



## 1 **The evaluating study of the momentum and heat exchange process of two** 2 **surface layer schemes during the severe haze pollution in east China**

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17 **Abstract.** The turbulent flux parameterization schemes in surface layer are crucial for air pollution modeling. The pollutants  
18 prediction by atmosphere chemical model exist obvious deficiencies, which may be closely related to the uncertainties of the  
19 momentum and sensible heat fluxes calculation in the surface layer. In this study, a new surface layer scheme (Li) and a  
20 classic scheme (MM5) were compared and evaluated based on the observed momentum and sensible heat fluxes in east  
21 China during a severe haze episode in winter. The results showed that it is necessary to distinguish the thermal roughness  
22 length  $z_{0h}$  from the aerodynamic roughness length  $z_{0m}$ , and ignoring the difference between the two led to large errors of  
23 the momentum and sensible heat fluxes in MM5. The error of calculated sensible heat flux was reduced by 54% after  
24 discriminating  $z_{0h}$  from  $z_{0m}$  in MM5. Besides, the algorithm itself of Li scheme performed generally better than MM5 in  
25 winter in east China and the momentum flux bias of the Li scheme was lower about 12%, sensible heat flux bias about 5%  
26 than those of MM5 scheme. Most of all, the Li scheme showed a significant advantage over MM5 for the transition stage  
27 from unstable to stable atmosphere corresponding to the  $PM_{2.5}$  accumulation. The momentum flux bias of Li was lower  
28 about 38%, sensible heat flux bias about 43% than those of MM5 during the  $PM_{2.5}$  increasing stage. This study result  
29 indicates the ability of Li scheme for more accurate describing the regional atmosphere stratification, and suggests the  
30 potential improving possibilities of severe haze prediction in east China by online coupling it into the atmosphere chemical  
31 model.

32 **Key words:** surface layer; turbulent flux parameterization; roughness length; numerical modeling; air pollution



### 33 **1 Introduction**

34 Adequate air quality modeling relies on accurate simulations of meteorological conditions, especially in planetary  
35 boundary layer (PBL) (Hu et al., 2010; Cheng et al., 2012; Xie et al., 2012). The PBL is closely coupled to the earth's surface  
36 by turbulent exchange processes. The surface layer (SL) close to the earth's surface reflects the surface state by calculating  
37 momentum, heat, water vapor and other fluxes, and influences the atmospheric structure by turbulent transport process. The  
38 SL provides important bottom boundary conditions, as the bottom layer of the PBL. In addition, atmospheric conditions in  
39 both the PBL and upper layers are strongly dependent on the turbulent fluxes which are computed in the SL (Ban et al.,  
40 2010). Flux parameterization in the SL plays an important role in studies of the hydrological cycle and weather prediction  
41 (Yang et al., 2001; Li et al., 2014).

42 In many numerical models, surface momentum, heat and moisture fluxes calculated by a SL scheme are coupled to a  
43 Land Surface Module, which in turn provides input to the PBL module. Therefore, an adequate SL scheme is crucial for the  
44 model performance (Jiménez et al., 2012). It was reported that the difference of 2-m temperature modeling in three PBL  
45 schemes is due to different calculation of sensible heat fluxes in the SL (Hu et al., 2010). Tymvios et al. (2017) evaluated the  
46 performance of Weather Research and Forecasting (WRF) model with a combination of several PBL and compatible SL  
47 schemes and emphasized the importance of SL schemes.

48 Most SL schemes used in numerical models are bulk algorithms which are based on Monin-Obukhov similarity theory  
49 (hereinafter MOST, Monin and Obukhov, 1954). In a bulk algorithm, vertical fluxes in the SL can be considered constant.  
50 The effects of shear stress and buoyancy on turbulent transport are discussed with the method of similarity theory and  
51 dimensional analysis. Turbulent fluxes in models are parameterized by wind, temperature, moisture in the lowest layer,  
52 surface skin temperature and humidity. Many international scholars verified the MOST using of field experiments and then  
53 proposed the universal functions, the commonly used of which is Businger-Dyer (BD) equation (Businger, 1966; Dyer,  
54 1967). With the development of observation technology, the coefficients in the BD equation have been further modified (e.g.,  
55 Paulson, 1970; Webb, 1970; Businger et al., 1971; Dyer, 1974; Högström, 1996). In addition to the BD equation, some  
56 other schemes have been put forward and they may perform better especially for the strongly stable stratification (e.g.,  
57 Holtslag and De Bruin, 1988, Beljaars and Holtslag, 1991, Cheng and Brutsaert, 2005). The schemes can be divided into  
58 two types according to the computing characteristics. One type is called as iterative algorithm (e.g., Paulson, 1970; Businger  
59 et al., 1971; Dyer, 1974; Högström, 1996; Beljaars and Holtslag, 1991), and it keep the MOST completely with less  
60 approximation so that the results can be more precise. However, it needs to take much more steps to converge and hence the  
61 CPU time is consuming which affects the ability and efficiency of modeling (Louis, 1979; Li et al., 2014); The other one is  
62 called as non-iterative algorithm (e.g., Louis et al., 1982; Launiainen, 1995; Wang et al., 2002; Wouters et al., 2012). Due to  
63 the approximate treatment, there is no need for loop iteration in calculation. It is much simpler and less CPU time-consuming,



64 but it may lead to a lower accuracy of the results.

65 Although many researches above focused on the effects of the SL schemes on PBL and meteorological elements, few  
66 studies discussed it based on a pollution episode corresponding various atmospheric states. The turbulent exchange of  
67 momentum, heat, and moisture at the ground surface is more important than large-scale transport for the accumulation and  
68 transport of pollutants when atmosphere is stable. In this paper, two kinds of surface flux calculation schemes were  
69 compared and evaluated during a haze episode using observational flux data. One is a new scheme proposed by Li et al.  
70 (2014; 2015, Li hereinafter), the other is MM5 similarity scheme (Zhang and Anthes, 1982, MM5 hereinafter) which is  
71 widely applied in modeling investigation (e.g., Hu et al., 2010; Wang et al., 2015a, b; Tymvios et al., 2017). As a new one,  
72 the Li scheme is not yet applied to the atmosphere chemical models, and few relevant articles evaluate this scheme using the  
73 observational data especially in a haze episode. In this scheme, the aerodynamic roughness length  $z_{0m}$  and thermal  
74 roughness length  $z_{0h}$  are distinguished each other and the effect of the roughness sublayer (RSL) is taken into account. In  
75 addition, this scheme can be applied to the full range of roughness status  $10 \leq \frac{z}{z_{0m}} \leq 10^5$  and  $-0.5 \leq \ln \frac{z_{0m}}{z_{0h}} \leq 30$  under  
76 whole conditions  $-5 \leq Ri_B \leq 2.5$ . Here  $z$  is the reference height and  $Ri_B$  is the bulk Richardson number. Compared with Li,  
77 the MM5 scheme does not consider the effect of both  $z_{0h}$  and the RSL. Further, in order to keep the stability of modeling,  
78 some limits have been used in MM5 such as a limit of -10 is used for both the stability parameter  $\zeta$  and universal functions.

## 79 2 Theory

80 The definition of the momentum and sensible heat flux are introduced, and the detailed algorithms of the Li and MM5  
81 schemes are explained.

### 82 2.1 Introduction of the momentum and sensible heat flux

83 The turbulent fluxes from ground surface are defined as follows:

$$84 \quad \tau = \rho u_*^2 \quad \text{and} \quad (1a)$$

$$85 \quad H = -\rho c_p u_* \theta_* \quad (1b)$$

86 Where  $\tau$  is the momentum flux,  $H$  is the sensible heat flux,  $\rho$  is the air density,  $c_p$  is the specific heat capacity at  
87 constant pressure.  $u_*$  and  $\theta_*$  are the friction velocity and the temperature scale, respectively, and they represent the  
88 intensity of the vertical turbulent flux transport and they are approximately independent on height in the SL.

89 Both the Li and MM5 schemes are calculated with bulk flux parameterization. As an important dimensionless parameter  
90 related with the stability, the bulk Richardson number  $Ri_B$  is defined as

$$91 \quad Ri_B = \frac{gz(\theta - \theta_g)}{\theta u_*^2} \quad (2)$$

92 Where  $g$  is the acceleration of gravity,  $z$  is the reference height which is the lowest level in the model,  $\theta$  is the mean



93 potential temperature at height  $z$ ,  $\theta_g$  is the surface radiometric potential temperature,  $u$  is the mean wind speed at height  $z$ .

94 Thus,  $Ri_B$  can be computed through meteorological data at least two levels.

## 95 2.2 The Li scheme

96 The basic idea of Li is to parameterize  $\zeta$  directly with  $Ri_B$ ,  $z_{0m}$  and  $z_{0h}$ , and then calculate turbulence fluxes. In the  
 97 scheme, bulk transfer coefficients of the momentum and sensible heat fluxes ( $C_M$ ,  $C_H$ ) are expressed as

$$98 \quad C_M = \frac{u_*^2}{u^2} = \frac{\tau}{\rho u^2} \quad \text{and} \quad (3a)$$

$$99 \quad C_H = \frac{u_* \theta_*}{u(\theta - \theta_g)} = -\frac{H}{\rho c_p u(\theta - \theta_g)}. \quad (3b)$$

100 Based on MOST and considering the RSL effect, the relationship between the bulk transfer coefficients and the profile  
 101 functions corresponding to wind and potential temperature are usually expressed as

$$102 \quad C_M = \frac{k^2}{\left[ \ln \frac{z}{z_{0m}} - \psi_M \left( \frac{z}{L} \right) + \psi_M \left( \frac{z_{0m}}{L} \right) + \psi_M^* \left( \frac{z}{L}, \frac{z}{z_*} \right) \right]^2} \quad \text{and} \quad (4a)$$

$$103 \quad C_H = \frac{k^2}{R \left[ \ln \frac{z}{z_{0m}} - \psi_M \left( \frac{z}{L} \right) + \psi_M \left( \frac{z_{0m}}{L} \right) + \psi_M^* \left( \frac{z}{L}, \frac{z}{z_*} \right) \right] \left[ \ln \frac{z}{z_{0h}} - \psi_H \left( \frac{z}{L} \right) + \psi_H \left( \frac{z_{0h}}{L} \right) + \psi_H^* \left( \frac{z}{L}, \frac{z}{z_*} \right) \right]}. \quad (4b)$$

104 Where  $k$  is the von Kármán constant which is 0.4 in both two schemes,  $R$  is the Prandtl number which is 1.0 in two  
 105 schemes,  $\psi_M$  and  $\psi_H$  are the integrated stability functions for momentum and sensible heat, respectively, which are also  
 106 called universe functions.  $L$  is the Obukhov length ( $\zeta = \frac{z}{L}$ ),  $\psi_M^*$  and  $\psi_H^*$  are the correction functions accounting for RSL  
 107 effect,  $z_*$  is the height of RSL. From above equations we can see that the calculation of the momentum and sensible heat  
 108 flux requires  $C_M$  and  $C_H$  (or  $u_*$  and  $\theta_*$ ), and there are 3 key points to get them:

109 1.  $z_{0m}$  and  $z_{0h}$ .  $z_{0m}$  and  $z_{0h}$  are two key parameters in the bulk transfer equations and their definitions and  
 110 influence will be given in Sect. 4.1.

111 2.  $\zeta$ . In the Li scheme, the determination of  $\zeta$  is the most crucial problem for calculation of turbulent fluxes. Li is a new  
 112 scheme based on the results of Yang et al. (2001), Wouters et al. (2012), Sharan and Srivastava (2014), and which is  
 113 proposed to approach the classic iterative computation results using multiple regressions. In particular, under stable  
 114 conditions, the calculation procedure for a given group of  $Ri_B$ ,  $z_{0m}$  and  $z_{0h}$  is the following: (1) find the region  
 115 according to  $z_{0m}$  and  $z_{0h}$  with Table 1 (see Li et al., 2014); (2) find the section according to the region and  $Ri_B$  with  
 116 Eq. (5) and coefficients in Table 2 (see Li et al., 2014); (3) calculate  $\zeta$  using Eq. (6) and Tables 3-10 (see Li et al.,  
 117 2014).

$$118 \quad Ri_{Bcp} = \sum C_{mn} (\log L_{0M})^m (L_{0H} - L_{0M})^n, \quad (5)$$

$$119 \quad \zeta = Ri_B \sum C_{ijk} Ri_B^i L_{0M}^j (L_{0H} - L_{0M})^k. \quad (6)$$

120 Where  $C_{mn}$  and  $C_{ijk}$  are the coefficients in Tables 3-10.  $L_{0M} = \ln \frac{z}{z_{0m}}$ ,  $L_{0H} = \ln \frac{z}{z_{0h}}$ ,  $m, n = 0, 1, 2$ , and  $m +$   
 121  $n \leq 3$ ;  $i, j, k = 0, 1, 2, 3$ , and  $i + j + k \leq 4$ . Similarly, under unstable conditions, eight regions are divided according to



122 the method from Li et al. (2015). For each of the regions,  $\zeta$  is carried out by following:

$$123 \quad \zeta = Ri_B \frac{L_{0M}^2}{L_{0H}} \sum C_{ijk} \left( \frac{-Ri_B}{1-Ri_B} \right)^i L_{0M}^{-j} L_{0H}^{-k}. \quad (7)$$

124 Where  $C_{ijk}$  is seen in Table 2 (Li et al., 2016), and  $i = 0, 1$ ;  $j, k = 0, 1, 2, 3$ ;  $i + j + k \leq 4$ .

125 3. Universal function. It is also a key factor in flux calculation. The form of universal function is adopted from CB05  
 126 (Chenge and Brutsaert, 2005) under the stable condition (Eqs. (8a), (8b)) and Paulson70 (Paulson, 1970) under the  
 127 unstable condition (Eqs. (9a), (9b)):

$$128 \quad \psi_M(\zeta) = -a \ln \left[ \zeta + (1 + \zeta^b)^{\frac{1}{b}} \right], \quad \zeta > 0 \text{ (stable)}, \quad (8a)$$

$$129 \quad \psi_H(\zeta) = -c \ln \left[ \zeta + (1 + \zeta^d)^{\frac{1}{d}} \right], \quad \zeta > 0 \text{ (stable)}, \quad (8b)$$

$$130 \quad \psi_M(\zeta) = 2 \ln \frac{1+x}{2} + \ln \frac{1+x^2}{2} - 2 \arctan(x) + \frac{\pi}{2}, \quad \zeta < 0 \text{ (unstable)}, \quad (9a)$$

$$131 \quad \psi_H(\zeta) = 2 \ln \frac{1+y}{2}, \quad \zeta < 0 \text{ (unstable)}. \quad (9b)$$

132 Where  $a = 6.1$ ,  $b = 2.5$ ,  $c = 5.3$ ,  $d = 1.1$ ,  $x = (1 - 16\zeta)^{1/4}$ ,  $y = (1 - 16\zeta)^{1/2}$ .

133 In addition, the RSL effect is taken into account in the Li scheme. In the RSL, turbulence is strongly affected by  
 134 individual roughness elements, and the standard MOST is no longer valid (Simpson et al., 1998). Therefore, it is  
 135 necessary to consider the RSL effect in the calculation of turbulent fluxes, especially for the rough terrain such as forest  
 136 or large cities. Ridder (2010) proposed the expression of  $\psi_M^*$  and  $\psi_H^*$ :

$$137 \quad \psi_M^* \left( \zeta, \frac{z}{z_*} \right) = \phi_M \left[ \left( 1 + \frac{v}{\mu_M z / z_*} \right) \zeta \right]^{\frac{1}{\lambda}} \ln \left( 1 + \frac{\lambda}{\mu_M z / z_*} \right) e^{-\mu_M z / z_*} \text{ and} \quad (10a)$$

$$138 \quad \psi_H^* \left( \zeta, \frac{z}{z_*} \right) = \phi_H \left[ \left( 1 + \frac{v}{\mu_H z / z_*} \right) \zeta \right]^{\frac{1}{\lambda}} \ln \left( 1 + \frac{\lambda}{\mu_H z / z_*} \right) e^{-\mu_H z / z_*}. \quad (10b)$$

139 Where  $v = 0.5$ ,  $\mu_M = 2.59$ ,  $\mu_H = 0.95$ ,  $z_* = 16.7 z_{0m}$ ,  $\lambda = 1.5$ .  $\phi_M$  and  $\phi_H$  are universal functions before  
 140 integration. Here, set  $\chi_M = 1 + \frac{v}{\mu_M z / z_*}$ ,  $\chi_H = 1 + \frac{v}{\mu_H z / z_*}$ :

$$141 \quad \phi_M(\chi_M \zeta) = 1 + a \frac{\chi_M \zeta + (\chi_M \zeta)^b [1 + (\chi_M \zeta)^b]^{\frac{1-b}{b}}}{\chi_M \zeta + [1 + (\chi_M \zeta)^b]^{\frac{1}{b}}}, \quad \zeta > 0 \text{ (stable)}, \quad (11a)$$

$$142 \quad \phi_H(\chi_H \zeta) = 1 + c \frac{\chi_H \zeta + (\chi_H \zeta)^d [1 + (\chi_H \zeta)^d]^{\frac{1-d}{d}}}{\chi_H \zeta + [1 + (\chi_H \zeta)^d]^{\frac{1}{d}}}, \quad \zeta > 0 \text{ (stable)}, \quad (11b)$$

$$143 \quad \phi_M(\chi_M \zeta) = (1 - 16\chi_M \zeta)^{-1/4}, \quad \zeta < 0 \text{ (unstable)}, \quad (12a)$$

$$144 \quad \phi_H(\chi_H \zeta) = (1 - 16\chi_H \zeta)^{-1/2}, \quad \zeta < 0 \text{ (unstable)}. \quad (12b)$$

145 The Li scheme is summarized as: firstly determine  $Ri_B$ ,  $z_{0m}$  and  $z_{0h}$  according to the observation data, and then  
 146 calculate  $\zeta$  with  $Ri_B$ ,  $z_{0m}$  and  $z_{0h}$ . Finally carry out the momentum and sensible heat fluxes under different stratification  
 147 conditions.



### 148 2.3 The MM5 scheme

149 In this scheme, no distinction is made between  $z_{0m}$  and  $z_{0h}$ , thus we express the roughness length with  $z_0$ . Under the  
 150 unstable condition, take Paulson70 with Eqs. (16a) and (16b), and under the stable condition, the atmospheric stratification  
 151 conditions are subdivided into three cases according to Zhang and Anthes (1982). In addition, this scheme does not consider  
 152 the RSL effect.

153 (1) Strongly stable condition ( $Ri_B \geq 0.2$ ):

$$154 \quad \psi_M = \psi_H = -10 \ln \frac{z}{z_0}. \quad (13)$$

155 (2) Weakly stable condition ( $0 < Ri_B < 0.2$ ):

$$156 \quad \psi_M = \psi_H = -5 \left( \frac{Ri_B}{1.1 - 5Ri_B} \right) \ln \frac{z}{z_0}. \quad (14)$$

157 (3) Neutral condition ( $Ri_B = 0$ ):

$$158 \quad \psi_M = \psi_H = 0. \quad (15)$$

159 (4) Unstable condition ( $Ri_B < 0$ ):

$$160 \quad \psi_M = 2 \ln \frac{1+x}{2} + \ln \frac{1+x^2}{2} - 2 \arctan(x) + \frac{\pi}{2}, \quad (16a)$$

$$161 \quad \psi_H = 2 \ln \frac{1+y}{2}, \quad (16b)$$

162 where  $x = (1 - 16\zeta)^{1/4}$ ,  $y = (1 - 16\zeta)^{1/2}$ .

163 This scheme calculates turbulent fluxes of the momentum and sensible heat with  $u_*$  and  $\theta_*$ . In order to avoid the  
 164 difference of  $u_*$  before and after is too large,  $u_*$  is arithmetically averaged with its previous value with Eq. (17), and a  
 165 lower limit of  $u_* = 0.1\text{m/s}$  is imposed in order to prevent the heat flux from being zero under very stable conditions.  
 166 According to the profile functions of wind and temperature near the ground,  $\theta_*$  then is deduced by Eq. (18).

$$167 \quad u_* = \frac{1}{2} \left( u_* + \frac{ku}{\ln \frac{z}{z_{0m}} - \psi_M} \right), \quad (17)$$

$$168 \quad \theta_* = \frac{k(\theta - \theta_g)}{R[\ln \frac{z}{z_{0h}} - \psi_H]}. \quad (18)$$

169 Overall, the universal functions in different conditions are determined by  $Ri_B$  and  $z_0$ . Then  $u_*$  and  $\theta_*$  will be  
 170 calculated with meteorological data and flux data. At last, the turbulent fluxes are derived by Eqs. (1a) and (1b).

### 171 3 Observational data and methods

172 The observational data was from Gucheng station (GC), which is in China Atmosphere Watch Network (CAWNET) and  
 173 located in the southwest of Beijing about 110km, at 115.40 °E, 39.08 °N. In winter, the station surface was covered with  
 174 wheat and the surrounding areas were mainly farmland and scattered villages (Fig. 1). The eddy correlation flux  
 175 measurement system is mainly composed of a three-dimensional (3D) Temperature measurement with a sonic anemometer



176 (CSAT3) and a fast response infrared gas analyzer (LI-7500) at 4m height. The data was collected from December 1, 2016 to  
177 January 9, 2017 including momentum fluxes, heat fluxes, wind speed and wind direction, air temperature, density of air and  
178 vapor, pressure with 30 minutes interval. Besides, there were radiation data provided by the net radiation sensor (CNR1)  
179 including the surface upward long wave radiation and the long wave radiation incident to the ground surface and PM<sub>2.5</sub> data  
180 provided by the Environmental Protection Station of China's Ministry of Environmental Protection (EPS/CMEP).

### 181 3.1 Data processing

182 In order to obtain accurate flux data, it needs quality control of the observational data, including eliminated the outliers  
183 and the data in rainy days, as well as correcting momentum by using a double axis rotation for the sonic anemometer tilt  
184 correction and correcting sensible heat fluxes by modifying sonic virtual temperature. In addition, we considered the effect  
185 of wind field on the roughness length. Fig. 2 shows distribution frequency of wind speed and wind direction at GC during  
186 observations (December 1, 2016 ~ January 9, 2017). The wind speed is stable during this period and the maximum is no  
187 more than 5m and most of them are about 1 ~ 2m/ s. The wind direction is relatively uniform except for the southeast wind  
188 (135 degrees). Therefore, to avoid the measurement error of the instrument, the wind speed data less than 0.5m/s are  
189 eliminated.

### 190 3.2 Determination of surface skin temperature

191 The surface skin temperature error caused by the CSAT3 is too large to be taken to calculate the flux as input. Therefore,  
192 the surface skin temperature is calculated from the radiation data detected by the CNR1 as:

$$193 R_{lw}^{\uparrow} = (1 - \varepsilon_s)R_{lw}^{\downarrow} + \varepsilon_s\sigma T_g^4, \quad (19)$$

194 where  $R_{lw}^{\uparrow}$  and  $R_{lw}^{\downarrow}$  are the surface upward longwave radiation and long wave radiation incident on the surface,  
195 respectively.  $\sigma$  is the Stephen Boltzmann constant,  $\sigma = 5.67 \times 10^{-8} \text{Wm}^{-2}\text{K}^{-4}$ .  $T_g$  is the surface skin temperature,  $\varepsilon_s$  is  
196 the surface emissivity which is the basis for calculating  $T_g$ . Many researches estimated  $\varepsilon_s$  and the range of the values is  
197 always 0.9 ~ 1 (Stewart et al., 1994; Verhoef et al., 1997). According to the semi-empirical method in Yang et al. (2008),  $\varepsilon_s$   
198 is estimated when the RMSE is minimal. In this paper, the Li and MM5 schemes were used to estimate the  $\varepsilon_s$  value (as  
199 shown in Fig. 3). It is clear that the  $\varepsilon_s$  value corresponding the minimum RMSE is not very sensitive to the choice of two  
200 schemes. When  $\varepsilon_s$  is 1, the RMSE has the minimum value. Thus, we take 1 as the optimal value of  $\varepsilon_s$  to calculate  $T_g$   
201 value.

## 202 4 Results and discussion

203 The concept of roughness and its influence on the calculation of turbulent flux are going to be described in detail, and  
204 then the value of  $z_{0m}$  and  $z_{0h}$  will be determined by theories above. Using  $z_{0m}$ ,  $z_{0h}$  and related observational data, we



205 will have offline tests on Li and MM5. Finally, the behavior of two schemes will be compared in a severe haze pollution at  
206 GC.

#### 207 4.1 The influence of roughness length on the calculation of turbulent flux

208  $z_{0m}$  is defined as a height at which the extrapolated wind speed following the similarity theory vanishes. It is mainly  
209 determined by land-cover type and canopy height after excluding large obstructions. In models,  $z_{0m}$  is always based on a  
210 look-up table which is related to land-cover type. In this paper,  $z_{0m}$  is simply classified based on the research of Stull (1988)  
211 and is listed in Table 1. It can be seen that the more rough land surface is, the higher value of  $z_{0m}$  is. Thus, different  
212 land-cover types have different effects on flux calculation.  $z_{0h}$  is a height at which the extrapolated air temperature is  
213 identical to the surface skin temperature, and it is also a scalar quantity. Some early researches assumed that  $z_{0m}$  was equal  
214 to  $z_{0h}$  (Louis, 1979; Louis et al., 1982). However, the assumption is not applicable in reality because  $z_{0m}$  and  $z_{0h}$  have  
215 different physical meanings. Thus, many following studies modified this assumption and made it more reliable in the  
216 situation that  $z_{0m}$  was not equal to  $z_{0h}$  or the difference between two values was much large (e.g., Song, 1998; Wouters et  
217 al., 2012; Li et al., 2014; Li et al., 2015).

218 With the Li scheme, we test the effect of the roughness length on flux calculation. In the process, take  $z = 10\text{m}$  as the  
219 reference height and set the range of  $Ri_B$  according to Louis82 (Louis et al., 1982) from -2 to 1. Firstly, discuss the effect of  
220  $z_{0m}$  on flux calculation. Set  $\frac{z_{0m}}{z_{0h}} = 1$ , corresponding to four cases:  $z_{0m} = 1, 0.5, 0.05, 0.001\text{m}$ . These cases correspond to  
221 large cities, forests, agricultural fields and wide water surface, respectively. Fig. 4 gives the relationship between  $C_M(C_H)$   
222 and  $Ri_B$  for different  $z_{0m}$  values. The effects of different land-cover types on  $C_M$  and  $C_H$  are significant under both the  
223 stable atmosphere ( $Ri_B > 0$ ) and the unstable atmosphere ( $Ri_B < 0$ ). The rougher the surface is (corresponding the larger  
224  $z_{0m}$  value), the larger the calculated momentum or sensible heat flux is. In addition, there is a corresponding relationship  
225 between  $C_M(C_H)$  and stability. The more unstable the atmosphere is, the larger difference the value of  $C_M(C_H)$  is  
226 and vice versa. Once the value of  $Ri_B$  exceeds the critical value (generally 0.2-0.25), the transfer coefficients decline  
227 sharply but above 0.

228 Secondly, discuss the effect of difference between  $z_{0m}$  and  $z_{0h}$  on flux calculation. The relationship between  $z_{0m}$   
229 and  $z_{0h}$  can be expressed as  $kB^{-1} = \ln \frac{z_{0m}}{z_{0h}}$ . Over the sea,  $z_{0m}$  is comparable to  $z_{0h}$ ; over the uniform vegetation surface  
230 (e.g., grassland, farmland, woodland),  $kB^{-1}$  is about 2 ( $z_{0m}/z_{0h} \approx 10$ ) (Garratt and Hicks, 1973; Garratt, 1978; Garratt and  
231 Francey, 1978); over the surface with bluff roughness elements, the  $\frac{z_{0m}}{z_{0h}}$  value may be very large. For example, in some  
232 large cities,  $kB^{-1}$  can reach 30 ( $z_{0m}/z_{0h} \approx 10^{13}$ ) (Sugawara and Narita, 2009). Therefore, the  $\frac{z_{0m}}{z_{0h}}$  value can varies over a  
233 wide range. Fig. 5 shows the relationship between  $C_M(C_H)$  and  $Ri_B$  for different  $\frac{z_{0m}}{z_{0h}}$  values. Set  $z_{0m} = 1, z_{0h} = 1, 0.01,$





234  $10^{-4}$ ,  $10^{-6}$ m, and The large difference derived from the different ratios in Fig. 5. The larger the ratio is, the slower  $C_M(C_H)$   
235 fails with a rising stability. These results show that distinguishing between  $z_{0m}$  and  $z_{0h}$  has great impact on flux  
236 calculation which is closely related to severe haze pollution. Ignoring the difference between the two may lead to large errors  
237 in flux calculation and finally in air quality modeling.

#### 238 4.2 The determination of roughness length $z_{0m}$ ( $z_{0h}$ )

239 Based on above description and discussion, it can be seen that the determination of the appropriate value of  $z_{0m}$  ( $z_{0h}$ )  
240 is a key and basis for calculation of surface turbulent fluxes. Using observational flux data with quality control,  $z_{0m}$  and  
241  $z_{0h}$  are derived by Eq. (20a) and (20b) following Yang et al. (2003) and Sicart et al. (2014).

$$242 \frac{u_*}{u} = \frac{k}{\ln \frac{z}{z_{0m}} - \psi_M}, \quad (20a)$$

$$243 \frac{\theta_*}{(\theta - \theta_g)} = \frac{k}{R[\ln \frac{z}{z_{0h}} - \psi_H]}. \quad (20b)$$

244 During the observation period, the crops stopped growing and the height did not exceed 0.1 m, so the zero-plane  
245 displacement height can be ignored. The observation time is too short (about 1 month) to consider the effect of seasonal  
246 variations on roughness. Thus, assume  $z_{0m}$  and  $z_{0h}$  are two fixed values. Given the observational data, a dataset of  $z_{0m}$   
247 ( $z_{0h}$ ) then is generated. Finally take median of the dataset as typical values of  $z_{0m}$  and  $z_{0h}$  for GC site:  $z_{0m} = 0.0419$ m,  
248  $z_{0h} = 0.0042$ m. These results are comparable to the typical values for agricultural fields ( $z_{0m} = 0.05$ ,  $z_{0m}/z_{0h} = 10$ )  
249 discussed above. Therefore, the results are considered credible.

#### 250 4.3 Comparison of two schemes for calculating momentum and sensible heat flux

251 Using the calculated roughness length and the relative observations, the Li and MM5 schemes are going to be tested  
252 offline to compare their calculations of the momentum and sensible heat flux (Fig. 6). Firstly, take  $z_{0m} = 0.0419$  and  
253  $z_{0h} = 0.0042$  in the Li scheme,  $z_0 = z_{0m} = 0.0419$  in the MM5 scheme to calculate the momentum and sensible heat  
254 fluxes and the comparison results are shown in Figs. 6a and 6b. Compared with MM5, Li performs better with higher  
255 regression coefficient and determination coefficient. For momentum fluxes, the regression coefficient in Li is 0.6795 and that  
256 in MM5 is 0.5598, indicating that the error of Li is 12% lower than that of MM5. For sensible heat fluxes, the regression  
257 coefficient in Li is 0.7967 and that in MM5 is 1.7994. The latter is much larger than 1 which says the MM5 scheme  
258 overestimate a lot. That is due to no distinction of roughness length in the MM5 scheme. In order to compare the difference  
259 of two schemes without considering the effect of roughness length, take  $z_0 = z_{0h} = 0.0042$  in the MM5 scheme to  
260 calculate the sensible heat fluxes as Fig. 6c. Compared with Fig. 6b, there is a great improvement after modifying  $z_0$  value  
261 that the regression coefficient in MM5 becomes 0.7363, which is indicated that the error of calculated sensible heat flux by  
262 MM5 was reduced by 54% after discriminating  $z_{0h}$  from  $z_{0m}$ . However, the error in Li is still 5% lower than that in MM5.



263 This illustrates that in addition to the effect of roughness length, the Li scheme itself (including the selection of universal  
264 functions and the consideration of the RSL effect) is more reasonable than the MM5 scheme.

#### 265 4.4 The specific performance of the two scheme in severe haze pollution

266 There were two obvious pollution processes during this observation period and one occurred during December 13 to 23,  
267 2016. Fig. 7 shows the time series of  $PM_{2.5}$  as well as the momentum fluxes and sensible heat fluxes both for calculation and  
268 observation in this pollution episode. For the research purpose significance, only the variation of above variables in the  
269 daytime (set from 8:00 a.m. to 20:00 p.m.) is taken into account. All analysis data are processed as hourly average. It needs  
270 to note that in MM5, take 0.0419 of  $z_0$  when calculate momentum fluxes and take 0.0042 of  $z_0$  when calculate sensible  
271 heat fluxes. As shown in Fig. 7, on the whole, the calculated results of momentum and sensible heat fluxes for the two  
272 schemes are consistent with the trend of the observed data. Specifically, for the momentum fluxes (Fig. 7a), when the  
273 observed momentum fluxes are large, the calculated results of the two schemes have little difference. When the observed  
274 momentum fluxes are small, the Li scheme results are close to or less than the observations, while the MM5 scheme results  
275 are always higher than observations because of the limit of  $u_* = 0.1$ . For the sensible heat fluxes (Fig. 7b), MM5 results are  
276 always lower than observations while Li results are closer to observations especially when the observed values are small.

277 Fig. 7 also shows the diurnal variation of  $PM_{2.5}$  during this process. According to the evolution characteristics of fluxes  
278 and  $PM_{2.5}$  concentration, the process is then divided into three stages: the no pollution stage (stage 1: 13~14), the  
279 accumulation stage (stage 2: 16~18) and the maintenance stage (stage 3: 21~22) to discuss and evaluate the two schemes. As  
280 shown in Fig. 7, before the pollution occurs (stage 1), the atmospheric stratification is unstable,  $PM_{2.5}$  concentration is low  
281 and there is a strong flux transport in the SL, the corresponding observations of the momentum and sensible heat flux are  
282 relatively high and the daily change of them is also great. In the accumulation stage (stage 2), the atmosphere is changing  
283 from unstable to stable corresponding with hazes formation, the momentum and sensible heat fluxes gradually decreases and  
284 the daily variation also decreases. In the maintenance stage, the atmospheric stratification is very stable, and flux transport in  
285 the SL is weak, both the momentum and sensible heat fluxes are at a low level.

286 Fig. 8 shows the probability distribution functions (PDF) of the difference of momentum (Figs. 8a, 8c, 8e, 8g) and  
287 sensible heat fluxes (Figs. 8b, 8d, 8f, 8h) calculated by using Li and MM5 schemes from the observations in different stages.  
288 In the whole pollution process, for momentum fluxes (Fig. 8a), compared with MM5, the distribution of bias from the Li  
289 scheme tends to cluster in a narrower range centered by 0, and the probability of Li bias within  $\pm 0.005N\ m^{-2}$  is 46.82%. The  
290 probability of MM5 bias within this range fall to 23.02%. For sensible heat fluxes (Fig. 8b), the distribution of bias from Li  
291 is still more concentrated around 0 than it is from MM5. The probabilities of Li and MM5 bias within  $\pm 2.5W\ m^{-2}$  are 32.54%  
292 and 13.49%, respectively. In stage 1, for momentum fluxes (Fig. 8c), the probability of Li bias within  $\pm 0.005N\ m^{-2}$  is 38.09%.  
293 The probability distribution of MM5 bias focus on area larger than 0, and its probability within  $\pm 0.005N\ m^{-2}$  is 14.29%. For



294 sensible heat fluxes (Fig. 8d), the probability of Li bias within  $\pm 2.5 \text{ W m}^{-2}$  is 38.09%, the same as momentum fluxes. The  
295 probability distribution of MM5 bias focus on area less than 0, and its probability within  $\pm 2.5 \text{ W m}^{-2}$  is 9.52%. In stage 2, the  
296 difference between the schemes is more obvious. The momentum and sensible heat fluxes bias from Li is the most  
297 concentrated around 0 in all cases, while the distribution of MM5 bias is similar to that in stage 1. Specifically, for  
298 momentum fluxes (Fig. 8e), the probabilities of Li bias and MM5 bias within  $\pm 0.005 \text{ N m}^{-2}$  are 56.25% and 25.00%. For  
299 sensible heat fluxes (Fig. 8f), the probabilities of Li bias and MM5 bias within  $\pm 2.5 \text{ W m}^{-2}$  are 40.62% and 6.25%. In stage 3,  
300 the difference between two schemes is small. For momentum fluxes (Fig. 8g), the probabilities of Li bias and MM5 bias  
301 within  $\pm 0.005 \text{ N m}^{-2}$  are 22.73% and 27.27%. For sensible heat fluxes (Fig. 8h), the probabilities of Li bias and MM5 bias  
302 within  $\pm 2.5 \text{ W m}^{-2}$  are both 36.36%.

303 Four common evaluation metrics were used to further test the abilities of the Li and MM5 schemes in calculating fluxes  
304 (Table 2). They are the mean bias (MB), normalized mean bias (NMB), normalized mean error (NME) and root mean square  
305 error (RMES). Table 2 shows that the Li scheme generally gives a better estimate than the MM5 scheme. In whole process,  
306 the momentum fluxes calculated by Li is underestimated by 3.63% relative to the observations, while the results calculated  
307 by MM5 is overestimated by 34.03%. The sensible heat fluxes calculated by Li and MM5 are both underestimated and the  
308 underestimations are 15.69% and 50.22%. In three selected stages, the Li scheme performs better than the MM5 scheme in  
309 first two stages. Especially in stage 2, that is, the atmosphere transforming from unstable to stable stratification, the  
310 difference between the Li and MM5 schemes are particularly significant. Both the Li and MM5 schemes have overestimates  
311 for momentum fluxes and the values are 7.68% and 45.56, respectively. Two schemes have underestimates for sensible heat  
312 fluxes and the values are 33.84% and 76.88%. It can be seen the Li scheme calculation error is much smaller than the MM5  
313 scheme error. This stage plays an important role in the generation and accumulation of pollutants. How to simulate the  
314 atmospheric state in a more reasonable way is also a critical issue for air pollution modeling. Therefore, the superiority of the  
315 Li scheme in the air pollution process, especially in this stage is of great reference value for improving the forecast of  
316 pollutant concentration in the current air quality model. In stage 3, the difference between the two schemes is not obvious.

## 317 5 Conclusions

318 The applicability in describing the atmospheric stratification related with severe haze in east China of the Li and MM5  
319 schemes are evaluated and discussed. The observed momentum and sensible heat fluxes, together with conventional  
320 meteorological data from December 1, 2016 to January 9, 2017, including a severe pollution episode from December 13 to  
321 23, are used to do that. The transitional stage of atmospheric stratification from unstable to stable, corresponding to  
322 accumulation of  $\text{PM}_{2.5}$ , is mainly discussed in this paper. The contributions of roughness lengths ( $z_{0m}$  and  $z_{0h}$ ) as well as  
323 the algorithms of the momentum and sensible heat flux calculation are discussed. The results are summarized as follows:



324 1)  $z_{0m}$  and  $z_{0h}$  have important effects on turbulent flux calculation.  $z_{0m}$  and  $\frac{z_{0m}}{z_{0h}}$  both reflect the condition of  
325 underlying surface and impact flux calculation greatly. Under the same condition, the larger  $z_{0m}$  (indicating rougher  
326 surface) is, the larger the calculated fluxes are. The fluxes over large cities ( $z_{0m} = 1$ ) is quite different from those over  
327 agricultural fields ( $z_{0m} = 0.05$ , similar to the value at GC). When  $z_{0m}$  is larger, the value of  $\frac{z_{0m}}{z_{0h}}$  should be larger, and  
328 the larger the value of  $\frac{z_{0m}}{z_{0h}}$  is, the greater the differences of calculated fluxes are. Especially, for a super city like  
329 Beijing, the value of  $\frac{z_{0m}}{z_{0h}}$  may be much larger than  $10^6$  and ignoring the difference between  $z_{0m}$  and  $z_{0h}$  may lead to  
330 much uncertainties in flux calculation. It is very necessary to distinguish between  $z_{0m}$  and  $z_{0h}$  in SL scheme, which  
331 is probably beneficial to improve simulation of regional atmosphere stratification over urban agglomeration with rough  
332 surface and then  $PM_{2.5}$  during hazes.

333 2) It could be seen from the regression coefficients and determination coefficients between calculated fluxes by the two  
334 schemes and observed fluxes of 40 days that the Li scheme was better than the MM5 scheme in general. For the  
335 momentum fluxes, the determination coefficients of Li and MM5 was about 0.41 and 0.40. Both schemes passed the  
336 significance level of 99.9%. The regression coefficient of Li was 0.68, and it generally reduced the error by 12%  
337 compared with MM5. When  $z_{0m}$  and  $z_{0h}$  took the same value ( $z_0 = z_{0m} = 0.0419$ ) in MM5, the sensible heat fluxes  
338 were obvious overestimated. When  $z_{0h}$  was taken into account ( $z_0 = z_{0h} = 0.0042$ ) in MM5, the calculated fluxes  
339 were significant improved and the error was reduced by 54%. However, this error was still higher about 5% compared  
340 with the Li scheme, illustrating that apart from the impact of roughness length, the different algorithms of the two  
341 schemes also achieves obvious differences in calculated fluxes.

342 3) During the heavy pollution process, the calculated momentum and sensible heat fluxes by the Li scheme were better  
343 than those by the MM5 scheme generally. Especially in the  $PM_{2.5}$  accumulated stage, the advantages of Li were more  
344 prominent. Compared with MM5, the probability distributions of both the momentum and sensible heat flux bias of Li  
345 tended to cluster in a narrower range centered by 0. The calculated momentum fluxes by Li were overestimated by 7.68%  
346 and this overestimation by MM5 was up to 45.56%. The calculated sensible heat fluxes by Li were underestimated by  
347 33.84% while this underestimation by MM5 was even up to 76.88%.

348 The offline study in this paper showed that Li scheme was superior to the MM5 scheme in general. This superiority was  
349 even more remarkable during the atmosphere transforming stage from unstable to stable stratification. However, the  
350 comparison of the two schemes focusing on more underlying surfaces (e.g., super cities and agricultural fields) could not be  
351 conducted at present due to the shortage of observed fluxes data, which should be discussed in detail in next paper when the  
352 sufficient data is available. The offline results of this paper only offer a basic and a possible way to improve PBL diffusion  
353 simulation and then  $PM_{2.5}$  prediction, which will be achieved in the follow-up work of online integrating of the Li scheme



354 into the atmosphere chemical model.

### 355 Acknowledgments

356 The study was supported by National Key Project of HePAP. (JFYS2016ZY01002213), the National (Key) Basic  
357 Research and Development (973) Program of China (2014CB441201), National Key R & D Program Pilot Projects of China  
358 (2016YFC0203304)

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- 448



449 **Table 1.** Typical values of  $z_{0m}$  corresponding to various land-cover types

$z_{0m}/m$	Land-cover types
5~50	Mountain (above 100m)
1~5	The center of large cities, hills or mountain area
0.1~1	Forests, the center of large towns
0.01~0.1	Flat grasslands, agricultural fields
$10^{-4}$ ~ $10^{-3}$	The snow surface, wide water surface, flat deserts
$10^{-5}$	The ice surface

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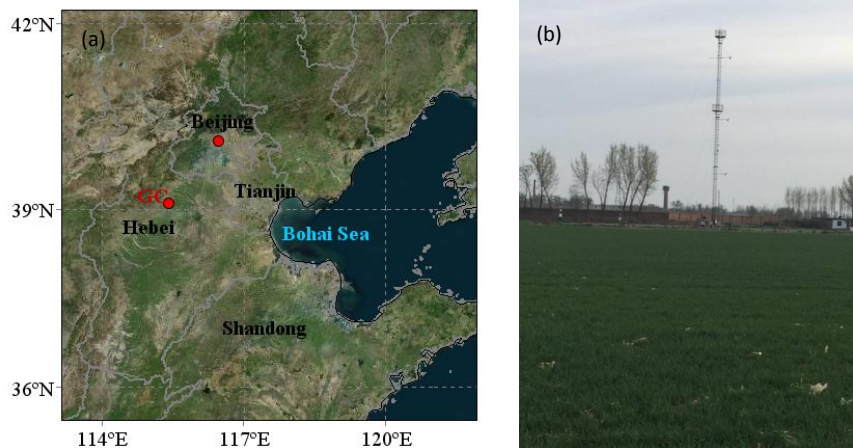
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453 **Table 2.** Statistics between the Li and MM5 schemes calculated turbulent flux.

		Li				MM5			
		MB	NMB	NME	RMSE	MB	NMB	NME	RMSE
Whole	$\tau$	-0.0006	-3.63%	54.29%	0.0142	0.0058	34.03%	63.59%	0.0143
process	H	-2.2723	-15.69%	52.73%	10.9649	-7.2735	-50.22%	69.68%	12.7946
Stage 1	$\tau$	0.0021	9.98%	55.90%	0.0172	0.0091	43.45%	66.66%	0.0169
	H	1.1775	5.79%	37.87%	10.5734	-7.1891	-35.34%	55.70%	13.1324
Stage 2	$\tau$	0.0013	7.68%	44.50%	0.0111	0.0079	45.56%	56.81%	0.0121
	H	-4.5752	-33.84%	50.28%	9.3995	-10.3924	-76.88%	81.40%	13.2553
Stage 3	$\tau$	-0.0024	-13.25%	59.13%	0.0144	0.0030	16.72%	56.34%	0.0138
	H	1.2818	11.39%	66.31%	11.4778	-1.7479	-15.52%	65.90%	10.4219

454 \*  $\tau$ : momentum flux; H: sensible heat flux; MB: mean bias; NMB: normalized mean bias; NME: normalized mean error;455 RMSE: root mean square error. The units of MB and RMSE:  $\mu\text{g} \cdot \text{m}^{-3}$ .

456



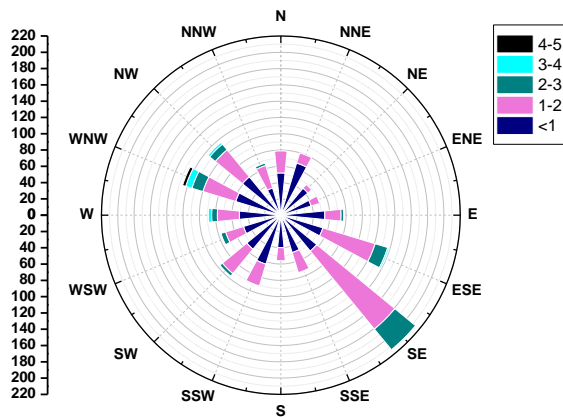
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458 **Figure 1.** Location (a) and geographical environment (b) at GC. The map is from Bing Maps.

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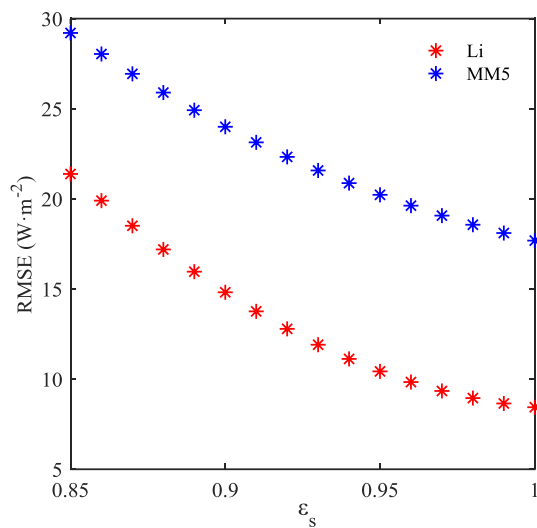
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463 **Figure 2.** Wind Rose map at GC from December 1, 2016 to January 9, 2017.

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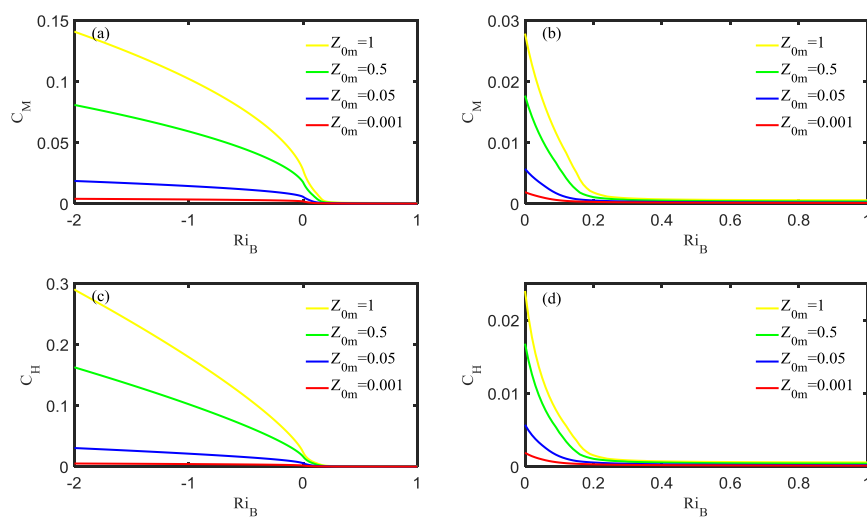
467

468 **Figure 3.** The surface emissivity  $\varepsilon_s$  dependence of RMSE between observed near-neutral heat fluxes and parameterized  
469 heat fluxes (red for Li and blue for MM5) at GC.

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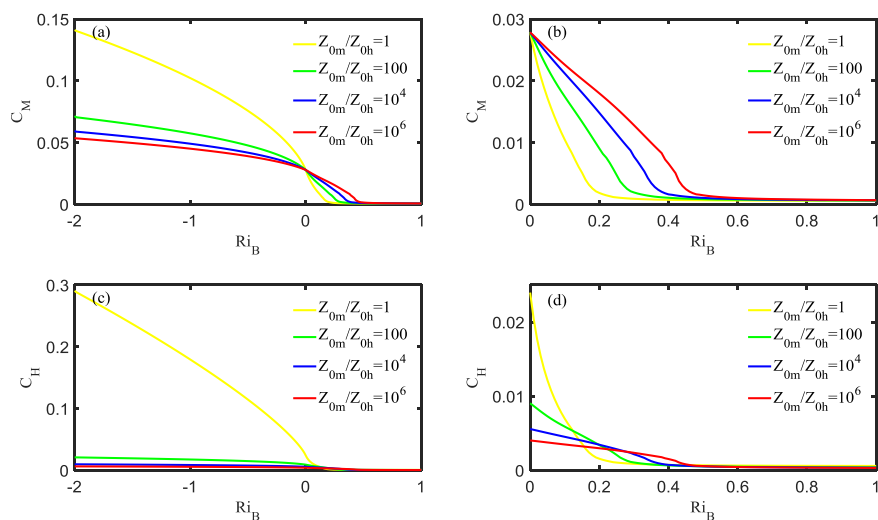
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473

474 **Figure 4.** The relationship between  $C_M(C_H)$  and  $Ri_B$  for different  $z_{0m}$  values.

475



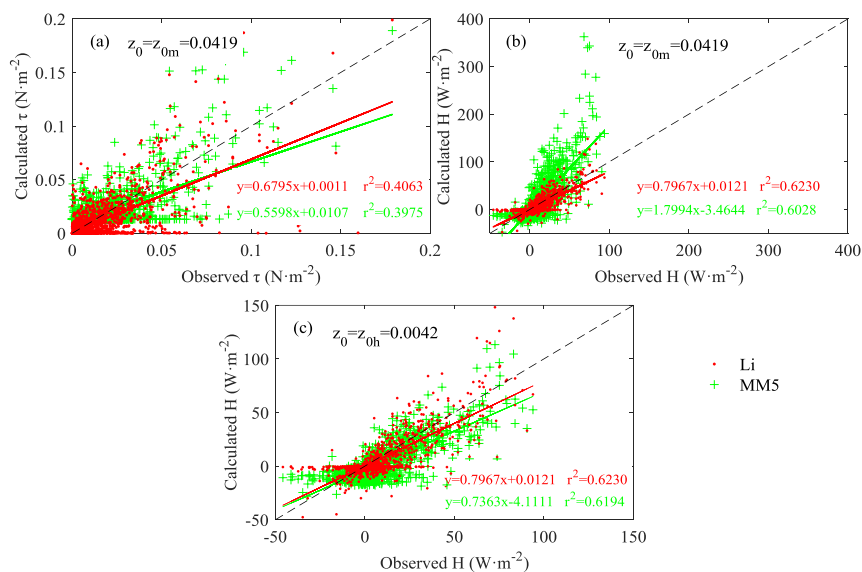
476

477 **Figure 5.** The relationship between  $C_M$  ( $C_H$ ) and  $Ri_B$  for different ratios of  $z_{0m}$  to  $z_{0h}$ .

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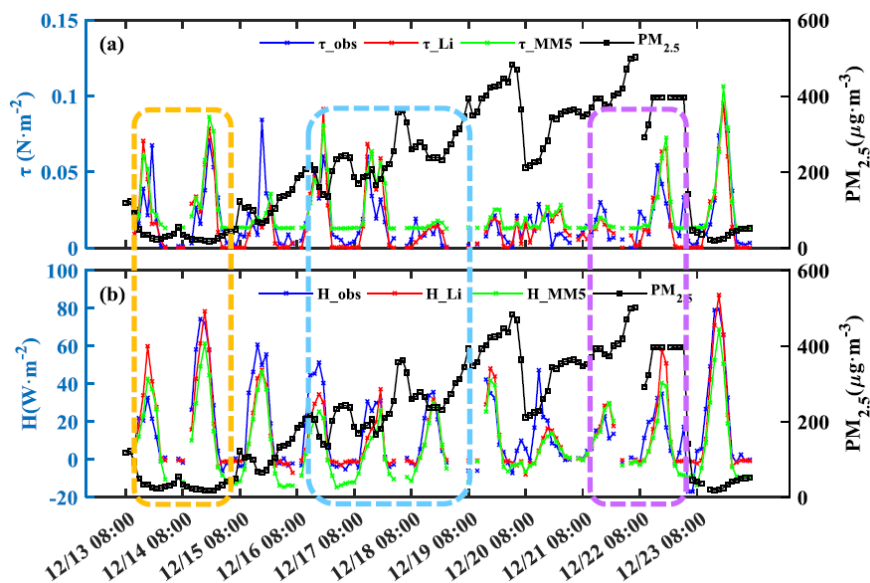
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481

482 **Figure 6.** Comparison of calculated and observed fluxes. (a) Momentum fluxes (MM5:  $z_0 = 0.0419$ ); (b) sensible heat  
483 fluxes (MM5:  $z_0 = 0.0419$ ); (c) sensible heat fluxes (MM5:  $z_0 = 0.0042$ ). Red dots: the Li scheme; green plus signs: the  
484 MM5 scheme.

485



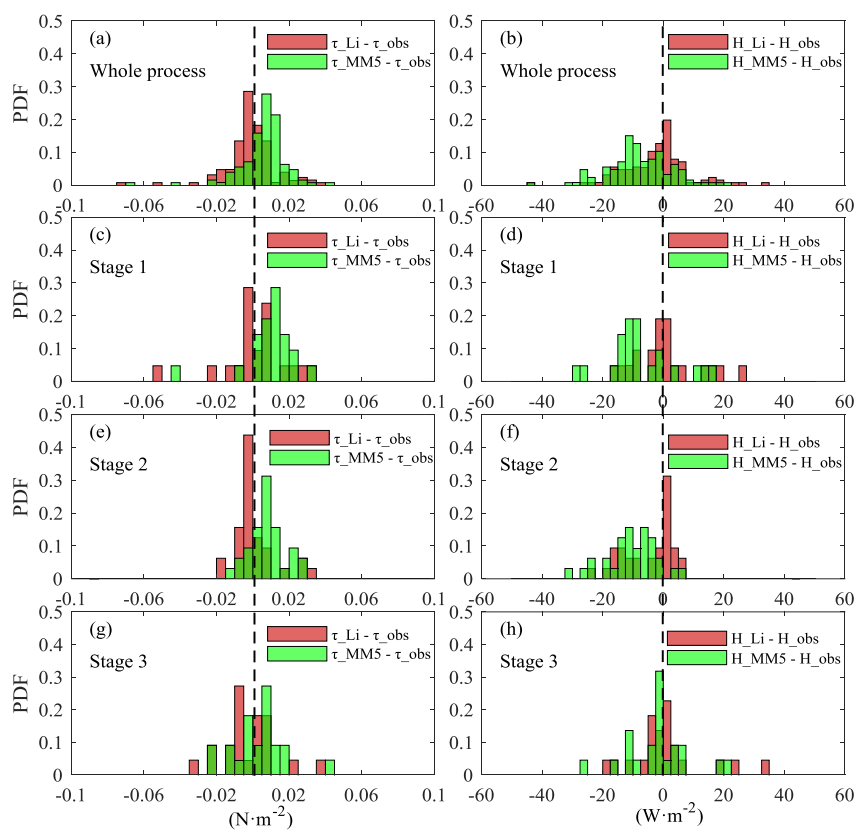
486

487 **Figure 7.** Variations of hourly turbulent fluxes and PM<sub>2.5</sub> at GC station in daytime. (a) Momentum fluxes  $\tau$  (blue line:  
488 observations; red line: the Li scheme; green line: the MM5 scheme) and PM<sub>2.5</sub> concentration (black line); (b) sensible heat  
489 fluxes  $H$  (the same as  $\tau$ ) and PM<sub>2.5</sub> concentration (black line). Yellow box: stage 1; blue box: stage 2; purple box: stage 3.

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493

494 **Figure 8.** Probability distribution functions (PDF) of the difference between calculated fluxes (momentum fluxes: left;  
495 sensible heat fluxes: right) by using two schemes (the Li scheme: red bars; the MM5 scheme: green bars) and observations in  
496 different stages (a-b: whole process; c-d: stage 1; e-f: stage 2; g-h: stage 3).

497