertical and seasonal distributions) in addition to the hemispheric ratio are also important contributors to errors shown in Figure 10. A careful design of the state vector that balances the resolution of OH distribution with the aliasing of OH and emissions should further improve the accuracy of the method but is beyond the scope of the current study.

5 Conclusions

We conducted observing system simulation experiments (OSSEs) to test the feasibility of monitoring global tropospheric OH concentrations using satellite observations of methane. We considered short-wave infrared (SWIR) TROPOMI and thermal infrared (TIR) CrIS as target candidate satellite instruments for this application, since methane retrievals from these instruments are expected to be available in the near future and will provide much improved coverage compared to current instruments. Through inversion of synthetic observations from these instruments sampling a “true” atmosphere, we jointly optimized gridded methane emission rates and the global tropospheric OH concentration (expressed as the methane-lifetime of a well-mixed tropospheric methane tracer against oxidation by tropospheric OH, τCH4 as given in Equation (1)). The
OSSE used different meteorological fields for the “true” atmosphere and for the inversion, and tested the effect of errors in the prior OH distributions.

Our results show that either SWIR or TIR observations can constrain $\tau_{\text{CH}_4}^{\text{OH}}$ with a precision better than 1%. This is an optimistic estimation of precision because we assume observational noise to be random while real retrieval errors are subject to a multitude of factors whereas it would have a systematic component that we cannot characterize. Nevertheless, the results show that the method has strong potential. Analysis of the posterior error covariance matrix shows that emissions and global OH concentrations can be separately retrieved because they have different signatures on the distribution of atmospheric methane. There is some error correlation, particularly for SWIR-only observations, but the posterior errors on global OH concentrations still improve considerably on the prior. Simulation experiments with perturbations to either global methane emissions and/or global OH concentration demonstrate that the method can distinguish changes in OH from changes in emissions as contributors to trends in atmospheric methane. Best performance is achieved by combining the SWIR and TIR observations.

The effect of prior errors in the seasonal and spatial distributions of OH concentrations was investigated by considering global 3-D monthly concentrations fields from the 12 ACCMIP models (Naik et al., 2013), which show considerable inter-model variability. We find that these errors limit the accuracy of our method but precision is not compromised, so that inter-annual OH trends can still be retrieved. The effect of errors in the OH distribution could be addressed by optimizing this distribution in the state vector for the inversion, and we show that the interhemispheric OH difference at least can be successfully retrieved within ~10% of the “true” value assumed in the inversion of methane concentrations are the principal limitation to the accuracy in inferring the global OH concentration. Using archived OH distributions from the 12 ACCMIP models, we find that the majority of the models can accurately retrieve global OH concentrations but a few are problematic when using TIR observations. Errors in the OH distribution do not degrade the ability to retrieve perturbations to OH fields and separate them from perturbations in emissions. Interhemispheric ratios of OH are also shown to be successfully constrained within ~10% of the “true” values if inversion optimizes hemispheric OH concentrations.

We conclude that satellite observations of methane are a potentially promising replacement for methyl chloroform as a proxy for global tropospheric OH concentrations. Based on our OSSE ensemble results, we estimate the precision of the method to be 0.75%, 0.46%, and 0.39% and accuracy 2.6%, 6.9%, and 6.0% for SWIR, TIR, and SWIR+TIR satellite observing systems, respectively. The accuracy is limited primarily by uncertainty in the OH distribution but inference of temporal trends in OH would not be affected if any bias in the OH distribution remains constant. These estimates are probably overoptimistic because of the idealized treatment of errors inherent in the OSSE approach. The availability of TROPOMI and CrIS data will soon provide an opportunity to test the method with actual observations.
Appendix

The posterior error covariance matrix ($\mathbf{S}$) in our inversion is a $1010 \times 1010$ matrix that characterizes the error covariance structure of gridded emission rates ($E_i$) in 1009 grid cells and global methane lifetime against oxidation by tropospheric OH ($\tau_{\text{CH}_4}^{\text{OH}}$). We condense $\mathbf{S}$ into a $2 \times 2$ matrix $\mathbf{S}_2$, which represents the error covariance of global total emissions ($E_T = \sum_{i=1}^{n} E_i$, where $n=1009$) and $\tau_{\text{CH}_4}^{\text{OH}}$:

$$\mathbf{S}_2 = \begin{bmatrix} \text{Var}(E_T) & \text{Cov}(E_T, \tau_{\text{CH}_4}^{\text{OH}}) \\ \text{Cov}(E_T, \tau_{\text{CH}_4}^{\text{OH}}) & \text{Var}(\tau_{\text{CH}_4}^{\text{OH}}) \end{bmatrix}$$

where $\text{Var}(\tau_{\text{CH}_4}^{\text{OH}})$ can be obtained directly from $\mathbf{S}$, and $\text{Var}(E_T)$ and $\text{Cov}(E_T, \tau_{\text{CH}_4}^{\text{OH}})$ can be computed from $\mathbf{S}$ with the following formulae:

$$\text{Var}(E_T) = \sum_{i=1}^{n} \text{Var}(E_i) + 2 \sum_{1 \leq i < j \leq n} \text{Cov}(E_i, E_j)$$

$$\text{Cov}(E_T, \tau_{\text{CH}_4}^{\text{OH}}) = \sum_{i=1}^{n} \text{Cov}(E_i, \tau_{\text{CH}_4}^{\text{OH}})$$

$\mathbf{S}_2$ can then be visualized as a bi-variate Gaussian distribution (Figure 67).

Acknowledgments. This work was funded by the Interdisciplinary Science (IDS) program of the NASA Earth Science Division. Y. Zhang was partially funded by the Kravis Scientific Research Fund at Environmental Defense Fund.

References


Table 1 OSSE conditions.

<table>
<thead>
<tr>
<th>“True” Atmosphere</th>
<th>Inversion—Prior estimate and Parameters</th>
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<tbody>
<tr>
<td>State Vector (x)</td>
<td></td>
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<tr>
<td>Grid Emission Rates(^a)</td>
<td>Posterior from GOSAT analysis(^b)</td>
</tr>
<tr>
<td>Global OH concentration ((\tau_{\text{OH}})) (^d)</td>
<td>8.6 years</td>
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</table>

**Parameters**

<table>
<thead>
<tr>
<th>OH Distribution</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>GEOS-Chem v5, ACCMIP (^e)</td>
<td>GEOS-Chem v11</td>
</tr>
<tr>
<td>GEOS-FP</td>
<td>MERRA-2</td>
</tr>
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</table>

\(^a\) Methane emission rates on a 4°×5° grid over ice-free land (1009 elements).

\(^b\) From Maasakkers et al. (2018).

\(^c\) Prior emissions are specified following Maasakkers et al. (2018). The prior estimate for the inversion uses anthropogenic emissions from EDGAR v4.3.2 (European Commission, 2017) except in the US (Maasakkers et al., 2016) and oil/gas in Canada and Mexico (Sheng et al., 2017), is used as the global default for anthropogenic emissions, but is replaced with Sheng et al. (2017) in Mexico and Canada for the oil and gas sector and Maasakkers et al. (2016) in the US. WetCHARTs is from Bloom et al. (2017). Sources from biomass burning, termite, and geological seeps are also specified with available emission inventories.

\(^d\) Expressed as the lifetime of a well-mixing tropospheric methane lifetime tracer against oxidation by tropospheric OH (equation (1)).

\(^e\) Sensitivity simulations in Section 4 use 11 global OH distributions from the ACCMIP ensemble (Naik et al., 2013).

\(^f\) Meteorological fields are for 2015.
Table 2  Uncertainty in $\tau_{\text{OH}}$ estimations with different satellite observing systems.

<table>
<thead>
<tr>
<th>Observing System</th>
<th>SWIR</th>
<th>TIR</th>
<th>SWIR+TIR</th>
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<tbody>
<tr>
<td>Precision ($\sigma_p$)</td>
<td>0.75%</td>
<td>0.46%</td>
<td>0.39%</td>
</tr>
<tr>
<td>Accuracy ($\sigma_a$) $^a$</td>
<td>2.6%</td>
<td>6.9%</td>
<td>6.0%</td>
</tr>
</tbody>
</table>

$^a$ Accuracy is derived from inversions using different OH distributions from 12 global models for the “true” atmosphere (Section 4).
Figure 1 Monthly methane loss rate from oxidation by OH in January and July 2015 computed with the GEOS-Chem model (Maasakkers et al., 2018; Wecht et al., 2014). The top panels show the column loss rates and the bottom panels show the zonally integrated loss rates.
Figure 2 Observing System Simulation Experiment (OSSE) framework to test the ability of SWIR and TIR satellite observations of atmospheric methane to simultaneously constrain methane emission rates ($E_i$) and the global mean tropospheric OH concentration expressed as methane lifetime against oxidation by tropospheric OH ($\tau_{\text{CH}_4}^{\text{OH}}$).
Figure 3 Differences in monthly mean methane dry air tropospheric column mixing ratios between two simulations with different meteorological fields (GEOS-FP minus MERRA-2) for January (left) and July (right).
Figure 3-4 Typical vertical sensitivities (column averaging kernels) for satellite observations of atmospheric methane in the SWIR and in the TIR. Adapted from Worden et al. (2015).
Figure 4-5 Optimization of the regularization parameter $\gamma$ in equation (4) for the SWIR+TIR satellite observing system for the inversion. Left: L-Curve plot (log-log plot of the squared errors of a regularized solution versus corresponding residual). The denoted numbers are $\gamma$ values of $\gamma$ corresponding to each point are indicated. The “turning corner” of the curve indicates an optimal choice of $\gamma$ (Hansen, 2000). Right: Ability of the inversion to match the “true” gridded methane emission field as a function of the regularization parameter $\gamma$ in equation (4) for the SWIR+TIR satellite observing system. The ability is measured by the RMSE.
Figure 5-6 Ability of SWIR, TIR, and SWIR+TIR systems to jointly constrain gridded methane emissions and global OH concentrations (as measured by the methane lifetime $\tau_{\text{CH}_4}^{\text{OH}}$) in our base 1-year inversion. The left panel shows the RMSE in fitting the “true” 4°x5° gridded emission rates. The right panel compares the posterior estimates of $\tau_{\text{CH}_4}^{\text{OH}}$ to the prior estimate and to the “true” value. The prior error standard deviation is shown as a vertical bar. Posterior error bars are too small to be shown, although this reflects overoptimistic error characterization in the inversion (see text).
Joint PDF of Errors in Posterior Global Methane Emissions and OH

Figure 6-7 Joint distribution of relative uncertainties in $\tau_{CH_4}^{OH}$ and total methane emissions, summarized as given by the posterior error covariance matrices, for different satellite observing systems. Contours represent confidence ellipses from probability 0.1 (innermost) to 0.9 (outermost) at an interval of 0.1. The correlation coefficients ($r$) between errors in $\tau_{CH_4}^{OH}$ and total methane emissions are inset.
Figure 7-8 OSSE experiments perturbing global emissions (E+10%), OH (OH-5%), and both (E+10% OH-5%) to test whether the inversion can retrieve separately these perturbations. Results are shown for different satellite observing systems (SWIR, TIR, and SWIR+TIR). Blue symbols represent posterior estimation of changes in emissions and red symbols posterior estimation of change in global OH concentration. The boxes represent the 75th, 50th, and 25th percentiles and the whiskers represent the maximum and minimum of the results using 12 different OH distributions in “true” simulations. Dashed lines are “true” changes in global emissions (blue) and OH concentration (red).
Figure 8–9 Variability of OH distributions across global models. The figure shows annual zonal mean OH concentrations for 13 different models used in the OSSE. GEOS-Chem v11 is used in the forward model for the inversion with $\tau_{\text{OH}} = 7.5$ years. GEOS-Chem v5 is used for the baseline “true” atmosphere with $\tau_{\text{OH}} = 8.6$ years. The other 11 distributions are from the ACCMIP model ensemble (Naik et al., 2013), with global scaling factors to impose $\tau_{\text{CH}_4}^{\text{OH}} = 8.6$ years in all cases, and are used in alternative representations of the “true” atmosphere.
Figure 9-10 Effect of error in OH distribution on the optimization of the global OH concentration (methane lifetime $\tau_{\text{CH}_4}^{\text{OH}}$) from satellite observations. The Figure shows the posterior estimation of $\tau_{\text{CH}_4}^{\text{OH}}$ using 12 different OH distributions (Figure 8) in simulations of the “true” atmosphere sampled by SWIR, TIR, and SWIR+TIR instruments, in comparison with “true” (dashed line) and prior (dotted line) $\tau_{\text{CH}_4}^{\text{OH}}$. The boxes represent the 75th, 50th, and 25th percentiles, solid lines inside the boxes represent the medians, the whiskers represent the maximum and minimum, and dots represent results for each OH distribution.
Figure 11 Relationship between errors in posterior estimates of $\tau_{CH_4}^{OH}$ and errors in the prior $\tau_{CH_4}^{OH,NH}/\tau_{CH_4}^{OH,SH}$ ratio for the entire year and for boreal winter (December, January, and February). Red dots represent the three cases with large positive errors in posterior estimates of $\tau_{CH_4}^{OH}$ in Figure 10 and blue dots represent the other nine cases. The plots show that the large errors in posterior estimates of $\tau_{CH_4}^{OH}$ are associated with large errors in the prior $\tau_{CH_4}^{OH,NH}/\tau_{CH_4}^{OH,SH}$ ratio in DJF months.
Figure 10–12  Ability of the inversion of satellite methane observations to retrieve the interhemispheric OH ratio defined by \( \frac{\tau_{\text{CH}_4}^{\text{OH,NH}}}{\tau_{\text{CH}_4}^{\text{OH,SH}}} \). Posterior inversion results using either SWIR or TIR or SWIR+TIR observations are compared to the “true” ratio from 12 different model OH distributions (Figure 89). The dashed vertical line represents the prior \( \frac{\tau_{\text{CH}_4}^{\text{OH,NH}}}{\tau_{\text{CH}_4}^{\text{OH,SH}}} \) common to all inversions.