General comment to reviewer I

We want to thank the two reviewers for the detailed reviews with many useful ideas and suggestions which, we think, have significantly increased the quality of the manuscript.

We have rewritten a substantial portion of the manuscript. In particular, we have added three new tables.

Table 1: Local time variations of background temperature,
Table 2: Local time variations of background water vapor,
Table 5: Local time variations of ice water content.

We shifted section 5.2 (old: Atmospheric background conditions) to a new section 2.2 (Mean state and local time variations of atmospheric background temperature and water vapor). The new section 2.2 discusses in detail new Tables 1 and 2.

We have rewritten section 6 (Latitudinal variations of local time dependence for ice water content) where we now discuss in detail the local time variations of IWC in terms of different thresholds and different latitudes. This includes a new discussion of SBUV thresholds presented in the new Table 5.

The abstract and conclusion sections have been adapted. Also, we have included several new references.

Finally, we decided to remove the old section 7 (Long-term variations 1997 - 2013) which contained a short presentation of possible trends in tidal IWC amplitudes. The reasons for this withdrawal are:

1) This section was rather short, included only one figure, and showed simply a trend behavior of one special IWC parameter, i.e. tidal amplitude, for one latitude and one threshold. The section lacked any discussion and physical interpretation regarding possible sources and causes of such trends.

2) We investigated in more detail the subject of trends in local time variations. It turned out that this is a complex topic which certainly needs further investigations. Several parameters, like latitude and thresholds, play a role which needs to nailed down regarding the impact on local time variations of different ice parameters. Furthermore the effects of possible tidal trends in temperature and water vapor have to be taken into account. Having all this in mind, we decided to cover these topics in near future in a separate paper, which appears to be a better and more systematic way compared to the previous manuscript version.
SUMMARY
This paper presents an analysis of local time variations in polar mesospheric cloud (PMC) properties using a 3-D atmospheric model (MIMAS). The results are compared to local time variations derived from lidar data at a single location (ALOMAR in Norway), as well as zonal average results from the SOFIE and CIPS instruments on the AIM satellite. MIMAS also calculates many parameters describing the background atmosphere [e.g. temperature, water vapor, ice particle radius] that are examined for their contributions to local time variations.

GENERAL COMMENT: For better or worse, we may never get a satellite measurement of PMCs with simultaneous SOFIE-level sensitivity and comprehensive global coverage. So if these model results are to be validated against satellite data, I think presenting curves based on some of those higher thresholds would be quite valuable. The authors might wish to primarily use qualitative statements in the main paper, and provide extra figures in an appendix or on-line supplement (since this paper is a “model study”). But since there is the possibility of non-linear behavior in going from no threshold in IWC to a SBUV-type threshold (for example), I think that providing such information somewhere would help the acceptance of the large variations shown in some aspects of this analysis.

The reviewer addresses an important point about SBUV-type thresholds. The SBUV instrument is typically measuring IWC with a threshold 40 g/km². SBUV has observed PMC since 1979. Long term variations in IWC derived from SBUV measurements have been presented by Hervig and Stevens [2014] and DeLand and Thomas [2015]. Most important is the local time correction of SBUV data in order to investigate long-term changes in PMC. We decided to add Table 5 and address this point in detail in section 6 (Latitudinal variations of local time dependence for ice water content).

See new text from page 17, line 23 to page 20, line 10.

This paper is well-written. Some suggestions and comments related to specific items are provided below.

SPECIFIC COMMENTS
1. p. 1, lines 23-24: So the relative strength of these components (where both are present) is actually a guide to lower atmosphere structure? This is relevant to comment #10.

Yes, according to classical theory published in the textbook by Lindzen and Chapman (1970) the diurnal tide is mainly excited by solar absorption of tropospheric water vapor whereas the semidiurnal tide is mainly excited by solar absorption of stratospheric ozone.

We mention the report by Lindzen and Chapman (1970). Please, have a look in the textbook at p. 139 ...show that ozone is considerably more important than water vapor in exciting semidiurnal oscillations. This is because ozone excitation occurs over a greater depth than water vapor excitation, and at higher altitudes...

and p.153, ... Thus we are not surprised that the contributions to the modes with negative h’s from water vapor (near the ground) are larger than the contributions from ozone (far above the ground). However, the contributions from water vapor absorption to the modes with
positive h’s are also larger. This is due to the short vertical wavelengths associated with these modes. The ozone excitation is distributed over a very considerable depth of the atmosphere (ca. 40 km). Thus, waves excited at one level can destructively interfere with waves excited at another level (see Buffer and Small (1963), and Lindzen (1966b), for a more detailed discussion of this process). For the (1,1) mode (wavelength ~ 28 km) the region of water vapor excitation is not sufficiently thick (ca. 18 km) for this process to be of great importance. This, however, is no longer true for the (1,3) and subsequent modes...

2. p. 2, lines 13-14: Please clarify that this limitation is due to local time sampling, not spatial coverage.

Done: This sentence was considered redundant and was removed.

3. p. 2, lines 15-18: Please note also that in contrast to the previous statement, the restricted spatial coverage of lidar data presents a limitation in terms of how well results from any single location can be generalized to other locations (both latitude and longitude).

Done: We insert … are geographically restricted but …

4. p. 5, lines 18-22: This seems like a reasonable choice because the model can probably form clouds more easily. However, the next paragraph (e.g. lines 25-27) seems to give a different result. Since local time variations are a perturbation on existing clouds, they presumably indicate increased sensitivity to the effectiveness of formation mechanisms. This sensitivity should be addressed later.

We agree that local time variations are a perturbation on existing clouds. We discuss this sensitivity in terms of background conditions of temperature and water vapor, see section 6, page 19, line 15.

As shown in section 2.2, phase positions of minimum temperature at PMC altitudes move to some extent during early morning hours backwards in time in poleward direction. Also the phase of the daily water vapor maximum tends to follow this time shift. We conclude that both temperature and water vapor phases cause the general early morning hour structure in IWC and its shift towards higher latitudes.

5. p. 6, lines 12-13: Please connect this concept to the ideas mentioned on the bottom of page 1 regarding how mesospheric thermal variations are being forced.

We comment: In the introduction we only wanted to give a basic information about the fact that diurnal and semidiurnal tides can be related to different heating by water vapor and ozone which deserve special consideration.

6. p. 6, lines 23-25: The magnitude of the model variations is significantly larger than the satellite results. Stevens et al. [2017; J. Geophys. Res. Atmos. 122, doi:10.1002/2016JD025349, Section 3.1] discuss the potential differences depending on whether “zero” values are included in averages, but these differences seem large even when that issue is considered.

Comment: Here we compare model variations with ground-based lidar backscatter data.
A comparison of modeled IWC with satellite data is presented in section 4 which shows that MIMAS values are consistent with those reported by AIM-SOFIE and AIM-CIPS.

Second, Stevens et al. (2017), see their Fig.6, published modeled IWC results for different latitudes including also one SOFIE point.

We added a new Table 5 (section 6), see our response to your general comment. This allows now to compare our modeled IWC with the Stevens results. We see that both model runs describing the local time variation of IWC with a threshold of 40 g/km² have similar absolute values and are consistent, page 18, line 11 to page 19, line 8.

Recently, Stevens et al. (2017) reported about model results of PMC IWC calculations with the NOGAPS-ALPHA model using a 1-d bulk ice model (Hervig et al., 2009b). The authors show that the IWC is largest at highest latitudes and yields a morning peak between 5 and 7 LT and a late afternoon minimum equatorward of 80 N regardless of threshold. Diurnally averaged IWC values (threshold of 40 g/km²) are near 100 g/km² and consistent with those calculated by MIMAS. NOGAPS-ALPHA results of IWC over a diurnal cycle show at 68 N a ratio between IWC maximum and minimum 5 of about 1.5 for a threshold of 40 (see Figure 6a,b in Stevens et al. (2017)) similar to a ratio of 1.7 from MIMAS calculations.

Concurrently, absolute IWC local time variations in NOGAPS-ALPHA increase towards higher latitudes and are threshold dependent. Again, these features are confirmed by MIMAS.

7. p. 6, lines 28-30: These results can be related to the diurnal and semi-diurnal mechanisms discussed on p. 1.

Again, see our response to your comment 4 and 5.

8. p. 9, line 5: This variation in IWC is still much larger than the fit to the SBUV data (~15-20% p-p), even given the uncertainty in that result because of the nature of the local time coverage. This makes me question the strength of the statement “compatible to a high degree” on lines 10-11.

We are a bit confused since there is neither a fit nor a comparison with SBUV data. We discuss two CIPS and one SOFIE data point. Indeed, the satellite values are compatible with model data. Perhaps you think about the factor of 2. We want to answer that local time variations strongly depend on thresholds, see discussion of new Table 5.

9. p. 9, lines 14-15: See “General Comment” at the beginning of this review. Does a threshold of 40 g/km² reduce the local time variation down to the magnitude shown in DeLand and Thomas [2015]?

Done: Yes, increasing thresholds will decrease (relative) local time variability, see new discussion of section 6. The results from our new Table 5 show a ratio between maximum and minimum of about 1.7 at latitudes 64°-74°N which might be not too far away from a value of 20%-30% reported by DeLand and Thomas [2015], see their Fig.8, 9 showing ratios of descending and ascending points.

10. p. 10, line 1: The physical arguments presented on p. 1 imply that large ratio values of A24/A12, as listed here, mean that tropospheric forcing of tidal variations is much more important for PMC formation and growth than stratospheric forcing. Is this an appropriate statement?
Your conclusion is highly speculative. Tropospheric water vapor and its longitudinal variations, tropospheric cloud coverage through release of latent heat will induce variations in the source strength of the tidal excitation of migrating and non-migrating diurnal tidal component. But propagating upwards, any tidal motion (being a sum of different Hough-modes) will experience different thermal background conditions. Also a variable structure of horizontal winds in vertical direction will vary tidal propagation conditions. Finally, one has to consider all kinds of dissipation mechanisms, e.g. turbulence, infrared cooling, wave-wave interaction with gravity waves etc., that will influence amplitude and phase of tides. So we have to state that the complexity and diversity of all these processes make individual and manual analysis impossible.

11. p. 12, lines 4-5: This result seems surprising given the discussion of high sensitivity to particle radius on p. 5, lines 13-15. Even a few nm matters with an \( r^6 \) dependence. Comments?

Comment: Here we discuss the PMC parameter of ice mass density with an \( n^*r^3 \) dependence. We simply try to analyze which of the two quantities (\( n \) versus \( r \)) has a larger relative contribution to local time variation in ice mass density. Also note that the remarks on page 8, line 19, focus on the discussion of a \( n^*r^6 \) dependence in backscatter.

12. p. 12, lines 15-16: This seems like a significant variation in PMC altitude, considering the small magnitude of quoted long-term variations in \( z_{PMC} \) by Berger and Lubken [2015].

The local time variation in PMC altitude is about 500 m. The long term trend in PMC altitude is about -150 m per decade, see by Berger and Lubken [2015] their Fig. 3c. Indeed, local time variations of NLC heights are in a comparable range as long-term trends.

13. p. 13, lines 16-17: What happens with a higher IWC threshold? DeLand et al. [2011] used OMI data (with IWC > 40 g/km\(^2\)) and found very little latitude dependence in the harmonic fits (although they did not plot change in IWC/brightness vs. latitude, as shown here).

Done: We address this issue in the discussion of our new Table 5, see section 6, that shows the local time dependence of IWC > 40 for three different latitude bands. Our model results suggest that relative effects in local time increase towards the pole.

14. p. 14, lines 1-4: Compare this figure to OMI results. The slope between 3-6 h LT is indeed very steep, but it includes many faint PMC and thus potentially larger variations in occurrence frequency.

Done, see page 19, line 9.

On the other hand, DeLand et al. (2011) published local time observations by the Aura OMI (Ozone Monitoring Instrument) satellite instrument which indicates maximum frequency and albedo values at approximately 9-10 h LT at 70 N for the NH 2007 season, with a smaller amplitude and a slight phase shift to 8 h LT at higher latitudes. Hence, model results from MIMAS deviate to some extent from these satellite measurements for 2007. Here we refer to
some year-to-year variations of phases in MIMAS (not shown here) which might explain to some extent these differences.

15. p. 14, lines 7-8: You can also consider the Stevens et al. [2017] discussion regarding definition of occurrence frequency and how it folds into such analysis.

In section 6 we now discuss all kinds of threshold, with and without frequency weighting, e.g. see discussion of Table 5, section 6.

16. p. 14, lines 13-14: Are the differences between these results for A24/A12 and the brightness ratios listed in Table 1 significant? Should the results in Table 2 for 61.5-64.5 N be considered as comparable to the “faint” cloud class in Table 1?

Comparable is the latitude band for 67.71 from Table 2 (now Table 4) with Table 1 (now Table 3). But have in mind, Table 4 applies for IWC zero counting, i.e. frequency weighting, whereas Table 3 uses brightness threshold intervals. We think, the identification of IWC with faint clouds is not justified.

17. p. 14, lines 17-19: You have already discussed the importance of threshold selection (beta_max, IWC) in deriving such local time variations. Can models give some guidance as to whether these variations are more (or less) important in such an analysis (e.g. SOFIE threshold vs. CIPS vs. SBUV)?

According to this point we have rewritten section 6 (Latitudinal variations of local time dependence for ice water content) where we now discuss in detail the local time variations of IWC in terms of different SBUV thresholds, see Table 5.

18. p. 15, lines 7-8: Recent intervals of 3-4 years in Figure 10(c) with locally larger amplitude and more year-to-year variability (e.g. 1993-1997, 2007-2010) are mostly correlated with solar minimum. Could the internal mechanism for model variations be tied to the level of solar activity?

This section has been removed, see our general comments.

19. p. 17, lines 13-14: Please add a note that increasing the IWC threshold to satellite measurement levels does change this amplitude significantly. Are different mechanisms (e.g. proportional to number of particles vs. proportional to particle size) more important for either the “no threshold” vs. “satellite threshold” analysis?

No, we don’t see different mechanisms. Your question about thresholds has been answered in the conclusions. See page 21, line 13.

We calculated a climatology of IWC local time variations from a 35-y average from 1979 to 2013 for different thresholds and latitude bands, which might be useful for satellite data analysis in order to perform local time corrections. Local time variations are found to depend on latitude and threshold conditions. For the latitude band 64–74 N and a threshold of IWC > 0 g/km2 IWC maximum and minimum values occur around 3 LT and 19 LT, respectively, with a ratio maximum to minimum of 6.6. For a threshold of IWC>40 g/km2 the local times for maximum and minimum are identical, but the ratio changes to 1.7. A phase shift exists for the IWC local time behavior towards the pole, which is independent of the threshold value. We find the absolute IWC local time variation to generally increase with latitude.
Furthermore, the IWC maximum moves backward in time from 8 LT at mid latitudes to 2 LT at high latitudes.

20. p. 17, lines 22-23: I don’t consider a 4 hour shift “remarkable” here, particularly when the overall variation is a superposition of three harmonic terms.

*Conclusions have been rewritten, ‘remarkable’ is absent.*
General comment to reviewer II

We want to thank the two reviewers for the detailed reviews with many useful ideas and suggestions which, we think, have significantly increased the quality of the manuscript.

We have rewritten a substantial portion of the manuscript. In particular, we have added three new tables.

Table 1: Local time variations of background temperature,
Table 2: Local time variations of background water vapor,
Table 5: Local time variations of ice water content.

We shifted section 5.2 (old: Atmospheric background conditions) to a new section 2.2 (Mean state and local time variations of atmospheric background temperature and water vapor). The new section 2.2 discusses in detail new Tables 1 and 2.

We have rewritten section 6 (Latitudinal variations of local time dependence for ice water content) where we now discuss in detail the local time variations of IWC in terms of different thresholds and different latitudes. This includes a new discussion of SBUV thresholds presented in the new Table 5.

The abstract and conclusion sections have been adapted. Also, we have included several new references.

Finally, we decided to remove the old section 7 (Long-term variations 1997 - 2013) which contained a short presentation of possible trends in tidal IWC amplitudes. The reasons for this withdrawal are:

1) This section was rather short, included only one figure, and showed simply a trend behavior of one special IWC parameter, i.e. tidal amplitude, for one latitude and one threshold. The section lacked any discussion and physical interpretation regarding possible sources and causes of such trends.

2) We investigated in more detail the subject of trends in local time variations. It turned out that this is a complex topic which certainly needs further investigations. Several parameters, like latitude and thresholds, play a role which needs to nailed down regarding the impact on local time variations of different ice parameters. Furthermore the effects of possible tidal trends in temperature and water vapor have to be taken into account. Having all this in mind, we decided to cover these topics in near future in a separate paper, which appears to be a better and more systematic way compared to the previous manuscript version.
**Anonymous Referee #2**  
Received and published: 12 November 2017

**General Comments:**
This manuscript reports results from the Mesospheric Ice Microphysics And tranSport (MIMAS) model using hourly output prescribed by the Leibniz Institute Middle Atmosphere (LIMA) model in order to draw a variety of conclusions on the variation of Polar Mesospheric Clouds (PMC) over the diurnal cycle. The authors compare their results to a suite of ground-based and satellite PMC datasets and extend their study to include all relevant PMC latitudes and cloud classifications. The authors furthermore draw conclusions about long-term trends in the amplitude of the migrating diurnal and semi-diurnal tidal components of PMC ice water content (IWC). The scope of the study is ambitious and if the results are robust, would significantly advance the state of knowledge on the spatial and temporal variation of some of the most important diagnostic PMC properties.

However, the reviewer is skeptical that MIMAS is properly characterizing the reported PMC variations. Although the model shows agreement with many of the datasets included in the study, the reviewer is suspicious that in many cases the agreement is fortuitous and does not validate the model ice properties or the model inputs. This is because the authors demonstrate a curious disregard of a variety of relevant observational and modeling studies that show quite different results in both the ice properties and the model inputs. The reviewer lists the concerns below.

**Specific Comments:**

1. The LIMA inputs largely control the variation of cloud properties over the diurnal cycle. Therefore, Section 5.2 (“Atmospheric background conditions”) should be moved to the beginning of Section 2 since everything else flows from those results.

   *Done, we shifted this section to section 2, see our general comments.*

Figure 6 (left) is especially important to the rest of the study and shows that the variation of temperature over the diurnal cycle is about +/- 1 K at 83 km at 69 N. The amplitude of this variation is in direct contrast to many other studies showing a much larger observed variation of +/- 3-4 K [Singer et al., 2003; Singer et al., 2005; Stevens et al., 2010; McCormack et al., 2014; Stevens et al., 2017]. The authors need to clarify why they believe their results are more reliable than all of these previous studies. If they cannot, then they need to show how their PMC results respond to this larger amplitude of the thermal tide at PMC altitudes.

   *Done, we also included a discussion of MIMAS inputs. We discussed local time variations of temperature and water vapor. We reference [Singer et al., 2003; Singer et al., 2005; Stevens et al., 2010; Stevens et al., 2017] and we compare tidal amplitudes, see discussion of Tables 1 and 2.*

2. To further clarify comment #1 and for more direct comparison with previous studies, the reviewer requests an additional table (immediately prior to Table 1) showing the tidal variations at the most relevant altitude that enables the PMC variations. The reviewer suggests in rows “All clouds”, “faint”, “long-term” and “strong” and in columns “T24 (K)”, “T12 (K)”, “H2O24 (ppmv)” and “H2O12(ppmv)”.


Done, these are the new Tables 1,2 and 5.

3. The authors need to provide additional details on the vertical distribution of condensation nuclei (CN) used in their simulation. There is reference to a Hunten distribution on page 3, line 4. If they refer to Hunten et al. [1980] they need to cite this work and they also need to evaluate the reliability of their results against more contemporary studies that include global-scale transport, that have much smaller CN densities [Bardeen et al., 2008; Megner et al., 2008; Rapp and Thomas, 2006].

In section 2.1 (MIMAS model description), page 3, line 12-13, we cite several references [von Zahn and Berger, 2003; Kiliani, 2014; Berger and Lübken, 2015]. We think that dust initialization is not of overriding importance. In MIMAS dust particles are initialized at mesopause heights and are quickly distributed over height regions typically at 84 – 93 km due. Besides 3-d transport, dust particle are affected by particle diffusion which provides an efficient vertical mixing. Secondly, as soon as dust particles are transported outside of an predefined spatial ice model domain (z<83 km, z>93 km, in latitude direction southward of 50N) these particles are randomly relocated into the ice domain near mesopause heights. This process ensures that during a complete ice season dust particles are always available. Of course there is an interaction between ice particles and dust particles. The more ice particles are formed the less dust particle are in total available since the total sum of ice and dust particles is limited to 40 million particles.

4. On the top of p. 14 (line 1) the authors state that “the amplitude of the local time dependence increases in absolute IWC values towards the pole”. Figure 9 is shown in support of this statement. The reviewer does not understand this result and would like an explanation. Are the authors saying that the magnitude of the thermal tide increases toward the pole? If so, that is in direct contrast to previous modeling and observational studies [Chang et al., 2008; Stevens et al., 2017]. If there is some other reason, then they need to state it explicitly.

No, the thermal tide is decreasing towards the pole, but the water vapor tide increases in poleward direction. For more details see discussion of Tables 1 and 2 (section 2.2) and discussion of Table 5 (section 6).

5. It would be very useful to see a comparison of IWC from CIPS against the results in Figure 8. To the author’s knowledge such has a model-data comparison has not yet been done. The authors should also know that Bailey et al. [2015] directly compared CIPS and SOFIE IWC and found CIPS was a factor of 2-3 too low when measuring at the same local time as SOFIE. This is also relevant to their comparison in Figure 3. The values near 80 N look comparable to the results of Stevens et al. (2017) but a large diurnal variation is inferred by the authors and this needs to be discussed in the text.

We agree with the reviewer. We also note that Bailey et al. [2015] find remarkable differences between SOFIE and CIPS IWC. We made some new analysis of CIPS data and find that the local dependence in CIPS data, both for ascending and descending branches, depends on latitude and varies from year to year too, see our supplementary plot (cips4.pdf). Hence, a precise comparison of CIPS data versus MIMAS results requires a comprehensive analysis including multiple plots. We think that up to now such a task is beyond the content of our actual paper.
But we will perform such an analysis in details in future.
We also included a discussion of Stevens 2017 results, see page 18, line 11 to page 19, line 8.
Recently, Stevens et al. (2017) reported about model results of PMC IWC calculations with the NOGAPS-ALPHA model using a 1-d bulk ice model (Hervig et al., 2009b). The authors show that the IWC is largest at highest latitudes and yields a morning peak between 5 and 7 LT and a late afternoon minimum equatorward of 80 N regardless of threshold. Diurnally averaged IWC values (threshold of 40 g/km2) are near 100 g/km2 and consistent with those calculated by MIMAS. NOGAPS-ALPHA results of IWC over a diurnal cycle show at 68 N a ratio between IWC maximum and minimum 5 of about 1.5 for a threshold of 40 (see Figure 6a,b in Stevens et al. (2017)) similar to a ratio of 1.7 from MIMAS calculations. Concurrently, absolute IWC local time variations in NOGAPS-ALPHA increase towards higher latitudes and are threshold dependent. Again, these features are confirmed by MIMAS.

6. In Section 7 and Figure 10 the authors report a long-term trend in the amplitudes of the diurnal and semi-diurnal tide. To the reviewer’s knowledge this has not been shown before. The reviewer is therefore frustrated that the authors reserve their explanation of this for a future study. If they cannot explain what causes this long-term trend, then they need to withdraw this conclusion from the manuscript until they know the cause.

This is perfectly true. We removed this section, see our general comments.

Technical Corrections:

1. General comment. In all figure captions and table captions for IWC, please explicitly indicate whether values of “IWC=0” are included in the results to avoid any confusion. Some in the field do not weight their IWC with PMC occurrence frequency and others do so it is important to be clear wherever possible.

Done. We included in all figure captions and table captions the IWC threshold and the information about zero counting (frequency weighting).

In the following comments 2-8 all refer to the abstract. We have completely rewritten the abstract and the conclusions.

2. Abstract, p. 1, line 3. Do the authors mean “: : :good agreement between model and lidar observations at 69 N”? Please be explicit.

3. Abstract, p. 1, line 5. “: : :from satellite observations” should be clarified. Please state which satellite observations. Also, the AIM satellite is in a sun synchronous orbit so both CIPS and SOFIE observations are locked in local time. Therefore, these observations are not easily tested against results from a model study on local time dependence. That does not mean that the AIM observations should not be used, but the authors need to better clarify how they are used.

4. Abstract, p. 1, line 7. The maximum to minimum ratio is strongly dependent on the threshold used and this need to be clarified here or the statement should be removed.

5. Abstract, p. 1, line 7-8. This conclusion will depend strongly on how the condensation nuclei are prescribed (see specific comment #3 and Rapp and Thomas (2006, Table 1)). If the conclusion is too uncertain given the model inputs then it should be removed.
6. Abstract, p.1, line 8-9. The reviewer is particularly skeptical of the conclusion about the absolute tidal variation increasing to the pole. Please see specific comment #4 and re-evaluate.

7. Abstract, p. 1, lines 9-12. Please see specific comment #6 and re-evaluate.

8. Abstract, lines 12-13. Please see specific comment #1 and re-evaluate. Also, to avoid confusion the authors need to state a temperature amplitude (i.e. +/- X K or +/- X ppmv) and the dominant tidal component.

9. p. 2, line 15. “Opposite to satellites” should be “In contrast to satellite measurements”.

Done.

10. P. 2, line 32. “with same” should be “with the same”.

Done.


Done.

12. Figure 1 caption (and throughout manuscript). In order to clearly distinguish what is observed and what is modeled, the reviewer requests that the authors not use the word “data” when reporting their model results. In the middle of the Figure 1 caption therefore “model data” should be “model results” and at the bottom of the Figure 1 caption, “MIMAS data” should be “MIMAS results”.

Done.

13. P. 8, line 12. In order to avoid all confusion, the authors should state here whether PMC frequency (or IWC=0 values) is included in the IWC results presented. This is clarified later but should be stated here.

At all discussion points, now, we always state which counting and threshold method has been applied.

14. P. 9, lines 14-15. The reviewer understands what the authors are trying to say, but this could be confusing. After all, if the PMC threshold is raised high enough then there will be no detections at the minimum so that the maximum/minimum is infinity. Perhaps it would be more clear instead to say “Hence, the strength of the local time variations is sensitive to the PMC occurrence frequency”.

We think that the ratio between maximum and minimum is a reasonable parameter. Of course, this ratio should be well defined.

15. P. 10, Figure 4. The reviewer is a little skeptical that A24/A8 can be determined to 3 significant figures. Could the authors please expand on their decision to include 3
components? For example, what does the solution look like with only a diurnal and semi-diurnal fit?

The reviewer is right. The fit curve would be almost identical using only a 24 h and a 12 h fit. Note that all new Tables 1, 2, and 5 contain only diurnal and semidiurnal information indicating that the terdiurnal mode is of minor importance. E.g. we included such a statement at page 15, line 1.

The fit is dominated by the diurnal and semidiurnal mode, the terdiurnal mode is of minor importance.

16. P. 14, Table 2. It appears from the discussion in the text that no threshold was applied to these numbers. If so, please say so explicitly in the table caption. Also, the numbers for A24/A12 seem quite a bit different from those reported by Stevens et al. (2017) for the same time period. Since the approach to simulating the ice particle formation is quite different between the two studies, it would be illustrative to show A24/A12 for temperature and A24/A12 for H2O, perhaps in a separate table, analogous to the request in specific comment 2.

The reviewer is right. No threshold was applied, and zero counting (frequency weighting) has been used. We added a new Table 5 (section 6), see our response to your general comment. This allows now to compare our modeled IWC with the Stevens results. We see that both model runs describing the local time variation of IWC with a threshold of 40 g/km^2 have similar absolute values and are consistent, page 18, line 11 to page 19, line 8.

Recently, Stevens et al. (2017) reported about model results of PMC IWC calculations with the NOGAPS-ALPHA model using a 1-d bulk ice model (Hervig et al., 2009b). The authors show that the IWC is largest at highest latitudes and yields a morning peak between 5 and 7 LT and a late afternoon minimum equatorward of 80 N regardless of threshold. Diurnally averaged IWC values (threshold of 40 g/km^2) are near 100 g/km2 and consistent with those calculated by MIMAS. NOGAPS-ALPHA results of IWC over a diurnal cycle show at 68 N a ratio between IWC maximum and minimum 5 of about 1.5 for a threshold of 40 (see Figure 6a,b in Stevens et al. (2017)) similar to a ratio of 1.7 from MIMAS calculations. Concurrently, absolute IWC local time variations in NOGAPS-ALPHA increase towards higher latitudes and are threshold dependent. Again, these features are confirmed by MIMAS.

17. Please re-evaluate and revise the conclusions given the specific and technical comments listed above. Thank you.

Conclusions have been revised. We also included a multiple of new references which can be identified in the colored track version. We also thank again for this very precise and detailed review. We know that perhaps we have not answered everything within 100 percent. But nevertheless we hope that the reviewer should have now a larger confidence to MIMAS model results.

References:
Bardeen, C.G. et al. (2008), Numerical simulations of the three-dimensional distribution of meteoric dust in the mesosphere and upper stratosphere, J. Geophys. Res., 113,
Local Time Dependence of Polar Mesospheric Clouds: A model study

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Abstract.

The Mesospheric Ice Microphysics And tranSport model (MIMAS) is used to study local time (LT) variations of polar mesospheric clouds (PMC) in the northern hemisphere during the period from 1979 to 2013. We investigate the tidal behavior of brightness, altitude and occurrence frequency and find a good agreement between model and lidar observations. Mean ice water content (IWC) values from MIMAS also match those from satellite observations. In the latitudinal band of 67.5°–70.5°N the IWC maximum throughout the day occurs at about 3 LT and the minimum around 18 LT with a ratio of maximum to minimum of 10. At the peak of the PMC layer the ice particle size varies by about 30% while the number density varies by a factor of 2 nanometers and the mean number density from 80 to 150 cm⁻³ throughout the day. Furthermore, the absolute tidal variation of IWC generally increases towards higher latitudes and the time of maximum IWC changes from about 4 to 8. We also analyze PMC in terms of ice water content (IWC) and show that only amplitudes of local time variations in IWC are sensitive to threshold conditions whereas phases are conserved. In particular, relative local time variations decrease with larger thresholds. Local time variations also depend on latitude. In particular, absolute local time variations increase towards the pole. Furthermore, a phase shift exists towards the pole which is independent of the threshold value. In particular, the IWC maximum moves backward in time from 8 LT for latitudes from 61°N to 81°N. In the period from 1979 to 2013 we find an increase of the tidal amplitudes. The linear trend terms of diurnal and semidiurnal variations are calculated to be 3.4 and 1.4 LT at mid latitudes to 2 e⁻³/day LT at high latitudes. The persistent features of strong tidal modulations local time modulations in ice parameters are caused by tidal local time structures in background parameters. The temperature varies by about 2 Kelvin and water vapor by about 3 nanograms per liter at the altitude of ice particle sublimation near 81.5 km altitude. At sublimation altitudes the water vapor variation is about 7 kilogram per cubic meter, leading to a change of the saturation ratio by a factor of about 2 throughout the day.

1 Introduction

Polar mesospheric clouds (PMC), also known as noctilucent clouds (NLC), consist of water-ice crystals. They occur at mid to high latitudes around 83 km altitude (e.g. Jesse, 1896; Gadsden and Schröder, 1998; Lübken et al., 2008). Such clouds form in summer in a supersaturated cold atmosphere with temperatures below 150 K and are sensitive to water vapor and mesospheric
temperatures. Therefore, PMC are thought to be sensitive indicators of climate change in the middle atmosphere (e.g. Thomas, 1996; Berger and Lübken, 2015; Hervig et al., 2016a). PMC often show a rich variability which provides information about thermal and dynamical processes on thermal background fields (Witt, 1962). The clouds have been shown to be subject to persistent local time variations (e.g. von Zahn et al., 1998; Chu et al., 2003; Fiedler et al., 2005). These variations were attributed to atmospheric thermal tides. Such tidal oscillations are globally forced due to absorption of solar irradiance throughout the day. While semidiurnal tides are dominantly generated through absorption of solar ultraviolet radiation by stratospheric ozone, water vapor in the troposphere absorbs solar radiation in the near-infrared bands forcing mainly the diurnal tidal component (Lindzen and Chapman, 1969). Generally, these tidal waves propagate upwards with exponential growth in amplitude, and are therefore also present at PMC altitudes in the summerly mesopause region at high latitudes.

A variety of spaceborne experiments have observed PMC since the late 20th century (e.g. Stevens et al., 2010; Russell et al., 2014; Hervig and Stevens, 2014). Many of these experiments are on satellites with sun-synchronous orbits and therefore only allow observations at fixed local times. The Solar Backscattered Ultraviolet Instruments (SBUV) on-board the National Oceanic and Atmospheric Administration (NOAA) satellites provide a data set of more than 35 years of PMC observations (e.g. Thomas et al., 1991). This data set was recorded by eight separate instruments with changing viewing conditions and different local times which introduces uncertainties in the long-term analysis when creating a single data set. Also the Solar Occultation For Ice Experiment (SOFIE) and the Cloud Imaging and Particle Size (CIPS) instrument on-board the Aeronomy of Ice in the Mesosphere (AIM) satellite perform observations in a sun-synchronous orbit. The Ozone Monitoring Instrument (OMI) on-board the Aura satellite is able to measure PMC at different local times, but only part of the diurnal cycle is covered, i.e. the afternoon is missing (DeLand et al., 2011). In order to quantify long-term natural or anthropogenic changes in PMC, it is therefore essential to understand their variations over the diurnal cycle (DeLand and Thomas, 2015).

Observations from satellites apparently have a limited ability to directly characterize local time effects on global scales.

Opposite to satellites, in contrast to satellite measurements, ground-based measurements are geographically restricted but have the ability to cover a full local time cycle. E.g. variations of PMC occurrence frequency and brightness as function of local time have been observed in detail with lidar instruments (von Zahn et al., 1998; Chu et al., 2006; Fiedler et al., 2005, 2009, 2011, 2017; Gerdig et al., 2013). All these data show evidence of a large PMC brightness variability with local time.

In this paper we discuss results from a three-dimensional Lagrangian transport model for PMC called MIMAS (Mesospheric Ice Microphysics And tranSport model), see also the data description in Berger and Lübken (2015). MIMAS covers the latitude and altitude range of PMC and the entire PMC season with a high temporal resolution. This allows for example to calculate latitude-dependent local time adjustments to retrieve PMC parameters with the observational filter of satellite instruments. In the next section we describe some important aspects of the MIMAS model which are relevant for the simulation of seasonal and local time variations in PMC. Sections 3.1 and 3.1.1, we also describe some mean atmospheric background conditions and we characterize local time variations of background temperature and water vapor as calculated by the model. Furthermore we give an overview of seasonal and local time variations in backscatter (section 3), ice water content (section 4), and ice particle radius, number density and ice mass density (section 5) seen in MIMAS and compared to observations of PMC. In section 5 we characterize local time variations of the background atmosphere as calculated by the model. lidar and satellite
observations. Finally, we discuss the latitude dependence and year-to-year changes of PMC latitudinal dependencies (section 6) of local time variations and their implications for the analysis of long-term changes in IWC and their possible implications when analyzing satellite data at fixed local times.

2 Model description

The MIMAS ice model

2.1 Model description

The MIMAS model is a 3-dimensional Lagrangian transport model designed specifically to model ice particles in the mesosphere/lower thermosphere (MLT) region. MIMAS is limited to mid and from mid to high latitudes (45–90° N) with a horizontal grid of 1° in latitude and 3° in longitude, and a vertical resolution of 100 m from 77.8 to 94.1 km (163 levels).

Typically, MIMAS calculates a complete PMC season from mid of May to end of August. Each of the seasonal simulations starts with the same water vapor distributions on constant pressure levels (Berger and Lübken, 2015). Then, the background water vapor is transported by 3-d winds, mixed by turbulent diffusion, and reduced by photo-dissociation from solar ultraviolet radiation. We use Lyman-α as a proxy for solar activity (available at http://lasp.colorado.edu/lisird/lya/).

Simultaneously, 40 million condensation nuclei (dust particles) are transported according to 3-d background winds, particle eddy diffusion, and sedimentation. The radii of the dust particles in the model vary according to a Hunten distribution between 1.2 and 3.6 nm (Berger and von Zahn, 2007). While each of the 40 million particles is transported on an individual 3-d trajectory with a time step of 45 s, a single dust particle will nucleate or an already existing ice particle will further grow, respectively, whenever the temperature and water vapor concentration of the background atmosphere provide conditions of supersaturation. In the case of undersaturated conditions a preexisting ice particle will start to sublimate. The local formation, growth, and sublimation of all ice particles are interactively coupled to the local background water vapor concentration which leads to a redistribution of H₂O with local freeze drying and water supply (von Zahn and Berger, 2003; Kiliani, 2014; Berger and Lübken, 2015).

In MIMAS temperatures, densities, pressure and wind fields are prescribed using hourly output data from the Leibniz Institute Middle Atmosphere (LIMA) model which especially aims to represent the thermal structure around mesopause altitudes (Berger, 2008). LIMA is a fully nonlinear, global, and three-dimensional Eulerian grid point model taking into account major processes of radiation, chemistry, and transport. LIMA extends from the ground to the lower thermosphere (0–150 km), and applies a triangular horizontal grid structure with 41804 grid points in every horizontal layer (∆x ≈ ∆y ≈ 110 km). This allows to resolve the fraction of the large-scale internal gravity waves with horizontal wavelengths of ≥ 500 km.

LIMA is nudged to tropospheric and stratospheric reanalysis data available from the European Centre for Medium-Range Weather Forecasts (ECMWF), Reading, United Kingdom. LIMA incorporates the 40 year ECMWF reanalysis data set (ERA-40) from 1960 to 2002 and ECMWF operational analysis thereafter. The nudging coefficient is altitude dependent with a constant value of 1/3.5 days⁻¹ from the ground to the middle stratosphere (35 km). Above 35 km, the coefficient linearly decreases to zero until 45 km. The nudging of ECMWF data introduces short-term and year-to-year variability. Above approximately 40 km, carbon dioxide and ozone concentrations as well as solar activity vary with time. For CO₂ we have used a monthly mean
time series for the entire period (1961–2013) as measured at Mauna Loa (from http://www.esrl.noaa.gov/gmd/ccgg/trends). For ozone, we take a temporal variation in the height region of the upper stratosphere and lower mesosphere (40–65 km) into account. More precisely, we have used relative anomalies at 0.5 hPa from 1979 to 2013 as measured by SBUV satellite instruments (from http://acd-ext.gsfc.nasa.gov/Data-services/merged/), for more details see Lübken et al. (2013). Before 1979 ozone data are taken from the World Meteorological Organization (WMO) report. Finally, daily Lyman-α fluxes from January 1961 until December 2013 are taken as a proxy for solar activity.

2.2 Mean state and local time variations of atmospheric background temperature and water vapor

Certainly, background conditions of temperature and background water vapor are of overriding importance controlling ice formation in the mesopause region. In the following we will shortly summarize some main MIMAS results of mean state and local time variation of the background. We show in Figure 1 examples of monthly and zonally averaged temperature and water vapor fields as a function of local time in the northern hemisphere for July 2009. We choose the altitude region 81–84 km in order to resolve typical background conditions of temperature and water vapor concentrations at PMC heights. We selected a single year, namely 2009, to be unaffected by possible long-term variations of the local time behavior. In addition, the year 2009 was analyzed in detail by previous studies (Kiliani et al., 2013; Kiliani et al., 2015). The monthly average shown in Figure 1 has been determined using a one hourly output of temperatures and water vapor from the MIMAS 1° × 3° × 100 m latitude-longitude-height grid. For each hourly data set, the actual longitudinal position on a latitudinal circle is transformed to a uniform local time. Hence, our local time resolution is defined by the number of 120 longitudinal grid points for a given hourly data set. Finally, we calculate the monthly July average from 31 (days) times 24 samples per day. We note that this averaging process resolves the mean sun-synchronous part of migrating tidal oscillations. In the following we name this procedure as ‘method 1’ that allows to identify mean local time variations basing on a monthly zonal average.

Another possibility to examine local time structures is to analyze straightforward time series of a single day based on hourly data for individual latitudinal and longitudinal grid points (‘method 2’). We then estimate from each daily data sample specific parameters of mean and maximum/minimum values including corresponding times. Additionally, sinusoidal fits are applied to this daily sample in order to calculate 24 h, 12 h and 8 h tidal amplitudes and phases. This procedure is repeated for every grid point taking into account the difference in local time on various longitudinal positions, and for every day during July. After averaging, we finally get mean values of parameters that describe monthly local time variations on the basis of local daily time series. Generally, method 1 generates smaller estimates of mean local time variations than method 2 since local time parameters are determined from a highly smoothed state in method 1. Conversely, method 2 uses single day time series, and therefor also records day-to-day variations of daily fluctuations which depends not only on variable tidal wave activity but also on variable planetary and large scale gravity wave activity, e.g. as observed by Baumgarten et al. (2018). However, our MIMAS simulations are driven by hourly inputs and not by a monthly zonal mean state. For this reason results from method 2 should better describe mean local time fluctuations of background conditions that effect ice formation. Table 1 summarizes some relevant numbers that describe the mean state and local time fluctuations of temperature resulting from method 2.
**Figure 1.** Local time variation derived from monthly and zonal means of temperature (left) and water vapor (right) in the latitude band 67°–71° N for July 2009, see text for more details.

Table 1. Local time variation derived from daily data of temperature [K] for two heights [km] at different latitudes for July 2009, see text for more details. Mean: mean temperature over a daily cycle; Max: maximum temperature over a daily cycle; Min: minimum temperature over a daily cycle; LT(Max): local time (LT) in hours of Max; LT(Min): local time (LT) in hours of Min; A24: diurnal amplitude from a harmonic fit including 24h and 12h components; A12: same but for the semidiurnal amplitude; P24: diurnal phase of A24 in LT hours of maximum; P12: same but for semidiurnal phase.

<table>
<thead>
<tr>
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<th>Height</th>
<th>Mean</th>
<th>Max</th>
<th>Min</th>
<th>LT(Max)</th>
<th>LT(Min)</th>
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<th>A12</th>
<th>P24</th>
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<td>154</td>
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<tr>
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We begin with a short discussion of the general mean background state of temperatures. Both averaging procedures from method 1 (Figure 1) and 2 (Table 1, 3rd column) result in identical monthly mean values of temperatures. The modeled temperatures closely match observed mesopause temperatures and altitudes. Monthly mean MIMAS temperatures at 69°N are very similar to the observed temperature climatology derived from rocket (falling spheres) measurements at ALOMAR (69°N) during summer (Lübken, 1999; Schöch et al., 2008). For example, the minimum temperature is ~130 K in MIMAS compared to ~130 K in the climatological observations for July, and also the summer mesopause altitude is basically identical (~88 km). At typical NLC heights at 83 km mean MIMAS temperatures are a bit higher with ~147 K compared to observed ~145 K. The MIMAS summer mesopause at 78°N (89 km/124 K) is colder and higher compared to lower latitudes. Lidar measurements of temperatures were performed in the upper mesosphere/lower thermosphere (MLT) at Spitsbergen (78°N) in the years 2001–2003. The July observations show that the summer mesopause is located at 90 km and is as cold as 122 K (Höffner and Lübken, 2007). At lower latitudes at 54°N the MIMAS mesopause is significantly lower (86 km), warmer (144 K), and less pronounced. Again, lidar observations of temperatures confirm these model results with for example a mean July mesopause (86 km/147 K) at Kühlungsborn (54°N) (Gerding et al., 2008). So far, we validated model temperatures of the summer mesopause region only with observational climatologies obtained from groundbased lidar facilities and rocket measurements which we think provide reliable data sets for the high latitude MLT-region. Furthermore, groundbased measurements with meteor radars indicate low temperatures around 90 km in summer typically in a range of 150–170 K at 54°N and 120–140 K at 69°N (Singer et al., 2003, 2005). Calculated temperatures from MIMAS fit to these observations, see Table 1. Stevens et al. (2017) also published temperatures for July 2009 observed by the SOFIE satellite instrument which show systematic and large differences compared to lidar data. For example, SOFIE temperatures indicate a mesopause at 88 km similar to lidars but with a mesopause temperature of ~140 K which is a difference of ~10 K. We note that such a warm mesopause would dramatically prevent ice nucleation and growth in MIMAS with resulting highly underestimated ice masses.

Figure 1 and Table 1 also show mean daily temperature fluctuations. Looking at Figure 1, local time variations calculated with method 1 have a value about 2–3 K near 83 km at 69°N. Applying our preferred averaging procedure from method 2 yields systematically larger local time variations, see Table 1. The analysis shows that in the height region 83–90 km local time variations of temperature decrease towards the pole, i.e. 10–30 K at 54°N, 6–22 K at 69°N, and 4–12 K at 78°N. Generally, the tidal analysis of temperatures indicates that diurnal and semi diurnal tides are mainly present whereas the terdiurnal component can be neglected. Thermal amplitudes increase with altitude and decrease with poleward direction as has been discussed in Stevens et al. (2017). Absolute values of diurnal and semi diurnal amplitudes from MIMAS are in the same order as has been calculated in the model study by Stevens et al. (2010, 2017). Also tidal temperature variations derived from Meteor radar observations around 90 km in summer show diurnal (semi diurnal) amplitudes of about 7 K (5 K) at 54°N, and amplitudes of about 4–8 K (2–4 K) at higher latitudes 69°N (Singer et al., 2003). These observations match the size of amplitudes estimated by MIMAS, see Table 1.
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<th>Latitude</th>
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<th>Max</th>
<th>Min</th>
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<tr>
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</tr>
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</tbody>
</table>

Table 2. Local time variation derived from daily data of H₂O [ppmv] for two heights [km] at different latitudes for July 2009, see text for more details. Mean: mean H₂O over a daily cycle ; Max: maximum H₂O over a daily cycle ; Min: minimum H₂O over a daily cycle; LT(Max): local time (LT) in hours of Max; LT(Min): local time (LT) in hours of Min; \(A_{24}\): diurnal amplitude from a harmonic fit including 24h and 12h components; \(A_{12}\): same but for the semidiurnal amplitude; \(P_{24}\): diurnal phase of \(A_{24}\) in LT hours of maximum; \(P_{12}\): same but for semidiurnal phase.

At PMC altitudes near 83 km diurnal tidal amplitudes are up to a factor two stronger than semidiurnal amplitudes. This means that local variations of temperatures are mainly affected by diurnal tidal modes. At mesopause altitudes diurnal and semidiurnal amplitudes get larger and are of similar size.

We also compared the phase structures as calculated by the two averaging procedures from method 1 and 2, and find that phases of maximum and minimum values as well as tidal phases remain almost unchanged. Interestingly, temperature phases change with latitude at PMC altitudes. Particularly, the local time of the daily minimum (Table 2, 7th column) is shifted backwards in time towards higher latitudes from 6.6 LT (54°N) to 4.4 LT (69°N) and 2.0 LT (78°N). Contrary to the shift of the minimum, the time of temperature maximum seems to occur steadily always between 15 LT and 17 LT. The superposition of diurnal and semidiurnal thermal tides causes predominantly lower temperatures during early morning hours and higher temperatures during afternoon hours, respectively.

Beside temperatures, water vapor plays an essential role for PMC formation. Figure 1 shows water vapor mixing ratios from MIMAS ice simulations at latitudes 67°–71°N for July 2009. In addition, Table 2 describes numbers, using method 2, of latitudinal dependencies for daily variations of water vapor. At 69°N the mean vertical water vapor profile maximizes at 81.5 km with 8 ppmv where ice particles sublimate and create a zone of enhanced hydration. SOFIE observations of water vapor at 73°N show a similar vertical structure with a water vapor peak of 8 ppmv near ~83 km (Hervig et al., 2016b). From Table 2 we find that effects of hydration (sublimation of ice) at 81.5 km and dehydration (freeze drying) near 84 km are intensified towards higher latitudes since colder mesopause temperatures permit larger nucleation rates of ice particles, and larger sedimentation paths lead to enhanced growth of ice particles that causes enhanced sublimation.

MIMAS results indicate that local time variations of water vapor in terms of absolute values are much stronger than thermal local time variations. At 69°N local time variability of background water vapor can reach values up to 7 ppmv at 81.5 km which is in the order of a 100 % variation. Consequently, tidal amplitudes of water vapor from harmonic fits show large tidal
components with an increase towards higher latitudes contrary to temperature amplitudes. The local time behavior of water vapor shows a pronounced maximum below PMC altitudes at 81.5 km during the morning between 5 and 7 LT. The phase position of maximum water vapor moves to some extent backwards in time in poleward direction, however, with a delay of approximately 3 hours when compared with temperature phases. Hence, both phase positions of low temperatures and large water vapor mixing ratios approximately coincide. For this reason we expect that the maximum strength of PMC formation should occur during morning hours as we will discuss in the next sections.

Generally, modeled PMC in MIMAS exist approximately poleward of 54°N where the degree of mean saturation $S$ is larger than unity. Saturation conditions are a combined effect of temperature, water vapor, ambient pressure, particle size and particle temperature. Figure 2 shows the saturation ratio $S$ at a fixed altitude of 82.7 km, which is the mean PMC altitude in the MIMAS simulation for the year 2009. The saturation ratio $S$ is approximated by $S \approx p_{H_2O}/p_{\infty}$ with equilibrium pressure $p_{\infty}$ and ambient partial pressure $p_{H_2O} = c(H_2O) \cdot p$, where $c(H_2O)$ is volume mixing ratio of water vapor and $p$ is pressure of air; for details see equations (1–3) in Berger and Lübken (2015).

It turns out that most of the time supersaturation exists, only in the afternoon hours the saturation ratio falls below $S = 1$. The July average shows nearly permanently supersaturated conditions throughout the day. Note that the vertical extent of supersaturation areas increase polewards because of colder and higher mesopause conditions. In the following sections we will present model results of different PMC parameters and compare these with observational data.
Figure 3. Mean seasonal variations of PMC occurrence frequency (upper panel), altitude (middle panel) and brightness $\beta_{\text{max}}$ (lower panel) between 2003 and 2013 at ALOMAR for faint (red), long-term (blue) and strong (green) clouds (for details see text). Left panels show model results for $67.5^\circ$–$70.5^\circ$ N, $40.5^\circ$–$43.5^\circ$ E, right panels show lidar observations from ALOMAR. The solid lines represent third-order polynomial fits based on daily means. Numbers in the Figure legends are seasonal mean values. Brightness ranges for cloud classes are scaled down by a factor of 4 for MIMAS data. Note the different scaling of the brightness axis for model and lidar data.
3 Seasonal variations

Comparison of MIMAS backscatter model results with ALOMAR lidar observations

3.1 Seasonal variation of backscatter

During the northern hemispheric summer PMC typically occur from end of May until mid of August (e.g. Thomas and Olivero, 1989; Gadsden and Schröder, 1998; Hartogh et al., 2010; Hervig et al., 2013). At the core of the ice season in July, lowest temperatures near 130 K have been observed at mesopause altitudes near 88 km at 69°N (Lübken, 1999). Hence, we expect PMC most frequently and bright during July.

Figure 3 shows the mean seasonal variations of basic PMC parameters as calculated by MIMAS and observed by the Rayleigh/Mie/Raman(RMR)-lidar at the Arctic Lidar Observatory for Middle Atmosphere Research (ALOMAR), located at 69°N, 16°E. MIMAS data results are limited to a latitudinal and longitudinal area of 67.5 – 70.5°N and 10.5 – 19.5°E to be close to the lidar position. We will use the volume backscatter coefficient of ice particles $\beta_{\text{max}}$, in units of $10^{-10}$ m$^{-1}$ sr$^{-1}$, as a measure for the cloud brightness. Both, model and observations cover the same time period of 11 years from 2003 to 2013. In order to take different cloud classes and the detection sensitivity of the lidar into account, we sort measurements and model results into different brightness ranges: $1 < \beta_{\text{max}} < 4$ (faint clouds), $\beta_{\text{max}} > 4$ (long-term detection limit of the lidar), and $\beta_{\text{max}} > 13$ (strong clouds) (e.g. Fiedler et al., 2003; Baumgarten et al., 2008).

In order to convert the model output from MIMAS to specific lidar measurements, we apply spherical Mie-theory calculations to modeled ice particle distributions while taking into account the laser wavelength (532 nm) and scatter geometry (180°). Finally, the transformed model results are sorted into brightness ranges. PMC brightness is proportional to the number of ice particles and depends approximately by the power of six on ice particle radius. For example, increasing the mean radius by only 25% from 32 nm to 40 nm would result into a brightness change by a factor of 4. It is this high sensitivity of cloud brightness to particle size that forms a hard benchmark for our complex ice model simulations. A small underestimation of the mean ice radius will dramatically decrease the brightness, on the other hand, a small overestimation will enhance the resulting backscatter signal by orders of magnitude. In order to match the mean occurrence frequencies of the lidar measurements we decreased the brightness ranges, defining the cloud classes, for the model results by a scaling factor of 4. Hence, the modeled occurrence frequencies contain a systematic bias. We think this deficiency is tolerable since our local time analysis relates to relative deviations from a mean. The scaling factor will only be used for the comparisons with lidar data in this and the following section.

The upper panels of Figure 3 show a general good agreement of modeled and observed PMC occurrence frequencies. We find maximum values in the long-term and strong cloud classes in mid July around days relative to solstice (DRS) 20 – 30. Faint clouds observed by lidar occur earlier in the season than modeled faint clouds. This gives a hint that the model perhaps underestimates the microphysical process of nucleation in ice formation which essentially determines the frequency of weak PMC consisting of small ice particles. We note that ice nucleation in MIMAS is described by the concept of critical radius (Turco et al., 1982; Berger and von Zahn, 2002; Berger and Lübken, 2015).

The middle panels of Figure 3 show modeled and observed PMC altitudes which coincide quite well. Generally, weak PMC are at higher altitudes compared to strong PMC. This altitude separation is caused by two reasons. First, the sedimentation
velocities of ice particles depend on their sizes. Weak PMC consist of ice particle distributions with smaller mean radii, typically in a range of 20 nm, whereas strong PMC consist of larger mean radii, e.g. 40 nm. As the sedimentation velocity increases with particle size (mass), larger particles can reach lower altitudes along their sedimentation path. Secondly, smaller ice particles start to sublimate at lower temperatures than larger ones due to the Kelvin effect. Thus, the negative vertical temperature gradient of the atmosphere causes smaller particles to sublimate at higher altitudes than larger particles. As a result larger ice particles, causing a higher brightness, are found at lower altitudes.

The lower panels of Figure 3 show modeled and observed PMC brightness. Here, the model data results are calculated according to a given brightness range as an arithmetic mean of all brightness values matching the limits. Again, the model seems to underestimate begin and end of the season. The scaling factor for the brightness ranges leads to lower modeled brightness values in the different cloud classes. Hence, multiplying the modeled values with the scaling factor of 4 approximately reproduces the brightness values observed by lidar.

We summarize that the modeled seasonal distributions of occurrence, altitude and brightness are fairly consistent with the ALOMAR RMR-lidar observations, especially for July conditions. Therefore we will concentrate our discussion of model results in the following sections on this core period of the northern PMC season.

4 Local time variations

3.1 Local time variation of backscatter

PMC preferentially occur during morning hours which is attributed to thermal tides of background temperatures in the mesopause region (Fiedler et al., 2011). In order to validate the structure of local time variations in MIMAS we compare our model data results to observations by the RMR-lidar at ALOMAR and to instruments on-board the AIM satellite. For comparison to lidar data we will apply a scaling factor of 4 regarding the brightness ranges, defining the cloud classes, as described in the previous section. As discussed above we will concentrate on the core period of the northern PMC season and will use only July data (31 days x 24 h) from MIMAS simulations for the PMC seasons 2003 – 2013. Tidal structures in the LIMA model have been discussed earlier by Herbrecht et al. (2007) and Fiedler et al. (2011).

3.2 Occurrence frequency, altitude, and brightness

Figure 4 shows the variation of PMC occurrence frequency, altitude, and brightness throughout the day for the integrated data set of July 2003 – 2013 and brightness classes as defined above. The curves are superpositions of four harmonic functions with periods of 24 h, 12 h, 8 h, and 6 h, which are fitted to hourly mean values as described in Fiedler et al. (2017). The geographic range is again restricted to the area around ALOMAR. We find pronounced and persistent features which indicate a strong influence of tides on PMC parameters. The occurrence frequency variation over a day is largest for strong clouds both in MIMAS and observations. Like in the observations, the model results show highest cloud occurrence during the morning hours. The local time dependencies of altitude and brightness are anti-correlated, i.e. on average ice clouds of higher brightness
Figure 4. Mean local time variations of PMC occurrence frequency (upper panel), altitude (middle panel) and brightness $\beta_{\text{max}}$ (lower panel) for July in the period from 2003 to 2013 at ALOMAR for faint (red), long-term (blue) and strong (green) clouds (for details see text). Left panels show model results for $67.5^\circ - 70.5^\circ$ N, $40.5^\circ - 49.5^\circ$ E, right panels show lidar observations from ALOMAR. The lines represent the sum of four harmonic fits using periods of 24 h, 12 h, 8 h, and 6 h to hourly mean values. Numbers in the Figure legends are daily mean values. Brightness ranges for cloud classes are scaled down by a factor of 4 for MIMAS data results. Note the different scaling of the brightness axis for model and lidar data.
are found at lower altitudes. In general, a predominant diurnal oscillation exists in agreement with the lidar observations. The lidar observations show additionally semidiurnal variations in all three PMC parameters, which seems to some extent underestimated by the model. Contrary, the modeled brightness shows a clear peak in the morning hours around 4:00 LT which is absent in the observations.

In order to investigate these different structures we calculated the ratios of diurnal to semidiurnal tidal amplitudes ($A_{24}/A_{12}$). The values in Table 1 show that both model and lidar fits have nearly the same amplitude ratios for a number of cloud parameter and class combinations. For example, for the long-term brightness the ratios are 1.82 (model) and 1.88 (lidar), meaning that tidal modes are very similar in both data sets. Thus the phase differences of modeled and observed data, especially for the semidiurnal modes, (not shown here) are mostly responsible for the differences visible in Figure 4. The superposition of diurnal and semidiurnal tidal modes yields a stronger morning peak in the modeled compared to the observed brightness.

In summary, observed local time variations of PMC occurrence and brightness at ALOMAR are fairly well reproduced by MIMAS.

<table>
<thead>
<tr>
<th>MIMAS</th>
<th>RMR-lidar</th>
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<td>OF</td>
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<tr>
<td>faint</td>
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Table 3. Ratio of diurnal to semidiurnal amplitudes ($A_{24}/A_{12}$) of harmonic fits to the modeled and observed occurrence frequency (OF), altitude, and brightness. The values are calculated for different cloud classes (for details see text) for July months in the period from 2003 to 2013 at ALOMAR according to Figure 4. Bold numbers mark values that agree within the relative uncertainty of about 15% (confidence level of 95%).

3.2 Ice-Water Content

Comparison of PMC brightness values between different instruments is affected by observational constraints, e.g. viewing geometry, lighting conditions, temporal overlap and wavelength. Stevens et al. (2005) suggested that integrated ice mass has the advantage to be less dependent on instrumental setups and thus should be more robust to be used for PMC comparisons. Therefore we present in this section model results of ice water content (IWC) which are calculated from the integrated ice mass density over the total vertical ice column. We analyze the time period 2007 – 2013 to cover the time range of the SOFIE instrument on-board the AIM satellite. The IWC is calculated from all longitudes in the latitude band 67.5° – 70.5°N. In order to resolve tidal structures we subdivide each latitudinal circle into 120 longitudinal segments and sort the model data according to actual local times at all segments. This method yields a total of 3:13 latitudes times 120 longitudes times 31 days.
times 24 h of values for July conditions. Finally, we average all IWC values corresponding to a certain local time with a local time resolution of one hour per day. The probability density distributions of all these IWC values show to a high degree an exponential behavior. Therefore we calculate two different averages (median and arithmetic mean), in order to characterize a mean ice water content as a function of local time during July.

In Figure 5 we compare our IWC model results in terms of median values with measurements from the CIPS and SOFIE instruments on-board the AIM satellite for the latitude band \([67.5^\circ - 70.5^\circ]N\) and IWC threshold of 10 g/km\(^2\) as a function of solar local time. The vertical bars represent the lower and upper quartile of the data. The black curve is a harmonic fit to the data with periods of 24 h, 12 h, and 8 h. Data from AIM satellite instruments including uncertainties for the same time range: SOFIE V1.3 (red - from http://sofie.gats-inc.com/sofie/index.php) and CIPS Level 3c (green - from http://lasp.colorado.edu/aim/download-data-pmc.php) for ascending and descending nodes.

Figure 5. Hourly median values of IWC from 2007 – 2013 (July) for \([67.5^\circ - 70.5^\circ]N\) and IWC threshold of 10 g/km\(^2\) as a function of local time. The vertical bars represent the lower and upper quartile of the data. The black curve is a harmonic fit to the data with periods of 24 h, 12 h, and 8 h. Data from AIM satellite instruments including uncertainties for the same time range: SOFIE V1.3 (red - from http://sofie.gats-inc.com/sofie/index.php) and CIPS Level 3c (green - from http://lasp.colorado.edu/aim/download-data-pmc.php) for ascending and descending nodes.

In Figure 5 we compare our IWC model results in terms of median values with measurements from the CIPS and SOFIE instruments on-board the AIM satellite for the latitude band \([67.5^\circ - 70.5^\circ]N\). The AIM satellite operates in a sun-synchronous orbit, hence only limited local times are available (Russell et al., 2009). For comparison with model results we take the different sensitivities of the two AIM instruments (SOFIE, CIPS) into account. The detection threshold for SOFIE is given as 0.5 g/km\(^2\) (Hervig et al., 2009a). In contrast to SOFIE, the CIPS instrument is less sensitive allowing only IWC events larger than 10 g/km\(^2\) to be detectable (Lumpe et al., 2013). Hence all IWC datasets (MIMAS, SOFIE, CIPS) are limited to this threshold. We find a good agreement between model results and the data points from SOFIE and CIPS inside the error bars. Generally, the modeled IWC has maximum values in the early morning hours between 1 and 4 LT and lowest values between 16 and 20 LT. On average the IWC varies by a factor of about two during a day. Interestingly, comparing SOFIE with CIPS data, the CIPS observation at 23\text{:}00 LT does not match the SOFIE point for midnight conditions. There is a substantial deviation between these values of (SOFIE: 60 g/km\(^2\), CIPS: 30 g/km\(^2\)) which might be due to some uncertainties in the CIPS threshold. The MIMAS value of 40 g/km\(^2\) is right in between the two different satellite observations. Nevertheless, all three data points coincide within their error bars.
We summarize that the MIMAS model results of PMC ice water content are compatible to a high degree with the satellite observations.

Figure 6 shows again the IWC local time variation for the latitude band 67.5°–70.5°N, but now without any threshold which means that IWC has been frequency weighted and IWC values of zero (no PMC) are included. This yields an IWC variation over day by a factor of ten compared to the factor two when considering the threshold used in Figure 5. The factor of ten derived from frequency weighted IWC is consistent with model results reported by Stevens et al. (2010) (see their Figure 7). Hence, the strength of local time variations is sensitive to the IWC threshold, meaning that larger thresholds induce smaller local time variations. See discussion in section 6. The times of IWC maxima and minima are close to those of occurrence frequency and the brightness as shown in Figure 4. We find the harmonic fit to be highly correlated to the median values (correlation coefficient of 0.99), meaning that the local time behavior of IWC medians is almost perfectly represented by the three harmonics of 24, 12, and 8 hours. The fit is dominated by the diurnal and semidiurnal mode, the terdiurnal mode is of minor importance. The amplitude ratios are $A_{24}/A_{12} = 2.66$ and $A_{24}/A_{8} = 5.84$.

5 Influence of atmospheric background conditions on the local time behavior of ice particles, particle radius, number, and ice mass density

In the previous sections we compared MIMAS simulations of backscatter and ice water content with observations in order to show that MIMAS provides realistic model results. Now we investigate in more detail the local time variations in ice parameters and the background atmosphere as calculated by MIMAS and LIMA to find out the underlying reasons for the observed
Figure 7. Ice parameters at $67.5^\circ$–$70.5^\circ$ N calculated from MIMAS simulations of all July months 2003–2013 for the altitude range near 83 km where $\beta_{\text{max}} > 0.4$. Upper panels: brightness and ice particle radius. Lower panels: ice mass density and particle number density. The boxes represent lower and the upper quartiles, median (red line), and arithmetic mean (green line). The dashed vertical bars indicate the minimum and maximum values.

### 5.1 Ice Particle Parameters

Our model simulations of PMC show that the number of ice particles is largest at mesopause altitudes between 86 and 89 km where the highest chance of nucleation is found. This altitude region serves as a reservoir of small ice particles. Then, slightly below mesopause altitudes the MIMAS model predicts the largest number density of ice particles to fall in the range 500
to 1500 cm$^{-3}$ (67°–71°N). The mean radius of ice particles stays generally below 15 nm, which is usually too small to produce significant lidar backscatter signals. Due to random diffusive transport processes a fraction of these small ice particles experiences enhanced growing. The increase in particle mass enhances downward sedimentation. Towards lower altitudes the amount of free background water molecules increases exponentially since air density increases exponentially. During their downward sedimentation path the growth of ice is stimulated until an ice particle reaches an altitude where supersaturated background conditions change into undersaturation. This is the height where the radius of ice particles maximizes and thus highest ice mass densities and largest backscatter signals occur.

In Figure 7 we present backscatter, mean radius, number density, brightness, and ice mass density at the altitude of maximum backscatter signal, assuming a threshold of $\beta_{\text{max}} > 0.4$, for the latitude band 67°–71°N during July. The plots show both median and arithmetic mean values. Median and arithmetic mean are generally different which indicates that the underlying distributions are not symmetric. We also

Mean ice radii vary between 35 and 45 nm. These numbers are in good agreement with AIM-SOFIE observations which also indicate ice radii of 35–40 nm (Hervig et al., 2009a). Mean ice particle densities fall in the range 80 to 150 cm$^{-3}$, which agrees with results from lidar observations (Baumgarten et al., 2008) and satellite measurements (Hervig et al., 2009a). Similar to ice radii, the mean ice mass density increases from the heights below the mesopause downward with mean values about 30 g/km$^3$ at PMC heights. It is interesting to note that the low altitude boundary of the backscatter at 69°N as simulated by MIMAS indicates a temperature of 150 K which agrees well with the observed temperature of 150 ± 2 K for the low altitude boundary of NLCs (Lübken et al., 1996).

Investigating the local time dependence of ice parameters we find that the ice number density maximizes in the morning hours between 3 and 5 LT, which corresponds with the maxima of ice mass density and $\beta_{\text{max}}$. The mean radius shows a smaller variation with local time and no pronounced maximum during in the morning. This indicates that the local time behavior of ice mass density is mainly determined by the number of ice particles and less by the ice particle radius. Our model results are confirmed by AIM observations which show that an increase in ice mass is significantly correlated with increasing number densities and less correlated with the size of ice particles (Hervig et al., 2009b). It is interesting to note. We mention that model calculations performed with the 1–d ice model CARMA show some controversial results, meaning that particle number density has no effect on ice mass and brightness (Megner, 2011).

### 5.1 Atmospheric background conditions

Hourly mean values of temperature (left) and water vapor (right) in the latitude band 67.5°–70.5°N for July 2009. The black lines correspond to the mean altitudes of $\beta_{\text{max}}$ for different cloud brightness classes: Strong (solid line), long term (dashed line), and faint clouds (dotted line).

In MIMAS local time dependencies in ice formation parameters are mainly forced by tidal variations in background temperature and water vapor. Figure 1 shows these parameters on geometric altitudes in the latitude band 67.5° as has been discussed in section 2.2. Local time dependence of brightness in terms of $\beta_{\text{max}}$ with a diurnal maximum near 4–70.5°N for July 2009. We selected a single year to be unaffected by possible long-term variations of the local time behaviour and have chosen season
2009 from the available years (1979 – 2013) because MIMAS model results show particular strong tidal effects on PMC during this year. In addition, the year 2009 was analyzed in detail by previous studies.

First of all we find that both background temperatures and water vapor have a pronounced tidal component. Furthermore, PMC altitudes of strong, long-term and faint cloud classes show variations of about 0.5 km with local time. Generally, bright PMC are found at lowest altitudes and LT follow nicely the temperature structure in the course of the diurnal cycle. Faint clouds are located about 1 with a diurnal minimum at 4–5 km higher compared to strong clouds. The local time behavior of water vapor shows a pronounced maximum during the morning. We LT, see Table 1. In addition, we find the maximum water vapor to occur between 5 and 10 and 7 LT and hence about 4–2–3 hours after the brightness maximum, cf. Figure 7. However, the minima of water vapor and \( \beta_{\text{max}} \) in the evening seem to match somewhat better. At the altitude of strong clouds temperature varies by about 2 K and water vapor by about 2 ppmv throughout the day. Around 81.5 km, which is roughly the altitude of sublimation, the variations are 2 K and 3 ppmv between minimum and maximum.

Saturation conditions are a combined effect of temperature, water vapor, ambient pressure and particle radius. Figure 2 shows the saturation ratio \( S \) at a fixed altitude of 82.7 km, which is the mean PMC altitude in the MIMAS simulation for the year 2009. Supersaturation \( (S > 1) \) is needed to allow the existence of ice whereas \( S < 1 \) will lead to sublimation of ice particles. It turns out that most of the time supersaturation exists, only in the afternoon hours the saturation ratio falls below \( S = 1 \). The July average shows nearly permanently supersaturated conditions throughout the day.

Hourly mean values of the saturation ratio \( (S = \frac{p_{\text{sat}}}{p_{\text{tot}}}) \) in the latitude band 67.5–70.5° N for July 2009 at a fixed altitude of 82.7 km as function of local time, taking into account the Kelvin effect. Grey lines show individual days and the blue line their mean.

In summary, the diurnal cycles of background and Table 2. We conclude that the local time phases in temperature and water vapor in the mesopause region show prevailing supersaturated conditions during the core of the PMC season at ALOMAR and drive the tidal variations of are the main drivers to determine the phase structure in ice parameters.

6 Latitudinal variations of local time dependence for ice water content

Our numerical simulations indicate that the local time variations of PMC are subject to significant latitudinal dependencies. Figure 8 shows modeled IWC values over latitude for selected local times in July 2007 – 2013. No threshold was applied so that the and IWC values had been frequency weighted so that median values include ‘zero’ PMC events. While at 6 LT IWC increases nearly linearly from 60° N to 84° N, the slopes are quite different throughout the rest of the day. This indicates that the phase of the local time behavior changes with latitude. As an example, the time of IWC maximum changes from the morning hours at mid latitudes to midnight hours at high latitudes. Figure 9 shows this phase variation in more detail for different latitude bands. It turns out that (1) the amplitude of the local time dependence increases in absolute IWC values towards the pole, (2) the ratio of maximum to minimum IWC decreases towards the pole (see Table 54), and (3) a slight phase shift can be seen with decreasing latitude: the IWC maximum around midnight near 81° N moves forward in time to 4 LT near 63° N.
IWC median values at mid latitudes are much smaller (about 100 times) than those at high latitudes. Therefore we also use the ratio of daily maximum to minimum IWC values as an additional indicator for local time variations, see Table 5. Please note that the ratios are calculated from median IWC values without any lower threshold, hence the occurrence frequency has a large influence on the median value. This is in particular important at the lowest latitude band (61.5°–64.5°N) where rather small PMC occurrence frequencies are modeled. E.g., assuming an IWC threshold of 5 g/km², the PMC occurrence frequency at this latitude band is only in the order of 5–10% during July whereas moving poleward it increases to about 50% at 67.5°–70.5°N and 100% at 73.5°–76.5°N. For this reason results for the lowest latitude band is omitted in further discussions (61°–65°N) in Table 4 include enhanced uncertainties.

Table 5 also includes tidal amplitude ratios obtained from fitting of 24 h, 12 h, and 8 h harmonic components. We find that for the three highest latitude bands the diurnal component is generally about two times larger than the semidiurnal component. Additionally, we find that the ratio of daily maximum to minimum IWC values as an additional indicator for local time variations, see Table 5. Please note that the ratios are calculated from median IWC values without any lower threshold, hence the occurrence frequency has a large influence on the median value. This is in particular important at the lowest latitude band (61.5°–64.5°N) where rather small PMC occurrence frequencies are modeled. E.g., assuming an IWC threshold of 5 g/km², the PMC occurrence frequency at this latitude band is only in the order of 5–10% during July whereas moving poleward it increases to about 50% at 67.5°–70.5°N and 100% at 73.5°–76.5°N. For this reason results for the lowest latitude band is omitted in further discussions (61°–65°N) in Table 4 include enhanced uncertainties.

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Figure 8. Median IWC values for July 2007–2013 as function of latitude for different local times. No threshold has been applied. IWC values of zero (no PMC) are included. The vertical bars represent the lower and upper quartile of the data.

calculated over three latitude bands used in SBUV trend analysis and for three thresholds with $IWC \geq 2013$. Figure 7 shows time series of July mean amplitudes and amplitude ratios for the 240 h and 12 g/km$^2$. IWC h components in the latitude band $67.5 > 10$ g/km$^2$, and $IWC > 40$ g/km$^2$. The latter threshold was used in SBUV trend analyses by DeLand and Thomas (2015) and Hervig and Stevens (2014). Both absolute means and absolute local time variations, expressed here as difference between maximum and minimum value, increase towards the pole. We find the ratio of maximum to minimum values, a measure for the relative IWC local time variation, to increase poleward too. Additionally, IWC ratios decrease with higher thresholds, e.g. at latitudes $64^\circ - 70^\circ - 74^\circ N$. The time series feature substantial year to year variations, e.g. from 6.6 (IWC > 0) to 2.4 (IWC > 10) and 1.7 (IWC > 40), see Table 5 (7th column).

Maximum values of up to 100 IWC occur in general during the early morning hours whereas minimum values are present in the afternoon hours. Local times of IWC maximum and minimum are independent of the selected threshold. There exists a time shift in latitudinal direction, e.g. at polar latitudes $74^\circ N$ from one year to the next, which is comparable to observations.
Figure 9. Diurnal variation of hourly median IWC values for July 2007–2013 for different latitude bands. No threshold has been applied. IWC values of zero (no PMC) are included. Dots indicate the data and solid lines are harmonic fits using periods of 24, 12, 8 h.

...of tidal amplitudes in PMC parameters at ALOMAR. The diurnal component dominates during all years and its amplitude is about twice as much compared to the semidiurnal component. Both amplitude time series are highly correlated (r = 0.97) at 62°N, the maximum occurs at 9.5 h. IWC values increase by a factor of about 3.8 over the entire time period, however, this increase originates mainly from the years after 1999. The result matches the break point used for trend calculations in the SBUV-PMC data set and accounts for a reversal in temperature trend at 63 LT for IWC > 40 g/km² whereas at mid latitudes 50°–64°N it is shifted forward in time to 8 LT. Recently, Stevens et al. (2017) reported about model results of PMC IWC calculations with the NOGAPS-ALPHA model using a 1-d bulk ice model (Hervig et al., 2009b). The authors show that the IWC is largest at highest latitudes and yields a morning peak between 5 and 7 LT and a late afternoon minimum equatorward of 80°N regardless of threshold. Diurnally averaged IWC values (threshold of 40 g/km²) from linear regression analysis follow slopes of 3.1 and ±1.2 are near 100 g/km² and consistent with those calculated by MIMAS. NOGAPS-ALPHA results of IWC over a diurnal cycle show at 68°N a ratio between IWC maximum and minimum of about 1.5 for a threshold of 40 (see Figure 6a,b in Stevens et al. (2017)) similar to a ratio of 1.7 from MIMAS calculations. Concurrently, absolute IWC local time variations in NOGAPS-ALPHA increase towards higher latitudes and are threshold dependent. Again, these features are confirmed by MIMAS.

Lidar observations of daily variations of mid-latitude NLC (54°N, Kühlungsborn, Germany) show highest rates at 5–6 LT which is similar to our model result (Gerding et al., 2013). On the other hand, DeLand et al. (2011) published local time observations by the Aura OMI (Ozone Monitoring Instrument) satellite instrument which indicates maximum frequency and albedo values at approximately 9–10 h LT at 70°N for the NH 2007 season, with a smaller amplitude and a slight phase shift to ~8 h LT at higher latitudes. Hence, model results from MIMAS deviate to some extent from these satellite measurements for 2007. Here we refer to some year-to-year variations of phases in MIMAS (not shown here) which might explain to some extent these differences.
As shown in section 2.2, phase positions of minimum temperature at PMC altitudes move to some extent during early morning hours backwards in time in poleward direction. Also the phase of the daily water vapor maximum tends to follow this time shift. We conclude that both temperature and water vapor phases cause the general early morning hour structure in IWC and its shift towards higher latitudes.

Generally, the time difference between IWC maximum and minimum is approximately constant with 12 hours at all latitudes and for all three thresholds. This indicates that a tidal decomposition of daily data reveals the significant role of the diurnal tidal oscillation. Indeed, all daily time series of IWC are approximated to a high degree by harmonic fits of a dominant 24 h and a minor 12 h component, the ratio \( A_{24}/A_{12} \) for the diurnal \( A_{12} \) varies between 4.5 and semidiurnal amplitude respectively, over the entire time period 1979–2013. Hence, semi diurnal fluctuations in IWC are of minor importance which again is explained by small semi diurnal tidal amplitudes in temperature and water vapor. We note that ter diurnal tidal components are also present. But on average 8–12 h amplitudes are in the order of 20. The ratio of diurnal to semi diurnal amplitudes remains almost constant in time with some variability. Interestingly, the diurnal and semi diurnal phases in IWC (not shown) remain quite constant over the years. % of 12 h amplitudes and therefore have a negligible impact.

In summary our MIMAS results show a We summarize that these results highlight the importance of taking tidal PMC variations into account when compiling data sets which are distributed over latitude and local time. It turns out that for IWC (1) local time variations depend on threshold conditions, e.g. relative local time variations decrease with larger thresholds; (2) local time variations depend on latitude, e.g. absolute local time variations increase towards the pole; (3) a phase shift exists towards the pole which is independent of the threshold value, e.g. the IWC maximum moves backward in time from 8 LT at mid latitudes to 2 LT at high latitudes. The IWC local time behaviour presumably exhibits year-to-year as well as long-term change in tidal amplitudes of IWC. They increase significantly which is presumably caused by an increase of tidal amplitudes of background temperature during this time period – variability which may effect the 35-y mean state given in Table 5. However, this topic needs more detailed investigations and will be subject of future simulations with LIMA/MIMAS work.

7 Conclusions

In this paper we presented a detailed investigation of tidal effects on PMC occurrence, altitude, brightness and microphysical properties of ice particles as calculated by the MIMAS model. As already discussed in several publications, the interpretation of PMC observations requires a careful treatment of the local time of the observations even for the investigation of long-term records (Fiedler et al., 2011; DeLand and Thomas, 2015; Stevens et al., 2017). We have compared our results to observations by ground-based lidar as well as satellite instruments and find a good agreement when taking into account instrumental sensitivity and local time dependence of observations. MIMAS reproduces the local time variations seen by lidar especially well in the core of the PMC season. In general diurnal, semi diurnal and semi diurnal components contribute to the tidal behavior of PMC parameters calculated by MIMAS.

The MIMAS simulations of PMC at ALOMAR show that the brightness varies PMC simulations for ALOMAR show in the latitude range 67°–71°N brightness variations throughout the day by up to a factor of 7, while the occurrence frequency
20 varies by a factor of 2 to 16 for faint and strong clouds, respectively. The median number density varies by a factor of 2 and the particle radius only by about 30. At the peak of the PMC layer the mean ice particle radius varies from 35 to 45 \( \mu \text{m} \) and the mean number density from 80 to 150 \( \text{cm}^{-3} \) throughout the day. All quantities show the maximum around a local time of 3±2 h. At the same latitude band the time of maximum IWC is about 3 LT and the minimum is found around 18 LT. Without thresholding the data, hourly IWC median values vary by a factor of 10 throughout the diurnal cycle in July (2007–2013).

In general diurnal and semidiurnal tides in temperature and water vapor contribute to the tidal behavior of PMC parameters whereas terdiurnal tidal structures are of minor importance.

Our analysis shows that the local time dependence becomes most evident when concentrating on one single season. When limiting the analysis to the season 2009 we find that the variation of temperature and water vapor at the altitude of brightest PMC (strong cloud class) throughout the day is 2 local time variations of temperature at 69°N are in a range of 6 K and 2 near 83 ppmv, respectively. At the altitude of sublimation (about 1 km altitude, at sublimation altitudes (near 81.5 km) we find a variation of 2 the water vapor variation is about 7 K and 3 ppmv between minimum and maximum. These variations lead ppmv. The variation in water vapor leads to a change of the saturation ratio from about 1.8 around midnight to 1 in the afternoon.

We find that the local time dependence of IWC is affected by latitude. Amplitudes increase towards the pole, but the ratio of daily maximum to minimum values decreases towards the pole. On average the IWC varies by a factor of 10 throughout the diurnal cycle. It is remarkable that the local time of maximum IWC changes from about 4 calculated a climatology of IWC local time variations from a 35-year average from 1979 to 01 LT for latitudes from 63° to 2013 for different thresholds and latitude.
bands, which might be useful for satellite data analysis in order to perform local time corrections. Local time variations are found to depend on latitude and threshold conditions. For the latitude band 64° N to 81–74° N, respectively.

PMC tidal amplitudes show substantial year to year variations as well as a mean increase from 1979 N and a threshold of IWC ≥ 2013. The linear trend terms of diurnal and semidiurnal components are calculated to be 3.1 and 1.40 g/km². IWC maximum and minimum values occur around 3 LT and 19 LT, respectively, with a ratio maximum to minimum of 6.6. For a threshold of IWC > 40 g/dec. Phases of both tidal components are fairly constant over the whole data set. km² the local times for maximum and minimum are identical, but the ratio changes to 1.7. A phase shift exists for the IWC local time behavior towards the pole, which is independent of the threshold value. We find the absolute IWC local time variation to generally increase with latitude. Furthermore, the IWC maximum moves backward in time from 8 LT at mid latitudes to 2 LT at high latitudes.

It should be noted that gravity waves could mask the influence of tides especially for the terdiurnal component and the year to year variations. Gravity waves are partly included in the LIMA-MIMAS model, but a detailed investigation regarding their effects on the tidal behavior of PMC is beyond the scope of this paper. However, we expect that the latitudinal and the year to year variations of the tidal amplitudes are robust and will help interpreting long-term observations with varying latitudes and fixed or variable local times.

Acknowledgements. We appreciate the financial support from the German BMBF for the ROMIC/TIMA project. This research was supported by the European Union’s Horizon 2020 Research and Innovation program under grant agreement No 653980. We thank the AIM community for providing us with SOFIE and CIPS data that are available online at http://sofie.gats-inc.com/sofie/index.php and http://lasp.colorado.edu/aim/download-data.php, respectively. The European Centre for Medium-Range Weather Forecasts (ECMWF) is gratefully acknowledged for providing ERA-40 and operational analysis data.
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