Our answers to reviewers are written in blue

Anonymous Referee #3

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This paper presents a new estimate of the shortwave direct radiative effect attributable to aerosols above clouds. The paper builds on the previous literature by advancing a technique that applies globally and utilizes the depolarization ratio method applied to global CALIOP observations. Use of the depolarization ratio method improves upon a widespread underestimate of aerosol optical thicknesses in the standard CALIOP retrieval products, but seems to struggle to capture cases of dust over clouds. The paper does a nice job of summarizing the studies that have come before, the variety of methods that have been applied to this problem, and the problems that hinder the precise quantification of the global radiative effect. The paper also does a nice job of placing their quantitative results in the context of other estimates. I have only some minor comments. After addressing these, the paper should be suitable for publication in ACP.

We thank the referee for their kind remarks and their very thorough reading of our lengthy manuscript.

1.a. AR#3: The analysis is restricted to clouds that are determined to be opaque, but the method by which opaque clouds are distinguished from clouds that are not opaque is not clear. In the appendix it is noted that the “CALIOP opacity flag” is used. There should be a brief mention in the body of the paper of the physical basis for the “opacity flag”.

Our answer: We now include this short description of the physical basis for the CALIOP opacity flag at the beginning of section 2.1:

“Because the CALIOP backscatter signal is totally attenuated below the lowest “feature” detected within any profile [Vaughan et al., 2009], this lowest feature is defined as being opaque. Approximately 69% of the time, the opaque feature detected in a profile is the Earth’s surface [Guzman et al., 2017]. In the remainder of the cases, the opaque feature is either a water cloud, an ice cloud, or, very rarely, an aerosol layer.” (…) “(1) only one cloud can be detected within a 5 km (15 shot) along-track average (…) and (2) this one cloud must be opaque (i.e., lowest feature detected in a column, and not subsequently classified as a surface return).”

1.b. AR#3: Are there particular regimes where low clouds are prevalent but transparent?

Our answer: Yes. As shown by Figure 5 in Leahy et al. [2012], while transparent low clouds occur globally, they are much more prevalent in the southern oceans and, to a lesser extent, in the northern Pacific.
1. c. AR#3: There is a vague reference to “clouds such as the ones reported in Leahy et al. (2012)” A more specific description would be better.

Our answer: Our revised description of the Leahy reference now reads as follows in section 2.1:

“However, because the DR retrieval technique requires backscatter measurements from opaque water clouds [Hu et al., 2007b], it cannot be used to retrieve AOD from aerosols lying above the low, transparent water clouds that are frequently observed over remote oceans, especially in the southern hemisphere (e.g., Leahy et al. [2012]; Mace and Protat [2018]; O et al. [2018]).”

2. AR#3: Figure 1 indicates that the Southern Ocean is the most prominent place on the globe for uniform single layer clouds, but panel b suggests that they are not suitable for the depolarization ratio method. Perhaps it is not of great importance if most of this region has little appreciable aerosol above the cloud layer. Nevertheless, I was left wondering why. Is it a quality of the clouds? Or merely a lack of aerosol optical thickness?

Our answer: Please see our response to the previous comment. The issue is the quality of the clouds; i.e., the clouds in the Southern Ocean are often transparent, and transparent clouds are not suitable for analysis using the DR method. We hope that the additional references (i.e., Mace and Protat [2018]; O et al. [2018]) will provide some further insights into the nature and causes of these geometrically and optically thin clouds.

3. AR#3: Panel d of figure 1 shows a substantial underestimate of cases of aerosol above cloud compared to a similar statistic based on the standard CALIOP aerosol optical thickness product for continents and for oceanic regions dominated by dust plumes. This is discussed in a couple of places in the manuscript, but nevertheless I remained confused as to the cause. The only indication in the body of the paper on line 316 where it says “. . .filtering out of ‘unobstructed’ but potentially aerosol-contaminated OWCs.” The paper does not make clear what “obstructed” or “unobstructed” means in this context or why such clouds would be filtered. This sentence is in dire need of some plain English.

Our answer: In response to the referee’s remark, we made numerous changes to the text in this paragraph. In particular, we replaced this sentence: “One reason for the lack of AAC cases offshore from the west coast of Africa in our dataset is the filtering out of “unobstructed” but potentially aerosol-contaminated OWCS (see section B3 in the appendix for more details)” with this more in-depth explanation: “The lack of AAC cases offshore from the southwest coast of Africa in the DR method dataset is the result of our conservative data filtering strategy. Because the IABs of aerosol-contaminated OWCS can differ significantly from those measured in pristine, aerosol-free conditions, OWCS suspected of being aerosol-contaminated (which are ubiquitous in this part of the world and very common over continents) are specifically excluded from our DR method analyses (see appendix section B3 for more details).”

4. AR#3: Another place where the description is so technical as to hide the point is in the discussion of the extinction-to-backscatter ratios in sections 3.2.2 and 3.2.3. My sense is that there is an important point in these sections and that differences in the probability distributions in figure 6 must be
significant. But it was not clear what that point is or what the significance to the main result of the paper is.

Our answer: This comment was particularly helpful to us. Thank you. The article under review is the result of many years of analysis. There was a time when this work was separated in two parts describing, on the one hand, our AAC aerosol optical depths (AOD) paired with CALIOP AAC extinction-to-backscatter values (S_AAC) and, on the other, the Direct Aerosol Radiative Effects above clouds (DARE_cloudy). The S_AAC values were there to illustrate the different aerosol types present above clouds.

Our ultimate goal in this paper now being the calculation of global DARE_cloudy, and knowing that S_AAC values are not needed in our calculation of DARE_cloudy, these S_AAC are more of a distraction to the reader. As a consequence, we have deleted section 3.2.2, 3.2.3, appendix B4 and all of its dependencies. We plan to publish these results separately.

5. AR#3: Minor point: In the sentence beginning in line 308 the authors state “...negative (positive) values in blue (red) show the number of AAC cases that are missed (gained)....” Way back in 2010 Prof. Robock pleaded with us to end this misuse of parentheses [Robock, A. (2010), Parentheses are (are not) for references and clarification (saving space), Eos Trans. AGU, 91(45), 419–419, doi:10.1029/2010EO450004]. My understanding is that one of the publishers in our field has specifically written it out of their style guide. I read pretty widely and the only genre of writing where I have experienced this application of parentheses is in the atmospheric sciences journals. I hope the authors will consider rewriting this sentence.

Our answer: We have re-written the sentence. Many thanks for the Robock reference.

Referee #2 Dr Abhay Devasthale

I will keep the review short and to the point. If not the lengthiest, it is one of the lengthiest manuscripts I have reviewed so far. So it took me some time to go through it few times and come to the grips of how the DARE_OWCs are actually computed. But once I started reading it carefully, it was easier to follow and understand. I appreciate the hidden efforts behind the work needed to bring onboard information from the suit of sensors. I also appreciate the way authors contrast and compare their results with the previous studies. Table 5 is a good idea and could be useful for evaluating models. As far as the methodology and results are concerned, I do not see anything that should raise a red flag.

Our answer: We thank Dr Devasthale for his kind words and thoughtful comments. We are pleased to announce that the manuscript will be shorter after deleting section 3.2.2, 3.2.3, appendix B4 and all of its dependencies (following one of reviewer #3’s comments).
I do however have one key concern as mentioned below. CALIOP offers two distinct advantages over passive sensors, namely its superiority in detecting aerosol layers and their precise altitudes. While the authors go to such a great length and detail to be as realistic and up-to-date in taking into account aerosol and cloud layers (and their properties) as possible, if I am not mistaken, the altitude of these layers is assumed to be constant globally. And I can’t help but wonder how this is going to affect their estimates, given the diversity in the verticality of aerosol and clouds in the AAC scenarios and its impact on DARE_OWCs. It is not even clear to me if only tropospheric aerosols were selected (maybe I missed reading it somewhere). I understand that the authors comment on this in Section 4.5, but I would really appreciate if the authors do a quick sensitivity study (e.g. maybe over one of the hot-spots) by incorporating realistic vertical distribution of aerosol and cloud layers, to be able to get an idea of the uncertainty.

We particularly appreciate Dr Devasthale’s comment on the impact of assumed aerosol and cloud vertical distribution on DARE_OWC. His suggestion has led us to substantially re-write and improve section 4.5. “assuming fixed aerosol and cloud vertical layers” to add more discussion of previous work on the subject. We are very grateful as we think this improves this section (and therefore our paper). As written in this section, multiple peer reviewed papers have emphasized the minimal impact of the height of the aerosols above clouds in the calculation of DARE_OWCs, as compared to the effect of changes in other parameters such as the AOD, SSA, or cloud albedo. For this reason we have not included any further sensitivity analysis varying the aerosol and cloud height in our calculations in the present work.

This is how section 4.5 reads now:

“Finally, Long Wave (LW) radiative forcing is particularly dependent on the vertical distribution of aerosols, especially for light absorbing aerosols [Chin et al., 2009]. This is because the energy these aerosols reradiate depends on the temperature, and hence their altitude. For example, Penner et al. [2003] emphasize the importance of soot and smoke aerosol injection height in LW TOA DARE\textsubscript{all-sky} (see Eq. 1) simulations (higher injection heights tend to enhance the negative LW radiative forcing). Quijano et al. [2000], Chung et al. [2005] and Chin et al. [2009] demonstrate the importance of an aerosol height, in relation to a cloud height (i.e., the aerosols located above, within or below the clouds) in an accurate estimation of SW TOA DARE\textsubscript{all-sky}. Chung et al. [2005], for example, show that varying the relative vertical distribution of aerosols and clouds leads to a range of global anthropogenic SW TOA DARE\textsubscript{all-sky} from -0.1 to -0.6 W m\textsuperscript{-2} (using a combination of MODIS satellite, AERONET ground-based observations and CTM simulations, see their Table 2).

However, here, we concentrate on cases of aerosol layers overlying clouds in order to compute SW TOA DARE\textsubscript{cloudy}. Aerosol and cloud layer heights are assumed constant over the globe in our study (see section 2.2). Future studies should incorporate mean gridded (i.e., 4ºx5º in this study)-seasonal CALIOP Level 2 aerosol and cloud vertical profiles into the calculation of DARE\textsubscript{OwC}. However, constraining clouds between 2 and 3km in our study does not seem unreasonable as our AAC AOD calculations using the DR method can only be applied to aerosols overlying specific low opaque water clouds with, among other criteria, an altitude below 3km (see Table B2). On the other hand,
constraining aerosols between 3 and 4km in our study is not realistic over many parts of the globe (e.g., see Fig. 7 of Devasthale et al. [2011]). For example, over the region of South East Atlantic during the ORACLES campaign, the HSRL team observed an aerosol layer located in average between 2 and 5km, and overlying a cloud at an average altitude of 1.2km. According to Zarzycki et al. [2010], the underlying cloud properties are orders of magnitude more crucial to the computation of DARE_{cloudy} than the location of the aerosol layer relative to the cloud, as long as the aerosol is above the cloud. In other words, the forcing does not seem to depend on the height of the aerosols above clouds as much as other parameters such as the AOD, SSA or cloud albedo. Zarzycki et al. [2010] investigated this assumption and found that over low and middle clouds, forcing changed by ~1-3% through the heights where the Black Carbon burden was the largest. These small changes in forcing are likely products of a change in atmospheric transmission above the aerosol layer [Haywood and Ramaswamy, 1998] (e.g., a change in the aerosol height linked to a change in the integrated column water vapor above the aerosol layer and this, in turn, would alter the incident solar radiation).”
Estimations of Global Shortwave Direct Aerosol Radiative Effects Above Opaque Water Clouds

Using a Combination of A-Train Satellite Sensors

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Abstract

All-sky Direct Aerosol Radiative Effects (DARE) play a significant yet still uncertain role in climate. This is partly due to poorly quantified radiative properties of Aerosol Above Clouds (AAC). We compute global estimates of short-wave top-of-atmosphere DARE over Opaque Water Clouds (OWC), DARE\textsubscript{OWC}, using observation-based aerosol and cloud radiative properties from a combination of A-Train satellite sensors and a radiative transfer model. There are three major differences between our DARE\textsubscript{OWC} calculations and previous studies: (1) we use the Depolarization Ratio method (DR) on CALIOP (Cloud Aerosol Lidar with Orthogonal Polarization) Level 1 measurements to compute the AAC frequencies of occurrence and the AAC Aerosol Optical Depths (AOD), thus introducing fewer uncertainties compared to using the CALIOP standard product; (2) we apply our calculations globally, instead of focusing exclusively on regional AAC “hotspots” such as the southeast Atlantic; and (3) instead of the traditional look-up table approach, we use a combination of satellite-based sensors to obtain AAC intensive radiative properties. Our results agree with previous findings on the dominant locations of AAC (South and North East Pacific, Tropical and South East Atlantic, northern Indian Ocean and North West Pacific), the season of maximum occurrence and aerosol optical depths (a majority in the 0.01-0.02 range and that can exceed 0.2 at 532 nm) over the globe. We find positive averages of global seasonal DARE\textsubscript{OWC} between 0.13 and 0.26 W\textsuperscript{-1}m\textsuperscript{2} (i.e., a warming effect on climate). Regional seasonal DARE\textsubscript{OWC} values range from -0.06 W\textsuperscript{-1}m\textsuperscript{2} in the Indian Ocean, offshore from western Australia (in March-April-May) to 2.87 W\textsuperscript{-1}m\textsuperscript{2} in the South East Atlantic (in September-October-November). High positive values are usually paired with high aerosol optical depths (>0.1) and...
low single scattering albedos (<0.94), representative of, e.g., biomass burning aerosols. Because we use different spatial domains, temporal periods, satellite sensors, detection methods, and/or associated uncertainties, the DARE\textsubscript{OWC} estimates in this study are not directly comparable to previous peer-reviewed results. Despite these differences, we emphasize that the DARE\textsubscript{OWC} estimates derived in this study are generally higher than previously reported. The primary reasons for our higher estimates are (i) the possible underestimate of the number of dust-dominated AAC cases in our study; (ii) our use of Level 1 CALIOP products (instead of CALIOP Level 2 products in previous studies) for the detection and quantification of AAC aerosol optical depths, which leads to larger estimates of AOD above OWC; and (iii) our use of gridded 4°x5° seasonal means of aerosol and cloud properties in our DARE\textsubscript{OWC} calculations instead of simultaneously derived aerosol and cloud properties from a combination of ATrain satellite sensors. Each of these areas is explored in depth with detailed discussions that explain both rationale for our specific approach and the subsequent ramifications for our DARE calculations.
ACRONYMS

AAC  Aerosol-Above-Clouds
AAOD  Absorption Aerosol Optical Depth
AOD  Aerosol Optical Depth
\(\tau_{\text{DR,AAC}}\)  Aerosol Optical Depth above clouds using the DR method
AeroCom  Aerosol Comparisons between Observations and Models
AERONET  AErosol RObotic NETwork
AMSR-E  Advanced Microwave Scanning Radiometer - Earth Observing System
ARCTAS  Arctic Research of the Composition of the Troposphere from Aircraft and Satellites
ASR  integrated Attenuated Scattering Ratio
BRDF  Bidirectional Reflectance Distribution Function
CAC  Clear Air above Cloud
CALIOP  Cloud Aerosol Lidar with Orthogonal Polarization
CALIPSO  Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observations
CERES  Clouds and the Earth's Radiant Energy System
CF  Cloud Fraction
CloudSat  NASA Earth observation satellite
COD  Cloud Optical Depth
CR      Color Ratio technique
DARE\textsubscript{all-sky}    Direct Aerosol Radiative Effect in all-sky conditions (cloudy and non-cloudy)
DARE\textsubscript{cloudy}    Direct Aerosol Radiative Effect in cloudy conditions
DARE\textsubscript{non-cloudy}    Direct Aerosol Radiative Effect in non-cloudy conditions (clear-skies)
DARE\textsubscript{OWC}    Direct Aerosol Radiative Effect above opaque water clouds
DISORT    DIScrete ORdinate Radiative Transfer solvers
DR      Depolarization Ratio technique
\(\delta\textsubscript{OWC}\)    layer-integrated volume depolarization ratio
\(f\textsubscript{AAC}\)    AAC frequency of occurrence
HSRL     High Spectral Resolution Lidar
IAB      Integrated Attenuated Backscatter
IBS      Integrated aerosol Backscatter
InWA     Indian ocean, offshore from West Australia
LUT      Look Up Table
LWP      Liquid Water Path
MBL      Marine Boundary Layer
MCD43GF    MODIS BRDF/Albedo/NBAR CMG Gap-Filled Products
MODIS     MODerate Imaging Spectroradiometer
\(\eta\textsubscript{OWC}\)    layer effective multiple scattering factor
<table>
<thead>
<tr>
<th>Acronym</th>
<th>Description</th>
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<tbody>
<tr>
<td>NEAs</td>
<td>North East Asia</td>
</tr>
<tr>
<td>NEPa</td>
<td>North East Pacific ocean</td>
</tr>
<tr>
<td>NWPa</td>
<td>North West Pacific ocean</td>
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<tr>
<td>OMI</td>
<td>Ozone Monitoring Instrument</td>
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<tr>
<td>ORACLES</td>
<td>ObseRvations of Aerosols above CLouds and their intEractionS</td>
</tr>
<tr>
<td>OWC</td>
<td>Opaque Water Cloud</td>
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<tr>
<td>POLDER</td>
<td>Polarization and Directionality of Earth’s Reflectances</td>
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<tr>
<td>PBL</td>
<td>Planetary Boundary Layer</td>
</tr>
<tr>
<td>$R_e$</td>
<td>Cloud droplet effective radius</td>
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<tr>
<td>RT</td>
<td>Radiative Transfer scheme</td>
</tr>
<tr>
<td>$S_a$</td>
<td>Aerosol extinction-to-backscatter (lidar) ratio</td>
</tr>
<tr>
<td>$S_c$</td>
<td>Cloud extinction-to-backscatter (lidar) ratio</td>
</tr>
<tr>
<td>SCIAMACHY</td>
<td>Scanning Imaging Absorption Spectrometer for Atmospheric Cartography</td>
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<tr>
<td>SEAs</td>
<td>South East Asia</td>
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<tr>
<td>SEAt</td>
<td>South East Atlantic ocean</td>
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<tr>
<td>SEPa</td>
<td>South East Pacific ocean</td>
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<tr>
<td>SEVIRI</td>
<td>Spinning Enhanced Visible and InfraRed Imager</td>
</tr>
<tr>
<td>SNR</td>
<td>Signal-to-Noise Ratio</td>
</tr>
<tr>
<td>SS</td>
<td>Single Scattering</td>
</tr>
<tr>
<td>SSA</td>
<td>Single Scattering Albedo</td>
</tr>
<tr>
<td>Code</td>
<td>Description</td>
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<tr>
<td>------</td>
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<tr>
<td>SW</td>
<td>Short Wave</td>
</tr>
<tr>
<td>TAt</td>
<td>Tropical Atlantic ocean</td>
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<tr>
<td>TOA</td>
<td>Top Of Atmosphere</td>
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</table>
1. Introduction

The Direct Aerosol Radiative Effect (DARE) is defined as the change in the upwelling radiative flux \((F')\) at the top of the atmosphere (TOA) due to aerosols. Measured values of DARE depend on the accuracy and the geometry of the observation(s), the concentrations of various atmospheric constituents (e.g., aerosols, clouds, and atmospheric gases) and their radiative properties, and the Earth’s surface reflectance. All-sky DARE \(\text{DARE}_{\text{all-sky}}\) combines contributions from DARE under cloudy conditions \(\text{DARE}_{\text{cloudy}}\) and DARE under cloud-free conditions \(\text{DARE}_{\text{non-cloudy}}\):

\[
\text{DARE}_{\text{all-sky}} = \text{DARE}_{\text{cloudy}} \times \text{Cloud Fraction} + \text{DARE}_{\text{non-cloudy}} \times (1 - \text{Cloud Fraction}) \quad \text{Eq. (1)}
\]

According to Yu et al., [2006], substantial progress has been made in the assessment of \(\text{DARE}_{\text{non-cloudy}}\) using satellite and in situ data. Further evidence is provided in a companion to our study, Redemann et al. [2019], which use A-Train aerosol observations to constrain \(\text{DARE}_{\text{non-cloudy}}\) and compares the results with AeroCom (Aerosol Comparisons between Observations and Models) results (see Appendix A for further details). However, traditional passive aerosol remote sensing techniques are limited only to clear-sky conditions and significant efforts are required to estimate \(\text{DARE}_{\text{cloudy}}\). Moreover, simulations of \(\text{DARE}_{\text{cloudy}}\) from various AeroCom models in Schulz et al. [2006] (see their figure 6) show large disparities. Our study focuses on Aerosol Above Cloud (AAC) scenes over the globe and subsequent estimates of \(\text{DARE}_{\text{cloudy}}\) (i.e., the instantaneous short wave (SW) upwelling TOA reflected radiative fluxes due to clouds only minus SW upwelling TOA fluxes due to clouds with overlying aerosols). Let us note that, ideally, TOA \(\text{DARE}_{\text{cloudy}}\) should include aerosols below, in-between and above clouds. Here we assume that TOA \(\text{DARE}_{\text{cloudy}}\) is only caused by aerosols above clouds. Table 1 lists TOA SW...
DARE_{cloudy} results that use satellite observations in the literature, together with assumptions in their calculations. Compared to the peer-reviewed studies of Table 1, our study marks a departure on three accounts. First, most peer-reviewed DARE_{cloudy} calculations focus primarily on the South East Atlantic (e.g., Chand et al., 2009, Wilcox et al., 2012, Peters et al., 2011, De Graaf et al., 2012, 2014, Meyer et al., 2013, 2015, Peers et al., 2015, Feng and Christopher, 2015) in Table 1). Second, our results use a combination of A-Train satellite sensors (i.e., MODIS-OMI-CALIOP), instead of the Look-Up-Table (LUT) approach used in the other studies of Table 1, to obtain estimates of the intensive aerosol radiative properties above clouds. Third, the peer-reviewed global DARE_{cloudy} calculations in Table 1 use standard products from the active satellite sensor Cloud Aerosol LIdar with Orthogonal Polarization (CALIOP) for either AAC Aerosol Optical Depth (AOD) and/or aerosol and cloud vertical distribution information in the atmosphere [Zhang et al., 2014, 2016, Matus et al., 2015, Oikawa et al., 2013]. In our case, we estimate DARE_{cloudy} globally by using an alternate method applied to CALIOP Level 1 measurements [Hu et al., 2007b; Chand et al., 2008; Liu et al., 2015] to obtain AAC AOD and the AAC frequency of occurrence. In the sections below, we explain why we have used such a method, instead of other passive or active satellite sensor techniques.

**Table 1:** TOA SW DARE_{cloudy} calculations that use satellite observations in the literature and specific assumptions in the calculations. See also the theoretical study by Chang and Christopher et al. [2017] (i.e. they impose fixed COD, Re, AOD, aerosol radiative properties, and aerosol / cloud vertical distribution) and the study by Costantino and Bréon et al. [2013] (their method uses MODIS-derived cloud microphysics that are not corrected for overlying aerosols). When not specified, the study uses the standard CALIOP data product; otherwise, it uses the DR (Depolarization Ratio) or CR (Color Ratio).
technique on CALIOP measurements. MODIS\textsuperscript{A} and MODIS\textsuperscript{T} respectively denote the AQUA or TERRA platform. SEAt: South East Atlantic. LUT: Look Up Table. See acronyms for satellite sensors MODIS, CALIOP, CloudSat, POLDER, CERES and AMSR-E.

<table>
<thead>
<tr>
<th>Reference</th>
<th>Domain</th>
<th>Satellite sensor(s) used for DARE\textsubscript{cloudy} calculations</th>
<th>Cloud properties (e.g. COD, albedo, fraction)</th>
<th>AOD</th>
<th>Aerosol radiative properties (e.g. SSA, g)</th>
<th>Vertical distribution of aerosol and cloud</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chand et al. [2009]</td>
<td>SEAt</td>
<td>MODIS\textsuperscript{T}</td>
<td>CALIOP\textsuperscript{CR}</td>
<td></td>
<td>Fixed value</td>
<td>Assumed constant</td>
</tr>
<tr>
<td>Wilcox [2012]</td>
<td>SEAt</td>
<td>MODIS\textsuperscript{A}, AMSR-E</td>
<td>CERES provides upwelling shortwave flux</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Peters et al. [2011]</td>
<td>Atlantic</td>
<td>MODIS\textsuperscript{A}, AMSR-E</td>
<td>CERES provides upwelling shortwave flux</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>De Graaf et al. [2012, 2014]</td>
<td>SEAt</td>
<td>Direct determination of DARE\textsubscript{cloudy} by building LUT of cloud and aerosol-free reflectances</td>
<td></td>
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<tr>
<td>Meyer et al. [2013]</td>
<td>SEAt</td>
<td>MODIS\textsuperscript{A}</td>
<td>CALIOP</td>
<td></td>
<td>LUT approach</td>
<td>CALIOP</td>
</tr>
<tr>
<td>Zhang et al. [2014, 2016]</td>
<td>Globe</td>
<td>MODIS\textsuperscript{A}, CALIOP (uses probability density function of CALIOP above-cloud AOD and underlying MODIS COD)</td>
<td>LUT approach</td>
<td></td>
<td>CALIOP</td>
<td></td>
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<tr>
<td>Meyer et al. [2015]</td>
<td>SEAt</td>
<td>MODIS\textsuperscript{A} (simultaneous retrieval of above-cloud AOD, COD and $R_e$)</td>
<td>LUT approach</td>
<td></td>
<td>Assumed constant</td>
<td></td>
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<tr>
<td>Peers et al. [2015]</td>
<td>SEAt</td>
<td>POLDER (simultaneous retrieval of above-cloud aerosol OD, size and single scattering albedo, cloud optical depth and cloud top height)</td>
<td></td>
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<tr>
<td>Feng and Christopher [2015]</td>
<td>SEAt</td>
<td>MODIS\textsuperscript{A}, CERES</td>
<td>CERES provides upwelling shortwave flux</td>
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Table 2 lists some passive (i.e., Spinning Enhanced Visible and InfraRed Imager, SEVIRI, Moderate Resolution Imaging Spectroradiometer, MODIS, Polarization and Directionality of Earth’s Reflectances, POLDER, Ozone Monitoring Instrument, OMI or the Scanning Imaging Absorption Spectrometer for Atmospheric Chartography, SCIAMACHY) and active (i.e., CALIOP and CloudSat) satellite sensors that were used to detect and quantify the AAC AODs. Among the peer-reviewed studies of Table 2, those few that present DARE\textsubscript{cloudy} results (see Table 1) are denoted by a “+” sign in the first column.

**Table 2:** Studies that observe AAC using passive and active satellite sensors (i.e., from left to right, SEVIRI, POLDER, CloudSat, OMI, MODIS, SCIAMACHY, CALIOP; see acronyms). When using CALIOP, the authors either use the standard Level 2 products (Std), the Depolarization method (DR) [Hu et al., 2007b] or the color ratio method (CR) [Chand et al., 2008]. SEAt stands for SE Atlantic,
SEAs for SE Asia, NEAs for NE Asia and TAt for Tropical Atlantic. The “+” sign in the first column denotes the presence of DARE cloudy calculations.

<table>
<thead>
<tr>
<th>Reference</th>
<th>Domain</th>
<th>Satellite sensor(s) used for aerosol-above-cloud detection</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 Chang and Christopher</td>
<td>SEAt</td>
<td>SEVIRI, POLDER, CloudSOMP, MODIS, SCIAMACHY, CALIOP</td>
</tr>
<tr>
<td>2 Waquet et al. [2013a]</td>
<td>Globe</td>
<td></td>
</tr>
<tr>
<td>3 Waquet et al. [2009, 2013b]</td>
<td>SEAt, TAt</td>
<td></td>
</tr>
<tr>
<td>4 Peers et al. [2015]</td>
<td>SEAt</td>
<td></td>
</tr>
<tr>
<td>5 Jethva et al. [2013, 2014]</td>
<td>SEAt, TAt</td>
<td></td>
</tr>
<tr>
<td>6 Torres et al. [2012]</td>
<td>SEAt</td>
<td></td>
</tr>
<tr>
<td>7 Peters et al. [2011]</td>
<td>Atlantic</td>
<td></td>
</tr>
<tr>
<td>8 De Graaf et al. [2012, 2014]</td>
<td>SEAt</td>
<td></td>
</tr>
<tr>
<td>9 Meyer et al. [2015]</td>
<td>SEAt</td>
<td></td>
</tr>
<tr>
<td>10 Feng and Christopher</td>
<td>SEAt</td>
<td></td>
</tr>
<tr>
<td>11 Sayer et al. [2016]</td>
<td>SEAt, SEAs</td>
<td></td>
</tr>
<tr>
<td>12 Matus et al. [2015]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>13 Alfaro-Contreras et al. [2016]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>14 Alfaro-Contreras et al. [2014]</td>
<td>SEAt, SEAs</td>
<td>Std</td>
</tr>
<tr>
<td>15 Devasthale and Thomas [2011]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>16 Yu et al. [2012]</td>
<td>SEAt, TAt</td>
<td>Std</td>
</tr>
<tr>
<td>17 Wilcox [2012]</td>
<td>SEAt</td>
<td>Std</td>
</tr>
<tr>
<td>18 Meyer et al. [2013]</td>
<td>SEAt</td>
<td>Std</td>
</tr>
<tr>
<td>19 Zhang et al. [2014, 2016]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>20 Oikawa et al. [2013]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>21 Chung et al. [2016]</td>
<td>Globe</td>
<td>Std</td>
</tr>
<tr>
<td>22 Chand et al. [2008]</td>
<td>SEAt</td>
<td>CR, DR</td>
</tr>
</tbody>
</table>
The brightening of clear patches near clouds [Wen et al., 2007] (i.e., “3-D cloud radiative effect” or “cloud adjacency effect”) can introduce biases into the current passive satellite AAC retrieval techniques (i.e., lines 1-11 of Table 2). To minimize these biases, this study relies primarily on CALIOP observations [Winker et al., 2009]. CALIOP is a three-channel elastic backscatter lidar with a narrow field of view and a narrow source of illuminating radiation, which limits cloud adjacency effects and the subsequent cloud contamination of aerosol data products [Zhang et al., 2005; Wen et al., 2007; Vármai and Marshak, 2009]. CALIOP measures high-resolution (1/3 km in the horizontal and 30m in the vertical in low and middle troposphere) profiles of the attenuated backscatter from aerosols and clouds at visible (532 nm) and near-infrared (1064 nm) wavelengths along with polarized backscatter in the visible channel [Hunt et al., 2009]. These data are distributed as part of the Level 1 CALIOP products. The Level 2 products are derived from the Level 1 products using a succession of sophisticated retrieval algorithms [Winker et al., 2009]. The Level 2 processing is composed of a feature detection scheme [Vaughan et al., 2009], a module that classifies features according to layer type (i.e., cloud versus aerosol) [Liu et al., 2010] and subtype (i.e., aerosol species) [Omar et al., 2009], and, finally, an extinction retrieval algorithm [Young and Vaughan, 2009] that retrieves profiles of aerosol backscatter and extinction coefficients and the total column AOD based on modeled values of the extinction-to-
backscatter ratio (also called lidar ratio and represented by the symbol $S_a$) inferred for each detected aerosol layer subtype.

A few studies use standard CALIOP Level 2 Aerosol and Cloud Layer products to determine AAC occurrence over the globe (see line 12-21 in Table 2). However, a study by Kacenelenbogen et al. [2014] demonstrates that the standard version 3 CALIOP aerosol products substantially underreport the occurrence frequency of AAC when aerosol optical depths are less than ~0.02, mostly because these tenuous aerosol layers have attenuated backscatter coefficients less than the CALIOP detection threshold. CALIOP’s standard extinction (and optical depth) data products are only retrieved between the tops and bases of detected features, and these boundaries may significantly underestimate the full vertical extent of the layer (Kim et al., 2017; Thorsen et al., 2017; Toth et al., 2018). Furthermore, the Kacenelenbogen et al. [2014] study found essentially no correlation between AAC AOD results reported by the CALIOP and collocated NASA Langley airborne High Spectral Resolution Lidar (HSRL). A subsequent study by Liu et al. [2015] shows that the CALIOP Level 2 standard aerosol data products underestimate dust AAC AOD by ~26% over the Tropical Atlantic and smoke AAC AOD by ~39% over the SE Atlantic.

For these reasons, a few studies in Table 2 (see line 22-26) use alternate methods on Level 1 CALIOP products, such as the Color Ratio (CR) [Chand et al., 2008] or the Depolarization Ratio (DR) [Hu et al., 2007b; Liu et al., 2015] methods, instead of using the AOD reported in the CALIOP standard Level 2 products.
In this study, we use the DR method and a combination of CALIOP Level 1 and Level 2 data products to compute global estimates of the AAC frequency of occurrence (i.e., $f_{\text{AAC}}$) and the AAC AOD (i.e., $\tau_{\text{AAC}}$) (section 2.1). We then use CALIOP results of $f_{\text{AAC}}$, $\tau_{\text{AAC}}$ and other A-Train satellite products to compute global DARE$_{\text{cloudy}}$ (section 2.2). Section 3 describes the geographical and seasonal distribution of global $f_{\text{AAC}}$ (section 3.1), $\tau_{\text{AAC}}$ (section 3.2) and DARE$_{\text{cloudy}}$ results (section 3.3). Section 4 revisits some of the limitations in the method and proposes ways to improve on these DARE$_{\text{cloudy}}$ calculations.

2. Method

2.1. AAC optical depth

Because the CALIOP backscatter signal is totally attenuated below the lowest “feature” detected within any profile [Vaughan et al., 2009], this lowest feature is defined as being opaque. Approximately 69% of the time, the opaque feature detected in a profile is the Earth’s surface [Guzman et al., 2017]. In the remainder of the cases, the opaque feature is either a water cloud, an ice cloud, or, very rarely, an aerosol layer.

The DR method, which is also known as the “constrained opaque water cloud method” [Liu et al., 2015], relies on Opaque Water Clouds (OWCs) as reflectivity targets. The OWCs in this study are selected using the five criteria listed in Table B2 of the appendix. Most importantly, (1) only one cloud can be detected within a 5 km (15 shot) along-track average (which means, for example, that marine stratus below thin cirrus are excluded), and (2) this one cloud must be opaque (i.e., lowest feature detected in a column, and not subsequently classified as a surface return). Furthermore, all OWCs must
be (3) spatially uniform (i.e., detected at single-shot resolution within every laser pulse included in the 5 km averaging interval), (4) assigned a high confidence score by the CALIOP cloud-aerosol discrimination (CAD) algorithm and (5) identified as a high confidence water cloud by the CALIOP cloud phase identification algorithm. When there is aerosol above OWCs, the lidar backscatter signal received from the underlying water cloud is reduced in direct proportion to the two-way transmittance of the aerosol layer above. However, because the DR retrieval technique requires backscatter measurements from opaque water clouds [Hu et al., 2007b], it cannot be used to retrieve AOD from aerosols lying above the low, transparent water clouds that are frequently observed over remote oceans, especially in the southern hemisphere (e.g., Leahy et al. [2012]; Mace and Protat [2018]; O et al. [2018]).

Based on Hu et al. [2007a, 2007b], Eq. (2) describes how we compute $\tau^{DRAAC}$ using the DR method above OWCs.

$$\tau^{DRAAC} = -0.5 \times \ln[I_{AB}^{OWCSSAAC} / I_{AB}^{OWCSSCAC}]$$

Eq. (2)

Here $I_{AB}^{OWCSSAAC}$ is the single scattering value (subscript SS) of the layer-integrated attenuated backscatter (IAB) for an OWC underlying one or more aerosol layer(s) above the cloud. $I_{AB}^{OWCSSCAC}$ is the single scattering value of the IAB for an OWC underlying Clear air Above Cloud (CAC). By CAC, we mean that there are no aerosols detected above the OWC. In this study, we consider $\tau^{DRAAC}$ valid when positive. According to Eq. (2), this means that $I_{AB}^{OWCSSAAC}$ needs to always be smaller in magnitude than $I_{AB}^{OWCSSCAC}$ and $\tau^{DRAAC}$ equals zero when $I_{AB}^{OWCSSAAC}$ equals $I_{AB}^{OWCSSCAC}$. 
Section B of the appendix provides additional information about the application of Eq. (2) and the various steps needed to derive $\tau_{\text{DR, AAC}}$. We list the selection criteria used to identify the OWC dataset in this study and describe the corrections required to obtain single-scattering estimates of IAB from measurements that contain substantial contributions from multiple scattering (B1). We also describe the technique used for distinguishing between CAC and AAC conditions (B2), and illustrate our derivation of an empirical parameterization of $I_{\text{AB, OWC}}^{\text{SS,CAC}}$ as a global function of latitude and longitude (B3).

As reported in Table 2, the CALIOP DR method was used to study the African dust transport pathway over the Tropical Atlantic [Liu et al., 2015] and the African smoke transport pathway over the South East Atlantic [Liu et al., 2015; Chand et al., 2008, 2009]. More recently, the CALIOP DR method was also used by Deaconu et al. [2017] to assess POLDER AAC AOD values [Waquet et al., 2009, 2013b and Peers et al., 2015] over the globe. In this study, we extend the previous regional studies of [Liu et al., 2015 and Chand et al., 2008, 2009] to derive global CALIOP-based AAC AOD estimates. Let us note that, in our study, the accuracy of $\tau_{\text{DR, AAC}}$ depends on measurements of targets of very high signal-to-noise ratio (SNR) such as OWCs in clear skies and OWCs underlying aerosol layers.

### 2.2. AAC Direct Aerosol Radiative Effects

Having first retrieved global values of $\tau_{\text{DR, AAC}}$ from the CALIOP measurements, we then compute global estimates of DARE$_{\text{cloudy}}$ using DISORT (DIScrete ORdinate Radiative Transfer; Stamnes et al., 1988, Buras et al., 2011), a six-stream plane-parallel radiative transfer model with molecular absorption characterized by a correlated-k scheme [Fu and Liou, 1992] that is embedded within the LibRadtran Radiative Transfer (RT) package [Emde et al., 2016]. Hereafter, our seasonally and spatially gridded (4°...
x 5°) averaged shortwave (SW) (250 nm to 5600 nm) global TOA DARE\textsubscript{cloudy} results will be called DARE\textsubscript{OWC}, as they pertain to a specific category of clouds (i.e., OWCs) defined according to the CALIOP data selection criteria set forth in Table B2. We list the following input parameters to DISORT in order to derive estimates of DARE\textsubscript{OWC}:

1. **Atmospheric profiles** of pressure, temperature, air density, ozone, water vapor, CO\textsubscript{2}, and NO\textsubscript{2} use standard US atmosphere profiles [Anderson et al., 1986].

2. **Aerosol intensive radiative properties** (i.e. properties that depend solely on aerosol species, and are unrelated to the aerosol amount) are informed by seasonal maps (4° x 5°, daytime in 2007) of combined MODIS-OMI-CALIOP (MOC) retrieved median spectral extinction coefficients, single scattering albedos and asymmetry parameters at 30 different wavelengths. As an example, Figure A1 in the appendix shows the seasonal maps of MOC SSA at 546.3 nm that were used in the calculation of DARE\textsubscript{OWC}. These MOC retrievals, described in section A of the appendix, are at the basis of a companion study [Redemann et al., 2019]. Let us note that we only use the shape of the MOC extinction coefficient spectra and not its actual magnitude; the MOC spectral extinction coefficient spectra is normalized to the seasonal 2008-2012 average value of either $\tau$\textsubscript{DR\_AAC} or $\tau$\textsuperscript{DR\_AAC} x $f$\textsubscript{AAC} within each grid cell. Our method assumes similar aerosol radiative properties above clouds and in near-clear-sky regions.

3. **Aerosol extensive radiative properties** (i.e., properties that depend on the aerosol amount present in the atmosphere) are informed by seasonal maps (4° x 5°, nighttime from 2008 to 2012) of either CALIOP $\tau$\textsubscript{DR\_AAC} (see Eq. 2) or CALIOP $\tau$\textsuperscript{DR\_AAC} x $f$\textsubscript{AAC}. We chose to use nighttime CALIOP
\( \tau_{\text{DR}}^{\text{AAC}} \) or \( \tau_{\text{DR}}^{\text{AAC}} \times f_{\text{AAC}} \) results in the estimation of \( \text{DARE}_{\text{OWC}} \) because, at nighttime, the CALIOP signal-to-noise-ratio (SNR) is not affected by ambient solar background and leads to a more accurate measurement of the aerosol signal (compared to daytime). By doing this, we implicitly chose a better accuracy in the aerosol extensive radiative properties over a temporal overlap between aerosol extensive (nighttime) and intensive (daytime) radiative properties.

(4) Cloud albedos are computed from cloud droplet effective radius (\( R_e \)) and Cloud Optical Depth (COD) information inferred from MODIS averaged monthly 1°x1° grids (i.e. liquid water cloud products of MYD08_M3: “Cloud Effective Radius Liquid Mean Mean” and “Cloud Optical Thickness Liquid Mean Mean” [Platnick et al. 2015]) from 2008 to 2012 (see Equations 1-9 of Peng et al. [2002]). These maps are then further gridded (to 4°x5°) and seasonally averaged to match the format of the aerosol radiative properties. Appendix figure A2 shows the seasonal maps of MODIS COD that were used in the calculation of \( \text{DARE}_{\text{OWC}} \).

(5) Aerosol and cloud layer heights are assumed constant over the globe (respectively between 3-4km and 2-3km in this study), similar to other studies in Table 1 (e.g., Meyer et al. [2015]).

(6) Earth’s surface albedo uses global gap-filled Terra and Aqua combined MODIS BRDF/albedo products. It uses the 16-day closest product (i.e., MCD43GF) to the middle of each season (i.e., Jan 15th for DJF, April 15th for MAM, July 15th for JJA and October 15th for SON). In the open ocean, the Cox and Munk [1954] sea surface albedo parameterization is applied with a wind speed of 10 ms\(^{-1}\).

Using these inputs, Daily \( \text{DARE}_{\text{OWC}} \) results for each of the 4° x 5° grid cells are obtained by averaging 24 LibRadtran RT calculations, corresponding to 24 different sun positions at each hour of the day.
3. Results

3.1. AAC Occurrence Frequencies

To provide the necessary context for interpreting our TOA radiative transfer calculations, we first establish the observational AAC occurrence frequencies from which we will subsequently compute estimates of DARE\textsubscript{OWC}. Figure 1 illustrates the annual gridded mean (5 years) global occurrence frequencies of a) single layer clouds, b) opaque water clouds that are suitable for the DR method and c) aerosol-above-clouds cases using the DR method. Figure 1d) shows the difference between the number of AAC cases using the DR method (i.e., number of cases with $t_{\text{DR, AAC}} > 0$) and the number of AAC cases using the standard Version 3 CALIOP product.
Figure 1: During nighttime, from 2008 to 2012 on a 4°x5°-grid: Occurrence frequencies of (a) uniform single layer clouds (C1-C3 of Table B2), (b) opaque water clouds suitable for the DR method (C1-C5 of Table B2; these clouds can be obstructed or unobstructed) and (c) AAC cases that show a positive $\tau_{\text{DR AAC}}$ at 532 nm. (d) shows the difference between the number of AAC cases using the DR method (i.e., number of cases with $\tau_{\text{DR AAC}} > 0$) and the number of AAC cases using the standard Version 3 CALIOP product (i.e., number of cases with $\tau_{\text{STD AAC}} > 0$); CALIOP AAC cases using the standard algorithm are defined as 5 km-columns showing an uppermost layer classified as aerosols and a cloud.
layer anywhere below that aerosol layer; the cloud itself does not have to satisfy any of the criteria of Table B2. Grid cells are 4° x 5° latitude/longitude. The percentages in (a)-(d) use the number of 5 km CALIOP samples within each grid cell as a reference. White pixels show either no CALIOP observations, no CALIOP OWC detection, a small number of CALIOP unobstructed OWCs or a small number of positive $\tau_{\text{DR}}$ values. The title of each map shows the global maximum, median and mean values.

Uniform single layer clouds (i.e. C1-C3 of Table B2) are detected in ~47% of all 5 km CALIOP samples over the globe (see Figure 1(a)). In other words, at any one time, approximately half of the globe is covered by uniform single layer clouds. As expected, the highest occurrence of those clouds is in the high and low latitude bands and especially over the southern oceans. According to Figure 1(b), OWCs suitable for the DR method (i.e. C1-C5 of Table B2) are mostly in the marine stratocumulus regions and represent a mean of 7% of all 5 km CALIOP samples over the globe. This significant reduction from half-the-globe coverage is explained by the five criteria used to select OWCs for the application of the DR method (i.e., C1-C5 of Table B2). The highest occurrence of OWCs can be found offshore from the west coasts of North and South America, southwest Africa and Australia. In particular, OWC cover ranges from 60 to 75 % over the region of SE Atlantic in August [Klein and Hartmann, 1993]. Also, the southeastern Pacific region off the Peruvian and Chilean coasts is the location of the largest and most persistent stratocumulus deck in the world [Klein and Hartmann, 1993]. The percentage of AAC cases (i.e., AAC cases showing positive $\tau_{\text{DR,AAC}}$) at the basis of our study is
very small compared to the total number of 5 km CALIOP profiles per grid cell (i.e. mean of 5% on Figure 1(c)). This is primarily due to a small number of low OWC used for the DR method over the globe (when comparing Figure 1(a) and 1(b)).

Figure 1(d) illustrates the difference in occurrence frequencies of AAC cases using the DR method compared to the standard Version 3 CALIOP product. Negative values, shown in blue, indicate the fraction of cases for which the DR method fails to detect above-cloud aerosols that are reported in the standard CALIOP product. Similarly, positive values, shown in red, indicate the number of cases for which above-cloud aerosols are detected by the DR method but not reported in the standard CALIOP data product. Unlike the AAC cases detected using the DR method, the AAC cases obtained from the CALIOP standard product do not impose any restrictions on the nature of the underlying clouds, irrespective of cloud thermodynamic phase. The blue regions in Fig. 1(d) show that, relative to the CALIOP standard product, our implementation of the DR method could be failing to detect AAC cases over most of land surfaces and over the Arabian Sea, the Tropical Atlantic, and the SE Atlantic regions. The lack of AAC cases offshore from the southwest coast of Africa in the DR method dataset is the result of our conservative data filtering strategy. Because the IABs of aerosol-contaminated OWCs can differ significantly from those measured in pristine, aerosol-free conditions, OWCs suspected of being aerosol-contaminated (which are ubiquitous in this part of the world and very common over continents) are specifically excluded from our DR method analyses (see appendix section B3 for more details). However, some regions such as the NE and SE Pacific exhibit up to 40% more AAC cases when using the DR method. The SE Pacific region, especially offshore from Chile, shows particularly...
tenuous aerosols, with attenuated backscatter values that typically fall below the CALIOP detection limit, thus hampering the detection of AAC using the standard CALIOP algorithm [Kacenelenbogen et al., 2014].

In the rest of this study, the frequency of occurrence of AAC, $f_{AAC}$, is defined as:

$$f_{AAC} = \frac{N_{AAC}}{N_{OWC}}$$  \hspace{1cm} \text{Eq. (3)}

where $N_{AAC}$ is the number of AAC cases (i.e., cases showing a positive $r^{DR}_{AAC}$ at 532nm) and $N_{OWC}$ is the number of OWCs within each 4°x5° grid cell. Let us note that different studies use different references when computing the frequency of occurrence of AAC. The definition in Eq. (3) is similar to the one in Zhang et al. [2016] (see their Eq. (1)) and different from Devasthale and Thomas [2011], where $f_{AAC}$ is defined as the ratio of AAC cases to the total number of CALIOP observations (similar to what is shown on Fig. 1(c)).

Figure 2 illustrates the global seasonal $f_{AAC}$ (see Eq. 3) from 2008 to 2012. We find a median global $f_{AAC}$ of 58% to 61% with regional values that can reach more than 80% in some regions such as the SE Atlantic, especially during the JJA season. The AAC occurrence frequencies in Fig. 2 generally agree with previous findings [Zhang et al., 2016; Devasthale and Thomas, 2011] on the location and season of highest $f_{AAC}$. 

\[\]
Figure 2: Global seasonal 4°x5° nighttime AAC occurrence frequency (noted $f_{\text{AAC}}$, see Eq. (3)) from 2008 to 2012. White pixels show either no CALIOP observations, a limited number of CALIOP unobstructed OWCs or a limited number of positive $\tau_{\text{IM},\text{AAC}}$ values. White pixels are not considered in the global mean and median $f_{\text{AAC}}$ values in the title of each map. The title of each map shows the global maximum, median and mean values.

3.2. AAC Optical Depths
Figure 3 introduces the global, nighttime and multi-year (2008-2012) AAC optical depths (τ^{DR}_{AAC}, see Eq. 2) dataset that was computed in this study.

![Figure 3: Global distribution of τ^{DR}_{AAC} at 532 nm. Positive (i.e., valid) τ^{DR}_{AAC} values are in dark blue (N~3.4M) and negative τ^{DR}_{AAC} values in grey (N~2.2M). These are nighttime CALIOP measurements from 2008-2012.](image)

About 40% (i.e. 2.2M data points) of the initial dataset (i.e. N~5.6M) shows negative τ^{DR}_{AAC} values and were flagged as invalid data (see Figure 3, in grey). When looking at all valid (i.e. positive) τ^{DR}_{AAC} values (blue), we show a majority of very small τ^{DR}_{AAC} values in the 0.01-0.02 AOD range. This agrees with the findings of Devasthale and Thomas [2011]. Let us note that averaging all data points per 4ºx5º grid cell (instead of the native resolution shown on Fig. 3) increases the AOD bin of maximum AAC occurrence globally from 0.01 (Fig. 3) to 0.03.

Table 3 shows four different ways of computing global seasonal and annual averages of aerosol optical depth above clouds: we use either τ^{DR}_{AAC} or τ^{DR}_{AAC} x f_{AAC} (see Case I-II or III-IV) and then either (i)
exclude all cases of $\tau_{\text{DR,AAC}} < 0$ from the average (i.e., as in Case I and Case III), or (ii) set all cases of $\tau_{\text{DR,AAC}} < 0$ to zero, and include these samples in the averages (i.e., as in Case II and Case IV). Let us note that using $\tau_{\text{DR,AAC}} \times \text{f}_{\text{AAC}}$ (instead of $\tau_{\text{DR,AAC}}$) acknowledges the fact that some OWCs present no overlying aerosols. In this case, we assume that when the DR technique retrieves an invalid AAC measurement, $\text{f}_{\text{AAC}} = 0$ and there are no aerosols above the cloud.

**Table 3:** Global seasonal and annual averages of $\tau_{\text{DR,AAC}}$ (Case I and II) or $\tau_{\text{DR,AAC}} \times \text{f}_{\text{AAC}}$ (Case III and IV) when assuming either (i) $\tau_{\text{DR,AAC}} < 0$ cases are excluded from the averages (Case I and III) or (ii) $\tau_{\text{DR,AAC}} < 0$ cases are set to zero and included in the averages (Case II and IV). Annual averages here (last column) are the mean of the seasonal averages.

<table>
<thead>
<tr>
<th>Global mean aerosol optical depth</th>
<th>DJF</th>
<th>MAM</th>
<th>JJA</th>
<th>SON</th>
<th>Annual</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Case I</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{DR,AAC}}$, invalid $\tau_{\text{DR,AAC}}$ excluded</td>
<td>0.04</td>
<td>0.05</td>
<td>0.05</td>
<td>0.05</td>
<td>0.05</td>
</tr>
<tr>
<td><strong>Case II</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{DR,AAC}}$, invalid $\tau_{\text{DR,AAC}} = 0$</td>
<td>0.02</td>
<td>0.02</td>
<td>0.02</td>
<td>0.02</td>
<td>0.02</td>
</tr>
<tr>
<td><strong>Case III</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{DR,AAC}} \times \text{f}<em>{\text{AAC}}$, invalid $\tau</em>{\text{DR,AAC}}$ excluded</td>
<td>0.03</td>
<td>0.03</td>
<td>0.04</td>
<td>0.03</td>
<td>0.03</td>
</tr>
<tr>
<td><strong>Case IV</strong></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>$\tau_{\text{DR,AAC}} \times \text{f}<em>{\text{AAC}}$, invalid $\tau</em>{\text{DR,AAC}} \times \text{f}_{\text{AAC}} = 0$</td>
<td>0.01</td>
<td>0.01</td>
<td>0.01</td>
<td>0.01</td>
<td>0.01</td>
</tr>
</tbody>
</table>

Figure 4 shows global seasonal nighttime median $\tau_{\text{DR,AAC}} \times \text{f}_{\text{AAC}}$ from 2008 to 2012 (i.e., as in Case III of Table 3). The title of each seasonal map (respectively DJF, MAM, JJA, SON) in Figure 4 shows the global maximum (respectively 0.11, 0.13, 0.22, 0.20), median (0.02 for all seasons) and mean (0.03 in DJF, MAM and SON and 0.04 in JJA) $\tau_{\text{DR,AAC}} \times \text{f}_{\text{AAC}}$ values.
Figure 4: Global seasonal 4°x5° nighttime median $t_{DR}^{AAC} \times f_{AAC}$ from 2008 to 2012. Underlying clouds satisfy the criteria in Table B2. White pixels show either no CALIOP observations, a limited number of CALIOP unobstructed OWCs or a limited number of positive $t_{DR}^{AAC}$ values. White pixels are not included when calculating the global mean and median $t_{DR}^{AAC}$ values in the title of each map (i.e., as in Case III in Table 3). Note that if the white pixels were set equal to zero, the seasonal and annual global $t_{DR}^{AAC}$ values would correspond to Case IV in Table 3. The title of each map shows the global maximum, median and mean values.
We do not expect the $\tau_{\text{DR}}^{\text{AAC}} \times f_{\text{AAC}}$ values of Figure 4 to be similar to the results of [Zhang et al., 2014, Devasthale and Thomas, 2011, Alfaro-Contreras et al., 2016 or Yu and Zhang, 2013] (see Table 2) as these studies use standard CALIOP Level 2 aerosol and cloud layer products for AAC observations, instead of using the DR method. On the other hand, the results of Figure 4 seem to be in qualitative agreement with the global AAC AOD derived from spaceborne POLDER observations [Waquet et al., 2013a]. Let us note that Waquet et al. [2013a] have to assume an underlying COD larger than 3 to ensure the saturation of the polarized light scattered by the cloud layer. Although Deaconu et al. [2017] make different assumptions in the application of the DR method on CALIOP measurements (e.g., they impose a constant cloud lidar ratio for OWCs with clear air above), they find that POLDER and CALIOP $\tau_{\text{DR}}^{\text{AAC}}$ are in good agreement over the SE Atlantic ($R^2 = 0.83$) and over the Tropical Atlantic ($R^2 = 0.82$) from May to October 2008.

### 3.3. AAC Direct Aerosol Radiative Effects

#### 3.3.1. Global results of $\text{DARE}_{\text{OWC}}$

Figure 5 shows the seasonal TOA SW $\text{DARE}_{\text{OWC}}$ estimates (W m$^{-2}$) that use CALIOP $\tau_{\text{DR}}^{\text{AAC}} \times f_{\text{AAC}}$ (see Fig. 4) as input to a radiative transfer model, together with the other parameters described in section 2.2. $\text{DARE}_{\text{OWC}}$ in Fig. 5 is set equal to zero (i.e., white pixels) if $\text{DARE}_{\text{OWC}}$ is invalid or missing.
Figure 5: Global seasonal 4ºx5º TOA SW DARE\textsubscript{OWC} estimates (W·m\textsuperscript{-2}, as described in section 2.2). A white pixel is counted as DARE\textsubscript{OWC}=0 in the global mean DARE\textsubscript{OWC} values in the title of each map. White pixels show a limited number of CALIOP OWCs, positive $\tau_{\text{DR, AAC}}$ values or auxiliary MODIS-OMI-CALIOP combined satellite observations. The title of each map shows the global minimum, maximum, and mean values.
Similar to TOA DARE\textsubscript{cloudy} values from combined A-Train satellites in Oikawa et al. [2013] (see their Fig. 10) and from General Circulation Models (GCMs) (e.g. SPRINTARS) in Shulz et al. [2006] (see their Fig. 6 and 7), TOA DARE\textsubscript{OWC} values in Fig. 5 are mostly positive (i.e., a warming effect due to less energy leaving the climate system) over the globe. We find, globally, 72\% positive 4°x5° DARE\textsubscript{OWC} values (i.e., N=4045) against 28\% negative values (i.e., N=1581) when considering all four seasons on Fig. 5. On the other hand, the highest negative TOA DARE\textsubscript{OWC} values on Fig. 5 (i.e., cooling effects shown in green pixels) are over the Tropical Atlantic (in MAM, JJA and SON), in the Pacific Ocean offshore from Mexico (in JJA) and at the periphery of the Arabian Sea (in JJA).

There are multiple ways to compute the global seasonal and annual DARE\textsubscript{cloudy} averages (i.e., DARE\textsubscript{OWC} in our case), and it is not clear which method would bring us closer to the true DARE\textsubscript{cloudy} state of the planet. For this reason, we list several different methods in Table 4. We either use CALIOP $\tau^{DR}\textsubscript{AAC}$ or CALIOP $\tau^{DR}\textsubscript{AAC} \times \text{AAC}$ (Case I-II or III-IV) and we either exclude invalid DARE\textsubscript{OWC} values or set invalid DARE\textsubscript{OWC} = 0 (Case I-III or II-IV). For completeness and as an intermediate step towards DARE\textsubscript{all-sky} (see Eq. 1), Case V and VI show the global seasonal averages of DARE\textsubscript{OWC} x Cloud Fraction (CF), instead of DARE\textsubscript{OWC}. The CF values use monthly MODIS AQUA MYD08\_M3 products (variable “Cloud Retreiva Fraction Liquid FMean”), which are seasonally averaged and 4°x5°-gridded.

Table 4: Global seasonal and annual averages of TOA SW DARE\textsubscript{OWC} estimates (W/m\textsuperscript{2}, as described in section 2.2). Annual averages (last column) are the mean of the seasonal averages (e.g., 0.53 for Case I is the average of 0.34, 0.52, 0.71 and 0.56); CF stands for Cloud Fraction.
Global averaged $DARE_{\text{cloudy}} (W \times m^{-2})$

<table>
<thead>
<tr>
<th>Case</th>
<th>$DARE_{\text{OWC}}, t^{DR}<em>{\text{AAC}}, \text{invalid} DARE</em>{\text{OWC}} \text{ excluded}$</th>
<th>DJF</th>
<th>MAM</th>
<th>JJA</th>
<th>SON</th>
<th>Annual</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case I</td>
<td>0.34</td>
<td>0.52</td>
<td>0.71</td>
<td>0.56</td>
<td>0.53</td>
<td></td>
</tr>
<tr>
<td>Case II</td>
<td>0.19</td>
<td>0.26</td>
<td>0.35</td>
<td>0.29</td>
<td>0.27</td>
<td></td>
</tr>
<tr>
<td>Case III</td>
<td>0.24</td>
<td>0.40</td>
<td>0.53</td>
<td>0.40</td>
<td>0.39</td>
<td></td>
</tr>
<tr>
<td>Case IV</td>
<td>0.13</td>
<td>0.20</td>
<td>0.26</td>
<td>0.21</td>
<td>0.20</td>
<td></td>
</tr>
<tr>
<td>Case V</td>
<td>0.11</td>
<td>0.16</td>
<td>0.25</td>
<td>0.19</td>
<td>0.18</td>
<td></td>
</tr>
<tr>
<td>Case VI</td>
<td>0.04</td>
<td>0.06</td>
<td>0.09</td>
<td>0.07</td>
<td>0.07</td>
<td></td>
</tr>
</tbody>
</table>

Global seasonal and annual $DARE_{\text{OWC}}$ averages (see titles in Fig. 5 and Table 4) in our study represent the surface area of each grid cell. Each valid $DARE_{\text{OWC}}$ value per pixel on each map of Fig. 5 is multiplied by the surface of the pixel. These values per grid cell are then summed up and divided by the sum of the surface of all valid grid cells.

Figure 5 corresponds to the setting of Case IV in Table 4. The reason why we have selected to showcase this setting is because it closely resembles the settings of the $DARE_{\text{cloudy}}$ calculations in Zhang et al. [2016]; i.e., it assumes $DARE = 0$ when CALIOP cannot detect an aerosol layer. Figure 5 shows positive global seasonal $DARE_{\text{OWC}}$ averages between 0.13 and 0.26 W m$^{-2}$ (and an annual average of 0.20 W m$^{-2}$ in Table 4) as well as the lowest $DARE_{\text{OWC}}$ values when compared to $DARE_{\text{OWC}}$...
values from Case I through Case IV in Table 4. These values are nonetheless much larger than the global annual ocean \( DARE_{\text{cloudy}} \) values reported in Zhang et al. [2016] and Schulz et al. [2006] (e.g., annual average of 0.015 \( \text{W} \times \text{m}^2 \) reported over ocean in Zhang et al. [2016]). Moreover, Matus et al. [2015] find (see their Table 2) a global TOA \( DARE_{\text{cloudy}} \) value of 0.1 \( \text{W} \times \text{m}^2 \) over thick clouds (these clouds are similar to our study), compensated by a global TOA \( DARE_{\text{cloudy}} \) value of -2 \( \text{W} \times \text{m}^2 \) over thin clouds.

Section 3.3.2 further analyzes \( DARE_{\text{OWC}} \) together with \( f_{\text{AAC}} \), \( z_{\text{DIP},\text{AAC}} \), SSA, and COD results in a few selected regions and compares these results to previous studies.

### 3.3.2. Regional results of \( DARE_{\text{OWC}} \)

The \( f_{\text{AAC}} \) results in Fig. 2 help us define six major AAC “hotspots” over the North East Pacific (NEPa), South East Pacific (SEPa), Tropical Atlantic (TAt), South East Atlantic (SEAt), Indian ocean, offshore from West Australia (InWA), and North West Pacific (NWPa). To assist in the analysis of the remaining figures in this study, Figure 6 and Table 5 briefly describe these six AAC hotspots.
Figure 6: Six regions of high AAC occurrence, further defined in Table 5. Background map is the global annual 4° x 5° nighttime AAC occurrence frequency ($f_{AAC}$, see Eq. 3 and Fig. 2 for seasonal $f_{AAC}$ maps). Global annual maximum, median and mean $f_{AAC}$ values are respectively 93%, 57% and 57%.

Table 5: Six regions of high AAC occurrence (see Fig. 6), their season of highest AAC occurrence and its corresponding mean $f_{AAC}$ value

<table>
<thead>
<tr>
<th>Region</th>
<th>[latitude; longitude]</th>
<th>Season of most $f_{AAC}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>North East Pacific Ocean (NEPa)</td>
<td>[16N, 52N; 170W, 120W]</td>
<td>MAM (80%)</td>
</tr>
<tr>
<td>South East Pacific Ocean (SEPa)</td>
<td>[49S, 2S; 126W, 80W]</td>
<td>DJF (55%)</td>
</tr>
<tr>
<td>Tropical Atlantic Ocean (TAI)</td>
<td>[10N, 30N; 45W, 18W]</td>
<td>JJA (80%)</td>
</tr>
<tr>
<td>South East Atlantic Ocean (SEAt)</td>
<td>[19S, 2N; 10W, 8E]</td>
<td>SON (87%)</td>
</tr>
<tr>
<td>Indian Ocean, offshore from West Australia (InWA)</td>
<td>[41S, 13S; 58E, 102E]</td>
<td>SON (60%)</td>
</tr>
<tr>
<td>North West Pacific Ocean (NWPa)</td>
<td>[40N, 55N; 145E, 180E]</td>
<td>MAM (90%)</td>
</tr>
</tbody>
</table>
Figure 7a illustrates the mean regional, seasonal or annual estimates of SW TOA DARE$_{OWC}$ (W m$^{-2}$) in each region of Table 5. Figure 7b-7f show the primary parameters used in the DARE$_{OWC}$ calculations (see section 2.2): the mean regional, seasonal or annual (b) percentage of grid cells that show valid (i.e., positive) f$_{AAC}$ x $\tau_{DR}^{AAC}$ values compared to the total number of 4º x 5º pixels in each region, (c) CALIOP f$_{AAC}$ values, (d) CALIOP f$_{AAC}$ x $\tau_{DR}^{AAC}$ values, (e) assumed overlying SSA values at 546.3 nm and (f) assumed underlying COD values from MODIS.
Figure 7: Mean regional, seasonal or annual (a) estimated SW TOA DARE$_{OWC}$ (W·m$^{-2}$), calculation is described in section 2.2), (b) percentage of grid cells that show valid $f_{AAC} \times \tau_{AAC}^D$ (i.e., positive) values compared to the total number of 4° x 5° pixels in each region, (c) CALIOP $f_{AAC}$ (%), (d) $f_{AAC} \times \tau_{AAC}^D$ (no unit), (e) assumed overlying SSA at 546.3 nm from a combination of MODIS-OMI-
CALIOP and (f) assumed underlying COD from MODIS in each region of Table 5. DARE\textsubscript{OWC} in (a) is computed using the case IV of Table 4.

Table 6 reports the estimated seasonal or annual, regional range, mean and standard deviations of our TOA DARE\textsubscript{OWC} dataset (i.e., values of Fig. 7a).

<table>
<thead>
<tr>
<th>Region</th>
<th>min, max</th>
<th>mean DJF</th>
<th>mean MAM</th>
<th>mean JJA</th>
<th>mean SON</th>
<th>mean ANN</th>
</tr>
</thead>
<tbody>
<tr>
<td>NEPa</td>
<td>-0.57, 5.10</td>
<td>0.12±0.18</td>
<td>0.62±0.79</td>
<td>0.47±0.78</td>
<td>0.18±0.25</td>
<td>0.35±0.50</td>
</tr>
<tr>
<td>SEPa</td>
<td>-0.21, 2.85</td>
<td>0.09±0.19</td>
<td>0.02±0.15</td>
<td>0.07±0.37</td>
<td>0.12±0.44</td>
<td>0.07±0.29</td>
</tr>
<tr>
<td>TAt</td>
<td>-1.02, 5.25</td>
<td>0.26±0.43</td>
<td>0.31±0.43</td>
<td>1.08±1.66</td>
<td>0.01±0.42</td>
<td>0.41±0.74</td>
</tr>
<tr>
<td>SEAt</td>
<td>0.20, 7.59</td>
<td>0.31±1.09</td>
<td>0.20±0.41</td>
<td>2.49±2.54</td>
<td>2.87±2.33</td>
<td>1.47±1.59</td>
</tr>
<tr>
<td>InWA</td>
<td>-0.39, 0.83</td>
<td>0.04±0.16</td>
<td>-0.06±0.10</td>
<td>0.01±0.11</td>
<td>0.04±0.27</td>
<td>0.01±0.16</td>
</tr>
<tr>
<td>NWPa</td>
<td>0.07, 5.72</td>
<td>0.11±0.14</td>
<td>1.98±1.85</td>
<td>1.01±1.65</td>
<td>0.68±0.46</td>
<td>0.95±1.02</td>
</tr>
</tbody>
</table>

We record positive TOA DARE\textsubscript{OWC} values above 1 W\textperem^{-2} in Fig. 7a over TAt in JJA (1.08±1.66), SEAt in JJA and SON (2.49±2.54 and 2.87±2.33) and NWPa in MAM (1.98±1.85). Let us note that the highest positive TOA DARE\textsubscript{OWC} values on Fig. 7a and in Table 6 may not be entirely representative of each region, because they are based on a smaller number of valid DARE\textsubscript{OWC} results (86% valid values in JJA in TAt, 58-88% in JJA-SON in SEAt and 69% in MAM in NWPa). SEAt and NWPa are the only regions showing an all-positive range of DARE\textsubscript{OWC} values in Table 6 (i.e., respectively within...
0.20 and 7.59 and within 0.07 and 5.72 W m\(^{-2}\)). The spread (i.e., standard deviation) on those mean regional DARE\(_{\text{OWC}}\) is of the same order of magnitude as the mean values themselves. For example, although TAt shows an annual mean DARE\(_{\text{OWC}}\) value of 0.41 W m\(^{-2}\), most points (i.e., about 68%, assuming a normal distribution of DARE\(_{\text{OWC}}\)) are within 0.41 ± 0.74 W m\(^{-2}\) (see Table 6). Those regions and seasons of highly positive DARE\(_{\text{OWC}}\) values are associated with the highest CALIOP \(\tau^{\text{pA}}_{\text{AAC}} \times \bar{f}_{\text{AAC}}\) values (see Fig. 7d: 0.12 in TAt, 0.12-0.13 in JJA-SON in SEAt and 0.10 in MAM in NWPa). They are also associated with lower SSA values (i.e., < 0.94 in Fig. 7e), typical of more light absorbing aerosols such as biomass burning. The underlying COD values are fairly constant (between ~5-10 on Fig. 7f), except for a noticeably higher COD over the NWPa region (between ~15-25 on Fig. 7f). NWPa is the region of highest latitudes in our study (i.e., between 40N and 55N). More variation in the COD at higher latitudes is also observed in Fig. A2 in the Appendix. This agrees with King et al. [2013], who show a larger zonal variation of COD (and increased uncertainty in the MODIS cloud property retrievals) in the higher latitudes of both hemispheres, particularly in winter (see their Fig. 12b).

When computing mean DARE\(_{\text{OWC}}\) results within the “SE Atlantic” region defined in Zhang et al. [2016] (i.e., [30S, 10N; 20W, 20E] instead of [19S, 2N; 10W, 8E] in our study), we find a small fraction of valid pixels (i.e., an average of ~37%) but a mean annual DARE\(_{\text{OWC}}\) value of 0.57 W m\(^{-2}\), which resides within their range of annual DARE\(_{\text{cloudy}}\) values (i.e., 0.1 to 0.68 W m\(^{-2}\) in Zhang et al. [2016]). Similar to Matus et al. [2015], the season of highest DARE\(_{\text{OWC}}\) is SON over the SE Atlantic (they find 10% of DARE\(_{\text{OWC}}\) larger than 10 W m\(^{-2}\) over thick clouds with COD > 1, see their Fig. 9d).

However, our DARE\(_{\text{OWC}}\) results are significantly higher than the ones in Zhang et al. [2016] in our...
SEAt region (defined as a smaller region and offshore from the “SE Atlantic” region in Zhang et al. [2016]) as well as in the TAt (similar latitude/longitude boundaries to the ones of region “TNE Atlantic” in Zhang et al. [2016]) and the NWPa (similar boundaries to “NW Pacific” in Zhang et al. [2016]) regions.

We emphasize that the DARE\textsubscript{OWC} estimates in this study are not directly comparable to many previous studies (see Table 1) because of different spatial domain, period, satellite sensors and associated uncertainties. This will lead to the detection of different fractions of AAC above different types of clouds and different AAC types over the globe. The calculations of DARE\textsubscript{cloudy} can also differ greatly depending on different AAC aerosol radiative properties assumptions above clouds (especially absorption) and different assumptions in aerosol and cloud vertical heights (see Table 1).

Apart from the major differences in methods and sensors, it seems reasonable to say that we are missing AAC cases over pure dust-dominant regions such as the Arabian Sea or the TAt region (compared to e.g. Zhang et al. [2016] and Matus et al. [2015]). Both Matus et al. [2015] and Zhang et al. [2016] use the CALIOP Level 2 standard products to distinguish among a few aerosol types and infer specific aerosol optical properties in their DARE\textsubscript{cloudy}. According to Figure 1(d), SEAt, TAt and the Arabian Sea are regions where we might be missing up to 40% of AAC cases when using the DR technique compared to the CALIOP standard products. The number of potentially missing AAC cases in our study is larger over the Arabian sea ([0-30°N and 40-80°E] due to the limited number of OWCs suitable for the DR method (see section B1 in the Appendix). Zhang et al. [2016] show that pure dust aerosols over these dust-dominant regions tend to produce a negative DARE\textsubscript{cloudy} when the underlying COD is below .
77 ~7 and this is the case for most of the clouds over these regions in their study. In summary, two factors
78 in the DR method seem to hamper the detection of AAC in these regions: the low cloud optical depths
79 of underlying clouds and very few cases of “clear air” above clouds. As a consequence, we propose that
80 the positive DARE_{OWC} values in our study should, in reality, be counter-balanced by more negative
81 dust-driven DARE_{cloudy} values over regions such as TA and the Arabian Sea. On the other hand, the
82 DARE_{cloudy} results from Matus et al. [2015] and Zhang et al. [2016] might also differ from the true
83 global DARE_{cloudy} state of the planet for different reasons. As described in Matus et al. [2015], using
84 CALIOP Level 2 standard products as in Matus et al. [2015] and Zhang et al. [2016] could lead to
85 possible misclassification of dust aerosols as clouds [Omar et al., 2009], specifically around cloud edges
86 in the TA region. Moreover, even if the AAC is correctly detected in Matus et al. [2015] and Zhang et
87 al. [2016], the amount of AAC AOD might be biased low due to their use of the CALIOP Level 2
88 standard products [Kacenelenbogen et al., 2014].

4. Uncertainties in our DARE above cloud results and the path forward

4.1. Detecting and quantifying the true amount of AAC cases

Our study uses mainly CALIOP Level 1 measurements to detect aerosols above specific OWCs that
satisfy the criteria given in Table B2. We suggest that the number of CALIOP profiles that contain
aerosols over any type of cloud (instead of only OWCs in this study) should be informed by a
combination of different techniques applied to CALIOP observations (e.g., the standard products, the
DR and the CR technique). Airborne observations such as those from the ObseRvations of Aerosols
above Clouds and their interactions (ORACLES) field campaigns [Zuidema et al., 2016] are well suited for providing further guidance on when to apply which technique.

To the best of our knowledge, the true global occurrence of aerosols above any type of cloud remains unknown. This question cannot be entirely answered with the use of CALIOP observations only. We suggest that a more complete global quantification and characterization of aerosol above any type of cloud should be informed by a combination of AAC retrievals from CALIOP, passive satellite sensors (e.g. POLDER [Waquet et al., 2013a,b, Peers et al., 2015, Deaconu et al., 2017] and MODIS [Meyer et al., 2013, Zhang et al., 2014, 2016], see Table 2) and model simulations [Schulz et al., 2006].

4.2. Considering the diurnal variability of aerosol and cloud properties

While we consider the diurnal cycle of solar zenith angles in our DAREcloudy calculations, we use MODIS for underlying COD and cloud Re information as well as a combination of MODIS, OMI and CALIOP for overlying aerosol properties (see section 2.2). By using A-Train satellite observations (i.e., the AQUA, AURA and CALIPSO platforms), with an overpass time of 1:30 PM local time at the Equator, we are only using a daily snapshot of cloud and aerosol properties and not considering their daily variability.

Min and Zhang [2014] show a strong diurnal cycle of cloud fraction over the SEAt region (i.e., a 5-year mean trend of diurnal cloud fraction using SEVIRI that varies from ~60% in the late afternoon to 80% in the early morning on their Fig. 4). According to Min and Zhang [2014] (see their Table 2), assuming a constant cloud fraction derived from MODIS/ AQUA generally leads to an underestimation (less positive) by ~16% in the DAREall-sky calculations (see Eq. 1). Further studies should explore the
implications of diurnal variations of COD and cloud $R_e$ on DARE$_{cloudy}$ results using, for example, geostationary observations from SEVIRI.

Daily variations of aerosol (intensive and extensive) radiative properties above clouds cannot be ignored either. Arola et al. [2013] and Kassaniov et al. [2013] both show that even when the AOD strongly varies during the day, the accurate prediction of 24h-average DARE$_{non-cloudy}$ requires only daily averaged properties. However, in the case of under-sampled aerosol properties, such as when using A-Train derived aerosol properties (this study), the error in the 24h-DARE$_{non-cloudy}$ can be as large as 100% [Kassaniov et al., 2013]. Xu et al. [2016] show that the daily mean TOA DARE$_{non-cloudy}$ is overestimated by up to 3.9 W·m$^{-2}$ in the summertime in Beijing if they use a constant MODIS/ AQUA AOD value, compared to accounting for the observed hourly-averaged daily variability. Kassaniov et al. [2013] propose that using a simple combination of MODIS TERRA and AQUA products would offer a reasonable assessment of the daily averaged aerosol properties for an improved estimation of 24h-DARE$_{non-cloudy}$.

### 4.3. Considering the spatial and temporal variability of cloud and aerosol fields

We have used coarse resolution (i.e., 4°x5°) seasonally gridded aerosol and cloud properties in our DARE$_{OWC}$ calculations (see section 2.2). As a consequence, sub-grid scale variability (or heterogeneity) of cloud and aerosol properties has not been considered. This approach is similar to assuming spatially and temporally homogeneous cloud and aerosol fields in our DARE$_{OWC}$ results.

Marine Boundary Layer (MBL) clouds show significant small-scale horizontal variability [Di Girolamo et al., 2010; Zhang et al., 2011]. Using mean gridded COD in DARE$_{cloudy}$ calculations, for example, can...
lead to significant biases in DARE\textsubscript{cloudy} calculations, an effect called the “plane-parallel albedo bias” 
[e.g., Oreopoulos et al., 2007, Di Girolamo et al., 2010, Zhang et al., 2011, Zhang et al., 2012]. Min and 
Zhang [2014] show that using a mean gridded COD significantly overestimates (by ~10% over the 
SEAt region) the DARE\textsubscript{cloudy} results when the cloud has significant sub-grid horizontal heterogeneity. 
Furthermore, this overestimation increases with increasing AOD, COD and cloud inhomogeneity. 
Future studies should examine the difference between DARE\textsubscript{cloudy} results calculated with gridded mean 
COD and cloud \textit{R}_e values (this study) and DARE\textsubscript{cloudy} results calculated with MODIS Level-3 joint 
histograms of MODIS COD and cloud \textit{R}_e (e.g., similar to Min and Zhang [2014]).

Aerosol spatial variation can be significant over relatively short distances of 10 to 100km, depending on 
the type of environment [Anderson et al., 2003; Kovacs, 2006; Santese et al., 2007; Shinozuka and 
Redemann, 2011; Schutgens et al., 2013]. Shinozuka and Redemann [2011] argue that only a few 
environments can be more heterogeneous than the Canadian phase of the ARCTAS (Arctic Research of 
the Composition of the Troposphere from Aircraft and Satellites) experiment where the airmass was 
subject to fresh local biomass emissions. In this type of environment, they observed a 19% variability of 
the AOD over a 20 km length (comparable in scale to a ~0.1°x0.1° area). They also found a 2% 
variability in the AOD over the same length in a contrasting homogeneous environment that occurred 
after a long-range aerosol transport event. As a consequence, similar to using a mean gridded 
underlying COD and cloud \textit{R}_e, using mean gridded overlying aerosol radiative properties could very 
well bias our DARE\textsubscript{EWC} results.
As a preliminary investigation into the sources and magnitudes of these potential biases, we have used TOA DARE\textsubscript{non-cloudy} (see Eq. 1) estimates derived using well-collocated aerosol properties (hereafter called “retrieve-then-average” or R-A) from a companion study (Redemann et al. [2019]; see section A of the appendix) and compared those to DARE\textsubscript{non-cloudy} estimates computed using seasonally gridded mean aerosol properties at seasonally gridded mean vertical heights (hereafter called “average-then-retrieve” or A-R). Both DARE\textsubscript{non-cloudy} results obtained with the two methods are compared over ocean and at a resolution of 4ºx5º.

A majority (i.e., ~58%) of A-R DARE\textsubscript{non-cloudy} results are within ±35% of the R-A DARE\textsubscript{non-cloudy} results. We find very few (i.e., ~1%) negative R-A DARE\textsubscript{non-cloudy} values paired with positive A-R DARE\textsubscript{non-cloudy} values and very few large differences between both methods (i.e., less than 1% of the differences are above ±10W m\textsuperscript{-2}). However, we find a weak agreement between A-R and R-A DARE\textsubscript{non-cloudy} values during each of the seasons (i.e., a correlation coefficient between 0.21 and 0.34). The A-R DARE\textsubscript{non-cloudy} values are generally biased high relative to the R-A calculations, as illustrated by positive mean and median values of the A-R to R-A differences (respectively 0.64 W m\textsuperscript{-2} and 0.92 W m\textsuperscript{-2}; standard deviation of 2.25). When computing the global seasonal mean A-R and R-A DARE\textsubscript{non-cloudy} values separately, we find that the global seasonal A-R DARE\textsubscript{non-cloudy} values overestimate the global seasonal R-A DARE\textsubscript{non-cloudy} values by 17%, 19%, 21%, and 17% in DJF, MAM, JJA and SON. Moreover, the seasonal median A-R DARE\textsubscript{non-cloudy} values overestimate the seasonal median R-A DARE\textsubscript{non-cloudy} values in all six regions of Table 5 (i.e., median differences between 0.28 W m\textsuperscript{-2} in NWPa in SON and 3.05 W m\textsuperscript{-2} in SEAt in JJA). The geospatial distributions of these differences in DARE calculation strategies are illustrated in Figure 8.
Figure 8: Seasonal maps showing the differences in SW TOA DARE_{non-cloudy} computed using the average-then-retrieve (A-R) and the retrieve-then-average (R-A) strategies. Positive values (in red) show regions where the A-R DARE calculations are larger, whereas negative values (in blue) show regions where the R-A DARE calculations are larger. The squares show different regions defined in Table 5. The title of each map shows the global minimum, maximum, median and mean values.

4.4. Assuming similar intensive aerosol properties above clouds and in near-by cloud-free skies
In the calculation of \( \text{DARE}_{\text{OWC}} \), we assume similar intensive aerosol properties above clouds and in near-by clear skies. This assumption might not be valid and should be investigated in future studies by comparing aerosol properties and their probability distributions over clear and cloudy conditions using observations from the ORACLES field campaign.

4.5. Assuming fixed aerosol and cloud vertical layers

Finally, Long Wave (LW) radiative forcing is particularly dependent on the vertical distribution of aerosols, especially for light absorbing aerosols [Chin et al., 2009]. This is because the energy these aerosols reradiate depends on the temperature, and hence their altitude. For example, Penner et al. [2003] emphasize the importance of soot and smoke aerosol injection height in LW \( \text{TOA DARE}_{\text{all-sky}} \) (see Eq. 1) simulations (higher injection heights tend to enhance the negative LW radiative forcing).

Quijano et al. [2000], Chung et al. [2005] and Chin et al. [2009] demonstrate the importance of an aerosol height, in relation to a cloud height (i.e., the aerosols located above, within or below the clouds) in an accurate estimation of SW \( \text{TOA DARE}_{\text{all-sky}} \). Chung et al. [2005], for example, show that varying the relative vertical distribution of aerosols and clouds leads to a range of global anthropogenic SW \( \text{TOA DARE}_{\text{all-sky}} \) from -0.1 to -0.6 W·m\(^{-2}\) (using a combination of MODIS satellite, AERONET ground-based observations and CTM simulations, see their Table 2).

However, here, we concentrate on cases of aerosol layers overlying clouds in order to compute SW \( \text{TOA DARE}_{\text{cloudy}} \). Aerosol and cloud layer heights are assumed constant over the globe in our study (see...
section 2.2). Future studies should incorporate mean gridded (i.e., 4°x5° in this study)-seasonal CALIOP Level 2 aerosol and cloud vertical profiles into the calculation of DARE_{OBC}.

However, constraining clouds between 2 and 3 km in our study does not seem unreasonable as our AAC AOD calculations using the DR method can only be applied to aerosols overlying specific low opaque water clouds with, among other criteria, an altitude below 3 km (see Table B2). On the other hand, constraining aerosols between 3 and 4 km in our study is not realistic over many parts of the globe (e.g., see Fig. 7 of Devasthale et al. [2011]). For example, over the region of South East Atlantic during the ORACLES campaign, the HSRL team observed an aerosol layer located in average between 2 and 5 km, and overlying a cloud at an average altitude of 1.2 km.

According to Zarzycki et al. [2010], the underlying cloud properties are orders of magnitude more crucial to the computation of DARE_{clouds} than the location of the aerosol layer relative to the cloud, as long as the aerosol is above the cloud. In other words, the forcing does not seem to depend on the height of the aerosols above clouds as much as other parameters such as the AOD, SSA or cloud albedo. Zarzycki et al. [2010] investigated this assumption and found that over low and middle clouds, forcing changed by ~1-3% through the heights where the Black Carbon burden was the largest. These small changes in forcing are likely products of a change in atmospheric transmission above the aerosol layer [Haywood and Ramaswamy, 1998] (e.g., a change in the aerosol height is linked to a change in the integrated column water vapor above the aerosol layer and this, in turn, would alter the incident solar radiation).
5. Conclusions

We have computed a first approximation of global seasonal TOA short wave Direct Aerosol Radiative Effects (DARE) above Opaque Water Clouds (OWCs), DARE\textsubscript{OWC}, using observation-based aerosol and cloud radiative properties from a combination of A-Train satellite sensors and a radiative transfer model. Our DARE\textsubscript{OWC} calculations make three major departures from previous peer-reviewed results:

1. They use extensive aerosol properties derived from the Depolarization Ratio, DR, method applied to Level 1 CALIOP measurements, whereas previous studies often use CALIOP Level 2 standard products which introduce higher uncertainties and known biases;
2. Our DARE\textsubscript{OWC} calculations are applied globally, while most previous studies focus on specific regions of high AAC occurrence such as the SE Atlantic; and
3. Our calculations use intensive aerosol properties retrieved from a combination of A-Train satellite sensor measurements (e.g., MODIS, OMI and CALIOP).

Our study agrees with previous findings on the locations and seasons of the maximum occurrence of AAC over the globe. We identify six regions of high AAC occurrence (i.e., AAC hotspots): South and North East Pacific (SEAt and NEPa), Tropical and South East Atlantic (TAt and SEAt), Indian Ocean offshore from West Australia (InWA) and North West Pacific (NWPa). We define $\tau\text{DR}_{\text{AAC}}$, the Aerosol Optical Depth (AOD) above OWCs using the DR method on CALIOP measurements, $f_{\text{AAC}}$, and the frequency of occurrence of AAC cases. We record a majority of $\tau\text{DR}_{\text{AAC}} \times f_{\text{AAC}}$ values at 532nm in the 0.01-0.02 range and that can exceed 0.2 over a few AAC hotspots. We find positive averages of global seasonal DARE\textsubscript{OWC} between 0.13 and 0.26 W\textcdot m\textsuperscript{-2} and an annual global mean DARE\textsubscript{OWC} value of 0.20 W\textcdot m\textsuperscript{-2} (i.e., a warming effect on climate). Regional seasonal...
DARE\textsubscript{OWC} values range from -0.06 W m\(^{-2}\) in the Indian Ocean, offshore from western Australia (in March-April-May) to 2.87 W m\(^{-2}\) in the South East Atlantic (in September-October-November). High positive values are usually paired with high aerosol optical depths (>0.1) and low single scattering albedos (<0.94), representative of e.g. biomass burning aerosols.

Although the DARE\textsubscript{OWC} estimates in this study are not directly comparable to previous studies because of different spatial domain, period, satellite sensors, detection methods, and/or associated uncertainties, we emphasize that they are notably higher than the ones from [Zhang et al., 2016; Matus et al., 2015 and Oikawa et al., 2013]. In addition to differences in satellite sensors, AAC detection methods, and the assumptions enforced in the calculation of DARE\textsubscript{cloudy}, there are several other factors that may contribute to the overall higher DARE\textsubscript{OWC} values we report in this study. The most likely contributors are (1) a possible underestimate of the number of dust-dominated AAC cases; (2) our use of the DR method on CALIOP Level 1 data to quantify the AAC AOD; and, in particular, (3) the technique we have chosen for aggregating sub-grid aerosol and cloud spatial and temporal variability. We discuss each of these in turn in the following paragraphs.

Two factors seem to be preventing the DR method from recording enough AAC cases in these regions: the low cloud optical depths of underlying clouds and very few cases of “clear air” above clouds. The DR method used in this study is restricted to aerosols above OWCs that satisfy a long list of criteria. The AAC dataset in this study underestimates (i) the total number of CALIOP 5 km profiles that contain AAC over all OWCs (i.e., not just suitable to the DR technique), (ii) the total number of CALIOP 5 km profiles that contain AAC over any type of clouds over the globe and (iii) the true global
occurrence of AAC over any type of clouds. To the best of our knowledge, the true amount of AAC in (i), (ii) and (iii) remains unknown. A better characterization of the “unobstructed” OWCs in the application of the DR technique on CALIOP measurements might bring us closer to answering (i). A combination of CALIOP standard, DR and CR techniques together with airborne observations (e.g., from the ORACLES field campaign) might answer (ii). Finally, (iii) cannot be answered with the only use of CALIOP observations. The results in this study should be combined with aerosol-above-cloud retrievals from passive satellite sensors (e.g. POLDER [Waquet et al., 2013a,b, Peers et al., 2015, Deaconu et al., 2017] or MODIS [Meyer et al., 2013, Zhang et al., 2014, 2016]) and model simulations [Schulz et al., 2006] to obtain a more complete global quantification and characterization of aerosol above any type of clouds.

Compared to other methods, the DR technique applied to CALIOP measurements retrieves $\tau_{\text{DR/AAC}}$ with fewer assumptions and lower uncertainties. Other global DAREcloud results (e.g., Matus et al. [2015] and Zhang et al. [2016]) use CALIOP standard products to detect the AAC cases, quantify the AAC AOD and define the aerosol type (and specify the aerosol intensive properties). These studies rely on the presence of aerosol in concentrations sufficient to be identified by the CALIOP layer detection scheme, and on the ability of the CALIOP aerosol subtyping algorithm to correctly identify the aerosol type and thus select the correct lidar ratio for the AOD retrieval. While several recent studies have taken various approaches to quantifying the amount of aerosol currently being undetected in the CALIOP backscatter signals, their general conclusions are unanimous. The CALIOP standard products underestimate above-cloud aerosol loading and the corresponding AAC AOD (Kacenelenbogen et al.,
and this in turn leads to underestimates of both $\text{DARE}_{\text{non-cloudy}}$ and $\text{DARE}_{\text{cloudy}}$ (Thorsen and Fu, 2015; Thorsen et al., 2017).

In this study, we have assumed spatially and temporally homogeneous clouds and aerosols in our DARE$_{\text{OWC}}$ calculations. As a preliminary investigation of such effects on our calculations, we have compared DARE calculations derived from well collocated aerosol properties (retrieve-then-average) to DARE calculations using seasonally gridded mean aerosol properties (average-then-retrieve). We have shown that the average-then-compute DARE results generally overestimate the retrieve-then-average results both on a global scale and in each of our selected regions. Further research and analysis are required to determine which of these two computational approaches provides the most accurate estimates of real-world DARE.
Appendix A: Method to obtain aerosol radiative properties in non-cloudy (i.e., clear-sky) conditions using MODIS, OMI and CALIOP and to estimate DARE_{non-cloudy}.

A companion paper, Redemann et al. [2019], develops and refines a method for retrieving full spectral (i.e., at 30 different wavelengths) extinction coefficients, Single Scattering Albedo (SSA) and asymmetry parameters from satellite aerosol products in non-cloudy (i.e., clear-sky) conditions. The method requires colocation of quality-screened satellite data, selection of aerosol models that reproduce the satellite observations within stated uncertainties, and forward calculation of aerosol radiative properties based on the selected aerosol models. They use MODIS-Aqua AOD at 550 and 1240 nm, CALIPSO integrated backscattering (IBS) at 532 nm and OMI Absorption Aerosol Optical Depth (AAOD) at 388 nm (see Table A1). The aerosol radiative properties resulting from this method are called MOC retrievals (for MODIS-OMI-CALIOP).
Table A1. Data sets currently used for global MODIS-OMI-CALIOP (MOC) retrievals of aerosol radiative properties [Redemann et al., 2019]; DT: Dark Target and EDB: Enhanced Deep Blue.

<table>
<thead>
<tr>
<th>Product</th>
<th>Source</th>
<th>Assumed Uncertainties*</th>
<th>Weight*,**</th>
</tr>
</thead>
<tbody>
<tr>
<td>550 nm AOD</td>
<td>MODIS Collection 6 (Ocean, DT-Land, EDB-Land)</td>
<td>±5% ± 30 Mm⁻¹</td>
<td>0.1488</td>
</tr>
<tr>
<td>1240 nm AOD</td>
<td>MODIS Collection 6 (extrapolated spectrally over land)</td>
<td>±5% ± 30 Mm⁻¹</td>
<td>0.1422</td>
</tr>
<tr>
<td>388 nm AAOD</td>
<td>OMI (OMAERO for ocean, OMAERUV for DT-land), MODIS EDB</td>
<td>±30% ± 50 Mm⁻¹</td>
<td>0.5542</td>
</tr>
<tr>
<td>532 nm IBS</td>
<td>CALIPSO V3-01</td>
<td>±30% ± 0.1 Mm⁻²sr⁻¹</td>
<td>0.1548</td>
</tr>
</tbody>
</table>

* For the values after division by CALIPSO layer depth
** The weight, \( w_i \), is used to calculate the cost function \( \chi = (\Sigma w_i (x - \hat{x}_i)^2)^{1/2} \) where \( x \) are the retrieved parameters, \( \hat{x}_i \) are the observables, and \( \sigma_i \) are the uncertainties in the observables.

The choice of OMI satellite algorithms (see Table A1) reflects their assessment of the representativeness of subsampling OMI data along the CALIPSO track; i.e., they compared the probability distribution (PDF) of the OMI retrievals along the CALIPSO track to the global PDF and chose the data set that had the best match between global and along-track PDF for the over-ocean and two over-land data sets, the latter being different in their use of MODIS dark target (DT) versus enhanced Deep-Blue (EDB) data as the source of AOD. They collocate the MODIS and OMI products within a 40x40 km² box centered at each CALIPSO 5-km profile location after Redemann et al. [2012].
For the OMAERUV data set, they choose the SSA product for the layer height indicated by the collocated CALIOP backscatter profile. Their aerosol models emulate those of the MODIS aerosol over-ocean algorithm [Remer et al., 2005]. Like the MODIS algorithm, they define each model with a lognormal size distribution and wavelength-dependent refractive index. They then combine two of these models, weighted by their number concentration, and compute optical properties for the bi-modal lognormal size distribution. Unlike the MODIS algorithm, they allow combinations of two fine-mode or two coarse-mode models. They use ten different aerosol models, which stem from some of the MODIS over-ocean models [Remer et al., 2005] but include more absorbing models, which was motivated by application of their methodology to the Arctic Research of the Composition of the Troposphere from Aircraft and Satellites (ARCTAS) field campaign data, requiring more aerosol absorption than included in the current MODIS over-ocean aerosol models. They use MOC spectral aerosol radiative properties to then calculate Direct Aerosol Radiative Effects (i.e., DARE\textsubscript{non-cloudy}, see Eq. 1) through a delta-four stream radiative transfer model with fifteen spectral bands from 0.175 to 4.0 µm in SW and twelve longwave (LW) spectral bands between 2850 and 0 cm\(^{-1}\) [Fu and Liou, 1992].

In order to use these MOC parameters (retrieved in clear-skies) in our DARE\textsubscript{OWC} calculations, we need to assume similar aerosol intensive properties in clear skies compared to above clouds and we need to spatially and/or temporally grid these MOC parameters. As discussed in section 2.2, we use seasonally averaged MOC spectral SSA, aerosol asymmetry parameter, and extinction retrievals on 4°x5° grids. Figure A1 illustrates seasonal maps of MOC SSA used in our calculations of DARE\textsubscript{OWC}.
Figure A1: Seasonal maps of MOC SSA at 546.3 nm in 2007 used in the calculations of DARE\textsubscript{OWC}.

The squares show different regions defined in Table 5.

The DARE\textsubscript{OWC} calculations in our study also require information about the underlying cloud optical properties. As discussed in section 2.2, we use seasonally mean gridded COD from MODIS such as illustrated in Figure A2.
Figure A2: Seasonal maps of COD used in the calculations of DARE\textsubscript{OWC}. COD information is inferred from MODIS seasonally averaged monthly 1°x1° grids (i.e. liquid water cloud products of MYD08\_M3: “Cloud Effective Radius Liquid Mean Mean” and “Cloud Optical Thickness Liquid Mean Mean” [Platnick et al. 2015]) from 2008 to 2012. The squares show different regions defined in Table 5.

**Appendix B: Method for AAC detection and AAC AOD computation**

The depolarization ratio (DR) method [Hu et al., 2007b] used to derive estimates of the optical depths (τ) of aerosols above clouds (AAC) is given in Eq. (2) and repeated here for convenience:

\[
\tau_{\text{DR\_AAC}} = -0.5 \times \ln[\text{IAB\textsubscript{OWC}\_SS\_AAC} / \text{IAB\textsubscript{OWC}\_SS\_CAC}]
\]  

(B1)
The subscripts SS and CAC represent, respectively, 'single scattering' and 'clear above clouds'. IAB^{\text{OWC}_{SS}} (i.e., either IAB^{\text{OWC}_{SS, AAC}} or IAB^{\text{OWC}_{SS, CAC}}) is the single scattering integrated attenuated backscatter (IAB), derived from the product of the measured 532 nm attenuated backscatter coefficients integrated from cloud top to cloud base, IAB^{\text{OWC}}, and a layer effective multiple scattering factor, $\eta^{\text{OWC}}$, derived from the layer-integrated volume depolarization ratio of the water cloud (called $\delta^{\text{OWC}}$) using:

$$\eta^{\text{OWC}} = \left[(1-\delta^{\text{OWC}})(1+\delta^{\text{OWC}})\right]^2$$ \hspace{1cm} (B2)

[Hu et al., 2007a]. The single scattering IAB is thus derived using:

$$\text{IAB}^{\text{OWC}_{SS,X}} = \eta^{\text{OWC}} \times \text{IAB}^{\text{OWC}_{\text{measured},X}}$$ \hspace{1cm} (B3)

for both aerosol above cloud cases ($X = \text{AAC}$) and those cases with clear skies above ($X = \text{CAC}$). An assumption of the DR method is that $\delta^{\text{OWC}}$ is negligibly affected by any aerosols that lie in the optical path between the OWC and the lidar.

Table B1 provides a high-level overview of the procedure we use to compute aerosol optical depth ($\tau^{\text{DR}_{\text{AAC}}}$) above OWCs over the globe. We chose to concentrate on night-time CALIOP observations only, as they have substantially higher signal-to-noise ratios (SNR) than the daytime measurements [Hunt et al., 2009].

Table B1: Steps required to compute $\tau^{\text{DR}_{\text{AAC}}}$. (*) we construct global maps of 4 x 5º pixels using median values. Superscripts 1 and 2 denote respectively CALIOP Level 1 and Level 2 aerosol or cloud layer products.
<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
<th>CALIOP, GEOS-5 and other computed products that are used in each step</th>
<th>More detail</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>Select specific Opaque Water Clouds (OWC) suitable for the DR technique</td>
<td>CAD Score(^2), Integrated Attenuated Backscatter Uncertainty (532)(^1), Integrated Volume Depolarization Ratio Uncertainty(^2), Horizontal Averaging, Opacity Flag(^2), Feature Classification Flags(^2), Layer Top Altitude(^2), Layer Top Temperature(^2), Surface Wind Speed(^2)</td>
<td>section B1, Table B2</td>
</tr>
<tr>
<td>S2</td>
<td>Select a subset of OWCs from (S1) with clear air above</td>
<td>Overlying Integrated Attenuated Backscatter (532)(^2), simulated molecular layer-integrated attenuated backscatter [Powell et al., 2002 and 2006] and OWCs from (S1)</td>
<td>section B2</td>
</tr>
<tr>
<td>S3</td>
<td>Process seasonal maps of median IAB(532)(<em>{SS,CAC}) and record number of IAB(532)(</em>{SS,CAC}) values per grid cell (^(*))</td>
<td>Integrated Attenuated Backscatter (532)(^2), Integrated Volume Depolarization Ratio(^2), and OWCs with clear air above from (S2)</td>
<td>section B3</td>
</tr>
<tr>
<td>S4</td>
<td>Compute (t_{DR}^{AAP}) along track</td>
<td>Total Attenuated Backscatter (532)(^1), Molecular Number Density(^1), Ozone Number Density(^1) Integrated Attenuated Backscatter (532)(^2), Integrated Volume Depolarization Ratio(^2), Layer Top Altitude(^2), Layer Base Altitude(^2) and seasonal maps of IAB(532)(_{SS,CAC}) from (S3)</td>
<td>Eq. (2) or Eq. (B1)</td>
</tr>
<tr>
<td>S5</td>
<td>Process seasonal maps of median (t_{DR}^{AAP}) and record number of (t_{DR}^{AAP}) values per grid cell (^(*))</td>
<td>(t_{DR}^{AAP}) of (S4) and we filter using number of IAB(532)(_{SS,CAC}) values per grid cell and per season from (S3)</td>
<td>Results in section 3.2</td>
</tr>
</tbody>
</table>

The first step (S1) is to identify OWCs that are suitable for the application of the DR method. The acceptance criteria used to identify these clouds are described below in section B1 and listed in Table B2. In the second step (S2), we use the overlying integrated attenuated backscatter (i.e., the 532 nm...
attenuated backscatter coefficients integrated from TOA to the OWC cloud tops) to partition the OWC into two classes: (i) “unobstructed” clouds, for which the magnitude of the overlying IAB suggests that only aerosol-free clear skies lie above; and (ii) “obstructed” clouds for which we expect to be able to retrieve positive estimates of $I_R^{\text{AAC}}$. Section B2 describes the objective method we have developed to separate unobstructed clouds (for which we can compute $I_R^{\text{OWC}_{\text{SS,CAC}}}$) from obstructed clouds (for which we calculate $I_R^{\text{OWC}_{\text{SS,AAC}}}$).

In step (S3), we construct global seasonal maps of median $I_R^{\text{OWC}_{\text{SS,CAC}}}$ using 5 consecutive years (2008-2012) of CALIOP nighttime data (see section B3). By doing this we can subsequently compute estimates of $I_R^{\text{AAC}}$ without invoking assumptions about the lidar ratios of water clouds in clear skies [Hu et al., 2007]. Throughout this study, we chose to compute global median values within each grid cell (instead of mean values) to limit the impact of particularly high or low outliers on our statistics.

In step (S4), we compute estimates of $I_R^{\text{AAC}}$ for all obstructed OWC within each grid cell using Eq. (2) or Eq. (B1) and the 5-year nighttime seasonal median values of $I_R^{\text{OWC}_{\text{SS,CAC}}}$ from (S3) (i.e., each $I_R^{\text{AAC}}$ value along the CALIOP track is computed using one median value of $I_R^{\text{OWC}_{\text{SS,CAC}}}$ per 4°x5° pixel and per season).

For the OWCs considered in this study, true layer base cannot be measured by CALIOP, simply because the signal becomes totally attenuated at some point below the layer top. Instead, what is reported in the CALIOP data products is an apparent base, which indicates the point at which the signal was essentially indistinguishable from background levels. Numerous validation studies have established the accuracy of the CALIOP cloud layer detection scheme (e.g., McGill et al., 2007; Kim et al., 2011;
Thorsen et al., 2011; Yorks et al., 2011; Candlish et al., 2013). Strong attenuation of the signal by optically thick aerosols above an OWC can, in some cases, introduce biases into the cloud height determination, which would lead to misestimates of $IAB^{OWC}$ and subsequent errors in $\tau^{DR,\text{WE}}$. To ensure the use of consistent data processing assumptions throughout our retrievals of $IAB^{DR}_{\text{AAC,WE}}$, we recalculated the components of $IAB^{OWC}$ (i.e., the “Integrated Attenuated Backscatter 532” and “Integrated Volume Depolarization Ratio”) using parameters in the CALIOP Level 1 product (“Total Attenuated Backscatter 532”, “Molecular Number Density” and “Ozone Number_Density”) and optimized estimates of cloud top and base altitudes based on the “Layer Top Altitude” and “Layer Base Altitude” values reported in the CALIOP Level 2 layer product.

Apart from the identification of specific OWCs in step (S1), the primary Level 2 CALIOP parameters used to calculate $\tau^{DR,\text{AAC}}$ (S2-S4 in Table B1) are (i) the integrated attenuated backscatter above cloud top to detect “clear air” cases (i.e. “Overlying Integrated Attenuated Backscatter 532” in step (S2)), (ii) the layer integrated attenuated backscatter of the OWC with clear air above (i.e. “Integrated Attenuated Backscatter 532” in step (S3)) and (iii) the cloud multiple scattering factor, derived as a function of the layer integrated volume depolarization ratio (i.e. the “Integrated Volume Depolarization Ratio” in S3 and S4).

Below, we list the potential sources of errors associated with those three products:

(a) the accuracy of the 532 nm channel calibrations,

(b) the signal-to-noise ratio (SNR) of the backscatter data within the layer,

(c) the estimation of molecular scattering in the integrated attenuated backscatter (section 3.2.9.1 of the

\[ (c) \] the estimation of molecular scattering in the integrated attenuated backscatter (section 3.2.9.1 of the...
CALIPSO Feature Detection ATBD, http://www-calipso.larc.nasa.gov/resources/pdfs/PC-SCI-202_Part2_rev1x01.pdf, and

(d) the accuracy of the depolarization calibration (see section 5 in Powell et al., [2009]).

Concerning (a), Rogers et al. [2011] show that the NASA LaRC HSRL and CALIOP Version 3 532 nm total attenuated backscatter agree on average within ~3%, demonstrating the accuracy of the CALIOP 532 nm calibration algorithms.

Concerning (b), we assume the influence of the SNR returned from the OWC is negligible as the OWCs are strongly scattering features and our dataset is composed of nighttime data only. However, the backscatter from tenuous and spatially diffuse aerosol layers with large extinction-to-backscatter ratios can lie well beneath the CALIOP attenuated backscatter detection threshold. When such layers lie above OWCs, the measured overlying integrated attenuated backscatter can fall within one standard deviation of the expected ‘purely molecular’ value that is used to identify CAC (or “unobstructed”) OWC in our dataset (S2; see Sect. B2). Within the context of this study, these tenuous and spatially diffuse aerosol layers can have appreciable AOD, and thus care must be taken to ensure that these sorts of cases are not misclassified as CAC OWC. Section B3 discusses such cases, possibly found, for example, over the region of SEAt.

B1. Select specific Opaque Water Clouds suitable for DR technique
Successful application of the DR method (Eq. 2 or Eq. B1) requires a very specific type of underlying cloud (step (S1) in Table B1). Table B2 lists the criteria we have applied to the CALIOP 5 km cloud layer products for the selection of these specific OWCs over the globe.

Table B2: Criteria used to select the Opaque Water Clouds (OWC) for the application of the DR method to obtain the AAC frequency of occurrence, AAC optical depth, AAC lidar ratio and DARE\textsubscript{OWC} in this study.

<table>
<thead>
<tr>
<th>criteria</th>
<th>metric</th>
<th>interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>C1</td>
<td>Number of cloud layers = 1</td>
<td>a single cloud in each column</td>
</tr>
<tr>
<td>C2</td>
<td>High CALIOP cloud-aerosol discrimination (CAD) score (90 ≤ CAD ≤ 100) and high SNR (IAB SNR &gt; 159, δ\textsubscript{OWC} SNR &gt; 2)</td>
<td>highly confident of cloud classification</td>
</tr>
<tr>
<td>C3</td>
<td>Cloud detected at 5 km averaging resolution with CALIOP single shot cloud cleared fraction = 0</td>
<td>cloud is spatially uniform over a 5 km averaging interval</td>
</tr>
<tr>
<td>C4</td>
<td>CALIOP opacity flag = 1; surface wind speed &lt; 9 m/s</td>
<td>cloud is opaque</td>
</tr>
<tr>
<td>C5</td>
<td>CALIOP phase classification is high confidence water; δ\textsubscript{OWC} &lt; 0.5; cloud top altitude &lt; 3 km; cloud top temperature ≥ -10° C</td>
<td>highly confident of cloud phase identification (water)</td>
</tr>
</tbody>
</table>

We ensure that each cloud is the only cloud detected within the vertical column (C1) and is guaranteed to be of high quality by imposing filters on various CALIOP quality assurance flags (C2). Imposing the “single shot cloud cleared fraction = 0” in criterion (C3) assures that the clouds are uniformly detected at single shot resolution throughout the full 5 km (15 shot) horizontal extent. As a result, we will
intentionally miss any broken clouds and any clouds that show a weaker scattering intensity within one
or more laser pulses with the 15 shot average. On the other hand, enforcing the single shot cloud
fraction = 0 criteria simultaneously ensures that all $\tau_{\text{DR, AAC}}$ values in this study will lie below a certain
threshold: larger values would attenuate the signal to the point that single shot detection of underlying
clouds is no longer likely. Consequently, some highly attenuating biomass burning events (e.g., with
$\tau_{\text{DR, AAC}} > 2.5$) can be excluded from the cases considered here.

At high surface wind speeds over oceans, the CALIOP V3 layer detection algorithm may fail to detect
surface backscatter signals underneath optically thick but not opaque layers. In such cases, CALIOP’s
standard algorithm may misclassify the column as containing an opaque overlying cloud. To avoid such
scenarios, we exclude all the cases with high surface wind conditions (C4). Let us note that this
condition was applied on the entire dataset, disregarding the surface type (i.e. land or ocean), as our
OWC dataset resides mostly over ocean surfaces (see Figure 1b).

Criterion (C5) requires that the OWC be both low enough (cloud top below 3 km) and warm enough
(cloud top temperature above -10°C as in Zelinka et al. [2012]) to ensure that it is composed of liquid
water droplets. After applying all the criteria of Table B2, the median OWC top height of our dataset is
~1.6 km. According to Hu et al. [2009], any feature showing a cloud layer integrated volume
depolarization ratio above 50% should correspond to an ice cloud with randomly oriented particles.
Criterion (C5) assures the deletion of such cases.

The averaged single-layer, high QA, uniform cloud (i.e. C1-C3 in Table B2) has a top altitude of ~8
km, a top temperature around -38°C and mean surface winds of ~6 m s$^{-1}$. Selecting only those clouds
with top temperatures above -10º C removes 30-40% of the observations. Subsequently filtering out clouds with top heights above 3 km removes an additional 30% of the observations. Finally, filtering out clouds with underlying winds above 9 m s\(^{-1}\) deletes another 20% of the observations. Among all single-layer, high QA, uniform clouds (i.e. C1-C3 in Table B2), we find that ~45-50% are opaque clouds (C4), and that ~11-12% satisfy all criteria (C1-C5) of Table B2.

**B2. Select a subset of Opaque Water Clouds with clear air above**

To distinguish between OWCs having clear skies above (i.e., unobstructed clouds, see S2 in Table B1) and those having overlying aerosols, we examine the overlying integrated attenuated backscatter reported in the CALIOP Level 2 cloud layer products. The total Integrated Attenuated Backscatter (IAB) value above a cloud (i.e., IAB\(_{\text{aboveCloud}}^\text{tot}\)) can be written as follows:

\[
IAB_{\text{aboveCloud}}^\text{tot} = \int_0^{\text{cloudtop}} \left[ \beta_a(r) T_a^2(0,r) T_a^2(0,r) \right] dr + \int_0^{\text{cloudtop}} \left[ \beta_m(r) T_m^2(0,r) T_m^2(0,r) \right] dr \tag{B4}
\]

Here \(\beta_a(r)\) and \(\beta_m(r)\) are, respectively, the aerosol and the molecular backscatter coefficients (km\(^{-1}\) sr\(^{-1}\)) at range \(r\) (km), and \(T_a^2(0,r)\) and \(T_m^2(0,r)\) are the two-way transmittances between the lidar (at range \(r = 0\)) and range \(r\) due to, respectively, aerosols and molecules.

Figure B1 shows simulated profiles of the integrated attenuated backscatter above any given altitude, \(z\), (IAB\(_{\text{mol, above z}}^\text{above z}\)) for a purely molecular atmosphere for both daytime (solid green curve) and nighttime conditions (dashed green curve). These data were generated by the CALIPSO lidar simulator [Powell et al., 2002; Powell, 2005; Powell et al., 2006] using molecular and ozone number density profiles.
obtained from the GEOS-5 atmospheric data products distributed by the NASA Goddard Global Modeling and Assimilation Office (GMAO). The error envelopes at ±1 standard deviation (light blue curves) and ±1.5 standard deviation (dark blue curves) around the mean represent measurement uncertainties for CALIPSO profiles averaged to a nominal horizontal distance of 5 km. The mean IAB$^{mol}_{above \, z}$ profiles represent an average of all data along the CALIPSO orbit track on 17 March 2013 that began at 03:29:28 UTC and extended from 78.8°N, 20.3°E to 77.3°S, 77.0°W. Spot checks of mean IAB$^{mol}_{above \, z}$ profiles from different seasons show variations of ~10% or less, depending on latitude, for altitudes of 3 km and below. The largest differences are found poleward of 30°. While the daytime and nighttime mean values are, as expected, essentially indistinguishable from one another, the error envelopes differ drastically due to the influence of solar background noise during daylight measurements. In this study, we use nighttime measurements only.

**Figure B1**: Nighttime (solid) and daytime (dashed) simulated vertical profile of integrated attenuated backscatter above any given altitude, z, IAB$^{mol}_{above \, z}$ (green curve). The light blue (respectively dark
blue) envelope shows 1 (respectively 1.5) standard deviation (σ) around the IAB$_{\text{mol, above z}}$ profile. Data was generated by the CALIPSO lidar simulator [Powell et al., 2002 and 2006]. The IAB$_{\text{mol, above z}}$ value associated to the median OWC top height of ~1.6 km in our dataset corresponds to 0.0093 sr$^{-1}$.

In this study, we assume “clear air” when IAB$_{\text{tot, above Cloud}}$ is within the simulated IAB$_{\text{mol, above Cloud}}$ value ± 1σ (i.e., the light blue envelope shown in Figure B1). This definition of “clear air above” conditions is somewhat more restrictive than those imposed in previous studies. For example, Liu et al. [2015] conducted an extensive study of AAC optical depths and lidar ratios using CALIOP measurements over the tropical and southeast Atlantic. To identify clear air above cloud cases, Liu et al. [2015] require that the integrated attenuated scattering ratio, defined as

$$\text{ASR} = \frac{\int_{0}^{\text{OWC top}} \left( \beta_{m}(r) + \beta_{d}(r) \right) \rho_{m}(0,r) \rho_{d}(0,r) \, dr}{\int_{0}^{\text{OWC top}} \beta_{m}(r) \rho_{m}(0,r) \, dr}$$

(B5)

, fall within the range of 0.95 < ASR < 1.05, irrespective of cloud top altitude. For comparison, at the maximum OWC top altitude used in our analyses (3 km), $\text{IAB}_{\text{mol, above Cloud}}$ / $\text{IAB}_{\text{mol, above Cloud}}$ = 1 ± 0.0380. This restriction tightens for lower cloud top heights; e.g., at our mean OWC top altitude of 1.6 km, $\text{IAB}_{\text{mol, above Cloud}}$ / $\text{IAB}_{\text{mol, above Cloud}}$ = 1 ± 0.0325.

The pioneering study by Chand et al. [2008], who first used the CALIOP DR method to assess the radiative effects of aerosols above clouds, took a different approach to identifying “clear above cloud” cases. Rather than examining the overlying IAB, they instead assumed clear air above conditions.
whenever $IAB^{OWCSS} > 0.025 \text{ sr}^{-1}$. As will be shown in section B3, in addition to the $IAB^{mol}_{aboveCloud}$ limits cited above, our study also enforces limits on $IAB^{OWCSS,CAC}$. This combination of limits on both $IAB^{mol}_{aboveCloud}$ and $IAB^{OWCSS,CAC}$ serves to more effectively reject aerosol-contaminated profiles from the “clear above” data set than either one alone.

B3. Process median seasonal maps of Integrated Attenuated Backscatter of Opaque Water Clouds showing Clear Air Above

Once we select specific OWCs (i.e., that satisfy the criteria of Table B2) and define which ones are “unobstructed” (see section B2), we can easily compute $IAB^{OWCSS,CAC}$ by using Eq. (B3). For clouds that totally attenuate the lidar signal (i.e., cloud optical depths greater than $\sim 6$ [Young et al., 2018]), $IAB^{OWCSS,CAC}$ in Eq. (2) or Eq. (B1) is related to the OWC lidar ratio (called $S_c$), so that

$$S_c = \frac{1}{(2 \times n^{OWC} \times IAB^{OWC,CAC})} = \frac{1}{(2 \times IAB^{OWCSS,CAC})}$$

where $n^{OWC}$ is the refractive index of the water cloud and $IAB^{OWC,CAC}$ is the Integrated Attenuated Backscatter of Opaque Water Clouds showing Clear Air Above.

[Platt, 1973]. OWC $S_c$ values are relatively stable at the visible and near infrared wavelengths [Pinnick et al., 1983, O’Connor et al., 2004], but show large variations over land [Pinnick et al., 1983; Hu et al., 2006]. $S_c$ is known to vary as a function of cloud droplet microphysics, and is especially sensitive to cloud droplet effective radius ($R_e$) and the imaginary part of the refractive index (see Fig. 8 of Deaconu et al. [2017]). Hu et al., [2006], Liu et al. [2015] and Deaconu et al. [2017] show that a decrease of $R_e$ is often paired with an increase of estimated $S_c$ at 532 nm for pure, non-aerosol-contaminated water clouds (i.e., cloud droplets having an imaginary refractive index of 0).
As an example, Figure B3a shows the median nighttime CALIOP $S_c$ values over the globe during 2008. Figure B3b shows MODIS AQUA-derived mean liquid water $R_e$ in 2008 (using MODIS Level 3 monthly product “Cloud Effective Radius Liquid Mean Mean”).

**Figure B3:** a) Global CALIOP yearly median nighttime “unobstructed” (i.e. clear air above) OWC lidar ratio, $S_c$, in 2008 that satisfy all criteria of Table B2. For the reasons outlined in this section, any OWC along the CALIOP track for which $S_c > 20$ sr or $S_c < 14$ sr is deleted before temporal and spatial averaging. White pixels show a limited number of OWCs; b) Global MODIS yearly mean daytime liquid water cloud droplet effective radius, $R_e$ (in $\mu$m, “Cloud Effective Radius Liquid Mean Mean” parameter from MODIS MYD08_M3 product).
Greater S_c values paired with lower cloud R_e can be seen offshore and close to the west coasts of Africa and the Americas on Figure B3. Other notable regions of low cloud R_e and high S_c on Figure B3 are above industrial regions like northern Europe, the eastern US and South East Asia. These results appear to support Twomey’s analysis [Twomey, 1977; Rosenfeld and Lensky, 1998], showing an enhancement of the cloud albedo through the increase of droplet number concentration and a decrease in the droplet size driven by increased aerosol concentration. On the other hand, Figure B3a mostly exhibits low S_c values (paired with large R_e) over the inter-tropical convergence zone (ITCZ), likely associated with deep convective regimes. In addition, Figure B3a generally shows larger OWC S_c values in the northern hemisphere than in the southern hemisphere, which we attribute to differences in sources of cloud condensation nuclei. Figure B3b shows patterns that are generally similar to those in Figure B3a, but of opposite intensity. Let us note that the polarization measurements from the space-borne POLDER sensor [Deschamps et al., 1994] were also used to estimate R_e of liquid water clouds over the globe [Bréon and Cozzy, 2000] and seem to be in qualitative agreement with the findings of Figure B3b.

During our assessment of 5 years of CALIOP data over the globe, we have observed significantly higher “unobstructed” OWC S_c values (i.e., S_c > 20 sr, not shown on Fig B3a) near the coasts of West Africa and over the region of SE Asia (e.g., see Young et al., [2018]). These may be physically plausible and either (1) associated with small cloud R_e, resulting from the Twomey’s effect as explained above or (2) associated with the presence of light-absorbing aerosols residing within the OWCs [Mishchenko et al., 2014; Chylek and Hallett, 1992; Wittbom et al., 2014]. These aerosols would be undetected in our IAB^mod_abovCloud clear air selection method (see section B2) and would impact the chemical composition of the cloud droplets, modifying their backscattered light. The latter is well...
illustrated in Fig. 8 of Deaconu et al. [2017], which shows simulations of cloud $S_c$ with an imaginary part of the refraction index equals to 0.0001, as a function of cloud droplet effective radius. Other reasons for these unusually high $S_c$ values could be the sources of uncertainty noted (a), (b), (c) and (d) in the beginning of section B, with (c) (i.e., the SNR of the backscatter data within the layer) possibly having a much higher impact on $S_c$ than all other factors. An additional source of uncertainty on the retrieval of $S_c$ could be a failure of the CALIPSO surface detection scheme. If CALIOP fails to detect the surface adequately, part of the Earth’s surface could be misclassified as an opaque water cloud and these misclassified clouds would have abnormally high $S_c$.

Let us note that the vast majority of the $S_c$ values reported in the literature (i.e., in Hu et al., [2006], Liu et al. [2015] and Deaconu et al., [2017]) are estimated using a Mie code and not directly measured. However, none of these results show $S_c$ values above 20 sr for non-aerosol-contaminated OWCs. On the other hand (and to add a lower bracket on our OWC $S_c$ calculations), none of these results show $S_c$ values below 14 sr. For this reason, we have imposed an additional threshold on the OWC $S_c$ values as part of step (S3) in Table B1: we delete any “unobstructed” OWC along the CALIOP track for which $S_c > 20$ sr (i.e., unrealistically small water cloud droplets) or an $S_c < 14$ sr (i.e., unrealistically large water cloud droplets). Every OWC $S_c$ value along the CALIOP track was then compiled to produce four global median seasonal $4^\circ \times 5^\circ$ maps of OWC $S_c$ using 5 years of night-time CALIOP data (from 2008 to 2012).
There is additional precedent for establishing an upper limit of $S_c = 20$ sr. Note that, from Eq. B6, the value of $I_{\text{OWC,SS,CAC}}$ corresponding to $S_c = 20$ sr is $0.025$ sr$^{-1}$. As mentioned earlier, this is the same OWC IAB threshold value used by Chand et al. [2008] to identify their "clear air above" cases.
Data Availability:

This study used the following A-Train data products: (i) CALIPSO version 3 lidar level 1 profile products (Powell et al. [2013]; NASA Langley Research Center Atmospheric Science Data Center; https://doi.org/10.5067/CALIOP/CALIPSO/CAL_LID_L1-ValStage1-V3-01_L1B-003.01; last access: 26 September 2018), (ii) CALIPSO version 3 lidar level 2 5 km cloud layer products (Powell et al. [2013]; NASA Langley Research Center Atmospheric Science Data Center; https://doi.org/10.5067/CALIOP/CALIPSO/CAL_LID_L2_05kmClay-Prov-V3-01_L2-003.01; last access: 26 September 2018), (iii) MODIS Atmosphere L2 Version 6 Aerosol Product (Levy and Hsu [2015]; NASA MODIS Adaptive Processing System, Goddard Space Flight Center, USA; http://dx.doi.org/10.5067/MODIS/MOD04_L2.006; last access: 26 September 2018), and (iv) L2 Version 3 OMI products OMAERO [Stein-Zweers and Veefkind, 2012] and OMAERUV [Torres, 2006].

Author contributions:

The overarching research goals were formulated by Dr Redemann. Dr. Kacenelenbogen, Dr. Young and Mr. Vaughan influenced the evolution of these research goals. Dr. Kacenelenbogen carried out the formal analyses, investigations and visualizations and wrote the original draft. All co-authors have reviewed and edited the multiple drafts of the manuscript. The methodology behind the global application of the DR method to CALIOP measurements was first developed by Dr. Hu, and adapted by Dr. Kacenelenbogen, Dr. Young, Mr. Vaughan, and Ms. Powell to accommodate the requirements of...
this study. The methodology for using this combination of A-Train satellites to infer aerosol intensive
radiative properties was conceptualized by Dr Redemann. The joint MODIS-OMI-CALIOP aerosol
radiative properties were developed and provided by Dr. Shinozuka, Mr. Livingston and Ms. Zhang. Dr.
LeBlanc performed the radiative transfer calculations that provided Direct Aerosol Radiative Effects
estimates in clear skies and above clouds.

Competing interests:
The authors declare that they have no conflict of interest.

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