Simultaneous determination of aerosol optical thickness and water leaving radiance from multispectral measurements in coastal waters

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Abstract. Retrieval of aerosol optical properties and water leaving radiance over ocean is challenging since the latter mostly accounts for \(~\sim\)10\% of satellite observed signal and can be easily contaminated by the atmospheric scattering. Such an effort would be more difficult in turbid coastal waters due to the existence of optically complex oceanic substances or high aerosol loading. In an effort to solve such problems, we present an optimization approach for the simultaneous determination of aerosol optical thickness (AOT) and normalized water leaving radiance (nL\textsubscript{w}) from multi-spectral measurements. In this algorithm, a coupled atmosphere-ocean radiative transfer model combined with a comprehensive bio-optical oceanic module is used to jointly simulate the satellite observed reflectance at the top of atmosphere and water leaving radiance just above the ocean surface. Then a full-physical nonlinear optimization method is adopted to retrieve AOT and nL\textsubscript{w} in one step. The algorithm is validated using Aerosol Robotic Network Ocean Color (AERONET-OC) products selected from eight OC sites distributed over different waters, consisting of observation cases covered both in and out of sun glint from the Moderate Resolution Imaging Spectroradiometer (MODIS) instrument. Results show a good consistency between retrieved and \textit{in situ} measurements in each site. It is demonstrated that more accurate AOT are determined based on the simultaneous retrieval method, particularly in shorter wavelengths and sun glint conditions, where the averaged percentage difference (APD) of retrieved AOT generally reduce by approximate 10\% in visible bands compared with those derived from the standard atmospheric correction (AC) scheme. It is caused that all the spectral measurements can be used jointly to increase the information content in the inversion of AOT and the wind speed is also simultaneously retrieved to compensate the specular reflectance error estimated from the rough ocean surface model. For the retrieval of nL\textsubscript{w}, over atmospheric correction can be avoided to have a significant improvement for the inversion of nL\textsubscript{w} at 412 nm. Furthermore, generally better estimates of band ratios of nL\textsubscript{w}(443)/nL\textsubscript{w}(554) and nL\textsubscript{w}(488)/nL\textsubscript{w}(554), which are employed in the inversion of chlorophyll \textit{a} concentration (Chl), are obtained using simultaneous retrieval approach with less root mean square errors and relative differences than those derived from the standard AC approach in comparison to the AERONET-OC products, as a result that the APD value of retrieved Chl decreases by about 5\%. On the other hand, the standard AC scheme yields a more accurate retrieval of nL\textsubscript{w} at 488 nm, prompting a further optimization of oceanic bio-optical module of current model.
1 Introduction

Aerosols monitoring is indispensable for evaluating the global energy budget and material exchange. They exert significant impacts on the radiation process through both direct and indirect effects (Boucher et al., 2013). Quantifying aerosols optical properties is also crucial for the remote sensing of ocean color (OC) as atmospheric backscattering, which is composed of aerosol and Rayleigh scattering, contributes a greater fraction of signals at the top of atmosphere than that of the spectral water leaving radiance ($L_w$) from ocean body (Gordon and Morel, 1983). Since the Rayleigh scattering can be determined in a high precision level by considering the effects of polarization, surface pressure and roughness (Gordon et al., 1988; Wang, 2002), accurate estimation of aerosols becomes an important mission in the determination of water leaving radiance and oceanic substances.

To derive the aerosol optical properties over ocean, some approaches compare observed and pre-calculated reflectance at selected channels assuming that the water leaving radiance can be neglected or empirically estimated. For example, the MODerate resolution Imaging Spectroradiometer (MODIS) Collection 5 operational over-ocean algorithm specifies zero water leaving radiance for all except at 550 nm where a value of reflectance 0.005 is assumed (Remer et al., 2005, 2006). When to evaluate the influence of aerosols in the remote sensing of ocean color, another approaches decouple the atmosphere and ocean using atmospheric correction procedures, which are performed in two steps. First, the aerosol reflectance, after the correction of Rayleigh scattering and surface reflectance, is estimated by comparing measurements with lookup tables (LUTs) in the red or near infrared (NIR) channels, where the water leaving radiance can be neglected due to the high absorption of ocean body at those bands. The LUTs contain pre-calculated radiation fields for sets of candidate aerosol modes, which are characterized by different optical properties and relative humidity values. Second, the best fitting aerosol modes are selected and extrapolated to shorter wavelengths to calculate the aerosol scattering and water leaving radiance in those band regions (Gordon and Wang, 1994; Fukushima et al., 1998: Antoine and Morel, 1999; Gao et al., 2000; Wang, 2010). In addition, other efforts or approaches have been made to compensate the traditional atmospheric correction procedures under more challenging measurement conditions in the presence of non-null water leaving radiance of turbid waters. Such methods use aerosol optical properties of nearby non-turbid areas or other spectral information, such as ultraviolet or shortwave infrared (SWIR) bands (Hu et al., 2000; Ruddick et al., 2000; Pan and Mao, 2001; Wang and Shi, 2007; He et al., 2012; Mao et al., 2013). Furthermore, in consideration of the insufficiency of aerosol modes in the LUTs approach, other research has expanded the LUTs to encompass more actual aerosol models derived from Aerosol Robotic Network (AERONET) observations (Ahmad et al., 2010) or combined with the aerosol scattering using linear combination method (Frouin et al., 2006; Shi and Nakajima, 2017). In this respect, after the process of atmospheric correction, the water leaving radiance, which only typically accounts for ~10% of satellite observed signal, are determined. To further reduce errors caused by the atmospheric correction algorithm and instrumental radiometric uncertainties, vicarious calibration is conducted to improve the accuracy of $L_w$ by comparing satellite-observed radiance with simulation using ground-truth
observation data (Gordon, 1998; Fougnie et al., 1999; Wang and Franz, 2000; Murakami et al., 2005; Yoshida et al., 2005; Franz et al., 2007).

However, many of these algorithms rely on the observation of only several spectral channels, the retrieved aerosol spectral properties are not always fully consistent with the measurements at other bands (Dubovik et al., 2011), as a result that the retrieved $L_w$ are sometimes negative due to the overestimation of aerosol scattering, particularly in short wavelengths (Fan et al., 2017). In the past decades, other feasible methods using a direct optimization-based inversion algorithm (Bricaud and Morel, 1987; Doerffer and Fischer, 1994; Zhao and Nakajima, 1997; Chomko and Gordon, 1998; Stamnes et al., 2003; Dubovik et al., 2008; Li et al., 2008; Kuchinke et al., 2009; Shi et al., 2016; Fan et al., 2017) or Bayesian methodology (Frouin and Pelletier, 2015) have been developed to complement prevailing atmospheric correction schemes. These one-step retrieval approaches involve a direct inversion scheme that simultaneously determines aerosols and oceanic substances with minimal assumption, which have an advantage in dealing flexibly with the inversion problems in the absorption aerosol loading conditions and increasing the available measurements information content. Most of these approaches adopt the radiative transfer (RT) model to enable simulated radiance to converge with observation by defining the appropriate retrieved parameters and estimation schemes or neutral network method, to make full use of the satellite observed data, as well as multiple geometry, pixel or polarization information (Dubovik et al., 2011; Hasekamp et al., 2011; Knobelspiesse et al., 2012; Xu et al., 2016).

To model the radiative transfer in the atmosphere and ocean system, simple methods use Fresnel-Snell law to combine the two non-uniformly refracting layered media for a flat ocean surface. However, better modeling schemes are required with respect to wind speed for the rough ocean surface, [Cox and Munk, 1954; Nakajima and Tanaka, 1983; Fischer and Grassl, 1984; Mobley, 1994; Fell and Fischer, 2001; Jin et al., 2006; Chowdhary et al., 2006; Ota et al., 2010; He et al., 2010; Zhai et al., 2010, 2017; Chami et al., 2015], particularly in the sun glint conditions. Sun glint is a major issue for the remote sensing of aerosols or ocean color. In sun glint contaminated satellite ocean imagery, the received radiation can be so bright that there may be significant errors in the satellite retrieval of atmospheric and oceanic components and sometimes obtaining relevant information is even impossible. This is related to the strong reflectance of the ocean surface, which is like a mirror and generates information that is more robust than that of atmospheric scattering and water leaving radiance. Therefore, satellite instruments, such as CZCS, SeaWiFS, and POLDER, have a tilting capacity to avoid sun glint observation. However, for the MODIS and MERIS that have no glint tilting function, glint contamination might be more severe. In this respect, traditional atmospheric correction methods perhaps fail, as a result of degrading of spatial coverage of useful products. Nevertheless, studies suggest that sun glint information can be valuable in many applications. For example, it can provide additional information content for the retrieval of aerosol optical properties and types including absorption aerosol (Kaufman et al., 2002; Ottaviani et al., 2013). In addition, the sun glint signal is useful in oil monitoring (Chust and Sagarminaga, 2007; Hu et al., 2009), investigation of below-surface conditions (Hu, 2011), and retrieval of wind speed over the ocean surface (Breon and Henriot, 2006; Harmel and Chami, 2012). To correct sun glint contamination in the atmospheric correction process, several approaches have been introduced using Cox-Munk sea surface model (Cox and
Munk, 1954) to calculate direct solar reflectance from the wind speed prediction (Wang and Bailey, 2001) or the spectral matching method (Steinmetz et al., 2011).

Recent studies suggest that there are still some questionable results in coastal waters using those improved atmospheric correction schemes (Jamet et al., 2011; Goyens et al., 2013), due to the existence of high aerosol loading or more optically complex oceanic substances, such as sediment or colored, dissolved organic matter (CDOM), than that in open waters where only chlorophyll $a$ concentration (Chl) dominates, as a result that the null water leaving radiance assumption breaks down. Besides, even the slight sun glint signals may also introduce large uncertainties in the retrieval of AOT and $L_w$. In an effort to cover such problems, we introduce a one-step inversion scheme in this study, which is simultaneous retrieval of aerosol optical thickness (AOT) and water leaving radiance from multi-spectral measurements in coastal waters. To minimize the uncertainties of spectral radiance from traditional atmospheric correction schemes in the decoupled atmosphere-ocean system, the forward radiation calculation is performed using a coupled radiative transfer model combined with a comprehensive bio-optical oceanic module. Then, a nonlinear optimization approximation approach constrained by a global three-dimensional spectral radiation-transport aerosol model (Takemura et al., 2000) is used to jointly estimate aerosol optical thickness (fine, sea spray and dust), wind speed and oceanic substances, which are consisted of Chl, sediment and CDOM, based on the multispectral observations. The spectral water leaving radiance is correspondingly estimated through the developed bio-optical module followed by a full-physical formulation for the calculation of transmission matrix of rough ocean surface simultaneously.

The objectives of this paper are 1) to calibrate the algorithm in the estimation of $L_w$ based on vicarious calibration, 2) to validate the availability of one-step retrieval algorithm from in situ measurements using Aerosol Robotic Network – Ocean Color (AERONET-OC) products, 3) to estimate the inversion accuracy in the condition of sun glint measurement. The general structure of the bio-optical module and design of retrieval algorithm are introduced in section 2. The datasets used and strict spatial-temporal match-up criteria are shown in section 3. Then, we present retrieval results derived from the MODIS instrument after vicarious calibration and compare them with in situ products collected from 8 AERONET-OC sites distributed over different ocean regions, as well as the products from the MODIS standard atmospheric correction scheme. As an illustration, retrievals are conducted using all available satellite data covering both in and out of sun glint observations. Finally, conclusion and perspectives are provided in the last section.

2. Procedure of retrieval algorithm

2.1 Atmospheric module

In this study, the forward RT simulation is performed by a vector coupled atmosphere-ocean model (Ota et al., 2010). The model employs the discrete ordinate and matrix operator method and was developed based on the Nakajima–Tanaka scheme (Nakajima and Tanaka, 1983, 1986, 1988). It has been proven to be highly accurate in simulating the radiation processes in the atmospheric system (Kokhanovsky et al., 2010). In this algorithm, six different atmospheric profiles, Mid-latitude
summer/winter, sub-arctic summer/winter, tropical and U.S. standard profiles are adopted based on the observation time and location. The atmosphere is divided into 15 layers with the top at 120 km above the surface. The gas absorption coefficient is calculated by a correlated k-distribution approach (Sekiguchi and Nakajima, 2008) where several main absorptive gases of water vapor, carbon dioxide, ozone, nitrous oxide, carbon monoxide, methane, and oxygen are considered. The atmospheric molecules scattering is viewed as Rayleigh scattering with the depolarization factor of 0.0279. For the aerosol, a more realistic scattering multi-component approach is adopted within the aerosol model, wherein the refractive index of each component of aerosol particle is calculated considering hygroscopic growth (Shettle and Robert, 1979; Yan et al., 2002). It is assumed that the external mixture aerosol model consists of fine particles, sea spray particles, and dust particles (which are defined as non-spherical particles); and that an internal mixture of water-soluble, dust-like and soot aerosols exist within the fine particles, of which the refractive index are calculated by the sum of each internal component contribution based on its volume fraction. The fine and sea spray particles are existed from the surface to 2 km height, while dust particles are added from 4 ~ 8 km height, where the vertical distributions of fine and dust particles are homogeneous on contrary to that of sea spray particles with exponential decrease. For each external particle type, the size distribution is assumed to follow log-normal (Nakajima and Higurashi, 1997; Higurashi et al., 1999; Dubovik and King, 2000) as follows,

\[
\frac{dV}{d \ln r} = C \exp\left[-\frac{1}{2} \left(\frac{\ln r - \ln r_m}{\ln s}\right)^2\right] 
\]

where \( C \) denotes the particle volume concentration, \( V \) is the aerosol volume density, \( r_m \) is the mode radius, and \( \ln s \) is the standard deviation of \( \ln r \). The phase matrix of aerosols is calculated by Mie theory for spherical particles and Dubovik et al.’s (2002) method for non-spherical particles. In general, the aerosol modes are summarized in Table 1.

### 2.2 Bio-optical oceanic module

The accuracy of RT scheme in the ocean system is conducted based on a comparison to the standard underwater RT problem proposed by Mobley et al. (1993) (Shi et al., 2015). In this study, we implement a three-component bio-optical module developed by Shi et al. (2016) to model the inherent optical properties (IOPs) of oceanic substances. A brief overview of procedures is shown in Table 2. However, we do make some slight changes to the module in relation to the seawater absorption coefficient based on a calibration between retrieval and measurement. It assumes that the ocean is divided into 4 layers with infinite depth, where the vertical distributions of oceanic substances are homogeneous except that of Chl defined as Gaussian (Morel and Maritorena, 2001). The Raman scattering is temporarily neglected in current model. After the modeling of IOPs of oceanic substances, the reflection and transmission matrices for each oceanic layer are obtained through the discrete ordinate solution. Then the adding theory is applied to determine the unknown integral constants and solve the inhomogeneous layer in the coupled atmosphere-ocean system (Ota et al., 2010). To connect the water leaving radiance with underwater light field, we develop a full physical technique to calculate \( L_w \) in the model, as:
\[ L_w(\lambda; \mu, \phi; [Chl], S_s, a_j(440)) = \sum_{m=0}^{M-1} L_w^n(\lambda; \mu; [Chl], S_s, a_j(440)) \frac{\cos m\phi}{\pi(1 + \delta_{0m})} \]  

(2)

where \( \lambda \) is the wavelength and \( \delta_{0m} \) denotes Kronecker’s delta; \( \mu \) and \( \phi \) are the cosine of the viewing zenith angle and relative azimuth angle, respectively. \([Chl], S_s\) and \(a_j(440)\) are concentrations of Chl, sediment and CDOM, respectively. \( L_w^n \) is the \( m \)th order Fourier component of \( L_w \) as calculated by:

\[ L_w^n(\lambda; \mu; [Chl], S_s, a_j(440)) = \sum_{i=1}^{N} L_w^n(\lambda; \tau_{a_i}; [Chl], S_s, a_j(440)) T^n(\lambda; \mu, \mu') \]  

(3a)

\[ T^n(\lambda; \mu, \mu') = \frac{1}{\mu} \int_{\mu=1/2}^{1} \int_{\mu'=1/2}^{1} T(\lambda; \mu, \mu'; \phi) \cos m\phi d\phi \]  

(3b)

where \( L_w^n \) denotes the \( m \)th order Fourier component of upward radiance just below the ocean surface \( (T_{a_i}) \), which can be calculated by the adding method in the model; \( \mu_i \) are the points for a discrete quadrature of \( N_s \) in the ocean system. \( T(\lambda; \mu, \mu'; \phi) \) is the diffuse transmission function of rough ocean surface related to the emergent and incident normal angles, \( \mu \) and \( \mu' \), just above and below the ocean surface, respectively. \( T(\lambda; \mu, \mu'; \phi) \) can be derived from wind speed values based on the ocean surface mode of Nakajima and Tanaka (1983). To be consistent with the conventional ocean color products using normalized water leaving radiance \( nL_w \), which is approximately the water leaving radiance in the absence of atmosphere, with the sun at the zenith and the mean earth-sun distance \( (Gordon and Clark, 1981) \), \( nL_w \) is computed as,

\[ nL_w(\lambda; [Chl], S_s, a_j(440)) = \frac{d_0}{d} \frac{L_w(\lambda; Nadir; [Chl], S_s, a_j(440))}{E_d^{0*}(\lambda)} F_d(\lambda) \]  

(4)

where \( d_0 \) is the Earth-Sun average distance where solar irradiance \( F_d \) is reported, \( d \) is the Earth-Sun distance when the measurement is conducted. \( E_d^{0*} \) is the downward irradiance just above the ocean surface.

2.3 Optimization approach for retrieval

In the nonlinear atmosphere and ocean system, the measurements vector \( y \), such as the observed radiance or reflectance in each channel, can be simplified by an expression of forward radiative transfer model \( F(x, b) \) with error \( \epsilon \), which is consist of measurement error and model error.

\[ y = F(x, b) + \epsilon \]  

(5)

where \( x \) is the state vector for a set of parameters being retrieved, and \( b \) comprises the quantities that influence the observation but not to be retrieved. The inversion problem is to determine \( x \) from the observations \( y \). Such an equation can be solved by Bayesian theory based on the assumption that the probability distribution function of measurement and
state vector are Gaussian distributions (Rodgers, 2000). Then the maximum a posteriori optimization approach is adopted to minimize the cost function under the condition that a priori information is constrained. The optimal solution of retrieved parameters is determined in an iterative way through the Newton iteration method optimized by the Levenberg-Marquardt algorithm (Levenberg, 1944; Marquardt, 1963) to accelerate the convergence of algorithm, as,

\[
x_{i+1} = x_i + \left[\left(K^T S^{-1} K + (1 + \gamma) S^{-1}_a\right)^{-1} \right] \left[ K^T S^{-1} \left( y - F(x) \right) - S^{-1}_a \left( x - x_a \right) \right]
\]

where \( x_i \) is the state vector to be retrieved at the \( i \)-th iteration; \( x_a \) denotes the priori values of the state vector; \( S_x \) is the measurement error covariance matrix, and \( S_a \) is the variance-covariance matrix defined by a priori state values; \( K \) is the Jacobian matrix or weighting function, which is derived by the forward model to the state vector as \( K = \partial F(x) / \partial x \). \( \gamma \) is a non-negative parameter chosen in each iteration to minimize the cost function using the method of Press (1994). Since the retrieved state vector is usually nonunique and also follows a Gaussian distribution with expect value \( \hat{x} \) and covariance \( \hat{S} \). The statistical uncertainties in retrieved parameters are given as,

\[
\hat{S} = (K^T S^{-1} K + S^{-1}_a)^{-1}
\]

Where the square roots of its diagonals are the 1 sigma uncertainties of each retrieved parameters. 

In this study, the state vector, \( x \), consisted of eight parameters needed to be retrieved: AOT of fine particles, AOT of sea spray, AOT of dust, volume soot fraction in fine particles, wind speed, \([Chl]\), \( S_x \), and \( a_s(440) \). The soot fraction in fine particles is assumed as the retrieval parameters to consider the inversion cases of absorptive aerosol loading. The spectral \( \text{nL} \) values are calculated based on Eq. (2)-(4) simultaneously. In terms to the priori information in the retrieval, a global three-dimensional spectral radiation-transport aerosol model named SPRINTARS (Takemura et al., 2000) is used to generate the apriori conditions of AOT for each type. Besides, the annual average and variance values of Chl from MODIS Level 3 products in 2009 are adopted as the priori constrain for the determination of Chl. The apriori values of sediment and CDOM are defined as 1.0 g m\(^{-3}\) and 0.1 m\(^{-1}\), respectively. The algorithm corrects the satellite-received reflectance using Ozone Monitoring Instrument (OMI) data for ozone absorption and relative humidity, surface temperature, pressure and wind speed from the National Centers for Environmental Prediction (NCEP) reanalysis data. A global averaged value of 35.5 PSU of oceanic salinity is used temporarily in current algorithm.

3. Data and statistical method

3.1 MODIS data

MODIS/Aqua level 1b radiances and geometry information obtained from the collection 6 dataset derived from the MODIS land and atmosphere team are used in this study, because of the highly accurate instrument calibration and wide observation bands used. Eight wavelengths measurement within the nominal central wavelengths of 412, 442, 488, 554, 678, 747, 867,
and 1628 nm are adopted in the joint inversion of aerosol and nLw. Those wavelengths are selected so that the number of the measurement vector is consistent with the number of unknown parameters; In addition, the selected spectral observations are sensitive to either variations in aerosols or oceanic substances.

3.2 In situ data

The AERONET-OC dataset is employed in this study to validate the accuracy of retrieved AOT and nLw using the simultaneous retrieval algorithm. The AERONET is a globally distributed ground-based aerosol monitoring system used for validating aerosol optical properties (Holben et al., 1998). Since 2006, a new component called AERONET Ocean Color (AERONET-OC) has been established and implemented to support long-term satellite ocean color investigation. It uses cross-site consistent and accurate measurements collected by modified sun photometers installed on offshore fixed platforms (Zibordi et al., 2009). Both the atmospheric circumstances, such as aerosol and Rayleigh optical thickness, and the oceanic condition, such as normalized water leaving radiance and chlorophyll a concentration, are provided by AERONET-OC high-level products. In this study, level 2 data released after good cloud-screening and from a quality-assured scheme of the NASA Goddard space flight center are adopted for validation. The AERONET-OC in situ spectral values of AOD and nLw are interpolated using a cubic spine function to the satellite bands.

In situ data are selected and collected from 8 AERONET-OC stations distributed in different ocean regions (as shown in Fig. 1) and then used to compare with satellite-derived results. The data are collected from four stations in the Pacific Ocean (Ieodo_Station, GOT_Seap prism, Lucinda and USC_SEAPRISM), two stations in the Atlantic Ocean (COVE_SEAPRISM and Thornton_C-power), and another two stations near Sahara Desert (Abu_Al_Bukhoosh and Galata_Platform, respectively). The period of the mostly available data used in this study is started from 2010 to 2015. The data are selected to enable consideration of the complexity and variation of local atmospheric and oceanic circumstances, with the aim of reaching an objective and reasonable assessment of the satellite retrieved data from one-step algorithm.

In addition, we also calculated the averaged and standard deviation of AOT at 550 nm, Chl, nLw in 412nm, 442nm, 488nm and 554nm (listed in Table 3) from all the observation values. It is demonstrated that there are distinct distribution for AOT and Chl within different ocean regions; high AOT loading can be seen at Ieodo_Station, GOT_Seaprim, and Abu_Al_Bukhoosh and high values of Chl are seen at Ieodo_Station, Thornton_C-power, and COVE_SEAPRISM.

3.3 Comparison between satellite and in situ data

In order to have a better comparison between satellite retrieved results and in situ values, several criteria are adopted to extract the available data in this study: (1) more than 9 pixels can be analyzed successfully in 5 × 5 pixel windows around each AERONET-OC site; (2) the time difference between AERONET observations and the satellite overpass is less than 1 hour; (3) cloudy scenes are determined when the reflectance at 488 nm is greater than 0.4, or the standard deviation of satellite reflectance of 550 nm in 3 × 3 pixels is greater than 0.0025 (Remer et al, 2005); (4) The sun glint is assumed when the reflected sun angle lies between 0° and 36° (Ackerman et al., 1998); (5) The retrieved or in situ chlorophyll a
concentration over 10 mg m\(^{-3}\) are excluded. By adopting strict spatial-temporal match-up criteria, 123 dataset are achieved consisting of 105 cases where sun glint is covered out and 18 cases where sun glint is covered in.

Several statistical parameters are used in the evaluation, such as root mean square error (RMSE), average percentage difference (APD), and mean percentage bias, which are calculated as follows,

\[
\text{RMSE} = \sqrt{\frac{\sum_{i=1}^{N} (y_i - x_i)^2}{N}} \tag{8a}
\]

\[
\text{APD} = \frac{1}{N} \sum_{i=1}^{N} \left| \frac{y_i - x_i}{x_i} \right| \times 100\% \tag{8b}
\]

\[
\text{Bias} = \frac{1}{N} \sum_{i=1}^{N} \frac{y_i - x_i}{x_i} \times 100\% \tag{8c}
\]

where \(x_i\) is AERONET-OC results, \(y_i\) is satellite retrieved values, \(N\) is the number of match-up datasets.

4. Results and discussion

4.1. Vicarious calibration

The vicarious calibration is indispensable to have a better estimation of \(n_L\) since the desired uncertainties on \(n_L\) cannot be achieved through instrument calibration and characterizations alone (Gordon, 1998) owing to the low proportion of \(L\) on the satellite observed radiance. To derive vicarious calibration coefficients, which force the satellite radiance to agree with the simulated radiance, the ground observed \(n_L\) as well as AOT are inputted to the forward radiative transfer model in this study. The effects of gas absorption, surface pressure, aerosols wet growth process and polarization, are all considered. However, we ignore the influence of whitecaps by limiting data with low surface wind speed.

In this study, the dataset of AOT at 550 nm and spectral \(n_L\) from one of AERONET-OC sites, i.e., Acqua Alta Oceanographic Tower (AAOT, also indicated as ‘Venise’), located in the northern Adriatic Sea at approximately 8 nautical miles from the main land, are adopted for the vicarious calibration. The site is selected since it provides an almost uninterrupted series of data with low uncertainties of \(n_L\) (Zibordi et al., 2015) in visible and near infrared bands and has also been successfully used by Mélin and Zibordi (2010) in the determination of calibration coefficients used in their algorithm. To have a set of quality proved satellite and \textit{in situ} measurement data, several criteria are adopted to select data. Generally, the match-up process is similar to those used for SeaWIFS from the study of Franz et al. (2007). (1) The chlorophyll \(a\) concentration is lower than 0.2 mg m\(^{-3}\); (2) the aerosol optical thickness in 865 nm is lower than 0.15; (3) the satellite zenith angle and solar zenith angle are lower than 56° and 70°, respectively; (4) the reflected solar angle is larger than 36° to exclude the sun glint conditions; (5) the wind speed at 10 meters just above the ocean surface is lower than 7 m s\(^{-1}\). Due to the extensive quality screening process, 18 available data are selected for the vicarious calibration. It is studied...
that the derived coefficients show no significant temporal or geometric dependencies, and the mean values can be stabilized after approximate 20 high-quality calibration samples (Franz et al., 2007). The ensembles of nL_w for each case are shown in Fig. 2, the average values of nL_w are denoted by black solid line.

We simulate radiance at the top of atmosphere using the above input data. Figure 3 demonstrates the averaged ratio of the simulated radiance using ground-truth data to the satellite observed radiance in the band range from 400 to 800 nm. The blue line shows the results in this study. It is demonstrated that the simulated radiance generally compare well with the satellite observation with the ratio near 1 in 412 nm. In the interval of 450–750 nm, the coefficients are slightly lower than 1, which indicates the simulated atmospheric contribution tends to be underestimated in comparison with the satellite measurements. Moreover, larger variability is shown at longer wavelength. The results from the study of Werdell et al. (2006), which uses the Marine Optical Buoy data for the vicarious calibration of MODIS, are also shown as a comparison and denoted by red line. In general, the coefficients obtained in this study are fairly consistent with the Werdell et al’s coefficients between 480 and 670 nm, while larger differences are demonstrated in the shorter and near infrared bands, which may be caused by different aerosol modes and radiative transfer model used in these two algorithms.

4.2. Using satellite measurements out of sun glint

Based on the obtained vicarious coefficients, retrievals are firstly performed for eight in situ sites (shown in Fig. 1) to assess the accuracy of algorithm using the satellite measurements out of sun glint. Figure 4 shows results of the comparison between satellite simultaneously retrieved AOT at 550 nm and nL_w in 412 nm, 443 nm, 488nm and 554 nm, with AERONET observation values. Here AOT refers to the total aerosol optical thickness, which is the sum of the optical thickness of fine, sea spray, and dust particles, and only the nL_w in shorter wavelengths are demonstrated in this study due to their more obvious sensitivity to the variation of Chl and more accurate measurements from AERONET-OC. It is noted that uncertainties for the AERONET-OC in situ nL_w data are estimated less than 5% in the 412–551 nm spectral range and of approximately 8% at 667 nm (Zibordi et al., 2009). In the Ieodo_Station, the retrieved AOT and nL_w are significantly consistent with the observation results shown in Fig. 4(a). High aerosol loading and water reflectance conditions are occurred due to the transportation from inland pollutant as a result of increase of oceanic substances or primary productivity (Tan et al., 2011). The retrieved Chl and sediment concentrations are mostly higher than those of other sites with averaged Chl and S_\text{S} up to 2.16 mg m^{-3} and 1.75 g m^{-3} in this study, since the location of this site is typically viewed as high turbid waters. In the GOT_SeaPrism, the retrieved AOT compare well with the AERONET reported values, nevertheless several inconsistent cases of nL_w are shown in Fig. 4(b), specifically, the derived nL_w in 488 nm are generally overestimated. For the retrieval results in the Lucida (Fig. 4(c)) located in the Southern Hemisphere, low aerosol loading occur in this station, however, the estimated nL_w are overestimated in several cases, where the general variability patterns are significantly similar to those of MODIS standard OC products (not shown) as well as those occurred in Abu_Al_Bukhoosh (Fig. 4(d)). In regards to the derived AOT in Galata_Platform and Abu_Al_Bukhoosh near the Sahara Desert, the simultaneous retrieval algorithm
has a good performance both in low and large aerosol concentration conditions, particularly for Abu_Al_Bukhoosh site, where obvious higher AOT of dust particles than those of other sites are derived with a good discrimination between sea spray and dust for the coarse aerosols in this study. In addition, the retrieved nLw are generally consistent to the observations with estimated Chl of 1.55 mg m$^{-3}$ averagely in Galata_Platform (Fig. 4(e)), which is similar to the AERONET reported values of 1.51 mg m$^{-3}$. In the Atlantic Ocean, two AERONET sites, COVE_SEAPRISM and Thornton_C-power, are selected for the validation of retrieval algorithm, which are located in the west and east coastal regions, respectively. Similar retrieval patterns are shown in Fig. 4(f) and 4(g). It is demonstrated that both the AOT and nLw can be well determined in this study with low aerosol concentration and unconspicuous changing pattern. Nevertheless, the retrieved nLw have larger amplitudes of temporal variations that maybe imply the constantly changing of oceanic environment. In the USC_SEAPRISM site located in the west coastal of United State, retrieved AOT are well consistent to the AERONET reported values with correlation coefficient and RMSE of 0.9242 and 0.0202, respectively, however, relatively slight temporal variations of nLw are shown in this site (Fig. 4(h)), which are obviously different to those of COVE_SEAPRISM (Fig. 4(f)) in east coastal regions.

Summaries of retrieved AOT at 550 nm, which can be jointly derived from current and MODIS standard atmospheric correction (AC) algorithms, versus AERONET-OC observations are shown in the scatter plots in Fig. 5(a) and 5(b), with the number of match-up pairs being 95. Results demonstrate that both algorithms have an accurate estimation of AOT in comparison to in situ measurements. However, current algorithm shows a more accurate retrieval of AOT than MODIS standard AC algorithm of which AOT are slightly overestimated. In addition, more cases can be determined in this study, particularly in the conditions of high aerosol loading demonstrated in Fig. 5(c), in which most of those occur at Ieodo_Station and Galata_Platform sites (shown in Fig. 4(a) and 4(e)). Furthermore, a comparison with AERONET-OC data demonstrates a better estimation of AOT for current algorithm in other bands. Specifically, the mean AOT derived by these two approaches are plotted in Fig. 5(d). A more consistence between measurements and estimation from current algorithm is identified, while the mean AOT retrieved by the standard AC scheme are generally overestimated, particularly in shorter wavelengths (412 nm–443 nm), as a result that the retrieved nLw in those bands are sometimes negative. Such overestimation of AOT values from the standard AC algorithm were also reported by Goyens et al. (2013) and Fan et al. (2017) based on more data intercomparison. On the other hand, the simultaneous scheme decreases the RMSE of retrieved AOT up to less than 0.04 and reduces almost by up to 10% APD values averagely compared with those derived from standard AC algorithm in the visible bands (shown in Fig. 5(e) and 5(f)). It is caused that all the spectral information can be used in current algorithm to increase the information content and more constrain in the inversion of AOT instead of conventional atmospheric correction schemes only using longer wavelengths, such as NIR or NIR/SWIR bands, and then extrapolating to shorter wavelengths. Moreover, the aerosol modes used in those two algorithms are different and may also influence the retrieval accuracy of AOT, of which current scheme adopts a three-component external mixture mode with internal mixture in each type in the consideration of soot particles viewed as absorptive aerosol, while MODIS standard AC algorithm uses the two-component model of Ahmad et al. (2010) based on data collected mainly at open ocean AERONET sites. On the
contrary, the retrieved AOT from these two algorithms are significantly similar in the NIR bands, with the differences of RMSE and APD of 0.001 and 1.31% at 867nm, respectively, even though the visible spectral information are also used in this study, which is also implied that the observation data in the NIR channels plays a major role in the inversion of AOT, particularly AOT at NIR bands, while simultaneous retrieval algorithm using multispectral measurements is more effective to derive AOT at visible bands.

Figure 6 shows comparisons of jointly retrieved nLw at 412, 442, 488 and 554 nm from simultaneous retrieval algorithm and MODIS standard AC algorithm with AERONET-OC observations. Results indicate that “over atmospheric correction” can be avoided to have a better estimation of nLw at 412 nm and 442 nm using simultaneous retrieval algorithm (shown in Fig. 6(a)), where several of nLw values derived from standard atmospheric correction scheme are negative (shown in Fig. 6(b)), which may be caused by the overestimation of AOT in those bands just as Fig. 5(d) shows. Particularly for the retrieval of nLw at 412 nm, the simultaneous algorithm can reduce APD by up to 15% with a significant improvement compared with the standard AC scheme shown in Fig. 6(d). However, MODIS standard algorithm has a better estimation of nLw at 488 nm than those from simultaneous retrieval approach with smaller values of RMSE and APD (Fig. 6c and 6d), even though more accurate retrieval of AOT at 488 nm using current scheme is identified shown in Fig. 5(d) – 5(f). Possible reasons may arise from the deficient modeling of IOPs of oceanic substances in the ocean module of RT model as small variations of IOPs might introduce large errors of nLw retrieval at blue bands just as Fig. (2) demonstrated, besides, the slight underestimation of AOT at 488 nm (shown in Fig. 5(d)) may also render the overestimation of nLw correspondingly. To develop empirical bio-optical schemes for the retrieval of Chl, band ratios of the normalized water leaving radiances are often used (O’Reilly et al., 1998). Figure 6(e) presents the comparison of ratios of nLw(442)/nLw(554) and nLw(488)/nLw(554) obtained from the two approaches with AERONET-OC observation values. Results demonstrate that simultaneous retrieval algorithm obtains better inversion of nLw(442)/nLw(554) and nLw(488)/nLw(554), with RMSE of 0.392 and 0.275, respectively, and APD of 16.30% and 11.34%, respectively. In contrast, values from MODIS standard AC algorithm is less consistent to AERONET-OC products, with RMSE of 0.491 and 0.379, respectively, and APD of 24.50% and 12.94%, respectively, even though there are not significant difference of RMSE and APD for the individual values of nLw at 442 and 554 nm shown in Fig. 6(c) and 6(d). As a result that the estimated Chl from current algorithm based on OC4V4 scheme (without nLw at 510 nm in this study) (O’Reilly et al., 1998) are more consistent to the AERONET Chl products (Fig. 6(f)), with the RMSE and APD of 0.571 mg m\(^{-3}\) and 36.35%, in comparison to those from MODIS standard AC approach of 0.849 mg m\(^{-3}\) and 41.27%, respectively. It may be caused by the different methods adopted in these two algorithms for the determination of Lw, where current scheme calculates Lw mostly based on underwater conditions from Eq. (3) while Lw derived by the MODIS operational scheme are obtained from the residual values of satellite radiance after atmospheric correction.

4.3. Retrieval results based on sun glint observation

In this study, the reflectance and transmission function of the ocean surface are calculated using the formulation of Nakajima and Takana (1983), these functions are derived using wind speed values, which is similar to the Cox and Munk’s ocean
model (Cox and Munk, 1954) but without offset. To investigate the retrieval accuracy using sun glint observation, a simulation retrieval experiment is conducted firstly. The simulation is run for a solar zenith angle of 45° and viewing angle in the total specular reflection and out of sun glint conditions. Five total AOT at 550 nm of 0.039, 0.084, 0.123, 0.181, 0.346, are used (Knobelspiesse et al., 2012) with the fine mode fraction of 70%. The ocean is modeled with a low wind speed of 3 m s\(^{-1}\) (Ottaviani et al., 2013) and values of Chl of 0.5 mg m\(^{-3}\), respectively, where sediment and CDOM are neglected. The accuracy of the satellite radiance in the measurement is set to 2%. Figure 7 shows the retrieval uncertainties in different AOT values from in glint and out of glint observation using eight MODIS wavelengths measurements. It is demonstrated that the retrieval uncertainty of coarse AOT increases significantly in high value conditions when the observation is covered in sun glint, while the relative magnitude of the uncertainty of fine AOT is not surprising with of less than 25% on average from the sun glint measurement. A more accurate retrieval of wind speed is achieved using sun glint observations due to the significant sensitivity to measurements (the apriori value of wind speed is set to 5 m s\(^{-1}\)). For the determination of chlorophyll \(a\) concentration, there is not significant difference of retrieval uncertainty using sun glint or not, it is caused by the unconspicuous influence of sun glint signal on the underwater filed, which is similar to the study of Ottaviani et al. (2013) using more observation information. Therefore, relatively accurate retrieval of AOT can be determined based on the simultaneous retrieval of wind speed in sun glint measurements, when the aerosol is dominated by fine mode particles or low value conditions.

The inversion algorithm is then applied to investigate the accuracy of retrieved AOT and nL\(_{w}\) using real satellite data covered in sun glint region. The NCEP data are used as the priori constrain of wind speed values in this study. Figure 8 shows the comparisons of retrieved AOT values, which can be jointly estimated from these two approaches, to the AERONET observations with the number of match-up pairs being 18. Results indicate that the sun glint do contaminate the estimation of AOT to introduce more retrieval error, where the accuracy reduced by up to 15% or more compared with those using out-of-sunglint measurements. Generally, the derived AOT at 550 nm from current algorithm are much more consistent with AERONET-OC data than those obtained from MODIS standard AC algorithm shown in Fig. 8(a) and 8(b), where the reported AOT are mostly overestimated in sun glint regions. Such overestimation conditions are also occurred in other bands shown in Fig. 8(c). Different to the retrieval cases based on the measurements out of sun glint (Fig. 5(d)), the mean AOT values from standard AC scheme are still larger a lot than AERONET-OC data at NIR bands. In general, the estimated AOT from one-step scheme compare well with the \textit{in situ} products, of which the RMSE and APD reduce by up to 0.023 and 45.25% in blue bands and 0.043 and 70.14% in green and even NIR bands, respectively, when compared with those derived from the standard AC algorithm shown in Fig. 8(d) and 8(e). This could be caused by the underestimation of the contribution of the direct solar beam reflection from the ocean surface to the satellite received signals and more AOT is reciprocally estimated. In contrast, wind speed is not fixed but simultaneously retrieved in this study to compensate the estimated specular reflectance error using Cox and Munk model (Cox and Munk, 1954) even though this model has been proved to be of good performance validated by satellite measurements (Zhang and Wang, 2010). However, the simultaneous
algorithm seems to over-correct the sun glint contamination to estimate the AOT values lower a lot than the standard AC scheme in high aerosol loading conditions, just as Fig. 8(a) and 8(b) shown. For the retrieval of $nL_w$ in sun glint region, the one-step algorithm has a significant improvement in the estimation of $nL_w$ at 412 nm with less RMSE and APD values and slight better inversion of $nL_w$ at 442 and 554 nm, but worse retrieval of $nL_w$ at 488 nm than those from the standard AC scheme in contrast to in situ measurements shown in Fig. 9(a) – 9(d). Such situations are also similar to that using the satellite measurements out of sun glint (Fig. 6(c) – 6(d)). In regards to the band ratios of $nL_w(443)/nL_w(554)$ and $nL_w(487)/nL_w(554)$, current algorithm estimates less values of RMSE but higher values of APD than the MODIS standard AC algorithm (Fig. 9(e)) compared with in situ products. The retrieved Chl in this study has a slightly better correlation coefficient and a smaller RMSE and APD than MODIS OC products in contrast to AERONET-OC data. It is shown that there are several cases that Chl are much more overestimated shown in Fig. 9(f), which may be caused by the overestimation of atmospheric contribution in the atmospheric correction procedure. Where most of them occur at Galata_Platform sites. Compared with the AERONET-OC products, MODIS operational AC scheme tends to overestimate the Chl values, which is contrary to current algorithm seemed to underestimate the Chl values generally, as those demonstrated in Fig. 6(f) and 9(f), using satellite measurements covered out of sun glint and in sun glint, respectively.

5. Conclusions and outlooks

Satellite remote sensing of aerosols and water leaving radiance in coastal waters remains a challenging problem due to the existence of optically complex water body or high aerosol loading. Besides, the direct sun glint reflected on the ruffled ocean also influences the retrieval accuracy due to its contamination on satellite measurements. Standard atmospheric correction (AC) schemes of ocean color, such as the ones implemented in MODIS instrument, use near infrared (NIR) bands or combined NIR and shortwave infrared (SWIR) bands to retrieve the aerosol optical properties based on the assumption of null water leaving radiance and then extrapolate to the shorter wavelengths using the derived aerosol modes from pre-calculated look up tables. However, the retrieved aerosol spectral properties are not always fully consistent with the observations at shorter wavelengths using conventional AC algorithm as a result that the AOT values are sometimes reported to be overestimated and the derived water leaving radiance is occasionally negative in those bands.

To deal with these problems and make full use of spectral information as well as shorter bands measurements in the joint determination of aerosol optical thickness and water leaving radiance, a different algorithm that simultaneously retrieves AOT and $L_w$ from multispectral measurements is developed in this study. In this algorithm, we use a coupled atmosphere-ocean radiative transfer (RT) model combined with a comprehensive oceanic bio-optical module, in consideration of influence of sediment and CDOM, as well as temperature and salinity, as the forward RT simulation. Then an optimization approximation scheme is developed to adjust the retrieved parameters consisted of AOT of fine, sea spray and dust particles, soot fraction in fine particle, wind speed, chlorophyll $a$ concentration, sediment and CDOM, to fit
observation with spectral measurements in an iterative manner. The adjustment of retrieved parameters allows the retrieval of water leaving radiance calculated by the developed oceanic module simultaneously.

We derived the vicarious calibration coefficients using ground-truth measurements for current algorithm firstly. The following retrievals are then performed based on the calibration results. Validation is carried out using the AERONET-OC products selected from 8 sites distributed over different ocean regions to investigate the accuracy and flexibility of the simultaneous retrieval algorithm in determining AOT and nLw. For the retrieval using satellite measurements out of sun glint, a good agreement between results is obtained at each station, including in the cases of high aerosol loading and turbid waters, such as at Ieodo Station in yellow sea. Generally, the retrieved spectral AOT values are more consistent to the AERONET products, particularly for the AOT in visible bands, with the averaged percentage difference (APD) reduced by up to 10% compared with those using standard AC scheme, where derived AOT values are tend to be overestimated. At NIR bands, the two algorithms have a similar estimation of AOT. For the retrieval of nLw, over atmospheric correction can be avoided to have a significant improvement for the inversion of nLw at 412 nm and slight better estimation of nLw at 443 nm. Band ratios of nLw(443)/nLw(554) and nLw(488)/nLw(554) derived from current algorithm has a less root mean square error (RMSE) and APD to obtain a better estimation of Chl than those from standard AC scheme, with the APD of Chl decreased by approximate 5%. Similar situations are also occurred using satellite measurements covered in sunglint, where the accuracy of derived AOT is improved more significantly than that from standard AC algorithm, where AOT values are mostly overestimated. It may be caused that the wind speed, which has significant weighting function in sun glint measurements, is also simultaneously retrieved in this study to compensate the specular reflectance error from the ocean surface. On the other hand, the standard AC scheme has a better retrieval of nLw at 488 nm generally, with the APD value of 5% lower than that from current algorithm, prompting a further improvement of oceanic bio-optical module in this study.

In future, optimization of the bio-optical model should be conducted using more extensive in situ observation data, such as the study of Maritorena et al. (2002), to have a better modeling of radiation process in the ocean system, since small variations of inherent optical properties of ocean substance may translate into large nLw retrieval errors. Moreover, improvement of algorithm adopting multi-pixel constrain technique (Dubovik et al., 2011; Xu et al., 2016; Hashimoto and Nakajima, 2017) and acceleration scheme (Takenaka et al., 2011) is also part of our ongoing work.

Acknowledgements:

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References:


Table 1. Aerosol modes used in this study

<table>
<thead>
<tr>
<th>Type</th>
<th>Components</th>
<th>Spherical</th>
<th>Height (km)</th>
<th>(r_m(\mu m))</th>
<th>(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fine</td>
<td>Water-soluble, dust-like and soot</td>
<td>Yes</td>
<td>0 ~ 2</td>
<td>0.175</td>
<td>2.240</td>
</tr>
<tr>
<td>Sea spray</td>
<td>Sea salt</td>
<td>Yes</td>
<td>0 ~ 2</td>
<td>2.200</td>
<td>2.010</td>
</tr>
<tr>
<td>Dust</td>
<td>Dust-like/Yellow sand(^a)</td>
<td>No</td>
<td>4 ~ 8</td>
<td>4.000</td>
<td>3.000</td>
</tr>
</tbody>
</table>

\(^a\)The yellow sand mode (Nakajima et al., 1989) is only used in the retrieval of AOT in Ieodo Station.
### Table 2. Bio-optical ocean module used in the RT model

<table>
<thead>
<tr>
<th>Component</th>
<th>Parameters</th>
<th>Formula(^a)</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td>Seawater</td>
<td>Real part of refractive index</td>
<td>[n_r(T,S,\lambda) = n_u \times [n_0 + (n_1 + n_2 T + n_3 T^2) S + n_4 T^2 + \frac{(n_5 + n_6 S + n_7 T)}{\lambda} + \frac{n_8}{\lambda^2} + \frac{n_9}{\lambda^3}]]</td>
<td>Hale and Querry (1973)</td>
</tr>
<tr>
<td></td>
<td>Imaginary part of refractive index</td>
<td>Cubic spline fitting</td>
<td>Smith and Baker (1981)</td>
</tr>
<tr>
<td></td>
<td>Absorption coefficient</td>
<td>[a_a(T,S,\lambda) = a_a(T_0,S_0,\lambda) + (T - T_0) \psi_a(\lambda) + (S - S_0) \psi_s(\lambda)]</td>
<td>Röttgers et al. (2010)</td>
</tr>
<tr>
<td></td>
<td>Scattering coefficient</td>
<td>[b_s(T,S,\lambda) = \frac{8\pi}{3} \beta_s(90',T,S,\lambda) \left(\frac{2 + \delta_s}{1 + \delta_s}\right)]</td>
<td>Zhang et al. (2009)</td>
</tr>
<tr>
<td></td>
<td>Phase function</td>
<td>[\beta_w(\Theta,T,S,\lambda) = \beta_w(90',T,S,\lambda)] \left(1 + \frac{1 - \delta}{1 + \delta \cos^2 \Theta}\right) \right]</td>
<td>Morel (1974)</td>
</tr>
<tr>
<td>Chl</td>
<td>Absorption coefficient</td>
<td>[a_{ph}(\lambda) = A(\lambda)[Chl]^{0.766}[\lambda / 660]^{0.39(\lambda)}]</td>
<td>Bricaud et al. (1995)</td>
</tr>
<tr>
<td></td>
<td>Scattering coefficient</td>
<td>[b_{ph}(\lambda) = 0.347[Chl]^{0.766}[\lambda / 660]^{0.39(\lambda)}]</td>
<td>Morrison and Nelson (2004)</td>
</tr>
</tbody>
</table>
|                 | Phase function \(^b\) | \[
\begin{align*}
P_{ph}(\Theta) &= \frac{1}{4\pi(1-\delta)^2} \delta_v \left[1 - (1 - \delta) - (1 - \delta)^2 - (1 - \delta)^2\right] \\
&\quad + [\delta(1 - \delta^2 - \delta^2(1 - \delta) \sin^2(\Theta / 2)] \\
&\quad + \frac{1 - \delta_{180}}{16\pi(\delta_{180} - 1)} \delta_{180}^2 (3\cos^2(\Theta - 1) \\
&\quad \times \frac{1}{3} (3 - \mu) / 2, \quad \delta = 4 / [3(n-1)] \sin^2(\Theta / 2)
\end{align*}\] | Fournier and Forand (1994) |
| Sediment        | Scattering coefficient | \[b_{awd}(\lambda) = b_s(550)(\lambda / 550)^n S_s\] | Tassan (1994)                       |
\[ P_{\text{scat}}(\Theta) = \frac{1}{4\pi(1 - \delta)^2 \delta v} \left( v(1 - \delta) - (1 - \delta^v) \right) \]
\[ + \left[ \delta(1 - \delta^v) - v(1 - \delta) \sin^2(\Theta / 2) \right] \]
\[ + \frac{1 - \delta^v}{16\pi(\delta_{180} - 1)\delta_{180}} (3\cos^2(\Theta) - 1) \]
\[ v = (3 - \mu) / 2, \quad \delta = 4 / [3(n - 1)]\sin^2(\Theta / 2) \]

**Phase function**

Fournier and Forand (1994)

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CDOM

Absorption coefficient

\[ a_y(\lambda) = a_y(440)\exp(-0.014(\lambda - 440)) \]

Bricaud et al. (1981)

---

* T (0–30) is temperature in degrees Celsius; S (0–40) is salinity in PSU (practical salinity units); \( \psi_T(\lambda) \) and \( \psi_S(\lambda) \) are the temperature and salinity correction coefficients for water absorption; \( \beta_w(90) \) is the volume scattering function at 90°; \( \delta_w \) is the depolarization factor defined as 0.039 by default (Zhang et al., 2009). \( S_s \) and \( a_y(440) \) are the concentration of sediment and absorption coefficient of CDOM in 440 nm. The absorption effect of sediment is neglect. Besides, CDOM is assumed as pure absorber.

b The phase function is an analytical approximation form of the scattering angular distribution of an ensemble of particles. It has a hyperbolic size distribution based on the exact Mie theory and is calculated using the real part of particles refractive index, \( n \), and slope parameter, \( \mu \). For chlorophyll, \( n \) and \( \mu \) are determined as 1.068 and 3.38 to derive the backscattering fraction is 0.0065 as Li et al. (2008). For sediment, \( n \) and \( \mu \) are fixed at 1.200 and 3.275 so that the backscattering fraction is corresponding to 0.015 as used by Tassan (1994).
Table 3. Mean values and the standard deviation of in situ AOT at 550 nm, Chl (mg m$^{-3}$) and nL$_w$ (mw sr$^{-1}$ cm$^{-2}$ µm$^{-1}$) at selected stations

<table>
<thead>
<tr>
<th>Station</th>
<th>AOT</th>
<th>[Chl]</th>
<th>nL$_w$ (412)</th>
<th>nL$_w$ (442)</th>
<th>nL$_w$ (488)</th>
<th>nL$_w$ (554)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ieodo_Station</td>
<td>0.250±0.191</td>
<td>2.070±0.443</td>
<td>1.502±0.351</td>
<td>2.075±0.469</td>
<td>2.852±0.580</td>
<td>2.827±0.684</td>
</tr>
<tr>
<td>GOT_Seaprism</td>
<td>0.248±0.118</td>
<td>0.301±0.149</td>
<td>0.870±0.278</td>
<td>0.873±0.211</td>
<td>0.847±0.145</td>
<td>0.329±0.077</td>
</tr>
<tr>
<td>Lucinda</td>
<td>0.075±0.035</td>
<td>2.049±0.892</td>
<td>0.776±0.403</td>
<td>1.084±0.542</td>
<td>1.435±0.695</td>
<td>1.303±0.706</td>
</tr>
<tr>
<td>Abu_Al_Bukhoosh</td>
<td>0.271±0.170</td>
<td>0.890±0.397</td>
<td>0.475±0.207</td>
<td>0.602±0.262</td>
<td>0.801±0.348</td>
<td>0.548±0.318</td>
</tr>
<tr>
<td>Galata_Platform</td>
<td>0.147±0.089</td>
<td>1.512±2.466</td>
<td>0.364±0.162</td>
<td>0.535±0.241</td>
<td>0.833±0.371</td>
<td>0.846±0.352</td>
</tr>
<tr>
<td>Thornton_C-power</td>
<td>0.125±0.092</td>
<td>5.057±4.407</td>
<td>0.418±0.186</td>
<td>0.591±0.284</td>
<td>0.934±0.464</td>
<td>1.181±0.503</td>
</tr>
<tr>
<td>COVE_SEAPRISM</td>
<td>0.087±0.062</td>
<td>2.602±0.975</td>
<td>0.428±0.241</td>
<td>0.624±0.300</td>
<td>0.977±0.426</td>
<td>1.057±0.485</td>
</tr>
<tr>
<td>USC_SEAPRISM</td>
<td>0.090±0.051</td>
<td>0.505±0.564</td>
<td>0.731±0.208</td>
<td>0.742±0.179</td>
<td>0.740±0.133</td>
<td>0.339±0.088</td>
</tr>
</tbody>
</table>
Figure 1: Locations of selected AERONET-OC stations (star symbols)
Figure 2: Spectra of AAOT nLw used for the calculation of vicarious calibration coefficients in this study. The gray lines represent the individual spectra, the black line shows the average spectrum, the dotted lines denote the average spectrum ±1 standard deviation.
Figure 3: Averaged vicarious calibration coefficient for each channel. Blue line represents the results in this study, red line are results from Werdell et al. (2006).
Figure 4: Comparison of satellite simultaneously retrieved AOT at 550 nm and nLw (mw sr\(^{-1}\) cm\(^{-2}\) \(\mu\)m\(^{-1}\)) with AERONET-OC observations. Red line represents the 1:1 line (a: Ieodo_Station; b: GOT_SeaPrism; c: Lucinda; d: Abu_Al_Bukhoosh; e: Galata_Platform; f: COVE_SeaPrism; g: Thornton_C-power; h: USC_SeaPrism).
Figure 5: Comparison of jointly retrieved AOT at 550 nm from simultaneous retrieval algorithm (a) and MODIS OC products (b) using satellite measurements out of sun glint with AERONET-OC in situ products; Comparison of retrieved AOT at 550nm in high aerosol loading conditions from current algorithm with AERONET-OC observation (c). Statistical mean AOT values (d), RMSE (e) and APD (f) results retrieved by these two approaches compared with AERONET-OC products at 412, 442, 488, 554, 670, 746, and 867 nm.
Figure 6: Comparison of jointly retrieved nLw at 412, 442, 488 and 554 nm from simultaneous retrieval algorithm (a) and MODIS OC products (b) using measurements out of sun glint with AERONET in situ observation; Statistical values of RMSE (c), APD (d), band ratios of nLw(442)/nLw(554) and nLw(488)/nLw(554) (e), and Chl (f) results retrieved by the two approaches compared with AERONET-OC products. The upper and lower black lines of (f) are 1:2 and 2:1, respectively.
Figure 7: Simulated retrieval absolute uncertainties (components of $\hat{S}$) as a function of total AOT at 550 nm. Results using sun glint observation are shown in solid lines, and those from out of sun glint are in dashed lines.
Figure 8: Similar to Fig. 5 but using the satellite measurements covered in sun glint.
Figure 9: Similar to Fig. 6 but using the satellite measurements covered in sun glint.