Amorphous and crystalline aerosol particles interacting with water vapor – Part 1: Microstructure, phase transitions, hygroscopic growth and kinetic limitations

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Abstract

Interactions with water are crucial for the properties, transformation and climate effects of atmospheric aerosols. Here we outline characteristic features and differences in the interaction of amorphous and crystalline aerosol particles with water vapor. Using a hygroscopicity tandem differential mobility analyzer (H-TDMA), we performed hydration, dehydration and cyclic hydration&dehydration experiments with aerosol particles composed of levoglucosan, oxalic acid and ammonium sulfate (diameters ∼100–200 nm, relative uncertainties <0.4%, relative humidities <5% to 95% at 298 K). The measurements and accompanying Köhler model calculations provide new insights into particle microstructure, surface adsorption, bulk absorption, phase transitions and hygroscopic growth. The results of these and related investigations lead to the following main conclusions:

1. Many organic substances (including carboxylic acids, carbohydrates and proteins) tend to form amorphous rather than crystalline phases upon drying of aqueous solution droplets. Depending on viscosity and microstructure, the amorphous phases can be classified as glasses, rubbers, gels or viscous liquids.

2. Amorphous organic substances tend to absorb water vapor and undergo gradual deliquescence and hygroscopic growth at much lower relative humidity than their crystalline counterparts.

3. In the course of hydration and dehydration, certain organic substances can form rubber- or gel-like structures (supra-molecular networks) and undergo stepwise transitions between swollen and collapsed network structures.

4. Organic gels or (semi-)solid amorphous shells (glassy, rubbery, ultra-viscous) with low molecular diffusivity can kinetically limit the uptake and release of water by submicron aerosol particles on (multi-)second time scales, which may influence the hygroscopic growth and activation of aerosol particles as cloud condensation nuclei (CCN) and ice nuclei (IN).
5. The shape and porosity of amorphous and crystalline particles formed upon dehydration of aqueous solution droplets depend on chemical composition and drying conditions. The apparent volume void fractions of particles with highly porous structures can range up to ~50% or more (xerogels, aerogels). Void fractions as well as residual water in dried aerosol particles that are not water-free (due to kinetic limitations of drying or stable hydrate formation) should be taken into account in Köhler model calculations of hygroscopic growth and CCN activation.

6. For efficient description of water uptake and phase transitions of amorphous and crystalline organic and inorganic aerosol particles and particle components, we propose not to limit the terms deliquescence and efflorescence to equilibrium phase transitions of crystalline substances interacting with water vapor. Instead we propose the following generalized definitions: Deliquescence is the transformation of a (semi-)solid substance into a liquid aqueous solution, whereby water is absorbed from the gas phase (“liquefaction upon humidification/hydration”). Efflorescence is the transformation of a substance from a liquid aqueous solution into a (semi-)solid phase, whereby water is evaporated (“solidification upon drying/dehydration”). According to these definitions, individual components as well as entire aerosol particles can undergo gradual or prompt, partial or full deliquescence or efflorescence.

1 Introduction

The interaction of aerosol particles with water vapour is a central issue of research in atmospheric and climate science (Martin, 2000; Kanakidou et al., 2005; Lohmann and Feichter, 2005; Pöschl, 2005; McFiggans et al., 2006; Fuzzi et al., 2006; Andreae and Rosenfeld, 2008; Rosenfeld et al., 2008; Wang et al., 2008a, b; Heintzenberg and Charlson, 2009, and references therein). Numerous studies have investigated the hygroscopicity of aerosol particles, i.e. their ability to absorb water vapour, as a function
of chemical composition and relative humidity (RH), and many researchers have noted that the hygroscopic properties of aerosol particles can substantially differ from those of the corresponding bulk material.

For example, aerosol particles composed of certain water-soluble inorganic salts can reversibly take up water vapour without the prompt deliquescence and efflorescence phase transitions and hysteresis effects typically observed for the corresponding crystalline bulk material: CaCl$_2$ and MnSO$_4$ (Cohen et al., 1987); NH$_4$NO$_3$ (Tang, 1980; Dougle et al., 1998; Cziczo and Abbatt, 2000; Lee and Hsu, 2000; Mikhailov et al., 2004; Schlenker et al., 2004; Schlenker and Martin, 2005; Svenningsson et al., 2006), NH$_4$HSO$_4$ (Tang and Munkelwitz, 1994; Cziczo et al., 1997; Cziczo and Abbatt, 2000; Lee and Hsu, 2000; Martin et al., 2003; Colberg et al., 2003, 2004; Schlenker et al., 2004; Schlenker and Martin, 2005), NaNO$_3$ (McInnes et al., 1996; Lee and Hsu, 2000; Gysel et al., 2002; Hoffmann et al., 2004).

Similar behaviour has been observed for certain organic compounds such as carbohydrates, dicarboxylic acids and multifunctional compounds: levoglucosan (Mochida and Kawamura, 2004; Chan et al., 2005; Svenningsson et al., 2006), mannansan and galactosan (Chan et al., 2005), maleic and malonic acid (Peng et al., 2001; Choi and Chan, 2002a; Brooks et al., 2003; Wise et al., 2003), malic and citric acid (Peng et al., 2001; Choi and Chan, 2002a), and protein macromolecules (Mikhailov et al., 2004).

Depending on the nature and proportion of substances involved, the internal mixing of organic and inorganic aerosol components usually leads to a decrease of deliquescence and efflorescence RH (Brooks et al., 2002, 2003; Choi and Chan, 2002b; Marcolli et al., 2004; Mikhailov et al., 2004; Parson et al., 2004; Moore and Raymond, 2008; Zardini et al., 2008) or to gradual reversible water uptake starting at very low RH (Dick et al., 2000; Peng and Chan, 2001; Choi and Chan, 2002b; Brooks et al., 2003; Prenni et al., 2003; Svenningsson et al., 2006; Zardini et al., 2008).

Mechanistically, the ability for continuous and reversible water uptake has been attributed to the presence of residual water in non-effloresced, (quasi-)liquid particles (Peng et al., 2001; Prenni et al., 2003; Mochida and Kawamura, 2004; Moore and
Raymond, 2008; Zardini et al., 2008) or to the morphology or amorphous state of (quasi-)solid particles (Cohen et al., 1987; Onasch et al., 2000; Peng and Chan, 2001; Marcolli et al., 2004).

Based on electron microscopy and infrared spectroscopy, Hoffman et al. (2004) concluded that the drying of aqueous NaNO₃ droplets yields solid amorphous particles that remain metastable at very low relative humidity as well as under vacuum conditions and undergo continuous hygroscopic growth. Using Raman spectroscopy, Tang and Fung (1997) found that the drying of levitated aqueous droplets of Ca(NO₃)₂ and Sr(NO₃)₂ yields solid amorphous microparticles that deliquesce at lower RH than their crystalline counterparts. Krueger et al. (2003) found similar deliquescence behavior of Ca(NO₃)₂ formed by heterogeneous reaction of CaCO₃ particles with gaseous nitric acid. Rosenoern et al. (2008) suggested that the hygroscopic properties of nanocrystalline aerosol particles may also deviate from those of crystalline bulk material, and several studies pointed out that the drying conditions have a strong influence on the morphology of solid aerosol particles (e.g., Mikhailov et al., 2004; Biskos et al., 2006; Rose et al., 2008; Rosenoern et al., 2008).

The formation of amorphous solid particles upon spray-drying of aqueous solutions of organic substances is a well-known standard process in the food and pharmaceutical industries, and the amorphous state of spray-dried organic materials was confirmed by X-ray diffraction, differential scanning calorimetry (DSC) and dynamic gravimetric vapor sorption methods (Corrigan, 1984; Roberts and Debenedetti, 2002; Price and Young, 2003; Burnett et al., 2004; Langrish and Wang, 2006, and references therein).

Recently, Murray (2008) and Zobrist et al. (2008) have shown that emulsified and bulk samples of atmospherically relevant aqueous organic and multi-component solutions can form glasses at low temperatures and may influence the interaction of aerosol particles with water in the upper troposphere, in particular the nucleation and growth of ice crystals. To our knowledge, however, the formation of solid amorphous aerosol particles upon drying of aqueous organic solution droplets has not yet been positively identified, and the relations between the deliquescence/efflorescence and the
microstructure of amorphous organic particles have not been characterized in earlier studies investigating the hygroscopic properties of atmospheric aerosols.

In this study, we have employed a hygroscopicity tandem differential mobility analyzer (H-TDMA) to investigate the water uptake and phase transitions of amorphous and crystalline aerosol particles in the size range of the atmospheric aerosol accumulation mode (∼100 nm) under ambient conditions. Here we present substance-specific results for pure levoglucosan, oxalic acid, and ammonium sulfate, and we outline general features and differences in the interaction of amorphous and crystalline aerosol particles with water vapor. Complementary results for aerosols consisting of internally mixed organic/inorganic and amorphous/crystalline components will be presented in a companion paper (Mikhailov et al., 2009).

2 Methods

2.1 Substances and deliquescence relative humidity of bulk samples

The following substances were used to prepare the investigated aerosols and bulk samples (provider, purity, molar mass and density at 298 K): crystalline ammonium sulfate ((NH₄)₂SO₄, Fluka, >99.5%, 132.16 g mol⁻¹, 1769 kg m⁻³), crystalline oxalic acid dihydrate ((COOH)₂·2H₂O, Fluka, >96%, 126.07 g mol⁻¹, 1653 kg m⁻³), crystalline levoglucosan (1,6-anhydro-β-D-glucopyranose, C₅H₁₀O₅, Fluka, >98%, 162.14 g mol⁻¹, 1600 kg m⁻³), crystalline glutaric acid (COOH-(CH₂)₃-COOH, Fluka, >96%, 132.12 g mol⁻¹, 1429 kg m⁻³), and deionised water (Millipore–Milli Q plus 185, 18.2 MΩ cm, 18.02 g mol⁻¹, 997.1 kg mol⁻¹).

To determine the deliquescence relative humidity of bulk samples, 7–8 g of the crystalline substances were placed in a plastic bottle (polyethylene, 3.5 cm i.d, 8.5 cm height), and liquid water was added to prepare a thoroughly mixed aqueous slurry with a thin liquid solution layer (∼2 mm) covering the solid sample substance (Wexler and Brombacher, 1951). A capacitive humidity sensor (Ahlborn A646, precision ±0.5% RH,
accuracy ±2% RH and ±0.1 K) was positioned in the center of the bottle over the liquid surface. Then the bottle was closed with a plastic lid, dipped into a water bath kept at (298.2±0.2) K, and equilibrated over several hours to days (until the measured RH was constant over several hours). The constant saturation RH measured over the bulk samples (RH\textsubscript{s,b}) was taken as the bulk deliquescence RH of the investigated crystalline substances (RH\textsubscript{d,b}).

The humidity sensors used in the bulk sample and aerosol experiments (H-TDMA) were calibrated over the range of 11–94% RH using saturated aqueous solutions/slurries of LiCl (11.3±0.3%), CH\textsubscript{3}COOK (22.±0.3%), MgCl\textsubscript{2} (32.8±0.2%), K\textsubscript{2}CO\textsubscript{3} (43.2±0.3%), Mg(NO\textsubscript{3})\textsubscript{2} (52.9±0.2%), NaCl (75.3±0.1%), (NH\textsubscript{4})\textsubscript{2}SO\textsubscript{4} (81.0±0.3%), KNO\textsubscript{3} (93.6±0.6%) (Greenspan, 1977) in the same setup as for the determination of RH\textsubscript{s,b}. The uncertainty of the calibration was of the order of ~1% RH (standard deviation of linear regressions).

2.2 H-TDMA setup and modes of operation

The hygroscopicity tandem differential mobility analyzer (H-TDMA) system and experimental procedures were essentially the same as described by Mikhailov et al. (2004), except for a few modifications aimed at minimizing experimental uncertainties (Fig. 1). Aerosols were generated by nebulization of aqueous solutions of the investigated substances in deionised water (solute mass fraction 0.1%). The solution droplets generated by nebulisation were dried using a couple of silica gel diffusion dryers (SDD) with an overall aerosol residence time of ~30 s; the residual relative humidity was <5% throughout all experiments (RH\textsubscript{1}, Fig. 1). All H-TDMA experiments were performed at ambient temperature and pressure (298±2 K, ~960 hPa).

The dry polydisperse aerosol was passed through a neutralizer (\textsuperscript{85}Kr, TSI, 2 mCi, Model 3077), and a monodisperse aerosol with the desired initial dry particle diameter was selected by the first differential mobility analyzer (DMA1). The size-selected particles were then passed through a conditioner (Nafion, Ansyco) with a residence time of 13 s (conditioner and subsequent lines leading to DMA2). The size distribu-
tion of the conditioned particles was measured with a scanning mobility particle sizer (SMPS) consisting of DMA2 (TSI Model 3071), a condensation particle counter (CPC, TSI 3025), and a computer (TSI AIM 4.3 software). The relative humidity and the temperature of aerosol and sheath inflow and exhaust outflow of DMA2 were measured with capacitive humidity sensors (Ahlborn A646) calibrated as described above. A fan was used to ventilate air through the housing of DMA2 to equilibrate the temperature and relative humidity of sheath flow and excess flow (agreement of RH3 and RH4 generally better than ±2% RH). Note that the uncertainties of humidity control in the H-TDMA system (up to ±2% RH) was generally larger than the uncertainty of measuring diameter changes and growth factors, respectively (<0.4%).

Based on Mikhailov et al. (2004), the H-TDMA system was used in three different modes of operation. These correspond to different sequences of humidification and drying (“RH histories”) of the aerosol particles as outlined in Table 1 and enable efficient investigation of different phenomena.

1. H-TDMA mode 1 (“hydration”) provides information about structural rearrangements and deliquescence phase transitions of dry particles and the hygroscopic growth of deliquesced particles (aqueous solution droplets) as a function of relative humidity upon particle sizing and conditioning (variable $X \approx RH2 \approx RH3 \approx RH4$).

2. H-TDMA mode 2 (“dehydration”) provides information about the efflorescence transition of deliquesced particles and the hysteresis loop between deliquescence and efflorescence transitions as a function of relative humidity upon particle sizing after conditioning and deliquescence at high RH (variable $X \approx RH4; RH2 \approx RH_{s,b} + 5\%;$ max. 95%). In this mode as well as in mode 3, DMA2 serves not only for particle sizing but also for particle drying (residence time ~7.5 s; Mikhailov et al., 2004).

3. H-TDMA mode 3 (“hydration & dehydration”, “h&d”) provides information about structural changes and/or partial evaporation of particles as a function of the maximum relative humidity experienced during a cycle of humidification and drying.
Note that in most other H-TDMA studies a pre-dryer has been applied before DMA2 when performing dehydration or h&d experiments. For the experiments presented in this manuscript, however, we have intentionally not used a pre-dryer before DMA2 in order to obtain information about kinetic limitations of dehydration processes. In our dehydration and h&d experiments with dry sheath air (RH3<5%), the average relative humidity in DMA2 obtained by equilibration of aerosol and sheath flow through diffusion of water vapour was in the range of <5% to ~10% (~0.1 × RH2). Model calculations solving the convective-diffusion equation with a finite element software package (FEMLAB & Matlab) for the applied DMA and operating conditions (TSI Model 3071; aerosol flow 0.3 l/min; sheath flow 3 l/min) show that the maximum radial deviations from the average relative humidity in DMA2 were reduced to ≤30% after 0.1 s (<5% after 0.5 s) and should have negligible influence on the experimental results. Only at high RH in the h&d experiments, the enhanced RH of the aerosol flow along (up to ~30% for ~0.1 s) may have had a significant influence on the measured mobility diameter, causing deviations up to ~1% or ~1 nm, respectively, according to the DMA model calculations described below.

To characterize the effects of combined drying and sizing of aerosol particles in DMA2, i.e., the influence of dehydration-related particle mobility changes inside DMA2, we performed DMA model calculations for aerosol particles undergoing size changes in the range of 200 nm to 100 nm (Wang and Flagan, 1990; Endo et al., 1997). The model results have the following implications: (1) If the dehydration processes (efflorescence, restructuring, or desorption) inside DMA2 are completed within ~0.1 s, then the
resulting changes in particle mobility diameter should be fully captured with deviations <1%. (2) Kinetically limited dehydration processes that lead to progressive changes of particle mobility on a time scale of \(\sim 0.1\)–\(10\) s should significantly influence the particle sizing (deviations >1%) and lead to a broadening of the measured size distributions (increase of geometric standard deviation, \(\sigma_g\)). (3) Dehydration processes progressing on time scales >\(10\) s should have no effect on particle sizing (no change of mobility diameter and no broadening of size distribution).

2.3 H-TDMA measurement data analysis and precision

The particle size distributions measured with the SMPS system (DMA2) were fitted with a log-normal distribution function (CPC raw counts on a linear scale vs. mobility equivalent diameter on a logarithmic scale with 64 channels per decade; TSI AIM 3.4 and Origin 7.5 software), and the modal diameter \(\left(\bar{D}_b\right)\) and geometric standard deviation \(\sigma_g\) of the fit function were used for further data analysis and plotting. The initial dry particle diameter \(\left(D_{b,i}\right)\), i.e. the modal diameter of unconditioned monodisperse aerosol size-selected with DMA1, was generally kept at \((99.5\pm0.2)\) nm. Mobility-equivalent particle growth factors, \(g_b\), were calculated relative to the minimum mobility diameter observed in H-TDMA operation mode 3 (h&d): \(g_b = \frac{\bar{D}_b}{\bar{D}_{b,h&d,\min}}\).

The precision of repeated mobility diameter measurements was generally about ±0.1% (relative standard deviation of five repeated measurements), the variability over the \(\sim 4\) h needed to perform a complete experiment in one of the H-TDMA operation modes (preceded by \(\sim 3\) h warm-up time) was generally less than ±0.2%, and the drift was less than 0.2% (Fig. 2a). Accordingly, the uncertainty of relative changes in \(\bar{D}_b\) and the uncertainty of \(g_b\) were less than 0.4%. The statistical uncertainty of \(\sigma_g\) was around 0.3% (relative standard deviation of five repeated measurements). High precision and accuracy of the measured and calculated values of \(\bar{D}_b\) and \(g_b\), respectively, were confirmed by good agreement of the measurement results for pure ammonium sulfate particles with a reference Köhler model (mean relative deviation <1%; Sect. 3.5.1).

Figure 2b shows the results of test experiments in which the residence time of the
aerosol between the two DMAs up to 30 s under dry conditions, to check if investigated organic aerosol components evaporated on the time scale of the reported experiments. No evaporative losses were detected for levoglucosan and oxalic acid, whereas glutaric acid particles evaporated rapidly at a rate of 2.5 nm s\(^{-1}\) (slope of linear fit).

3 Results and discussion

3.1 General concepts

3.1.1 Water uptake by crystalline substances

Figure 3 outlines some basic processes and differences in the uptake of water vapor by aerosol particles consisting of crystalline or amorphous substances. The envelope shape of solid crystalline particles is often not spherical, and polycrystalline materials and agglomerates may also be porous. The porosity of crystalline sub-micron aerosol particles generated by spray drying, however, is usually not very high (apparent void fractions <20%; Krämer et al., 2000; DeCarlo et al., 2004; Mikhailov et al., 2004). Upon hydration (increase of relative humidity), crystalline substances typically adsorb only a small amount of water at the surface, which may lead to microstructural rearrangements and compaction of the particle (change of shape or porosity and decrease of mobility equivalent diameter) due to capillary effects or partial dissolution and recrystallization (Krämer et al., 2000; Mikhailov et al., 2004; Biskos et al., 2006; Zardini et al., 2008). Bulk absorption of water into the crystalline material may occur in case of hydrate formation (uptake of crystal water), but this appears not relevant for the inorganic salts that are most abundant in the atmosphere and it does normally not lead to a major increase of particle diameter.

At a substance-specific threshold relative humidity, pure substances (particles) that are crystalline and water-soluble undergo prompt deliquescence transitions, i.e., first-order phase transitions in which the solid substances (particles) are transformed into
saturated aqueous solutions (liquid droplets). Note, however, that crystalline multi-component mixtures can exhibit a stepwise onset of deliquescence (eutonic point) followed by further gradual water uptake until complete dissolution. Upon dehydration (decrease of RH), the evaporation of water and crystallization of the solute (efflorescence transition) typically occurs at a lower relative humidity than the deliquescence transition (hysteresis effect), which is due to the persistence of metastable aqueous solution droplets that are supersaturated with respect to the corresponding crystalline phases. For most water-soluble crystalline substances of atmospheric relevance the deliquescence relative humidity is higher than 50% (Martin, 2000). Ammonium sulfate is a typical example for such substances, and the surface adsorption of water, microstructural rearrangements and phase transitions of ammonium sulfate aerosol particles will be illustrated below (Sect. 3.2).

3.1.2 Water uptake by amorphous substances

Water uptake by amorphous substances typically proceeds in a gradual way, and their transition from solid to liquid state may involve intermediate semi-solid stages. Amorphous substances have no long-range atomic order and are classified as solid glasses when their viscosity exceeds $10^{12}$ Pa s (Angell, 1995; Debenedetti and Stillinger, 2001). Semi-solid amorphous substances like rubbers and gels have lower viscosities but still tend to retain their envelope shape (Roberts and Debenedetti, 2002).

The rubbery state usually occurs in polymeric substances, in which the individual macromolecules are entangled or cross-linked by covalent or hydrogen bonds, van der Waals forces, or other types of interaction (Erman and Mark, 1997; Cowie and Arrighi, 2007; Sperling, 2006). In food science and pharmaceutical research, however, the term rubber is also used for semi-solid amorphous substances with low molecular mass such as monosaccharides (Roos and Karel, 1991, 1992; Roos et al., 1999; Hancock and Zografi, 1997; Bhandari and Howes, 1999; Burnett et al., 2004).

Gels are two-phase mixtures of liquids dispersed in (semi-)solid amorphous matrices (supramolecular networks; Flory, 1974; Keller, 1995; Abdallah and Wise, 2000;
Sangeetha and Maitra, 2005; He et al., 2007), and the uptake of water into a gel can involve gradual swelling as well as stepwise volume increases related to thermodynamically well-defined phase transitions (Dusek and Patterson, 1968; Tanaka, 1978; Erman and Mark, 1997). Upon drying, gels can form highly porous structures (xerogels/aerogels; Kistler et al., 1935; McNaught and Wilkinson, 1997).

Ultra-viscous or highly viscous liquids exhibit viscosities that are close to the viscosity of glasses (>10^{10} Pa s) or at least several orders of magnitude higher than the viscosity of water at ambient conditions (>10^4 Pa s vs. ~10^{-3} Pa s; Hecksher et al., 2008). Such liquids can also be regarded as semi-solids when they behave in a non-ergodic manner, i.e., when the relaxation times of relevant properties are comparable to or longer than the time scales of imposed changes and observations, respectively (Lubchenko and Wolynes, 2007). For example, highly viscous liquids may exhibit fluid behavior such as viscous flow over long times scales (≥ minutes/hours). On short time scales (<minutes/hours), however, they may not be able to respond to mechanical forces or changes of ambient conditions (temperature, humidity) and thus appear (semi-)solid rather than liquid (non-ergodic behavior due to kinetic limitations).

The transition from the glassy state to a semi-solid state (rubbery, gel-like or ultra-viscous liquid) is called glass transition and characterized by the glass transition temperature, \( T_g \) (Angell, 1995; Debenedetti and Stillinger, 2001; Roberts and Debenedetti, 2002; Zobrist et al., 2008). At the glass transition, discontinuous changes can be observed in thermodynamic properties such as molar volume, enthalpy or entropy, but dynamic properties such as viscosity and diffusivity change only gradually. Thus, glass transitions are different from classical first-order phase transitions (crystal-to-liquid: melting or prompt deliquescence; liquid-to-crystal: freezing or prompt efflorescence) or second-order phase transitions (solid-to-solid: crystal lattice transformation). This is most evident by the fact that the glass transition temperature depends on the history of the glass formation process: large cooling rates usually result in higher \( T_g \) values than small cooling rates (Debenedetti and Stillinger, 2001; Zobrist et al., 2008).

Due to the very low molecular diffusivity of glasses, the uptake of water vapor by
glassy aerosol particles may often be limited to surface adsorption – at least on the time scales that are most relevant for the processing of particles suspended in the atmosphere or in laboratory experiments (seconds to hours; Parker and Ring, 1995; Burnett et al., 2004; He et al., 2006). In contrast, amorphous particles in a rubbery, gel-like or viscous liquid state \( (T>T_g) \) can efficiently absorb water into the particle bulk (Slade and Levine, 1991; Hancock, 1993; Mackin et al., 2002; Price and Young, 2003; Burnett, 2004; Dawson et al., 2009). Moreover water can act as a plasticizer and reduce the glass transition temperature of amorphous solids (Slade and Levine, 1991; Roos and Karel, 1991; Hancock and Zografi, 1997; Lourdin et al., 1997; Zobrist et al., 2008).

For example, the glass transition temperature of spray-dried lactose particles decreases with increasing relative humidity from 373 K under dry conditions to 298 K at 30% RH (Burnett et al., 2004). Accordingly, the increase of relative humidity over glassy lactose at 298 K leads to a phase transition (“moisture-induced glass transition”) that occurs at a “glass transition relative humidity” of \( \text{RH}_g \approx 30\% \). At \( \text{RH}_g \) the solid glass is transformed into a semi-solid state (rubbery, gel-like, ultra-viscous) that can absorb water and swell accordingly. Continued absorption converts the (semi-)solid particles into concentrated aqueous solution droplets that may be metastable (supersaturated/supercooled) with regard to crystalline phases but are in equilibrium with the relative humidity of the surrounding gas.

Overall, the transformation of (semi-)solid amorphous particles (glassy, rubbery, gel-like, or ultra-viscous) into liquid aqueous solution droplets by uptake of water vapor (combined humidification and liquefaction) can be regarded as a deliquescence transition (“amorphous deliquescence”). Similar to the glass transition (“amorphous melting”), the amorphous deliquescence can be a non-equilibrium phase transition when the particles are not in thermodynamic equilibrium with the surrounding water partial pressure. Alternatively the amorphous deliquescence can also be an equilibrium process when it is due to the transition between collapsed and swollen gel-like structures (Dusek and Petterson 1968; Tanaka, 1978; Erman and Mark, 1997), as detailed below.
in Sect. 3.3.2.

Due to the high viscosities and low molecular diffusivities of (semi-)solid amorphous substances, their deliquescence is likely to be kinetically limited (non-ergodic) on short time scales (≤ minutes/hours for sub-micron and micron-sized particles). In analogy to the dependence of $T_g$ on the rate of temperature change, RH$_g$ is expected to depend on the rate of humidity change, whereby higher rates of RH increase should lead to higher RH$_g$ values. For example, Burnett et al. (2004) observed an increase of RH$_g$≈30% at $d$RH$/dt$=2% h$^{-1}$ to RH$_g$≈40% at $d$RH$/dt$=10% h$^{-1}$ for spray-dried lactose at 298 K.

The absorption of water vapor or other gas molecules into the bulk of particles and droplets can be kinetically limited by surface processes (mass accommodation or surface accommodation and surface-bulk transfer, respectively) or by diffusion in the particle bulk (Seinfeld and Pandis, 2006; Pöschl et al., 2007). In case of highly viscous substances, the uptake of water is likely to be limited by bulk diffusion, leading to kinetically limited, gradual deliquescence transitions. The uptake of water into particles consisting of molecules with higher molecular mass will generally lead to a decrease of viscosity and increase of diffusivity. Thus, the process should be self-accelerating and may lead to temporary formation of core-shell structures with higher diffusivity in the outer shell, because water uptake begins at the surface (Zobrist et al., 2008).

Structural defects such as veins and pores in the particle bulk can accelerate the water uptake and reduce or abrogate diffusion-related kinetic limitations of deliquescence (Zardini et al., 2008). On the other hand, some organic substances (“gelators”, including carbohydrates and proteins) are able to form gel-like structures (supramolecular networks) that may inhibit molecular diffusion in the particle bulk and reinforce kinetic limitations of deliquescence (Farhat et al., 1997; Abdallah and Weiss, 2000; Estroff and Hamilton, 2004; He et al., 2007). Moreover, the filling or formation of aqueous pockets in gel-like structures can lead to stepwise swelling in the course of hydration and gradual deliquescence of amorphous aerosol particles (see results reported below and by Mikhailov et al., 2004).

While multicomponent mixtures may be thermodynamically stable in an amorphous
state (Marcolli et al., 2004; Cappa et al., 2008), amorphous (semi-)solids consisting of pure compounds or mixtures of a small number of components are usually metastable (supercooled/supersaturated) with regard to corresponding crystalline phases. The rates at which amorphous and dissolved organic substances crystallize are generally low and depend strongly on the presence of seed materials for crystal nucleation (e.g., Hilfiker, 2006). At room temperature and relative humidities of 50–70% the crystallization of spray-dried lactose and other sugars was found to proceed on time scales of hours (Burnett et al., 2004; Wang and Langrish, 2007), and no crystallisation was observed for micron-sized lactose particles of high purity (Price and Young, 2003). Accordingly, crystallization of organic compounds is not likely to occur in nanometer-sized aerosol particles unless they contain suitable seeds.

Upon dehydration of deliquesced organic particles (aqueous droplets) on time scales of seconds to minutes, continuous desorption of water vapor is expected to gradually convert the aqueous solution droplets into (semi-)solid amorphous particles. (“amorphous efflorescence”). The desorption of water and gradual efflorescence transition can be kinetically limited by the formation of gel-like structures or core-shell structures with low diffusivity in the outer shell (glassy, rubbery, ultra-viscous) where equilibration with the gas phase begins (Zobrist et al., 2008). Limitations of mass transport and charge effects may also lead to the formation of porous structures and irregular envelope shape, which can be particularly pronounced in case of organic substances mixed with inorganic salts (Mikhailov et al., 2004).

3.1.3 Generalized definitions of deliquescence and efflorescence

For efficient description of water uptake and phase transitions of amorphous and crystalline organic and inorganic aerosol particles and particle components, we propose not to limit the terms deliquescence and efflorescence to equilibrium phase transitions of crystalline substances (salts) interacting with water vapor. Instead we propose the following generalized definitions:
1. Deliquescence is the transformation of a (semi-)solid substance into a liquid aqueous solution, whereby water is absorbed from the gas phase (“liquefaction upon humidification/hydration”).

2. Efflorescence is the transformation of a substance from a liquid aqueous solution into a (semi-)solid phase, whereby water is evaporated (“solidification upon drying/dehydration”).

According to these definitions, individual components as well as entire aerosol particles can undergo gradual or prompt, partial or full deliquescence or efflorescence, which is indeed the case not only for amorphous organic substances but also for mixtures of crystalline inorganic substances. If required, the attributes gradual/prompt, partial/full and amorphous/crystalline should enable a clear and unambiguous distinction between the various types of deliquescence and efflorescence transitions that may occur upon humidification or drying of aerosol particles. Thus, we consider the broad definitions proposed above more useful and suitable for aerosol research than alternative approaches that might restrict the terms deliquescence and efflorescence exclusively to prompt dissolution or formation of crystalline substances, respectively.

The definitions proposed above are also consistent with the definition proposed by IUPAC (http://goldbook.iupac.org/D01582.html) and the various definitions used throughout chemistry, biology and medicine, which are usually not restricted to crystalline substances (e.g.: http://www.merriam-webster.com/dictionary/deliquescence, http://www.biology-online.org/dictionary/Deliquescence, http://medical.merriam-webster.com/medical/deliquesce, http://chemistry.about.com/od/chemistryglossary/a/deliquescencedf.htm, etc.).

Note that the proposed general definition of deliquescence does not include gradual hygroscopic growth and water uptake (dilution) of liquid aqueous solution droplets, because the latter does not involve the liquefaction of (semi-)solid phases. As shown below and in earlier studies, the hygroscopic growth of liquid aqueous droplets (fully deliquesced particles) usually leads to a smooth continuous change of particle size.
with relative humidity. In contrast, the onset, transformation of intermediate stages (semi-solid gel or shell structures, kinetic limitations) and completion of the deliquescence and efflorescence transitions of (semi-)solid amorphous substances are usually related to discontinuities in the variation of aerosol particle size with relative humidity (distinct changes in the slope and curvature of $D_b$, $g_b$, $\sigma_b$, and $N_{ML}$ plotted against RH; see below). In this regard and in general, the above definitions are also consistent with the definitions given by Martin (2000) in a review of phase transitions in atmospheric aerosols, including the deliquescence and efflorescence of (crystalline) salt particles.

In the following section (Sect. 3.2) we present results from high precision H-TDMA experiments with crystalline ammonium sulfate particles, which are the basis for a systematic comparison of amorphous and crystalline particle behavior and comprise a new approach of measuring surface adsorption of water vapor. However, readers interested only in amorphous particle behavior might want to skip Sect. 3.2 and proceed to Sect. 3.3.

3.2 Ammonium sulfate particles

3.2.1 Phase transitions and hygroscopic growth

Figure 4a shows the mobility equivalent growth factors observed for pure ammonium sulfate (AS) particles as a function of relative humidity (RH) in the H-TDMA operation modes of hydration and dehydration, respectively (Table 1, Sect. 2.2). It illustrates the typical behavior of crystalline inorganic salt aerosol particles interacting with water vapor (Martin, 2000).

Upon hydration, a steep increase of particle diameter due to a prompt deliquescence transition was observed at $\sim$80% RH in good agreement with bulk measurements and literature data of $R_{H_d}$ for crystalline AS (Table 2). The hysteresis loop observed upon dehydration is characteristic for crystalline salt particles; it is due to the persistence of metastable aqueous solution droplets which are supersaturated with respect to crystalline AS (Martin, 2000). The efflorescence transition resulting in the formation of salt
crystals and the evaporation of liquid water was observed at ~30% RH in good agreement with literature data of $\text{RH}_e$ for submicron ammonium sulfate particles (Table 2). Both the deliquescence and efflorescence transitions are also reflected by a broadening of the measured particle size distributions (increase of geometric standard deviation, Fig. 4b) which can be attributed to non-uniformity of the size-selected particles and experimental conditions (Weingartner et al., 2002; Mikhailov et al., 2004; Biskos et al., 2006). For Köhler model calculations of the hygroscopic growth see Sect. 3.5.

3.2.2 Microstructure and surface adsorption

Upon hydration from ~20% to ~50% RH, the mobility equivalent diameter of the investigated ammonium sulfate aerosol particles decreased by ~3%, which can be attributed to the transformation of porous or irregularly shaped particles into compact near-spherical particles (Krämer et al., 2000; Gysel et al., 2004; Brooks et al., 2004; Mikhailov et al., 2004). The difference between the mobility diameters of dry AS particles (RH<20%) observed in the hydration and in the dehydration experiments, respectively, can be explained by differences in the drying process before and after size selection in the H-TDMA system (Mikhailov et al., 2004; Biskos et al., 2006). Most likely the AS particles generated by nebulization carried excess electric charges and formed slightly porous or irregularly shaped structures upon drying (apparent volume void fraction ~4%, Table 2). As pointed out before (Mikhailov et al., 2004; Biskos et al., 2006; Rose et al., 2008), not only the charge state but also the exact conditions and rate of drying are important for the microstructure of aerosol particles generated by nebulization of aqueous solutions. In test experiments with increased residual relative humidity in the diffusion dryer (less dry silica gel), the mobility diameter reduction upon hydration decreased to ~2% at RH1=9% and to ~1% at RH1=15%, respectively. Similarly, Gysel et al. (2002) and Biskos et al. (2006) had reported mobility diameter reductions of 1–2% upon hydration of AS particles.

On the other hand, the AS particles formed upon dehydration and efflorescence of size selected particles (mostly carrying only a single elementary charge) appear to
have been compact and spherical. The mobility diameter of dry particles in the dehydration experiment \(D_{b,h,min}\) was nearly the same as the minimum mobility diameter observed in the hydration\&dehydration (h\&d) experiment \(D_{b,h,min} \approx D_{b,h&d,min}\), Table 2), and Köhler model calculations based on \(D_{b,h&d,min}\) as the mass equivalent dry particle diameter \(D_{m,s}\) are in excellent agreement with the observed hygroscopic growth curve. These findings confirm the compactness and spherical shape of dry particles with \(D_{b} \approx D_{b,h,min} \approx D_{b,h&d,min}\) (Sect. 3.5).

The higher geometric standard deviation of the particles observed at RH<50% in the dehydration experiment \(\sigma_{g} \approx 1.08\) compared to the hydration experiment \(\sigma_{g} \approx 1.06\), Fig. 4b) can be explained by the size selection of particles with the same mobility but different porosity/shape in the first mobility analyzer of the H-TDMA (DMA1). Upon conditioning and deliquescence/efflorescence in the H-TDMA the particles become more compact and spherical, and the original differences in porosity/shape are converted into differences in size (mass conservation). Particles that were more porous prior to conditioning are smaller after conditioning and lead to a spread of the size distribution measured with the second mobility analyzer (DMA2).

As illustrated in Fig. 5a, b, the difference between the mobility diameters observed in the hydration experiments and in the h\&d experiments provide information about the amount of water adsorbed on the surface of crystalline aerosol particles prior to deliquescence. Upon hydration, DMA2 is operated under humidified conditions and measures mobility diameter of particles with adsorbed water \(D_{b,h}\), whereas the h\&d mode enables the measurement of dry particle size \(D_{b,h&d}\) at RH<5% to 12%. At RH≤45% the differences between the hydration and h\&d operation modes can be attributed to differences in the kinetically limited microstructural rearrangement process (Mikhailov et al., 2004), which appears to be more efficient when the particles are not only humidified (hydration) but also re-dried (h\&d).

At RH≈50–70% the mobility diameter observed in the h\&d mode was practically independent of RH \(D_{b,h&d} \approx D_{b,h&d,min}\), indicating that the restructuring and compaction of the particles were completed. The increase of \(D_{b,h&d}\) at RH>80% may be due to
changes of particle microstructure resulting from the cycle of deliquescence and efflorescence that occurs in the course of h&d experiments at RH>RH\(_d\) or to the influence of particle drying on particle sizing in DMA2 (Sect. 2.2).

Assuming that the compacted particles at RH\(\approx\)50–70% were spherical and that the thickness of a monomolecular layer (ML) of water adsorbed on the surface is \(\sim 0.2\) nm (Romakkaniemi et al., 2001), we have converted the difference between the mobility diameters observed in hydration and h&d experiments into an equivalent number of water ML: \(N_{ML} = (D_{b,h} - D_{b,h&d}) / (0.4\ \text{nm})\) with the particle diameters given in units of nm. As detailed in the experimental section, the H-TDMA measurement precision was generally better than \(\sim 0.2\) nm; thus the uncertainty of \(N_{ML}\) is assumed to be less than \(\pm 1\) ML.

As illustrated in Fig. 5b, we obtained a near constant surface coverage by \(\sim 2\) ML of water for the RH range of 50–70% and an apparent increase up to \(\sim 10\) ML over the range of 70–77% RH.

The findings are consistent with earlier H-TDMA studies of water adsorption on AS particles. Romakkaniemi et al. (2001) found 0.5–1.5 ML of water on AS particles with 15 nm diameter in fair agreement with theoretical calculations considering the Kelvin effects and various types of adsorption isotherms. The adsorption of \(\sim 2\)–3 ML of water on the surface of ammonium sulfate at 50–70% RH is in good agreement with the BET (Brunauer, Emmett, Teller) calculations presented by Romakkaniemi et al. (2001). Biskos et al. (2006) also observed a gradual increase of the mobility diameter of AS particles in the range of 50–80% RH and attributed it to water adsorption. For particles in the size range of 40–60 nm they reported a diameter increase of 2–3% at \(\sim 79\)% RH, corresponding to \(\sim 3\) ML of water adsorbed on the surface. Moreover, they demonstrated that stronger increases of mobility diameter prior to deliquescence observed in earlier H-TDMA experiments (apparent non-prompt deliquescence) can be explained by measurement artifacts (deviations of RH in aerosol and sheath flow).

Accordingly, we attribute the apparent mobility diameter increase observed in our experiments at RH>70% (equivalent to up to \(\sim 10\) ML of adsorbed water) to deviations between aerosol and sheath flow RH in DMA2. The adsorption of \(\sim 10\) and more ML
of water on the surface crystalline aerosol particles prior to deliquescence appears unlikely, because this would essentially correspond to bulk condensation rather than surface adsorption of liquid water. In contrast to the gradual absorption of water into the bulk of amorphous substances, a swelling of crystalline salt particles due to bulk absorption of water appears not plausible.

In any case, the results of this and earlier studies show that care needs to be taken to avoid artifacts in the measurement and interpretation of H-TDMA and other experimental data with regard to surface adsorption or bulk absorption of water vapor by aerosol particles. In particular, the potential influence of particle microstructure (shape and porosity) should not be neglected in aerosol experiments. As illustrated in Fig. 5a, b, restructuring induced by hydration can have stronger effects on particle mobility diameter than the adsorption or absorption of water at low RH.

3.3 Oxalic acid particles

3.3.1 Particle composition and stability

Several studies have shown that dicarboxylic acids can evaporate on time scales of seconds and lead to artefacts in H-TDMA experiments (Cruz and Pandis, 2000; Prenni et al., 2001, 2003; Kumar et al., 2003; Bilde et al., 2003). As demonstrated by test experiments with increasing particle residence time under dry conditions in our H-TDMA setup (Fig. 2b), the oxalic acid particles (OA) generated and investigated in our study did not evaporate on the time scale of our experiments (up to ∼30 s, relative change of $D_b < 0.4\%$ and $|dD_b/dt| < 0.03 \text{ nm s}^{-1}$, respectively). In contrast, we could observe rapid evaporation of glutaric acid particles under the same conditions ($dD_b/dt = -2.5 \text{ nm s}^{-1}$), although the equilibrium vapor pressure of glutaric acid (132 g mol$^{-1}$) is an order of magnitude lower than that of anhydrous oxalic acid (90 g mol$^{-1}$) at 298 K: $7.8 \times 10^{-6}$ Torr vs. $8.3 \times 10^{-5}$ Torr (Saxena and Hildemann, 1996).

The most plausible explanation for the high stability (effective non-volatility) of the investigated OA particles is that they were not anhydrous but composed of oxalic acid...
hydrates. Indeed also the Köhler model calculations presented and discussed below (Sect. 3.5) suggest that the particles observed under dry conditions consisted of oxalic acid dihydrate or non-stoichiometric hydrates with 1–3 water molecules per oxalic acid molecule. Besides hydrates also dimer formation and surface kinetic effects might play a role in making OA particles less volatile than glutaric acid particles (surface vs. bulk accommodation, adsorption & desorption rate coefficients, etc.; Pöschl et al., 2007).

In any case, our results are consistent with those of earlier H-TDMA experiments by Prenni et al. (2001), who also observed evaporative losses for glutaric acid but not for oxalic acid and could describe the hygroscopic growth of OA particles under the assumption that the “dry” particles consisted of oxalic acid dihydrate.

3.3.2 Phase transitions and hygroscopic growth

Figure 4c shows the mobility equivalent growth factor observed upon hydration and dehydration of OA aerosol particles. Upon hydration up to ~40% RH, the mobility diameter of the OA particles decreased by ~7%. As discussed below, this can be explained by microstructural rearrangements and indicates that the investigated OA particles obtained by nebulisation and diffusion drying of aqueous solution droplets were not liquid-like but (semi-)solid and highly porous. At ~43% RH the particles exhibited a small but significant stepwise increase of mobility diameter by ~3%, which is accompanied by a pronounced broadening of the measured particle size distribution (peak of $\sigma_g$, Fig. 4d). These observations indicate a deliquescence transition, which is the transformation of (semi-)solid amorphous OA particles into aqueous droplets that starts at much lower RH than for crystalline OA (RH$_{b,s}$=96.7%, Table 2).

The continuous hygroscopic growth and the approximate coincidence of hydration and dehydration curves above ~50% RH confirm that the particles were at least partially deliquesced aqueous droplets (Fig. 4c). However, the multiple wiggles in the growth curves and the large offset in the geometric standard deviations observed upon hydration and dehydration over the range of ~50–80% RH (Fig. 4c, d) are untypical and not plausible for fully deliquesced particles. With regard to the growth curves,
the observed deviations are at the edge of experimental precision, which is limited primarily with regard to RH, but for \( \sigma_g \) they are clearly larger. Only above \( \sim 80\% \) RH did the growth factors and geometric standard deviations agree within experimental uncertainty, indicating that the particles were fully deliquesced liquid aqueous solution droplets.

The most plausible explanation for these observations is a gradual deliquescence transition that involves the formation and swelling of gel-like structures in the highly concentrated aqueous OA droplets, which is consistent with the tendency of OA to form hydrogen bonds and hydrates (Hermida-Ramon et al., 2004; Chitra et al., 2004; Wenger and Bernstein, 2007). The formation and collapse of gel-like structures and related kinetic limitations of a gradual efflorescence transition are also the most plausible explanation for the stepwise \( \sim 3\% \) diameter decrease and the concurrent peak of \( \sigma_g \) observed at \( \sim 50\% \) RH in the dehydration experiment (Fig. 4c, d). Apparently, the oxalic acid and water molecules form a hydrogen-bonded network that breaks down when the volume fraction of water exceeds \( \sim 50\% \) (corresponding to \( g_b \geq 1.2 \) at \( RH \geq 80\% \)). Similar deliquescence and efflorescence transitions of amorphous organic aerosol particles and the formation of gel-like droplets have already been reported for aerosol particles composed of protein macromolecules (bovine serum albumin, BSA, 67 kg mol\(^{-1}\); Mikhailov et al., 2004): stepwise 3\% change of mobility diameter at \( \sim 40\% \) RH, wiggly growth curves, kinetic limitations of water uptake and release.

Most likely the stepwise diameter increase at \( \sim 40\% \) RH is related to a phase transition between collapsed and swollen gel structures (Dusek and Patterson, 1968; Tanaka, 1978; Erman and Mark, 1997), which might be triggered by a moisture-induced glass transition (Brownsey et al., 2003; Farahnaky et al., 2005; Zobrist et al., 2008). Whether or not the onset of deliquescence was triggered by a glass transition, further swelling and stepwise transformation of gel-like network structures appear to be the most plausible explanation for the wiggly particle growth curve and the size distribution broadening that persisted upon hydration up to \( \sim 80\% \) RH. On the other hand, a collapse of gel-like structures most plausibly explains the stepwise diameter decrease
that occurred upon dehydration at a relative humidity higher than the stepwise diameter increase observed upon hydration (∼50% vs. ∼43%, Fig. 4c).

3.3.3 Microstructure and bulk absorption

The ∼7% mobility diameter decrease observed upon hydration from ∼10% to ∼40% RH can be attributed to the transformation of porous or irregularly shaped solid particles into more compact near-spherical particles (Krämer et al., 2000; Gysel et al., 2004; Brooks et al., 2004; Mikhailov et al., 2004). As for AS, the difference between the mobility diameters of dry OA particles (RH<∼10%) observed in the hydration and in the dehydration experiments, respectively, can be explained by differences in the drying process before and after size selection in the H-TDMA system (Mikhailov et al., 2004). Most likely the OA particles generated by nebulization carried excess electric charges and upon rapid diffusion drying they formed highly porous xerogel structures (apparent volume void fraction ∼40%, Table 2).

On the other hand, the OA particles formed upon dehydration and efflorescence of size selected particles (mostly carrying only a single elementary charge) appear to have been compact and spherical. The mobility diameter of dry particles in the dehydration experiment ($D_{b,h,min}$) was nearly the same as the minimum mobility diameter observed in the hydration&dehydration (h&d) experiment ($D_{b,h,min}$≈$D_{b,h&d,min}$, Table 2), and Köhler model calculations based on $D_{b,h&d,min}$ as the mass equivalent dry particle diameter ($D_{m,s}$) were in fair agreement with the observed hygroscopic growth curve (Sect. 3.5). As for AS, the higher geometric standard deviation of the particles observed at RH<80% in the dehydration experiment ($\sigma_g$≈1.08–1.12) compared to the hydration experiment ($\sigma_g$≈1.06–1.08, Fig. 4d) can be explained by the size selection of particles with the same mobility but different porosity in the first mobility analyzer of the H-TDMA.

Figure 5c and d shows the difference between the mobility diameters observed in hydration experiments and h&d experiments with OA particles and the corresponding monolayer numbers ($N_{ML}$). At RH<40% the differences were apparently dominated
by more efficient restructuring in the h&d mode, as already discussed above for AS particles. At RH≈40% the restructuring was essentially completed (D_{b,h&d}≈D_{b,h&d, min}). The value of N_{ML}≈5 suggests that bulk absorption of water had already begun at 40% RH (albeit not as strongly as for LG particles with N_{ML}≈10, Fig. 5f, Sect. 3.4.2), because stronger surface adsorption than on AS particles appears unlikely (N_{ML}≈2–3 at 40–70% RH, Fig. 5b).

The pronounced particle swelling observed at RH≈43% corresponds to a water uptake of ≈15 ML or ≈15% of the particle volume, respectively, and the persistence of N_{ML}≈15 over the range of ≈43–55% RH (plateau in Fig. 5d) supports the idea that a metastable gel was formed (He et al., 2007). At RH>55% the absorption of water vapor continued, but as discussed above, wiggles in the growth curve up to ≈80% RH (Fig. 5c) indicate ongoing transformations of gel-like network structures rather than gradual uptake of water into an homogeneous aqueous solution droplet as observed at RH>80% (for OA as well as for AS).

3.3.4 Related earlier studies

Three earlier studies have reported hygroscopic growth measurements for oxalic acid aerosol particles: the H-TDMA study by Prenni et al. (2001), an electrodynamic balance (EDB) study by Peng et al. (2001), and an aerosol flow tube Fourier transform infrared spectroscopy (AFT-FTIR) study by Braban et al. (2003).

Prenni et al. (2001) observed similar growth factors as shown in Fig. 5a upon hydration from ≈45% to ≈91% RH (303 K, no dehydration experiments reported). Due to a lack of measurement data at low RH and higher measurement uncertainties (≈4%) they did not report details about the onset of the deliquescence transition. They assumed that the aerosol particles generated by nebulisation, heating and diffusion drying of aqueous OA (initial diameters: 50–100 nm) were not completely dry but rather concentrated solution droplets, and they reported that the measured hygroscopic growth agreed well with Köhler model calculations assuming that the initially generated particles consisted of oxalic acid dihydrate. We suggest that these particles may also
have consisted of solid amorphous OA but were less porous due to different drying conditions which involved also a heating step.

Peng et al. (2001) reported hydration and dehydration experiments with OA particles in the range 10–20 µm diameter and 5–94% RH (298 K). Upon hydration they observed no deliquescence but a small increase of particle mass at RH > 80%, which may be due to uptake of water into cracks on the solid particle surface (adsorption or capillary condensation). Upon dehydration they observed a gradual efflorescence transition that was completed at 52–57% RH, which is close to the stepwise ~3% diameter decrease and the concurrent peak of $\sigma_g$ observed at ~50% RH in our dehydration experiment (Fig. 5a, b). Peng et al. (2001) suggested that efflorescence transition led to crystallization of anhydrous oxalic acid. If this is the case, gel-like structures and their collapse might also play a role in the crystallization of organic substances from aqueous solution droplets. Alternatively, the effloresced particles might have consisted of amorphous oxalic acid – possibly non-stoichiometric hydrates, because the formation of anhydrous oxalic acid usually requires very low relative humidity (Mod et al., 1973; de Wit et al., 1983; Apelblat, 1986).

Braban et al. (2003) performed hydration and dehydration experiments with polydisperse sub-micrometer OA aerosol particles at 283–293 K and reported that it was difficult but possible to generate anhydrous particles at RH < 5%. Upon hydration of anhydrous particles they observed a transition from anhydrous oxalic acid to oxalic acid dihydrate at ~10–30% RH and a deliquescence transition at ~97–99%. Upon dehydration efflorescence was not observed, and unfortunately experimental data for comparison with the dehydration curves observed in our experiments were not reported. Braban et al. (2003) did not specify how and how often the difficulties in generating anhydrous particles could be overcome, but we hypothesize that the formation of anhydrous crystalline particles occurred preferentially in the larger particles of the investigated polydisperse aerosol and that it was limited by crystal nucleation kinetics and statistics, respectively. The size distribution of the investigated aerosol was not characterized, but a reference to Cziczo et al. (1997) indicates a lognormal distribution with
a count median or geometric mean diameter of about 0.45 µm. The geometric standard deviation was not reported, but most likely micrometer-sized particles dominated the surface and mass size distributions of the aerosol and thus also the optical properties measured in the AFT-FTIR experiment. The strong particle size dependence of crystallization kinetics and statistics (Onasch et al., 1999; Pruppacher and Klett, 2000; Koop et al., 2007) can explain why the formation of anhydrous crystalline oxalic acid may have been observed by Peng et al. (2001) and Braban et al. (2003) working with micrometer-sized particles but not in the experiments of by Prenni et al. (2001) and in the present study dealing with particles ≤100 nm. Moreover, it seems that some of the observations of Peng et al. (2001) and Braban et al. (2003) could also be explained by the formation of (amorphous) oxalic acid hydrate particles instead of (crystalline) anhydrous oxalic acid particles.

Unexpected water uptake has also been reported for other dicarboxylic acids. For malonic acid with crystalline bulk deliquescence at ~72% RH, Braban et al. (2003) observed deliquescence and efflorescence transitions at ~10% RH. For maleic acid aerosol particles (crystalline bulk deliquescence at ~89% RH), Brooks et al. (2003) reported substantial water uptake at ~20% RH and attributed it to surface adsorption. We suggest that in both cases moisture induced glass transitions and/or gel-like swelling of (semi-)solid amorphous particles may have occurred.

### 3.4 Levoglucosan particles

#### 3.4.1 Phase transitions and hygroscopic growth

Figure 4e shows the mobility equivalent growth factors observed upon hydration and dehydration of levoglucosan (LG) aerosol particles. Upon hydration, we measured a small gradual increase of mobility diameter over the range of ~10–30% that may be explained by surface adsorption and minor bulk absorption of water vapor into compact spherical particles as discussed below. At ~30% RH, we observed a strong increase in the slope of the growth curve (Figs. 4e, 5e, 5f) and a broadening of the particle size
distribution (Fig. 4f) that continued up to ~60% RH and indicate a kinetically limited deliquescence transition. Above ~60% RH, the good agreement of the hydration and dehydration curves for both $g_b$ and $\sigma_g$ indicates that the particles were fully deliquesced. The deliquescence RH range of 30–60% was much lower than the saturation relative humidity of the crystalline LG bulk sample (RH$_{s,b} = 81.9\%$, Table 2), which confirms the amorphous nature of the investigated LG aerosol particles.

As detailed below, the kinetically limited deliquescence transition can be explained by a gradual transformation of the amorphous LG particles from a glassy or semi-solid (rubbery or ultra-viscous) state into a highly viscous or gel-like matrix that absorbs water vapor at rates limited by diffusion or structural rearrangements (swelling). When the water content of the particles exceeded a volume fraction of ~20% (corresponding to $g_b = 1.12$ at ~60% RH), the viscous (or gel-like) organic matrix apparently became so dilute (or fully dissolved), that it ceased to inhibit the reversible hygroscopic growth that is characteristic for liquid aqueous solution droplets.

Upon dehydration, the mobility diameters observed at RH<60% were substantially higher than upon hydration, which can be attributed to the persistence of highly viscous aqueous droplets due to kinetic limitations of evaporation and efflorescence. At ~15% RH the particle diameter observed in the dehydration experiment remained ~4% larger than in the hydration and h&d experiments. This can be explained by the different drying conditions in the SDD prior to size selection with DMA1 (drying over ~30 s at RH<5%) and upon dehydration and sizing in DMA2 (RH conditioning and sizing over ~7 s). Apparently, the liquid water content of the aqueous LG droplets did not immediately evaporate upon mixing with the dry sheath flow in DMA2 as it is usually observed in experiments with aqueous solution droplets of inorganic salts (see AS particles above and Mikhailov et al., 2004). Instead, the particles retained residual water throughout the drying and sizing process in DMA2 (volume fraction ~12% at ~15% RH), which is confirmed by the stable value of $\sigma_g$ and by the results of h&d experiments (Fig. 5e: gradual increase of $D_{b,h&d}$ with RH from $D_{b,h&d,min} = D_{b,h,min}$ to $D_{b,h&d,max} = 1.04 D_{b,d,min}$).
The inhibition of efflorescence observed upon dehydration of LG particles is consistent with the kinetic limitation of deliquescence observed upon hydration. As detailed below, it can be explained by the formation of a gel or of a semi-solid shell (glassy, rubbery or ultra-viscous) with low molecular diffusivity. Kinetic limitations of water absorption/desorption and inhibition of related phase transitions (moisture-induced glass transition, crystallisation) have also been reported for amorphous lactose particles and other amorphous organic particles generated by spray-drying (Burnett et al., 2004; Wang and Langrish, 2007; Price and Young, 2003).

3.4.2 Microstructure, surface and bulk uptake, kinetic limitations

The amorphous LG particles exhibited no shrinking upon hydration, i.e., in none of the H-TDMA modes did the mobility diameter decrease with increasing RH. Apparently, the amorphous LG particles formed upon nebulization and thorough drying were perfectly compact spheres \(D_{b,i}=D_{b,h,\text{min}}=D_{b,h&d,\text{min}}\); Table 2). This is unlike the amorphous OA particles investigated in this study but consistent with the behavior of amorphous protein particles reported by Mikhailov et al. (2004).

Figures 5e and 5f shows the difference between the mobility diameters observed in hydration experiments and h&d experiments with LG particles and the corresponding monolayer numbers \(N_{ML}\). Up to 30% RH, \(N_{ML}\) increased gradually to \(\sim 3\) ML, which can be explained by surface adsorption and/or minor bulk absorption onto and/or into compact glassy or semi-solid LG particles. At \(\sim 30\%\) RH, the slope of the growth curve increased by a factor of \(\sim 5\) (from \(\sim 0.1\) ML per \% RH to \(\sim 0.5\) ML per \% RH), which indicates a gel-like swelling that may have been triggered by a moisture-induced glass transition and accelerated water absorption into the resulting ultra-viscous or rubbery amorphous phase.

According to Zobrist et al. (2008, Fig. A1), moisture induced glass transitions of LG may indeed occur at the temperature level of our experiments \((\sim 298\,\text{K})\). Their best estimate for the glass temperature of pure LG is, however, somewhat lower \((\sim 280\,\text{K})\), and thus the investigated LG particles may have been in a semi-solid rather than glassy
amorphous state already before they were humidified.

In any case, the additional steps/wiggles in the growth curve (40–50% RH, Figs. 4e and 5f) and the persistent broadening of the particle size distributions (up to ~60% RH, Fig. 4f) suggest that the formation and transformation of gel-like structures or non-uniform concentration gradients (e.g., semi-solid shells) played a role in the kinetically limited deliquescence transition. Gelation and/or the formation of a semi-solid shell with low molecular diffusivity can also plausibly explain the inhibition of evaporation and efflorescence, i.e., the retention of absorbed water upon dehydration (Fig. 4e).

As mentioned above, it has long been known in food and materials science that carbohydrates and other organic compounds can form glasses, rubbers, gels and ultraviscous liquids with low molecular diffusivity (Slade and Levine, 1991; Bhandari and Howes, 1999; Keller, 1995; Sangeetha and Maitra, 2005; Sperling, 2006; Ray et al., 1998; Farhat et al., 1997; Laurence, 2006).

Further investigations will be required to explore under which conditions glassy, rubbery or gel-like structures may be important for the composition, transformation and environmental effects of atmospheric aerosols. Nevertheless, our results show that they can indeed kinetically limit the uptake and as well as the release of water by organic aerosol particles on (multi-)second time scales and may thus influence the hygroscopic growth and possibly also the activation of aerosol particles as cloud condensation nuclei (CCN) or ice nuclei (IN) under lower tropospheric conditions.

3.4.3 Related earlier studies

The hygroscopic properties of levoglucosan particles have been investigated in several earlier studies with H-TDMA (Mochida and Kawamura, 2004; Koehler et al., 2006; Svenningsson et al., 2006) and electrodynamic balance methods (Chan et al., 2005). Mochida and Kawamura (2004) and Chan et al. (2005) performed hydration and dehydration experiments, while Koehler et al. (2006) and Svenningsson et al. (2006) performed only hydration experiments. None of these studies reported phase transitions, and Mochida and Kawamura (2004) and Chan et al. (2005) found no differences be-
between hydration and dehydration. Thus all studies concluded that the investigated particles were not completely dry, which is consistent with our observation that LG particles retain absorbed water upon gentle drying (\(\sim 7\) s at \(\text{RH} \geq 14\%\)) and release all water only upon intense drying (\(\sim 30\) s at \(\text{RH} < 5\%\)). For comparison with literature data we have also calculated growth factors referring to the minimum diameter observed in our dehydration experiments (\(D_{b,\text{de},\text{min}} = 103.8\) nm, Table 2), and these were in good agreement with the results of Mochida and Kawamura (2004) and within the range of experimental uncertainties of the other studies. Thus, it seems that the volume fraction of residual water in the LG particles investigated in earlier studies was similar to the residual volume fraction of water observed in our dehydration experiments (\(\sim 10\%\)).

Since our study appears to be the first one in which the mass equivalent diameter of the investigated LG particles is well known, we recommend using these data and the Köhler model parameters presented below (Sect. 3.5.3) to describe the hygroscopic properties of pure levoglucosan.

### 3.5 Köhler model calculations of hygroscopic growth

#### 3.5.1 Ammonium sulfate

In Fig. 6a the mobility equivalent growth factors observed for deliquesced ammonium sulfate particles are compared with the mass equivalent growth factors calculated with a full Köhler model (Sect. A1) and with a simplified Köhler model (volume-additivity model with surface tension of pure water; Sect. A2). Both models are based on a water activity parameterization derived from the Aerosol Inorganics Model (AIM, Clegg et al., 1998a, b) and on the minimum mobility equivalent diameter observed in the h&d experiments (H-TDMA operation mode 3; \(D_{m,\text{AS}} = D_{b,\text{h&d},\text{min}} = 95.7\) nm), and both models are in very good agreement with the measurement results and with each other. Averaged over the whole range of 30–95% RH, the mean relative deviations between measurement and model results as well as the between the different models were <1%.
Since the AIM can be regarded as an accurate reference for the water activity in aqueous ammonium sulfate solutions (Rose et al., 2008), the good agreement between model an measurement results confirms that the AS particles with $D_{b,h,min}$ were compact and spherical. Mikhailov et al. (2004) had obtained similar results for NaCl particles, demonstrating that h&d experiments (H-TDMA operation mode) enable efficient and precise experimental determination of particle mass equivalent diameters as required for accurate K"ohler model calculations and interpretation of H-TDMA and CCN counter experiments (Rose et al., 2008). The agreement between the two models also confirms that the partial molar volume of water and the surface tension of deliquesced AS particles can be effectively approximated by the molar volume and surface tension of pure water, even at low relative humidity and high concentration of AS.

Figure 7a shows the water activity-based growth curve ($g_b$ vs. $a_w$) obtained by converting measured RH values into corresponding water activity ($a_w$) values as described in Sect. A3.5 (correction for Kelvin effect assuming volume additivity and the surface tension of water). The measurement results can be accurately represented by a 3-parameter fit as proposed by Kreidenweis et al. (2005), and the corresponding best-fit parameters are listed in Table 3 ($k_1-k_3$; Eq. A14, Sect. A3.5). A 1-parameter fit based on the $\kappa$-K"ohler model approach (best fit value $\kappa=0.51$; Table 3; Eq. A17, Sect. A3.6) yields good agreement at high $a_w$ but deviates significantly at low $a_w$.

As illustrated in Fig. 7b, the deviations of the 1-parameter fit are due to a pronounced dependence of the effective hygroscopicity parameter $\kappa$ on $a_w$ and solute concentration in the aqueous particles, respectively. Figure 7b also shows that the concentration dependence of $\kappa$ can be well described with the best-fit parameters of the 3-parameter fit from Fig. 7a ($k_1-k_3$, Table 3, Eq. A18, Sect. A3.6). Moreover, the H-TDMA measurement-based $\kappa$ values are in good agreement with AIM-based model calculations (Sect. A3.6), except for very low $a_w$ in very highly concentrated solution droplets close to efflorescence. Note that the AIM-based $\kappa$ values exhibit a steep increase at high $a_w$, going from $\kappa\approx0.5$ at $a_w\approx0.95$ to $\kappa\approx0.7$ at $a_w\approx1.0$, which is consistent with measurement and model results for the CCN activation of AS particles (Rose et
As outlined by Pöschl et al. (2009) and detailed in the Appendix (Sect. A3.6), assuming volume additivity and the surface tension of water for Köhler model calculations implies that the effective hygroscopicity parameter $\kappa$ can be regarded as an “effective Raoult parameter” ($\kappa_R$) which can be directly converted into a van’t Hoff factor ($i_s$) or into an osmotic coefficient ($\Phi_s$) respectively (Eq. A19; Rose et al., 2008; Gunthe et al., 2009). Accordingly, the secondary y-axis of Fig. 7b translates the $\kappa$ values into van’t Hoff factors, which can be intuitively interpreted as effective dissociation numbers of the solute substance explaining the reduction of water activity according to Raoult’s law (Pruppacher and Klett, 2000; Seinfeld and Pandis, 2006; Pöschl et al., 2009). This is useful for comparison with related studies applying the parameters $i_s$ or $\Phi_s$ and for the interpretation of the Köhler model results for different types of organic substances as discussed below (Sects. 3.5.2 and 3.5.3).

Overall, the Köhler model results are in good agreement with earlier H-TDMA and CCN counter experiments characterizing the hygroscopic growth and CCN activation of AS particles (e.g., Gysel et al., 2002; Kreidenweis et al., 2005; Petters and Kreidenweis, 2007; Rose et al., 2008, and references therein). With regard to the high precision of the H-TDMA and CCN experiments with ammonium sulfate as well as with sodium chloride (NaCl) aerosol particles presented in this study and related earlier studies (Mikhailov et al., 2004; Rose et al., 2008), we point out that the good agreement between the H-TDMA and CCN measurement results for both AS and NaCl with AIM-based Köhler model results re-confirm the validity of the AIM as an accurate reference for water activity in concentrated as well as in dilute aqueous solutions of AS as well as of NaCl.

This may appear trivial for experts in the investigation of water activity in aqueous solutions, but from very recent discussions we know that the usefulness and validity of the AIM as a reference is not generally acknowledged in the aerosol and cloud research community. For example, recent studies of the CCN activation of atmospheric and laboratory-generated aerosols still use constant values or linear extrapolations of...
κ or \( i_s \) for the calibration of CCN instruments with AS particles. As illustrated in Fig. 7b, however, κ and \( i_s \) are not constant in dilute aqueous solutions of AS and depend in a non-linear way on \( a_w \) and solute concentration, respectively. As demonstrated and discussed in detail by Rose et al. (2008), small deviations in κ and \( i_s \) lead to substantial deviations in the calibration of CCN counters with regard to water vapor supersaturation (relative deviations up to \( \sim 20\% \)). Since these deviations are propagated and can be further enhanced in the calculation of CCN measurement results such as effective hygroscopicity parameters, we would like to renew the recommendation of Rose et al. (2008) to use AIM-based or equivalent Köhler models in experiments and calibrations involving the hygroscopic growth and CCN activation of AS particles.

3.5.2 Oxalic acid

In Fig. 6b the mobility equivalent growth factors observed for deliquesced OA particles are compared with the mass equivalent growth factors calculated with an ideal solution model (IS, Sect. A3.2) assuming different initial composition of the OA particles, i.e., anhydrous oxalic acid and hydrates containing 1–3 molecules of water per oxalic acid molecule. The agreement between model and measurement results was best under the assumption that the OA particles initially consisted of oxalic acid dihydrate. The agreement was similarly good for RH<85\% when assuming a trihydrate and for RH>85\% when assuming a monohydrate. When assuming anhydrous oxalic acid, the model results were generally too high.

In Fig. 6c the measured growth factors and the IS model results for oxalic acid dihydrate are compared to the results of volume-additivity (VA) Köhler models based on different water activity formalisms: UNIFAC (Sect. A3.3) and Flory-Huggins (FH, Sect. A3.4). The best-fit value of the FH interaction parameter \( \chi = 0.46 \) was close to 0.5, which indicates near-ideal solution behavior according to Flory-Krigbaum theory (compensation of excess enthalpy and entropy factors; Flory, 1953; Cowie and Arrighi, 2007). Indeed, the FH model results were similar to the IS model results and agreed also fairly well with the measurement data. At RH>85\% both the IS and FH model
results were too low, which can be explained by an increase of non-ideal behavior of oxalic acid (dissociation) with increasing dilution. In contrast, the UNIFAC model results for oxalic acid dihydrate were in fair agreement with the measurement data at high RH but far too high at low RH, which may be due to inappropriate group interaction parameters (Sect. A3.4). When assuming that the OA particles initially would have consisted of anhydrous oxalic acid, the positive offset of the UNIFAC model was even higher (results not shown).

Figure 7c shows the water activity-based growth curve of the investigated OA particles (\( g_b \) vs. \( a_w \); Sect. A3.5). As for AS particles (Fig. 7a), the measurement results are well represented by a 3-parameter fit, and the corresponding best-fit parameters are listed in Table 3 (\( k_1-k_3 \); Eq. A14, Sect. A3.5). A 1-parameter \( \kappa \)-Köhler model fit yields good agreement at low \( a_w \) but deviates significantly at high \( a_w \) (best fit value \( \kappa = 0.23 \); Table 3; Eq. A17, Sect. A3.6).

As illustrated in Fig. 7d, the deviations of the 1-parameter fit are due to a pronounced increase of \( \kappa \) with \( a_w \). As for AS particles, the concentration dependence of \( \kappa \) can be well described with the best-fit parameters of the 3-parameter fit (\( k_1-k_3 \), Table 3, Eq. A18, Sect. A3.6) and the \( \kappa \) values can be converted into van’t Hoff factors \( i_s \) as shown by the secondary x-axis of Fig. 7d. The \( i_s \) values calculated under the assumption that the OA particles initially consisted of oxalic acid dihydrate confirm the results and interpretation of the IS model calculations, i.e., that oxalic acid behaves like an ideal solute when it is highly concentrated \( (i_s \approx 1 \text{ at } a_w \leq 0.8) \) and exhibits enhanced dissociation with increasing dilution \( (i_s > 1 \text{ at } a_w > 0.8) \). Indeed, the observed increase and the value of \( i_s \approx 1.1 \) at \( a_w \approx 0.9 \) and \( g_b \approx 1.5 \), respectively, is fully consistent with the further increase of \( i_s \) in more dilute aqueous oxalic acid droplets as reported by Varga et al. (2007) based on measurements of osmolality and surface tension \( (i_s \approx 1.5 \text{ at } g_b = 3 \text{ and } a_w \approx 0.985 \text{ up to } i_s \approx 2 \text{ at } g_b \approx 10 \text{ and } a_w \approx 0.999) \). Varga et al. (2007) and other studies (Koehler et al., 2006) also show that oxalic acid as well as levoglucosan have very little influence on the surface tension of aqueous solution droplets, which confirms the validity of assuming water surface tension in the presented VA Köhler
model calculations (Sect. A2).

When assuming that the OA particles would initially have been anhydrous, the obtained \( i_s \) values remain well below one throughout the investigated range of conditions, which is not plausible (dotted line, Fig. 7d). Overall, the Köhler model results confirm that the investigated OA particles did not consist of anhydrous oxalic acid. They suggest that the amorphous OA particles initially consisted of oxalic acid dihydrate or of a non-stoichiometric hydrate containing about 2 water molecules per oxalic acid molecule.

### 3.5.3 Levoglucosan

In Fig. 6d the mobility equivalent growth factors observed for LG particles are compared with IS, UNIFAC and FH model results. Neither the IS nor the UNIFAC model were able to reproduce the measurement results. Mochida and Kawamura (2004) had observed similar deviations and attributed these to inappropriate group interaction parameters in the UNIFAC model. In contrast, the FH model with a best-fit value of \( \chi = 0.26 \) was in good agreement with the growth curves observed at RH > 60% and right in between the kinetically limited growth factors observed at RH < 60%. The results suggest that FH models may be suitable to describe not only polymers but also the hygroscopic growth of non-dissociating organic substances with low molecular mass.

Figure 7e shows the water activity-based growth curve of the investigated LG particles (\( g_b \) vs. \( a_w \); Sect. A3.5). As for AS and OA particles (Figs. 7a, c), the measurement results are well represented by a 3-parameter fit, and the corresponding best-fit parameters are listed in Table 3 (\( k_1 - k_3 \); Eq. A14, Sect. A3.5). A 1-parameter \( \kappa \)-Köhler model fit yields good agreement at high \( a_w \) but deviates significantly at low \( a_w \) (best-fit value \( \kappa = 0.23 \); Table 3; Eq. A17, Sect. A3.6).

As illustrated in Fig. 7f, the deviations of the 1-parameter fit are due to an apparent decrease of \( \kappa \) with \( a_w \), which can be described with the best-fit parameters of the 3-parameter fit. As discussed above, the LG particle properties observed at low RH and low \( a_w \), respectively, can be explained by kinetic limitations and non-ergodic behavior.
of a semi-solid phase (glassy, rubbery or ultra-viscous). Thus, the κ values obtained at \( a_w \leq 0.8 \) should not be regarded as thermodynamic equilibrium parameters. On the other hand, the κ values obtained at \( a_w > 0.8 \) are in very good agreement with the best-fit value of \( \kappa = 0.23 \), indicating that the effects of LG on water activity in dilute solutions is not strongly concentration-dependent. Our best-fit value of \( \kappa \) is somewhat higher than the effective hygroscopicity parameter that Petters and Kreidenweis (2007) calculated based on Svenningson et al. (2006; \( \kappa \approx 0.21 \)) and on Koehler et al. (2006; \( \kappa \approx 0.17 \)), which may be due to an underestimation of growth factors in the earlier H-TDMA studies because of incomplete drying of the initially size-selected particles (Sect. 3.4.3).

As outlined by Pöschl et al. (2009) and detailed in the Appendix (Sect. A3.6), \( \kappa \) can be interpreted as an effective Raoult parameter, i.e., as an effective or equivalent molar density of water-soluble ions or molecules in the aerosol particle or chemical component, respectively, normalized by the molar density of water molecules in liquid water (~55 mol L\(^{-1}\); Eq. A19; Rose et al., 2008; Gunthe et al., 2009). With regard to dilute solutions of strong electrolytes with low molar mass, including most atmospherically relevant water-soluble inorganic salts and strong acids, the effective molar density of ions or molecules is usually close to the actual molar density of ions/molecules of the solute, i.e., the van’t Hoff factor is close to the stoichiometric dissociation number and the osmotic coefficient is close to unity (e.g., AS: \( \nu_s = 3, i_s \approx 2–3, \Phi_s \approx 0.7–1 \)). For weak electrolytes and acids, however, the van’t Hoff factor tends to be smaller than the stoichiometric dissociation number, and the osmotic coefficient tends to be less than unity (e.g., OA: \( \nu_s = 3, i_s \approx 1–2, \Phi_s \approx 0.3–0.7 \)). On the other hand, organic compounds with high molar mass and volume usually exhibit van’t Hoff factors that are larger than their stoichiometric dissociation number and osmotic coefficients that are larger than unity (e.g., LG: \( \nu_s = 1, i_s \approx \Phi_s \approx 1.4 \); BSA (protein): \( \nu_s = 1, i_s \approx \Phi_s \approx 1–100 \); Mikhailov et al., 2004).

For LG and similar (non-electrolytic) organic aerosol components it appears thus more suitable to describe and interpret the relation between the effective hygroscopicity or Raoult parameter, molar mass and density (Eq. A19) with regard to osmotic
effects, rather than describing and interpreting $i_s$ as an effective “ion dissociation number” or referring to an equivalent “ion density” (Rissler et al., 2006; Wex et al., 2007; Gunthe et al., 2009). Osmotic coefficients, van’t Hoff factors, or related parameters like osmolality are available for many organic and inorganic substances and can be efficiently measured or approximated with well-established physicochemical techniques and formalisms (e.g., Kiss and Hansson, 2004; Mikhailov et al., 2004; Köhler et al., 2006; McFiggans et al., 2006; Rosenorn et al., 2006; Varga et al., 2007; Clegg et al., 2008; Ekström et al., 2009, and references therein). However, care should be taken to avoid confusion of relevant quantities, units and conversion factors, which seems not always to be the case.

In a companion paper (Mikhailov et al., 2009) and further follow-up studies, the Köhler model results will be further discussed and used to predict the hygroscopic growth of aerosol particles consisting of internal mixtures of the above and other aerosol components.

4 Summary and conclusions

In this study we have characterized the interaction of amorphous and crystalline aerosol particles with water vapor by H-TDMA experiments and Köhler model calculations. With regard to the generation of crystalline ammonium sulfate particles by spray-drying, we found that the apparent void volume fractions indicating deviations from compact spherical shape decreased with increasing residual RH (from $\sim$4% at RH<5% to $\sim$1% at RH≈15%). Based on cyclic hydration&dehydration (h&d) experiments, we could measure $\sim$2 monomolecular layers of water adsorbed at the surface of ammonium sulfate crystals in the RH range of 50–70%.

The spray-drying of aqueous oxalic acid yielded amorphous solid particles with a highly porous structure (xerogel with apparent void volume fraction of $\sim$40%) composed of oxalic acid dihydrate (or a non-stoichiometric hydrate with about 2 water molecules per oxalic acid molecule). Upon hydration the particles underwent massive
restructuring and compaction, and substantial bulk absorption of water began at \( \sim 40\% \) RH, which is well below the threshold of crystalline bulk deliquescence (97% RH). These observations imply that the particles were neither crystals nor liquid droplets but amorphous solids. In the range of 40–80% RH we observed gradual deliquescence and efflorescence transitions, and differences between the growth factors and geometric standard deviations observed upon hydration and dehydration suggest the formation of gel-like structures (supramolecular networks). Especially the stepwise diameter changes and broadenings of the particle size distributions in the range of 40–50% RH indicate transitions between swollen and collapsed network structures. Fully deliquesced liquid droplets were formed only at RH > 80% where the volume fraction of absorbed water exceeded \( \sim 50\% \).

Unlike the electrolytes ammonium sulfate and oxalic acid, the non-electrolyte levoglucosan formed compact spherical particles upon spray-drying. Upon hydration, substantial bulk absorption of water began at \( \sim 30\% \) RH, which is also well below the threshold of crystalline bulk deliquescence (82% RH) and proves that the particles were not crystalline. Over the range of 30–60% RH, stepwise diameter changes and a broadening of the particle size distribution indicated a gradual deliquescence transition that was kinetically limited by an ultra-viscous or gel-like organic matrix with low molecular diffusivity. Fully deliquesced liquid droplets were formed at RH > 60% when the volume fraction of absorbed water exceeded \( \sim 30\% \). Upon dehydration, the gel-like structures or a semi-solid shell (glassy, rubbery or ultra-viscous) inhibited efflorescence, and at low RH (<20%) the particles firmly retained substantial amounts of absorbed water (volume fractions >10%).

Based on these findings and on the results of related studies, we come to the following general conclusions and implications:

1. Many organic substances (incl. carboxylic acids, carbohydrates and proteins) tend to form amorphous rather than crystalline phases upon drying of aqueous solution droplets, which can be explained by the low rates of crystallization that are characteristic for most organic substances. Compared to pure substances,
the multi-component mixtures typically present in atmospheric aerosols are even more likely to form amorphous rather than crystalline phases (Marcolli et al., 2004; Cappa et al., 2008), and besides drying also cooling can lead to the formation of amorphous organic solids in the atmosphere (Murray, 2008; Zobrist et al., 2008). Due to the low degree of structural order, amorphous organic substances appear less likely than their crystalline counterparts to induce ice nucleation, which may be particularly relevant for oxalic acid (Zobrist et al., 2006).

2. Amorphous organic substances tend to absorb water vapor and undergo gradual deliquescence and hygroscopic growth at much lower relative humidity than their crystalline counterparts, which supports earlier suggestions that organic aerosol particles are likely to be in a liquid state under most atmospheric conditions (Bertram et al., 2005; Martin et al., 2004; Marcolli et al., 2004). Again, the multi-component mixtures typically present in atmospheric aerosols are even more likely to remain in aqueous solution than the pure substances investigated in this study (Marcolli et al., 2004).

The results of this and related studies suggest that the deliquescence (liquefaction) of amorphous organic solids at $\sim$298 K effectively begins when the amount of absorbed water reaches 10–20% of the solid/dry particle volume ($g_b \approx 1.03–1.07$, gel-like swelling) and is completed when the amount of absorbed water is in the range of 30–50% of the of the solid/dry particle volume ($g_b \approx 1.1–1.2$, complete dissolution). Reversely, the efflorescence (solidification) of amorphous organic solids appears to begin when the volume fraction of water decreases into the range of 50–30% (formation of gel-like structures or semi-solid shells with low molecular diffusivity) and may be completed when the volume fraction of water drops below $\sim$10% (formation of xerogels, rubbers, or glasses).

For most organics, including carboxylic acids, carbohydrates and protein macromolecules, the RH threshold for the onset of gel-like swelling and deliquescence appears to be in the range of 30–40% RH. The RH threshold for complete dissolu-
tion appears to vary over a broader range of \(\sim 60\%\) for compounds with relatively high solubility and hygroscopicity such as levoglucosan, to \(\sim 80\%\) for compounds with lower solubility and/or stronger hydrogen bonding, and \(\sim 90\%\) for compounds with low hygroscopicity such as protein macromolecules.

3. In the course of hydration and dehydration, certain organic substances can form rubber- or gel-like structures (supra-molecular networks) and undergo stepwise transitions between swollen and collapsed network structures. Gel-like structures are most likely to be formed at intermediate relative humidities around \(\sim 50\%\). They may not only influence and introduce steps in the gradual deliquescence and efflorescence of amorphous particles, but they may also play a role in the crystallization of organic substances from aqueous solution droplets (Peng et al., 2001).

4. Organic gels or (semi-)solid amorphous shells with low molecular diffusivity can kinetically limit the uptake and release of water by submicron aerosol particles on (multi-)second time scales, which may influence the hygroscopic growth and activation of aerosol particles as cloud condensation nuclei (CCN) and ice nuclei (IN) in field and laboratory measurements as well as in the atmosphere. Murray (2008) and Zobrist et al. (2008) have already pointed out that glassy solids formed upon cooling of aqueous organic substances may impede water uptake, nucleation and growth of ice as well as heterogeneous chemical reactions in organic-enriched aerosols at upper tropospheric temperatures. We suggest that amorphous organic substances (glasses, rubbers and gels) may influence and kinetically inhibit these and other multiphase processes in aerosol and clouds also at the temperatures and relative humidities of the lower troposphere and atmospheric boundary layer. The influence of mass transport kinetics on CCN activation in field and laboratory experiments, models, and reality is presently not well understood (Asa-Awuku and Nenes, 2007; Engelhart et al., 2008; Ruehl et al., 2008; Asa-Awuku et al., 2009; Pöschl et al., 2009). With regard to unraveling the
molecular mechanisms and kinetics of water uptake/evaporation and deliquescence/efflorescence of both amorphous and crystalline particles, we suggest that a clear distinction between surface and bulk processes is important (Ammann and Pöschl, 2007; Pöschl et al., 2007) and that relevant information can be obtained by high-precision H-TDMA measurements (including h&d experiments).

5. The shape and porosity of amorphous and crystalline particles formed upon dehydration of aqueous solution droplets depend on chemical composition and drying conditions, including the electrolytic properties of the solutes and electric charging of the particles. At least under laboratory conditions, the apparent volume void fractions of spray-dried aerosol particles can reach up to \( \sim 50\% \) (Mikhailov et al., 2004; and this study), which is characteristic for xerogels. With other techniques of aerosol generation, the apparent particle void fractions may reach up to \( \sim 90\% \) (Krämer et al., 2000), which is characteristic for aerogels (Kistler, 1935).

Void fractions as well as residual water in dried aerosol particles that are not water-free (due to kinetic limitations of drying or stable hydrate formation) should be taken into account in Köhler model calculations of hygroscopic growth and CCN activation. Inaccuracies in the determination of the mass equivalent diameters, residual water and solute amount of substance can easily exceed the uncertainties and deviations caused by solution non-ideality and different modeling approaches (approximations and parameterizations of water activity, etc.; Mikhailov et al., 2004; Rose et al., 2008). For example, the higher effective hygroscopicity parameters and van’t Hoff factors of levoglucosan in dilute aqueous solution determined in this study (\( \kappa \approx 0.23, i_s \approx 1.3 \)) compared to earlier studies (\( \kappa \approx 0.17–0.21, i_s \approx 1.0–1.2 \)) are likely due to more completed drying of the investigated aerosol particles. On the other hand, the conversion of effective hygroscopicity parameters into van’t Hoff factors can provide information about the hydration state of spray-dried aerosol particles (“dry” OA particles composed of oxalic acid dihydrate with \( \kappa \geq 0.23 \) and \( i_s \geq 1.0 \)).
6. For efficient description of water uptake and phase transitions of amorphous and crystalline organic and inorganic aerosol particles and particle components, we propose not to limit the terms deliquescence and efflorescence to equilibrium phase transitions of crystalline substances interacting with water vapor. Instead we propose the following generalized definitions: Deliquescence is the transformation of a (semi-)solid substance into a liquid aqueous solution, whereby water is absorbed from the gas phase (“liquefaction upon humidification/hydration”). Efflorescence is the transformation of a substance from a liquid aqueous solution into a (semi-)solid phase, whereby water is evaporated (“solidification upon drying/dehydration”). According to these definitions, individual components as well as entire aerosol particles can undergo gradual or prompt, partial or full deliquescence or efflorescence, which is indeed the case not only for amorphous organic substances but also for mixtures of crystalline inorganic substances.

Complementary experiments with internally mixed AS-LG-OA particles confirm that the above conclusions and implications are relevant also for aerosols composed of mixed organic, inorganic, amorphous and crystalline substances. Depending on the proportion of amorphous substance, the hygroscopic growth and properties of mixed aerosol particles can be similar either to those of purely amorphous substances or to those of purely crystalline substances (gradual vs. prompt deliquescence and efflorescence, etc.). The results of these experiments will be presented and discussed in a companion paper (Mikhailov et al., 2009).
Appendix A

Köhler theory and models

A1 Full Köhler model

According to Köhler theory, the relation between relative humidity and the size and composition of a spherical droplet formed on a soluble particle is given by (Pruppacher and Klett, 2000; Seinfeld and Pandis, 2006):

\[ s_w = \frac{RH}{100\%} = a_w \exp \left( \frac{4 \sigma \overline{V}_w}{R T D_m} \right), \quad (A1) \]

where \( s_w \) is the water vapor saturation ratio or fractional relative humidity (RH/100%).

In Kelvin term \( \sigma \) is the surface tension of the solution droplet, \( \overline{V}_w \) is the partial molar volume of water in solution, \( R \) is the ideal gas constant, \( T \) is the droplet temperature and \( D_m \) is the droplet diameter (geometric diameter = mass equivalent diameter for compact spherical particle).

The partial molar volume of water in the droplet solution can be expressed by (Brechtle and Kreidenweis, 2000)

\[ \overline{V}_w = \frac{M_w}{\rho} \left( 1 + \frac{x_s}{\rho} \frac{d\rho}{dx_s} \right), \quad (A2) \]

where \( \rho \) is the density of the solution, \( \rho_s \) is the density of the solute, and \( x_s \) is the mass fraction of solute in the droplet. The differential quotient \( d\rho/dx_s \) reflects the influence of molecular interactions that change with changing solute mass fraction.

For aqueous solutions of ammonium sulfate and other atmospherically relevant salts, Tang and Munkelwitz (1994) and Tang (1996) have presented parameterizations of \( \rho \).
as a function of $x_s$, and $d\rho/dx_s$ can be derived accordingly:

$$\rho = \rho_w + \left[ \sum_q A_q (100 x_s)^q \right] \times 10^3 \text{ kg m}^{-3}, \quad (A3)$$

$$\frac{d\rho}{dx_s} = \left[ \sum_q A_q q (100 x_s)^{q-1} \right] \times 10^3 \text{ kg m}^{-3}, \quad (A4)$$

For ammonium sulfate the polynomial coefficients are (Tang and Munkelwitz, 1994): $A_1=5.92 \times 10^{-3}$; $A_2=-5.036 \times 10^{-6}$; $A_3=1.024 \times 10^{-8}$.

The surface tension of the aqueous solution can be calculated based on a relationship proposed by Hänel (1976):

$$\sigma = \sigma_0 + \sigma_T \cdot (T_0 - T) + \sigma_\mu \cdot \mu_s, \quad (A5)$$

where $\sigma_0=0.0756 \text{ N m}^{-1}$ is the surface tension of pure water at $T_0=273.15 \text{ K}$, the coefficient $\sigma_T =1.53 \times 10^{-4} \text{ N m}^{-1} \text{ K}^{-1}$ accounts for the influence of temperature, and the coefficient $\sigma_\mu=2.17 \times 10^{-3} \text{ N m}^{-1} \text{ kg mol}^{-1}$ (for ammonium sulfate) accounts for the influence of droplet composition (solute molality, $\mu_s$). Solute molality, $\mu_s$, mass fraction, $x_s$, and molar mass, $M_s$ are related by:

$$\mu_s = \frac{x_s}{M_s (1 - x_s)} \quad (A6)$$

The ratio of the aqueous droplet diameter, $D_m$, to the mass equivalent diameter of a particle consisting of the dry solute, $D_{m,s}$, is defined as the mass equivalent growth factor, $g_m$:

$$g_m = \frac{D_m}{D_{m,s}} = \left( \frac{\rho_s}{x_s \rho} \right)^{1/3} \quad (A7)$$
Equations (A1–A7) can be used to model the hygroscopic growth of aerosol particles, i.e., to calculate \( g_m \) and \( D_m \), respectively, as a function of \( D_{m,s} \) and RH.

For efficient comparison and clear distinction against other Köhler modeling approaches, we designate the combination of Eq. (A1) with parameterizations of all relevant quantities (\( a_w, \sigma, \overline{V}_w, \rho \), etc.) as a “full Köhler model”. In the present study, we apply a full Köhler model only for ammonium sulfate particles, using the parameterizations given above for \( \rho \) and \( \sigma \) and water activity from an ion interaction model (Aerosol Inorganics Model, AIM Clegg et al., 1998a, b).

In the full Köhler model calculations, \( a_w \) was taken as the primary variable and the corresponding solute molality \( \mu_s \) was obtained by interpolation of tabulated AIM data (Sect. A3.1). \( \sigma \) and \( x_s \) were calculated from Eq. (A5) and Eq. (A6), respectively; \( \overline{V}_w \) was calculated from Eq. (A2) with \( \rho \) from Eq. (A3) and \( d\rho/dx_s \) from Eq. (A4). \( g_m \) and \( D_m \) were calculated with Eq. (A7) assuming \( D_m = D_{b,h\&d,min} = 95.7 \) nm (Table 2). Finally, \( a_w, \sigma, \overline{V}_w, \) and \( D_m \) were inserted in Eq. (A1) to obtain the RH values corresponding to \( D_m \) and \( g_m \), respectively.

A2  Volume-additivity Köhler models

Under the assumption that the volume of the solution droplet is given by the sum of the volumes of the dry solute and of the pure water contained in the droplet (“volume-additivity”, VA), the mass equivalent growth factor is given by (Brechtel and Kreidenweis, 2000; Mikhailov et al., 2004):

\[
 g_m = \left( \frac{\rho_s}{\mu_s M_s \rho_w} + 1 \right)^{1/3}, \tag{A8}
\]

where \( \rho_w \) is the density of the water.

The VA assumption implies that the density of the droplet is a linear combination of the densities of the dry solute and of pure water, and that the partial molar volumes of water and of the solute in solution are equal to the molar volumes of pure water.
and pure solute, respectively: $\bar{V}_w = V_w = \rho_w / M_w$ and $\bar{V}_s = V_s = \rho_s / M_s$. Accordingly the full Köhler equation (Eq. A1) can be reduced to the following simplified form (“VA Köhler equation”):

$$\frac{RH}{100\%} = a_w \exp \left( \frac{4 \sigma \rho_w}{M_w RT g_m D_{m,s}} \right)$$

(A9)

Moreover, the VA assumption implies that the mole fraction of water in the droplet ($X_w$) is given by:

$$X_w = \frac{n_w}{n_w + n_s} = \frac{g_m^3 - 1}{(g_m^3 - 1) + \frac{M_w \rho_s}{\rho_w M_s}}$$

(A10)

where $n_w$ and $n_s$ are the mole numbers (amount-of-substance) of water and solid in the droplet, respectively.

For the VA Köhler model calculations presented in this study, we assumed that the mass equivalent diameter of the dry solute particle equals minimum mobility equivalent diameter measured in the h&d experiments ($D_{m,s} = D_{b,h&d,\text{min}}$). $g_m$ was taken as the primary variable, different formalisms detailed below were used to calculate the corresponding value of $a_w$, and RH was calculated by inserting $g_m$ and $a_w$ in Eq. (A9).

In the VA model calculations we assumed that surface tension of the solution droplet equals the surface tension of pure water ($\sigma = \sigma_w = 0.072 \, \text{N} \, \text{m}^{-1}$ at 298 K). According to the available data, this should be a good approximation not only for AS but also for OA and LG as detailed by Koehler et al. (2006).

Depending on the applied models, approximations and parameterizations for $a_w$, we distinguish three types of VA Köhler models that have been used to simulate the hygroscopic growth of the investigated particles and to determine characteristic parameters, respectively. The different approaches of describing water activity are detailed in the following sections: ideal solution (Eq. A3.2), UNIFAC (Eq. A3.3), and Flory-Huggins (Eq. A3.4).
A3 Water activity representations

A3.1 Ion interaction model (AIM)

For aqueous ammonium sulfate particles the relation between $a_w$ and $\mu_s$ was calculated with an ion interaction model (Pitzer-Simonson-Clegg model). We ran the Aerosol Inorganics Model (AIM; Clegg et al., 1998a, b; http://www.aim.env.uea.ac.uk/aim/aim.html; Model II) for $(\text{NH}_4)_2\text{SO}_4$ at 298.15 K, and we obtained a table of $a_w$ vs. $\mu_s$ covering the range of $a_w=0.3$–0.97 and $\mu_s=0.8$–40 mol kg$^{-1}$, respectively (23 data points, four significant digits). For model calculations bridging the gap from H-TDMA to CCN measurement data, i.e., at $a_w \geq 0.97$ (Fig. 7a, b), we used the approach and supplementary data of Rose et al. (2008). Upon plotting and further analysis, the calculated growth curves were interpolated with a polynomial fit (B-spline, Origin 7.5 software). Note that according to Clegg and Wexler (2007) and Rose et al. (2008), the AIM can be regarded as an accurate reference standard for the activity of water in dilute aqueous solutions of ammonium sulfate.

A3.2 Ideal solution model

In an ideal solution, the activity of water is given by its mole fraction (Raoult’s law):

$$a_w = X_w.$$  \hspace{1cm} \text{(A11)}

In the ideal solution model calculations for aqueous levoglucosan and oxalic acid particles we have thus calculated $a_w$ from Eqs. (A10) and (A11). For oxalic acid, different potential hydration states of the initial “dry” particles have been considered: anhydrous oxalic acid ($(\text{COOH})_2; \ M_s=90.03 \text{ g mol}^{-1}; \ \rho_s=1.90 \text{ g cm}^{-3}$), a monohydrate ($(\text{COOH})_2\cdot\text{H}_2\text{O}; \ M_s=127.07 \text{ g mol}^{-1}; \ \rho_s=1.75 \text{ g cm}^{-3}$), the dihydrate ($(\text{COOH})_2\cdot2\text{H}_2\text{O}; \ M_s=127.07 \text{ g mol}^{-1}; \ \rho_s=1.65 \text{ g cm}^{-3}$), and a trihydrate ($(\text{COOH})_2\cdot3\text{H}_2\text{O}; \ M_s=144.09 \text{ g mol}^{-1}; \ \rho_s=1.56 \text{ g cm}^{-3}$). Note that mono- or trihy-
drates are not known to be stable but were included to test a realistic range of non-stoichiometric compositions around the stable dihydrate.

The densities of the hypothetical mono- and tri-hydrates were calculated assuming linear additivity of the densities of pure anhydrous oxalic acid and pure water \( \rho_s = \rho_{(COOH)_2} x_{(COOH)_2} + \rho_{H_2O} x_{H_2O} \), where \( x_{(COOH)_2} \) and \( x_{H_2O} \) are the mass fractions of the two components. For oxalic acid dihydrate this approximation yields \( 1.64 \text{ g cm}^{-3} \) which is close to literature value of \( 1.65 \text{ g cm}^{-3} \) and confirms the applicability of the approach.

### A3.3 Activity coefficient model (UNIFAC)

In a real solution, the activity of water can be described by

\[ a_w = \gamma_w X_w, \tag{A12} \]

where \( \gamma_w \) is the mole fraction-based activity coefficient of water and accounts for non-ideal interactions in the mixture. The universal functional group activity coefficient model (UNIFAC, Fredenslund et al., 1975) was used to calculate \( \gamma_w \) as a function of \( X_w \) as described in earlier studies (Barton, 1991; Ming and Russell, 2002; Marcolli, 2004). Group interaction parameters for oxalic acid and levoglucosan were taken from Raatikken and Laaksonen (2005) and Hansen et al. (1991), respectively, and group volume and surface area parameters \( (R_k, Q_k) \) were based on Bondi (1968). In the model calculations, \( g_m \) was taken as the primary variable to calculate \( X_w \) from Eq. (A10), the corresponding value of \( \gamma_w \) was determined with UNIFAC, and \( a_w \) and RH were calculated with Eqs. (A12) and (A9), respectively.
A3.4 Flory-Huggins model

According to Flory (1953), the activity of water in aqueous solutions of organic substances can be described by

$$\ln a_w = \ln (1 - \phi_s) + \left(1 + \frac{1}{f}\right) \phi_s + \chi \phi_s^2,$$  \hspace{1cm} (A13)

where $\phi_s$ is the volume fraction of the organic solute, $f$ is the ratio of the molecular volumes of solute and solvent, and $\chi$ is the Flory-Huggins (FH) solute-solvent interaction parameter. Earlier studies have shown that the FH approach is suitable to describe the absorption of water by polymerized organic aerosol particles (Petters et al., 2006) and by water-miscible organic solids that are in a rubbery state (Hancock and Zografi, 1993; Zhang and Zografi, 2000; Zhang and Zografi, 2001). For FH modeling, we assumed $\phi_s = g_m^{-3}$ and $f = (M_s/\rho_s)/(M_w/\rho_w)$ based on volume additivity, and we inserted $a_w$ from Eq. (A13) in Eq. (A9). The resulting equation was fitted to the measured growth curves. We assumed $g_b = g_m (D_{m,s} = D_{b,\text{h\&d, min}})$ and used the data points of coinciding hydration and dehydration curves (RH $\geq 60\%$ for OA and LG) to obtain best-fit values of $\chi$ (non-linear least squares fitting, Origin 7.5 software).

A3.5 Three-parameter fit

As proposed by Kreidenweis et al. (2005), hygroscopic growth curves can be approximately described with a polynomial 3-parameter fit function of the following form:

$$g_m = \left(1 + k_1 + k_2 \cdot a_w + k_3 \cdot a_w^2\right) \times \frac{a_w}{1 - a_w}$$

To convert the measured RH-based growth curves ($g_b$ vs. RH) into water activity-based growth curves ($g_b$ vs. $a_w$), we assumed $g_b = g_m$ and divided the RH values through the exponential term (Kelvin term) on the right hand side of Eq. (A9). The activity-based growth curves (Fig. 7) were then fitted with Eq. (A14) to determine best-fit values of $\chi$. 

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the parameters \(k_1\), \(k_2\) and \(k_3\) (non-linear least squares fitting, Origin 7.5 software). These best-fit parameters are listed in Table 3 and will be used in a companion paper (Mikhailov et al., 2009) and further follow-up studies describing the hygroscopic growth of aerosol particles consisting of internal mixtures of the investigated compounds. As detailed below, the parameters \(k_1-k_3\) can also be used to describe the dependence of the effective hygroscopicity parameter \(\kappa\) on \(a_w\), RH or solute concentration, respectively.

A3.6 Effective hygroscopicity parameter (\(\kappa\)) and van’t Hoff factor (\(i_s\))

As proposed by Petters and Kreidenweis (2007), the hygroscopic properties of aerosol particles can be approximately described by a single hygroscopicity parameter \(\kappa\):

\[
a_w = \frac{D_{m}^3 - D_{m,s}^3}{D_{m}^3 - D_{m,s}^3 (1 - \kappa)}.
\]

(A15)

Under the assumption of volume additivity, Eq. (A15) can be rewritten as:

\[
\kappa = \frac{(g_{m}^3 - 1)(1 - a_w)}{a_w}.
\]

(A16)

or

\[
g_{m} = \left(\kappa \frac{a_w}{1 - a_w} + 1\right)^{1/3}.
\]

(A17)

As described above, we have used Eq. (A9) to convert the measurement data points of \(g_b\) vs. RH into data pairs of \(g_b\) vs. \(a_w\), and from each of these data pairs we have calculated a \(\kappa\) value using Eq. (A16) under the assumption \(g_b=g_m\) (Fig. 7). According to Eqs. (A14) and (A17), the dependence of \(\kappa\) on \(a_w\) can be described by:

\[
\kappa = k_1 + k_2 \cdot a_w + k_3 \cdot a_w^2
\]

(A18)
To obtain a single best-fit value approximating effective hygroscopicity over the investigated range of $a_w$ and RH, respectively, we have also fitted the activity-based growth curves (Fig. 7) with Eq. (A17) (non-linear least squares fitting, Origin 7.5 software). The best-fit values of $\kappa$ as well as the coefficients $k_1-k_3$ are listed in Table 3 and will be used in a companion paper (Mikhailov et al., 2009) and further follow-up studies to describe the hygroscopic growth of aerosol particles consisting of internal mixtures of the investigated compounds.

As outlined above, the hygroscopicity of an aerosol particle defined as its ability to absorb water vapor depends on the influence of the particle material (solute) on the activity of water (Raoult effect) and on the partial molar volume of water and the surface tension of the aqueous droplet (Kelvin effect). As discussed by Pöschl et al. (2009), the effective hygroscopicity parameter $\kappa$ as defined and applied in the above Eqs. (A15–A17) describes the overall influence of chemical composition on the hygroscopicity of an aerosol particle: water activity, partial molar volume and surfactant effects, i.e., Raoult effect plus Kelvin effect. Assuming volume additivity and that the surface tension of the aqueous droplet equals the surface tension of pure water, the effective hygroscopicity parameter $\kappa$ can be interpreted as an effective Raoult parameter ($\kappa_R$), i.e., as an effective molar density of soluble molecules or ions in the dry particle material normalized by the molar density of water molecules in liquid water ($\rho_w/M_w \approx 55$ mol L$^{-1}$, Rose et al., 2008a; Gunthe et al., 2009; Pöschl et al., 2009):

$$\kappa_R = i_s \frac{\rho_s M_w}{\rho_w M_s} \approx \nu_s \Phi_s \frac{\rho_s M_w}{\rho_w M_s}$$

(A19)

$i_s$ is the van’t Hoff factor and $\nu_s \Phi_s$ is the product of the stoichiometric dissociation number and the molal osmotic coefficient of the solute. In dilute solutions $i_s$ equals $\nu_s \Phi_s$, in concentrated solutions $i_s$ and $\nu_s \Phi_s$ can be related through a series expansion as detailed by Kreidenweis et al. (2005). Thus, effective hygroscopicity or Raoult parameters, respectively, can be converted into van’t Hoff factors or osmotic coefficients, if the density and molar mass of the solute are known (Rose et al., 2008; Gunthe et al., 2009).
2009). For AS we have compared the $\kappa$ values derived from the H-TDMA measurement data (Eq. A16) and the corresponding values of $i_s$ (Eq. A19 with $\kappa=\kappa_R$) to the $\kappa$ and $i_s$ values that can be calculated from AIM reference data ($a_w$ vs. $\mu_s$) based on the following relation and Eq. (A19) with $\kappa=\kappa_R$, respectively (Rose et al., 2008):

$$i_s = \left( \frac{1}{a_w} - 1 \right) (\mu_s M_w)^{-1}. \quad (A20)$$

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**References**


Brooks, S. D., Wise, M. E., Cushing, M., and Tolbert, M. A.: Deliquescence


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2009.


Table 1. Sequence of relative humidities (“RH history”) experienced by the investigated aerosol particles in the key elements of the H-TDMA system (DMA1, conditioner, DMA2) during different types of H-TDMA experiments (modes of operation, Sect. 2.2). For each type of experiment, X represents the independent variable, i.e., the RH value taken for plotting and further analysis of the measurement results.

<table>
<thead>
<tr>
<th>H-TDMA experiment (operation mode)</th>
<th>DMA 1 (size selection) RH1 (%)</th>
<th>Conditioner (humidification) RH2 (%)</th>
<th>DMA 2 (size measurement) RH3 (%)</th>
<th>RH4 (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>hydration (1)</td>
<td>&lt;5</td>
<td>X</td>
<td>X</td>
<td>X</td>
</tr>
<tr>
<td>dehydration (2)</td>
<td>&lt;5</td>
<td>RH_{s,b} + 5^a</td>
<td>&lt;5</td>
<td>X</td>
</tr>
<tr>
<td>hydration&amp;dehydration (h&amp;d, 3)</td>
<td>&lt;5</td>
<td>X</td>
<td>&lt;5</td>
<td>≤10^b</td>
</tr>
</tbody>
</table>

^a In dehydration experiments (mode 2) RH2 was kept 5% higher than the relevant crystalline bulk deliquescence relative humidity RH_{s,b} (Table 3). For oxalic acid particles, RH2 was kept at 95%.
^b In h&d experiments (mode 3) the increase of RH2 from <5% to 95% led to an increase of RH4 from <5% to ∼0.1×RH2.
Table 2. Parameters characterizing the microstructural rearrangement and phase transitions of the investigated aerosol particles/substances: minimum mobility diameters observed in hydration, dehydration and h&d experiments ($D_{b.h.min}$, $D_{b.d.min}$, $D_{b.h&d.min}$; Figs. 4 and 5); apparent volume void fraction of particles upon initial size-selection ($f_{v,i} = (D_{b.i}^{3} - D_{b.h&d.min}^{3}) / D_{b.h&d.min}^{3}$, $D_{b.i} = 99.5$ nm); relative humidities of deliquescence and efflorescence as observed in the HTDMA experiments of this study ($RH_{d}$, $RH_{e}$); relative humidity measured over saturated aqueous bulk samples in this study ($RH_{s,b}$); deliquescence relative humidities reported in earlier studies ($RH_{d,\text{lit}}$).

<table>
<thead>
<tr>
<th>Substance</th>
<th>$D_{b.h.min}$ (nm)</th>
<th>$D_{b.d.min}$ (nm)</th>
<th>$D_{b.h&amp;d.min}$ (nm)</th>
<th>$f_{v,i}$ (%)</th>
<th>$RH_{d}$ (%)</th>
<th>$RH_{e}$ (%)</th>
<th>$RH_{d,b}$ (%)</th>
<th>$RH_{d,\text{lit}}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ammonium sulfate (AS)</td>
<td>96.5</td>
<td>95.7</td>
<td>95.7</td>
<td>4</td>
<td>80</td>
<td>30</td>
<td>79.4</td>
<td>79.9&lt;sup&gt;a&lt;/sup&gt;, 80.2&lt;sup&gt;b&lt;/sup&gt;, 80&lt;sup&gt;c&lt;/sup&gt;, 80&lt;sup&gt;d&lt;/sup&gt;, 79.9&lt;sup&gt;e&lt;/sup&gt;, 79&lt;sup&gt;f&lt;/sup&gt;</td>
</tr>
<tr>
<td>Oxalic acid (OA, dihydrate)</td>
<td>92.3</td>
<td>89.0</td>
<td>89.0</td>
<td>40</td>
<td>45–80</td>
<td>20–80</td>
<td>96.7</td>
<td>97.8&lt;sup&gt;b&lt;/sup&gt;, 93.0&lt;sup&gt;c&lt;/sup&gt;, 97.3&lt;sup&gt;d&lt;/sup&gt;, 99&lt;sup&gt;e&lt;/sup&gt;</td>
</tr>
<tr>
<td>Levoglucosan (LG)</td>
<td>99.5</td>
<td>103.8</td>
<td>99.5</td>
<td>0</td>
<td>30–60</td>
<td>&lt;14</td>
<td>81.9</td>
<td>80.0&lt;sup&gt;j&lt;/sup&gt;, 81.5&lt;sup&gt;k&lt;/sup&gt;</td>
</tr>
</tbody>
</table>

<sup>a</sup> Robinson and Stokes (1970), bulk solution measurements  
<sup>b</sup> Marcolli et al. (2004), bulk solution measurements  
<sup>c</sup> Gysel et al. (2002), HTDMA measurements  
<sup>d</sup> Tang and Munkelwitz (1993), electrodynamic balance measurements  
<sup>e</sup> Onasch et al. (1999), FTIR spectroscopy measurements  
<sup>f</sup> Biskos et al. (2006), HTDMA measurements  
<sup>g</sup> Brooks et al. (2002), bulk solution measurements, 24°C  
<sup>h</sup> Peng et al. (2001), bulk solution measurements, 25°C  
<sup>i</sup> Prenni et al. (2001), thermodynamic model  
<sup>j</sup> Mochida and Kawamura (2004), bulk solution measurements at 20°C  
<sup>k</sup> Parson (2006) optical microscope coupled to a flow cell
Table 3. Parameters characterizing the hygroscopic growth of the investigated aerosol particles/substances: best-fit values (±standard errors) for the three-parameter fit ($k_1$, $k_2$, $k_3$; Eq. A14) and for the single-parameter fit ($\kappa$, Eq. A17) to the water activity-based growth curves ($g_b$ vs. $a_w$; Fig. 7). $i_s$ is the van’t Hoff factor corresponding to the best-fit value of $\kappa$. $n$ and $R^2$ are the number of data points and the correlation coefficients of the fits, respectively.

<table>
<thead>
<tr>
<th>Substance</th>
<th>$k_1$</th>
<th>$k_2$</th>
<th>$k_3$</th>
<th>$R^2$</th>
<th>$\kappa$</th>
<th>$i_s$</th>
<th>$R^2$</th>
<th>$n$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ammonium sulfate (AS)</td>
<td>1.2384±0.0971</td>
<td>−1.0377±0.2443</td>
<td>0.2475±0.1536</td>
<td>0.9987</td>
<td>0.510±0.007</td>
<td>2.11</td>
<td>0.9827</td>
<td>40</td>
</tr>
<tr>
<td>Oxalic acid (OA, dihydrate)</td>
<td>0.6185±0.1064</td>
<td>−1.2315±0.2773</td>
<td>0.9511±0.1784</td>
<td>0.9952</td>
<td>0.233±0.003</td>
<td>0.98</td>
<td>0.9758</td>
<td>54</td>
</tr>
<tr>
<td>Levoglucosan (LG)</td>
<td>0.6208±0.2063</td>
<td>−0.8205±0.5223</td>
<td>0.4273±0.3260</td>
<td>0.9943</td>
<td>0.231±0.003</td>
<td>1.29</td>
<td>0.9896</td>
<td>27</td>
</tr>
</tbody>
</table>
Fig. 1. Experimental setup of the hygroscopicity tandem differential mobility analyzer (H-TDMA) system: RH – relative humidity sensor, SDD – silica gel diffusion dryer, NL – aerosol neutralizer, DMA – differential mobility analyzer, CPC – condensation particle counter.
Fig. 2. Measurement precision and dry particle stability characterized by test measurements of particle mobility diameter ($D_b$) over time: (a) Initial mobility diameter ($D_{bi}$) as selected with DMA1 and measured with DMA2 for ammonium sulfate particles over the full duration of an H-TDMA experiment (~7 h). Symbols and error bars represent the arithmetic mean and standard deviations ($\pm 1$ s) of five repeated measurements; open symbols indicate warm-up time. The slope of the linear fit indicates a drift of 0.018 nm h$^{-1}$ (<0.2%). (b) Mobility diameter of oxalic acid, glutaric acid, and ammonium sulfate particles under dry conditions plotted against residence time between DMA1 and DMA2 (conditioner and tubing). The slope of the linear fit indicates an evaporation rate of (2.5±0.2) nm s$^{-1}$ for glutaric acid particles, whereas no significant evaporation was observed for oxalic acid and ammonium sulfate (<0.03 nm s$^{-1}$).
**Fig. 3.** Water uptake by aerosol particles consisting of crystalline or amorphous (semi-)solid substances: surface adsorption and bulk absorption, restructuring, and liquefaction/dissolution (deliquescence).
Fig. 4. Growth factors and geometric standard deviations observed in hydration and dehydration experiments with aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA), or levoglucosan (LG).
Fig. 4. Mobility equivalent growth factors ($g_b$, panels a, c, e) and geometric standard deviations ($\sigma_g$, panels b, d, f) observed in hydration experiments and dehydration experiments with aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA), or levoglucosan (LG). The growth factors refer to the minimum mobility particle diameters observed in h&d experiments (Fig. 5, Table 2). The line in panel (f) is a polynomial fit to guide the eye.
Fig. 5.

Mobility equivalent diameters observed in hydration experiments and in hydration & dehydation (h&d) experiments ($D_b$, panels a, c, e) and equivalent numbers monomolecular layers of water corresponding to the diameter difference ($N_{ML}$, panels b, d, f) for aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA) or levoglucosan (LG). Where $D_b,h&d$ increased rather than decreased with RH (open green triangles), $N_{ML}$ was calculated from the difference between $D_b,h$ and $D_b,h&d_{min}$. Open grey circles indicate RH range where the difference between $D_b,h$ and $D_b,h&d$ appears dominated by restructuring rather than water uptake. Lines are polynomial fits to guide the eye.
Fig. 5. Mobility equivalent diameters observed in hydration experiments and in hydration & dehydration (h&d) experiments (\(D_b\), panels a, c, e) and equivalent numbers monomolecular layers of water corresponding to the diameter difference (\(N_{ML}\), panels b, d, f) for aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA) or levoglucosan (LG). Where \(D_{b,h&d}\) increased rather than decreased with RH (open green triangles), \(N_{ML}\) was calculated from the difference between \(D_{b,h}\) and \(D_{b,h&d,min}\). Open grey circles indicate RH range where the difference between \(D_{b,h}\) and \(D_{b,h&d}\) appears dominated by restructuring rather than water uptake. Lines are polynomial fits to guide the eye.
Fig. 6. Mobility equivalent growth factors ($g_b$, data points) observed for ammonium sulfate (a), oxalic acid (b, c) and levoglucosan (d) particles in comparison to mass equivalent growth factors calculated with different Köhler models ($g_m$, lines; Sect. 3.5; Appendix A).
Fig. 7.

3-parameter (κ1-κ3) and 1-parameter (κ) fits to water activity-based growth curves (g_b vs. a_w; panels a, c, e) and dependence of effective hygroscopicity parameter κ and corresponding van’t Hoff factor i_s on water activity (panels b, d, f) for aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA) or levoglucosan (LG). Data points are from H-TDMA experiments (deliquesced particles) with a_w calculated from RH assuming volume additivity and water surface tension. Lines in panels b, d, f correspond to three-parameter fits in panels a, c, e (eq. A18).

Fig. 7.
Fig. 7. 3-parameter ($k_1 - k_3$) and 1-parameter ($\kappa$) fits to water activity-based growth curves ($g_b$ vs. $a_w$; panels a, c, e) and dependence of effective hygroscopicity parameter $\kappa$ and corresponding van’t Hoff factor $i_s$ on water activity (panels b, d, f) for aerosol particles composed of ammonium sulfate (AS), oxalic acid (OA) or levoglucosan (LG). Data points are from H-TDMA experiments (deliquesced particles) with $a_w$ calculated from RH assuming volume additivity and water surface tension. Lines in panels (b, d, f) correspond to three-parameter fits in panels (a, c, e) (Eq. A18).