Characterization of Tropospheric Emission Spectrometer (TES) CO₂ for carbon cycle science

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Abstract

We present carbon dioxide (CO$_2$) estimates from the Tropospheric Emission Spectrometer (TES) on the EOS-Aura satellite launched in 2004. For observations between 40° S and 45° N, we find about 1 degree of freedom with peak sensitivity at 511 hPa. The estimated error is $\sim$10 ppm for a single target and about 1.3 ppm for monthly averages on spatial scales of 20° × 30°. Monthly spatially-averaged TES results from 2005–2008 processed with a uniform initial guess and prior are compared to CONTRAIL aircraft data over the Pacific ocean, aircraft data at the Southern Great Plains (SGP) ARM site in the southern US, and the Mauna Loa and Samoa surface stations. Comparisons to Mauna Loa observatory show a correlation of 0.92, a standard deviation of 1.3 ppm, a predicted error of 1.2 ppm, and a ~2% low bias, which is subsequently corrected, and comparisons to SGP aircraft data over land show a correlation of 0.67 and a standard deviation of 2.3 ppm. TES data between 40° S and 45° N for 2006–2007 are compared to surface flask data, GLOBALVIEW, the Atmospheric Infrared Sounder (AIRS), and CarbonTracker. Comparison to GLOBALVIEW-CO$_2$ ocean surface sites shows a correlation of 0.60 which drops when TES is offset in latitude, longitude, or time. At these same locations, TES shows a 0.62 and 0.67 correlation to CarbonTracker with TES observation operator at the surface and 5 km, respectively. We also conducted an observing system simulation experiment to assess the potential utility of the TES data for inverse modeling of CO$_2$ fluxes. We find that if biases in the data and model are well characterized, the averaged data have the potential to provide sufficient information to significantly reduce uncertainty on annual estimates of regional CO$_2$ sources and sinks. Averaged pseudo-data at 10° × 10° reduced uncertainty in flux estimates by as much as 70% for some tropical regions.
1 Introduction

Carbon dioxide (CO$_2$) is the most important anthropogenic greenhouse gas (IPCC, 2007). It is long-lived with a current global average tropospheric-mixing ratio of about 385 parts per million (ppm), and is increasing at a rate of about 2 ppm/yr. Superimposed on this upward trend is a seasonal cycle reflecting the uptake and release of CO$_2$ by the terrestrial biosphere and oceans, and which, as shown in Fig. 1, is markedly more pronounced in the Northern Hemisphere than the Southern Hemisphere (Matsueda et al., 2002; Tans and Conway, 2005; Bösch et al., 2006). Currently about 55% of the anthropogenically emitted CO$_2$ remains in the atmosphere (IPCC 2007, Chapter 7), whereas the remainder is removed by the ocean and land biosphere; but the spatial and temporal distribution of the uptake has large uncertainties. Recent studies have shown that emissions of CO$_2$ from fossil fuel combustion have been increasing faster than predicted (Raupach et al., 2007) and the southern hemispheric oceans’ capacity for CO$_2$ uptake may be diminishing (Le Quéré et al., 2007). An improved quantitative understanding of the sources and sinks of atmospheric CO$_2$ is essential for reliably predicting future atmospheric CO$_2$ levels, for assessing the impact of land use changes on atmospheric CO$_2$, developing mitigation strategies, and for treaty verification.

Inverse modeling, which uses an atmospheric transport model to estimate fluxes from a set of atmospheric CO$_2$ observations, has emerged as an important tool for quantifying CO$_2$ sources and sinks. This approach, pioneered by Tans et al. (1990) and Enting and Mansbridge (1991), has become more sophisticated, but is limited by the fact that the current observational network is sparse and consequently does not have the information content to provide reliable constraints on carbon fluxes at regional scales (e.g., Rayner et al., 1996; Gloor et al., 2000; Suntharalingam et al., 2003). Studies using simulated data have demonstrated the potential utility of space-based measurements of CO$_2$ for providing improved estimates of regional CO$_2$ fluxes (e.g., Pak and Prather, 2001; Rayner and O’Brien, 2001; Houweling et al., 2004; Chevallier
et al. 2007; Baker et al., 2006; Feng et al., 2009). For example, Rayner and O’Brien (2001) showed that satellite measurements of CO$_2$ column abundances with a precision of 2.5 ppm, averaged monthly and on spatial scales of $8^\circ \times 10^\circ$, would offer more information on CO$_2$ fluxes than can be obtained from the existing surface network. Houweling et al. (2004) showed that CO$_2$ observations, such as those from the Atmospheric Infrared Sounder (AIRS), with sensitivity only in the upper troposphere, would lead to significant reductions of CO$_2$ source and sink errors as compared to the in situ observation network. Chevallier et al. (2005) found, however, that inversions with AIRS CO$_2$ are sensitive to latitude-dependent biases larger than about 0.3 ppm and Chevallier et al. (2009) found that AIRS radiance assimilation, while improving surface flux uncertainties, did not perform as well as the flask network. Baker et al. (2006) performed inversions of the same surface data using different models and found significant differences in flux estimates from transport error, suggesting measurements in the mid-troposphere would add value in addition to surface sites.

Space-based measurements of CO$_2$ are currently available from the Scanning Imaging Absorption Spectrometer for Atmospheric Chartography (SCIAMACHY), the Infrared Atmospheric Sounding Interferometer (IASI), the Greenhouse gases Observing Satellite (GOSAT), and the Atmospheric Infrared Sounder (AIRS). AIRS was launched on the EOS-Aqua platform in 2002 and several different techniques have been used to retrieve atmospheric CO$_2$ abundances from AIRS radiances. The AIRS retrievals have estimated peak sensitivity ranging between 200 and 600 hPa (e.g., Chahine et al., 2005, 2008; Crevoisier, 2003; Engelen et al., 2004; Strow et al., 2008; Maddy et al., 2008). SCIAMACHY was launched on the Envisat platform in 2001 and measures reflected sunlight at UV-SWIR wavelengths, with peak sensitivity near the surface. Buchwitz et al., (2005, 2007), Bösch et al. (2006) and Barkley et al. (2006) have presented daytime CO$_2$ retrievals over land from SCIAMACHY data. IASI, onboard the European MetOp platform, was launched in October 2006 and Crevoisier et al. (2009) have recently presented a tropical ($20^\circ$ N–$20^\circ$ S) ocean CO$_2$ product from IASI with peak sensitivity near 200 hPa. In January, 2009, the GOSAT instrument was launched specif-
ically to study greenhouse gases (http://www.jaxa.jp/projects/sat/gosat/index_e.html) with a mission target of 4 ppm accuracy for a 3 month regional average using a combination of SWIR and IR channels (Hamazaki et al., 2004a,b). The Orbiting Carbon Observatory (OCO) (Crisp et al., 2004) was lost as a result of a launch mishap in February 2009. This NASA satellite for dedicated CO\textsubscript{2} observations aimed to measure CO\textsubscript{2} columns with a precision of \~1 ppm for a single target (Miller et al., 2007).

We present here atmospheric CO\textsubscript{2} retrievals of the Tropospheric Emission Spectrometer (TES) satellite instrument. TES is a Fourier transform spectrometer that measures thermal infrared emission. We find that the TES nadir profile retrievals of CO\textsubscript{2} have peak sensitivity in the middle troposphere, near 500 hPa. The individual TES retrievals have errors of about 10 ppm at 511 hPa, but monthly averaging reduces the errors to about 1.3 ppm for 20° \times 30° and about 1.9 ppm for 10° \times 10°. We show that TES CO\textsubscript{2} has the potential to reduce uncertainty in regional estimates of CO\textsubscript{2} fluxes through an observing system simulation experiment (OSSE). In a subsequent study by Nassar et al. (in preparation) we present an inversion analysis using the TES CO\textsubscript{2} data and compare the information provided by TES with that obtained from the in situ observing network for constraining CO\textsubscript{2} sources and sinks.

2 The TES instrument

TES is on the Earth Observing System Aura (EOS-Aura) satellite and makes high spectral resolution nadir measurements in the thermal infrared (660 cm\textsuperscript{-1}–2260 cm\textsuperscript{-1}, with unapodized resolution of 0.06 cm\textsuperscript{-1}). It was launched in July 2004 in a sun-synchronous orbit at an altitude of 705 km with an equatorial crossing time of 13:38 (local mean solar time) and with a repeat cycle of 16 d. In standard “global survey” mode, 2000–3000 observations are taken every other day (Beer, 2006). There are additional targeted “special observations”, which account for about 10% of TES data over mid-latitude Pacific in 2006, and which are not used in this analysis as they are less spatially and temporally uniform. TES level 2 data provide profile retrievals for
atmospheric temperature (Herman et al., 2009), water (Shephard et al., 2008), HDO (Worden et al., 2004), ozone (Worden et al., 2007; Nassar et al., 2008; Osterman et al., 2008; Richards et al., 2008), carbon monoxide (Rinsland, 2006; Luo et al., 2007a,b), methane (Payne et al., 2009), as well as surface temperature, emissivity, and cloud information (Eldering et al., 2008). For details on the TES instrument, see Beer (2006), and for information on the retrieval process see Bowman et al. (2006) and Kulawik et al. (2006).

3 In situ observations of atmospheric CO₂

3.1 In situ and other datasets used for validation of TES CO₂

TES CO₂ data over oceans between 2005–2008 are compared to Comprehensive Observation Network for TRace gases by AIrLiner (CONTRAIL) flask data and to surface data from Samoa and Mauna Loa. The CONTRAIL dataset contains in situ aircraft flask measurements taken on commercial flights between Australia and Japan. The data are collected primarily between 10 and 11 km one to two times per month at 12 latitudes between 24° S and 35° N (Matsueda et al., 2002, 2008; Machida et al., 2008). The CONTRAIL dataset is extremely useful for satellite validation as it occurs in the middle upper troposphere over all seasons in both the Northern and Southern Hemispheres. We compare to sets of CONTRAIL data in the Northern Hemisphere between 13–35° N, and in the Southern Hemisphere between 10–25° S. We also compare to the Mauna Loa site, which is at 3.4 km altitude, 19.5° N, 155° W and is part of the NOAA Earth System Research Laboratory (ESRL)/Global Monitoring Division (GMD) Carbon Cycle Greenhouse Gases network (http://www.esrl.noaa.gov/gmd/ccgg/index.html). This site is useful as it has monthly averaged data at an altitude somewhat lower but comparable to TES peak sensitivity at 5 km. The GMD Samoa site (54.5° S, 154° E) provides surface measurements complementary to the Southern Hemisphere CONTRAIL data. Together these data bracket the altitudes of TES sensitivity. A map of validation sites
and TES data is shown in Fig. 2. In the Pacific, we also compare to one of the AIRS CO₂ datasets (Chahine et al., 2005, 2008), which is gridded (2×2.5°) monthly data available from http://mirador.gsfc.nasa.gov/ (keyword AIRX3C2M). The retrieved parameter is a scaling factor applied to a CO₂ profile and has peak sensitivity at 300 hPa for mid-latitudes (Olsen, 2009).

For land validation for 2006–2008, we compare to aircraft flask measurements taken at the Southern Great Plains (SGP) Atmospheric Radiation Measurement (ARM) site with up to 12 measurements between 0.3 and 5.3 km altitude up to 8 times per month. This site is located in the southern United States at 36.8°N, 97.5°W, and has data starting in 2006.

For TES CO₂ retrievals between 40°S and 45°N, we compare to surface station flask data from the NOAA GMD network (Conway et al., 2008), the GLOBALVIEW dataset (GLOBALVIEW-CO₂, 2008), and CarbonTracker (Peters et al., 2007, http://carbontracker.noaa.gov). The GLOBALVIEW dataset interpolates and extends data from surface flask measurements to provide weekly CO₂ measurements at surface flask site locations. There are 39 stations (25 ocean and 14 land) between 35°S and 40°N with data in 2006–2007, although some do not have continuous data. Ocean sites are expected to compare better with TES measurements because of better agreement between the surface and free troposphere. CarbonTracker is a data assimilation system that uses in situ observations with a model to produce three dimensional estimates of tropospheric CO₂ distributions as well as estimates of sources and sinks. The CO₂ distributions have global daily output on 34 pressure levels ranging from the surface to 0.1 hPa. TES is compared to CarbonTracker at the surface and at 500 hPa with and without the TES averaging kernel.

3.2 Observed variability in CO₂ at the surface and in the free Troposphere

This section compares in situ data at different locations and altitudes to provide context for TES results. Surface station flask data shows seasonal variability of 2–15 ppm, with larger variability observed over land and in the Northern Hemisphere, and the
highest seasonal variability towards the north pole. Over the northern mid-latitude Pacific Ocean, comparisons were made between monthly averaged surface data from the Guam ground station (at 13.7° N, 144° E), CONTRAIL aircraft flask data at 10–11 km, and the Mauna Loa ground station (at 3.5 km elevation). There is good agreement at these different longitudes, latitudes, and altitudes (with perhaps a one-month temporal lag in CONTRAIL for January through April). This indicates that CO₂ over the Pacific is fairly uniform in latitude (between 15–35° N), longitude, and altitude (between 0–12 km). The seasonal cycle is about 5 ppm in these data.

In contrast, aircraft measurements taken at the SGP site in the southern United States show a seasonal variability of ~10.0 ppm in the 0–2 km data, with a seasonal pattern peaking sooner than Mauna Loa whereas the 2–7 km data from SGP have ~5 ppm seasonal variability with a similar pattern to Mauna Loa. Variability within each month drops off with altitude with intra-monthly variability of 3.9 ppm for the 0–2 km data. For the 2–4 km data and the 4–7 km data, the intra-monthly variability is 1.8 ppm and 1.4 ppm, respectively. The 2–4 km and 4–7 km data showed very similar seasonal patterns.

In the Southern Pacific Ocean, the Samoa ground station and CONTRAIL aircraft data between 10–30° S both show ~3 ppm seasonal variation, with Samoa showing an irregular monthly increase, and CONTRAIL perhaps showing a peak around July of each year. Both show variability within each month of ~0.5 ppm. A surface station at Cape Ferguson, Australia (19° S, 147° E), close to the CONTRAIL flight path, shows the same yearly increase with different monthly variability. The CONTRAIL data, on average, have a 0.5–1 ppm high bias versus the surface stations, which, when looking at data averaged over several years, appears to occur between May and August. In summary, the Southern Hemisphere shows little seasonal variability, but shows differences between different surface sites and CONTRAIL data month by month.
4 TES retrievals of atmospheric CO$_2$

4.1 Challenges of CO$_2$ retrievals

Estimating CO$_2$ from remote sensing measurements is challenging for a number of reasons. The horizontal variability of CO$_2$ at regional scales is small (≈0.5%–3%) compared to most trace gases (e.g., ozone variability is ≈30%). Moreover, the spectral signature of CO$_2$ variations is small compared to spectral effects of temperature and water variability, as demonstrated in Fig. 3. As a result, CO$_2$ spectral lines are often used to estimate atmospheric temperature, where CO$_2$ concentrations are assumed to be fixed. Such an approximation is not valid for CO$_2$ retrievals, and could lead to a circular dependence between CO$_2$ and temperature. As shown in this paper, moderate temperature biases propagate into untenably large CO$_2$ errors, but this can be mitigated by jointly retrieving atmospheric temperature and CO$_2$ for monthly and regional averages.

Additionally, spectroscopy used for infrared CO$_2$ retrievals is estimated to have ≈1% accuracy for the laser bands (around 1000 cm$^{-1}$) (Devi et al., 2003; Dana et al., 1992). A 4% bias of these results with respect to previous work by Johns and Noel (1988) in the laser bands indicates that similar biases may also occur in the Johns and Vanderauwera (1990) measurements of the $\nu_2$ band (near 700 cm$^{-1}$). A 1% spectroscopy bias translates to a ≈4 ppm error in CO$_2$. On the positive side, a uniform bias could be easily corrected. Radiometric calibration and stability errors can propagate into CO$_2$; an effect which may not be noticed in other more variable atmospheric constituents. Estimates of TES radiometric accuracy are 0.1 K (Kerola et al., 2009); this would result in ≈2.5 ppm CO$_2$ error. However, if this is an RMS error, it averages out; and if it is a bias error, it can again be corrected.
4.2 Retrieval setup

The development of TES CO₂ relied on a combination of guidance from validation with in situ CO₂ data and predictive calculations of error and information content which has been used to develop previous TES products, as described in Worden et al. (2004). The main validation data sets used were the CONTRAIL aircraft flask data, Mauna Loa and Samoa surface stations, and SGP aircraft flask data for land validation. A coarse vertical grid, consisting of 5 levels (surface, 511, 133, 10, and 0.1 hPa) was chosen for the retrieval, which minimize contributions from the a priori state information at each retrieval level. The retrieved parameters for CO₂ are log of the volume mixing ratio at the above levels.

Testing was done with a prototype code based on the TES production code written in the IDL language (http://www.ittvis.com/ProductServices/IDL.aspx). Comparisons to validation data and examination of spectral residuals and other quality factors were used to iteratively update and refine the retrieval approach.

4.3 Retrieval methodology and error analysis

CO₂ is estimated by iteratively minimizing a cost function using the Levenberg-Marquardt non-linear least squares (NLLS) algorithm. The cost function, \(C(z)\), is the combination of the norm difference between the observed and predicted radiances and a penalty term based on the a priori knowledge of the atmosphere:

\[
C(z) = \|L_{\text{obs}} - L(z, b)\|^2_{S_m} + \|z - z_a\|_A \tag{1}
\]

\(L_{\text{obs}}\) is the observed radiance vector, which follows the additive noise model:

\[
L_{\text{obs}} = L(z_{\text{true}}, b_{\text{true}}) + \epsilon \tag{2}
\]

where \(\epsilon\) is the radiance error. \(L(z, b)\) is the predicted radiance evaluated for the retrieved state \(z\) and non-retrieved state \(b\). The cost function terms are weighted by...
the inverse of $S_m$ (the radiance error covariance) and $\Lambda$ (the constraint matrix). The constraint vector, $z_a$, is also used for the initial state. Note that $\|A\|_B^2 = ABA^T$.

When differences between radiances calculated at the true state and a priori vector are spectrally linear, the nonlinear retrieval can be represented by the linear equation:

$$x_{\text{est}} = x_a + G\varepsilon + GK_b(b_{\text{true}} - b_{\text{est}}) + A(x_{\text{true}} - x_a)$$ (3)

where:

- $A$ is the averaging kernel (which describes the sensitivity of the measurement to the true state),
- $x_a$ is the a priori constraint vector,
- $x_{\text{true}}$ is the true state,
- $G$ is the gain matrix (describing the sensitivity of the measurement to changes in radiance),
- $\varepsilon$ is the radiance error vector,
- $K_b$ is the Jacobian matrix (describing the sensitivity of the radiance to each parameter, $K_{ij}^b = \partial L_i / \partial b_j$) of the interferent parameters, and
- $b$ are the interferent parameters.

The retrieved state $z$ and the full state vector $x$ (over which the forward model is calculated) are related through interpolation or mapping, and represent the log of the volume mixing ratio for CO$_2$. The retrieval algorithm is described in more detail in Bowman et al. (2006).

The second-order stochastic characterization of the atmospheric state and the spectral measurement noise are described by the a priori and measurement error covariances:

$$S_a = \text{cov}(x_{\text{true}} - x_a)$$ (4a)

$$S_m = \text{cov}(\varepsilon)$$ (4b)
Using Eq. (3), the covariance of the error between the retrieved and true state, $S_{err} = \text{cov}(x_{est} - x_{true})$, can be calculated:

$$S_{err} = \underbrace{G S_m G^T}_{\text{Measurement}} + \underbrace{G K_b S_{berr} (G K)^T}_{\text{Interferent}} + \underbrace{(1 - A_{xx}) S_{a,xx} (1 - A_{xx})^T + A_{xy} S_{a,yy} (1 - A_{xy})^T}_{\text{Cross-state}} + \underbrace{A_{xy} S_{a,yy} (1 - A_{xy})^T}_{\text{Smoothing}}$$

The measurement and interferent errors come from terms 2 and 3 of the right side of Eq. (3), respectively. The 4th term of Eq. (3) splits into “smoothing” and “cross-state” errors (which are described in Worden et al., 2004), where CO$_2$ indices are denoted by $x$, and the indices of co-retrieved species denoted by $y$. The cross-state component is due to the propagation of error from co-retrieved species into CO$_2$; these errors should decrease with target averaging over regional scales. However, when targets with the same true state are averaged, the smoothing term enters as a bias into the retrieved state and does not decrease with averaging.

The predicted total error covariance for an $n$ target average is:

$$S_{err} = \left( S_{meas} + S_{int} + S_{\text{cross-state}} \right) / n + S_{\text{smoothing}}$$

$$S_{err} = S_{obs} / n + S_{\text{smoothing}}$$

The observation error and smoothing error covariances in Eq. (5) are included in the TES products (Osterman et al., 2009). The predicted error for a particular level is the square-root diagonal of the predicted error covariance at that level, and the off-diagonal terms describe correlated errors between levels. Spectroscopic and calibration errors, which may contribute an additional bias and/or random error, are not included in Eq. (5).

4.3.1 The observation operator

The TES averaging kernel and a priori constraint vector are used in the “observation operator”, $H(x) = x_a + A(x - x_a)$ (Jones et al., 2003). This estimates a TES measurement of CO$_2$ given an input CO$_2$ profile $x$, which may be derived from an in-situ measurement
or a model forecast:

\[ x_{\text{obs}} = x_a + A(x - x_a) \]  

(7)

This operator uses the sensitivity calculated in the averaging kernel which is provided in the TES standard product. When a TES measurement is compared to \( x_{\text{obs}} \), the expected discrepancy is the “observation error” which is the sum of the measurement error, interfering species error, and cross-state error, shown in Eq. (5), and provided in the TES standard product.

4.4 The predicted sensitivity

The approximations assumed in the linear retrieval in Eq. (3) can be validated, as described in Kulawik et al. (2008), by comparing non-linear retrievals using two different a priori vectors, \( x_a \) and \( x'_a \). The non-linear retrieval using \( x'_a \) is compared to the non-linear retrieval using \( x_a \) followed by a linear transformation of the a priori vector from \( x_a \) to \( x'_a \) using the expression:

\[ x'_{\text{est}} = \hat{x} + A(x'_a - x_a) \]  

(8)

where \( \hat{x} \) is the non-linear retrieval obtained with \( x_a \), and \( x'_{\text{est}} \) is the linear estimate of the NLLS retrieval with a priori vector \( x'_a \). \( x'_{\text{est}} \) from Eq. (8) can be compared to the \( \hat{x}' \), the non-linear retrieval obtained using a priori vector \( x'_a \). This analysis is done in Sect. 5.4.

4.5 Radiances and Jacobians

TES filters used in normal operation span from the spectral region 660 cm\(^{-1}\) to 2260 cm\(^{-1}\) with gaps from 910–950 cm\(^{-1}\) and 1320–1891 cm\(^{-1}\). There is significant CO\(_2\) signal in the radiance between 660–770 cm\(^{-1}\), 930–1090 cm\(^{-1}\) and near 2100 cm\(^{-1}\). The signal near 2100 cm\(^{-1}\) has a low signal to noise ratio and was not used, and 990–1070 cm\(^{-1}\) was excluded because of interference from the 10 \( \mu \)m ozone band. Figure 4 shows the radiance and Jacobians for the 3 CO\(_2\) sensitive spectral
regions considered. Although the $\nu_2$ band (near 700 cm$^{-1}$) has a stronger spectral signature, the laser bands (near 1000 cm$^{-1}$) show up stronger because of better spectral noise.

The mean and standard deviation of radiance residuals, which is the difference between the observed and forward model spectra, following CO$_2$ retrievals highlight problem spectral lines and regions. Spectral regions with standard deviation $>1.2 \times$ the NESR (Noise Equivalent Spectral Radiance), or with mean residual $>0.5 \times$ the NESR for a large set of retrievals were taken from the window list. The impact on CO$_2$ sensitivity was minor (less than 0.05 DOF). The full window list is shown in Table 1.

4.6 Retrieval strategy

The retrieval strategy selected in light of the temperature and water error impact on CO$_2$ jointly retrieves atmospheric temperature, surface temperature, emissivity (over land), water vapor, and CO$_2$. The constraints and retrieval levels are the same used operationally for TES water retrievals, however the emissivity constraint was updated to allow more variation in emissivity. The temperature constraint was also tightened from $\sim$2 K to $\sim$0.6 K variability to allow more degrees of freedom for CO$_2$ for these results. Ozone was not jointly retrieved as it was found that retrieving ozone had no impact on the carbon dioxide monthly average values.

Table 2 shows the total degrees of freedom with different TES spectral windows and different species combinations. Table 2 shows that if CO$_2$ were retrieved by itself, i.e. assuming temperature and water are adequately known, CO$_2$ would have more than double the degrees of freedom as when it is co-retrieved with temperature and water. However, as the next section shows, the temperature must have a very low average bias for this strategy to work. Table 2 also shows that the laser bands contain more independent CO$_2$ information as compared to the $\nu_2$ band (by comparing rows 1 and 2) and that only about 0.1 additional degree of freedom is available for CO$_2$ beyond the windows selected (by comparing rows 3 and 4). The degrees of freedom available for
CO₂ would also increase if more windows are included which independently determine temperature, water, etc., effectively freeing up shared information for estimating CO₂. Additionally, averaging strategies which reduce measurement error could improve CO₂ sensitivity.

### 4.7 A priori covariance and constraint

The a priori covariance, used for calculating smoothing error, is set to the same values globally, although the atmospheric variability of CO₂ is significantly lower in the Southern Hemisphere. The square root values of the diagonal of the a priori covariance are set to: 4, 3.5, 2.5, 2, and 2 ppm at the surface, 511, 133, 10, and 0.1 hPa, respectively. The surface variability is based on the average GLOBALVIEW variability (3.5 ppm variability) which is increased to 4 because of the higher variability over land (e.g. 10 ppm variability for SGP aircraft data). The 511 hPa variability is based on measurements of Mauna Loa variability. The 133 hPa variability is based on CONTRAIL variability, and the variability of the higher levels are slightly reduced from CONTRAIL variability. The off-diagonal correlations in the a priori covariance matrix are 0.8 for the first two levels, based on correlations of monthly averaged SGP data for the first two levels, and 0.9 for the second two levels, based on correlations of Mauna Loa and CONTRAIL data, and 0.9 for all other adjacent levels.

As seen in Eq. (1), the constraint determines how much weight is given to the a priori knowledge of the atmosphere. The relative constraint strengths for CO₂ and temperature also determine the partitioning of shared degrees of freedom between CO₂ and temperature. The selection of a reduced set of retrieval levels or linearly scaling a profile can also be represented in the a priori framework and expressed as a constraint matrix. The effect of the constraint can be seen by applying the observation operator (Eq. 7) to a model or aircraft profile to simulate the degraded vertical resolution seen by TES.

The constraints are calculated based on the method of Kulawik et al. (2006) with the variability of the CO₂ covariance enhanced to 5.4% at the surface and 2.8% in the mid-
troposphere which increases both the sensitivity to CO$_2$ and the measurement error. As seen in Sect. 4.2, this loose constraint results in a large uncertainty for a single target and $\sim$1.3 ppm error with averaging.

5 Characterization of results

5.1 Sensitivity and errors of a single target

Averaging kernel rows for Ocean (in Pacific Ocean, 13–35° N) and Land (near SGP, 31–46° N) averages are seen in Fig. 5. Thermal contrast drives sensitivity in the infrared, with higher sensitivity correlated with higher surface temperatures. Summertime, daytime, land cases have the most sensitivity, however tropical ocean locations have more sensitivity than land locations when averaged over day and night, and all seasons. The averaging kernels show sensitivity for the retrieved value at the surface, 511 hPa, and 133 hPa. The peak sensitivity is at 511 hPa with about 45% sensitivity near the 511 hPa level, about 10% sensitivity near the surface, and about 25% sensitivity around the 133 hPa level, with the remainder coming from the prior.

Figure 6 shows the predicted errors for both a single target and a 100-target average for TES CO$_2$ retrievals. The single target predicted error is about 6 ppm at 511 hPa, which is dominated by cross-state error, primarily from atmospheric temperature, but also from water, surface temperature, and cloud properties. The 100-target average error at 511 hPa is about 1.4 ppm, dominated by the smoothing error.

The thermal infrared radiation signal strength observed by TES depends on the surface temperature and surface properties. Because of this, sensitivity to CO$_2$ depends on latitude as shown in Fig. 7. Because of the sensitivity decrease with higher latitudes, only 40° S to 45° N is used from TES data. Results at higher latitude do not compare well to aircraft validation data at 65° N at Poker Flats (not shown).
5.2 Predicted and actual errors for averaged profiles

In this section we test Eq. (6) by calculating the actual and predicted errors for various numbers of averaged profiles in boxes of 10×10, 15×15, 20×20, and 20×30°. 3 yr of TES data are compared to Mauna Loa (with and without the TES observation operator) and CONTRAIL data as shown in Fig. 8. All comparisons show error reduction as the numbers of profiles averaged increases, as predicted. Equation (6) shows that the error of TES versus Mauna Loa or CONTRAIL should fit to \( \sqrt{S_{obs}/n + S_{\text{smoothing}}} \) and the error of TES versus Mauna Loa with the TES observation operator should fit to \( \sqrt{S_{obs}/n} \). Fits of the data shown in Fig. 8 to the form of Eq. (6) indicated that the observation error is 12.3 ppm (rather than the predicted 6 ppm) and the smoothing error is 1.1, about as predicted. The largest uncertainty in the smoothing error is the a priori covariance, which predicts the initial uncertainty in the atmospheric state. The dominant error of observation error is the cross-state error, which includes temperature and water errors. CO\(_2\) error is not found to be very sensitive to the initial water uncertainty but increasing the temperature a priori uncertainty from about 2 K to 5 K resulted in a 12 ppm predicted error for CO\(_2\). However, 5 K is larger than the expected initial error in TES temperature, and this suggests another source of error for CO\(_2\), e.g. a variable calibration error, which averages out similarly to the observation error.

5.3 Impact of temperature errors

The effects of temperature errors were studied by setting the temperature to the initial guess or the initial guess perturbed by +0.1 K throughout the profile. The difference in retrieved CO\(_2\) (holding temperature fixed) for the two initial temperature values was calculated and compared to the predicted change using Eq. (3). Based on a case study of about 100 non-linear retrievals, it was found that a +0.1 K temperature error resulted in a +2.5 ppm CO\(_2\) error. This agreed with the predicted propagation of temperature error, as given by the quantity \( GK_b \) (0.1 K) from Eq. (3). As the uncertainties
in the TES initial temperature (from NASA’s Global Modeling and Assimilation Office GEOS-4 meteorological fields) are \( \sim 2 \) K compared to sondes (Herman et al., 2009), temperature errors resulting from fixing the temperature to the initial value would translate into unacceptable errors in CO\(_2\), of up to 50 ppm, for a single target. However, when temperature and water are jointly retrieved along with CO\(_2\), the temperature and water errors partially cancel, and result in predicted errors of \( \sim 6 \) ppm for a single target, and less when averaged over many targets.

### 5.4 Validation of predicted sensitivity

Starting the retrieval with a different prior and initial guess is used to validate the averaging kernel and retrieval linearity. TES data in the Northern Hemisphere Pacific Ocean (13–35\(^\circ\) N, 128–158\(^\circ\) E) were processed using both a 360 ppm (360IG) and a 380 ppm (380IG) initial guess and prior value (both the a priori vector and initial guess are set to the specified values for all pressures and all dates) for 2006–2008. Both results are compared to Mauna Loa to determine the effect of starting at a “bad” initial guess and prior, and compared to each other to determine if both results are consistent given the TES predicted sensitivity. Figure 9 shows 360IG compared to Mauna Loa with the TES observation operator (Eq. 7). The consistency of these results validate TES’s averaging kernel, with the averaging kernel row at 511 hPa averaging \( \sim 0.8 \). However, 380IG correlates somewhat better than 360IG with Mauna Loa (0.95 versus 0.91 correlation), showing that the initial guess and prior do make some difference in the resulting accuracy. Monthly averaged 380IG values were converted using Eq. (8) to a 360 ppm a priori vector to create the 360EST dataset. 360EST averaged 1.2 ppm higher than 360IG, with a 0.8 ppm rms. The bias between 360EST and 360IG is likely because the degrees of freedom are 0.05 smaller for 360IG, which results because the averaging kernel is calculated at the retrieved state, which is lower for 360IG.

Conversion using the averaging kernel on the TES 66-level pressure grid versus on the 5-level CO\(_2\) retrieval level grid yielded very similar results. Applying Eq. (8) to individual targets and then creating monthly averages yielded a larger standard deviation.
(4 ppm vs. 0.8 ppm) and a smaller bias (0.4 ppm vs. 1.2 ppm) versus first averaging and then converting with Eq. (8). Operationally, the initial error is not expected to be more than 5 ppm. These findings validate the reported sensitivity and indicate that the results are fairly robust under changes to the a priori vector (e.g., as described in Kulawik et al., 2008).

5.5 Bias characterization

TES results show a low bias relative to all validation data of about 6 ppm which is most likely some combination of calibration and spectroscopic error. The bias changes when spectral windows or constraints are changed or when using v003 versus v004 radiances. This bias, however, appears to be stable over the 3 yr of uniformly processed v003 data. Whether the bias is spectroscopic or calibration, it can be represented as a radiance error which propagates into \( \text{CO}_2 \) using the equation \( \Delta x = G \Delta L \), where \( \Delta x \) is the error in \( \log(\text{VMR}) \), \( G \) is the gain matrix, and \( \Delta L \) is the radiance error. If it is from a line intensity error, the Jacobian error is of the form \( \Delta K = f K \), making the radiance error \( \Delta L = f K x \), where \( x \) is the log of the true state, so the error in the retrieved value is \( f A x \). This is the format assumed for the error. The value for \( f \) was set by comparisons to data from the Mauna Loa observatory, as these data had the highest correlation with the retrieved TES values. The best fit for \( f \) was 0.021, or 2.1%. Applying the correction factor did not impact the correlation but did improve the bias. TES v004 radiances, which have an update to the frequency calibration, had a similar but slightly larger bias of about 0.023. Ideally the comparison would be to oceanic well-mixed aircraft data covering the altitudes of TES sensitivity (surface through \( \sim 11 \) km) with the TES observation operator applied rather than to a uniform profile set to the Mauna Loa surface value with the TES observation operator applied. However, this correction factor is easy to update, as it is applied post-processing using the averaging kernels in the product.
6 Comparisons to in situ data, AIRS, and CarbonTracker

The validation data for CO\textsubscript{2} is far more comprehensive than for many other atmospheric constituents. We compare to 39 surface stations between 35\degree S and 40\degree N, which report daily or monthly values, to aircraft data taken over the United States (SGP) and to aircraft data taken in the Pacific between Japan and Australia (CONTRAIL), data from the AIRS instrument, and to CarbonTracker.

6.1 CONTRAIL, Mauna Loa, and AIRS in the Northern Hemisphere

In Fig. 10 we compare CONTRAIL aircraft measurements of CO\textsubscript{2} in the Northern Hemisphere to TES data processed from the same vicinity, with locations described in Fig. 2. The TES data are also compared to data from the Mauna Loa surface site and to AIRS measurements from the same latitude and longitude ranges as TES. The Mauna Loa and CONTRAIL data, at 3.5 and 10.5 km, respectively, are useful in that they bracket the altitude of maximum TES sensitivity, around 5 km. The version of AIRS CO\textsubscript{2} used here (Chahine et al., 2005) has peak sensitivity around 300 hPa, corresponding to a higher altitude than TES CO\textsubscript{2}. Figure 10 shows a time series of the datasets (top panel), the difference between TES and Mauna Loa with TES observation operator (middle panel), and correlations of TES to the other measurements (lower panel). For the application of the TES observation operator, the true value is set to the Mauna Loa value for all pressures. TES is most correlated with Mauna Loa (0.92) and CarbonTracker (0.95) and correlated with CONTRAIL and AIRS at about 0.85. The correlations represent a combination of yearly and seasonal trends.

As seen in Fig. 10 TES begins to show a low bias versus Mauna Loa without the TES observation operator, starting in mid-2008, when CO\textsubscript{2} deviates significantly from the a priori value of 380 ppm. The bias is improved with the application of the TES observation operator, which takes into account the TES sensitivity. For assimilation of data, it is most important to have the sensitivity accurately characterized, as demonstrated by the good comparison of the TES average (red) and Mauna Loa with TES
observation operator (orange).

6.2 CONTRAIL, Samoa, AIRS in the Southern Hemisphere

As seen in Fig. 1, the seasonal variability of the Southern Hemisphere CO₂ is far less than the Northern Hemisphere, although with a similar yearly increase. Figure 11 shows comparisons of CONTRAIL, AIRS, CarbonTracker, and the Samoa surface site with TES based on the locations as described in Fig. 2. The TES variability is larger than expected as compared to the validation data. The TES data also show a dip in the early part of each year. Correlations with CONTRAIL, AIRS, and Samoa are shown in Fig. 11, as well as the bias versus Samoa over time.

6.3 Seasonal variations from 2005–2008 monthly averages

Figure 12 shows 3 yr of data, from June 2005 to June 2008, averaged by month (i.e. all data from August 2005, 2006, and 2007 averaged) to show seasonal variability. In the Northern Hemisphere, TES agrees well with the Mauna Loa data transformed with the TES observation operator (purple dashed line), which has less seasonal variability than the raw Mauna Loa data (purple solid line). CarbonTracker shows a similar seasonal pattern with less variability, especially considering that the data do not have the TES observation operator applied. AIRS, at a higher altitude, shows the same seasonal pattern with less variability. The CONTRAIL data, at 10–11 km, appear to show approximately the same seasonal variability as Mauna Loa, with faster transitions. In the Southern Hemisphere, the seasonal variability of all datasets is markedly less, and the agreement is less striking. TES shows higher values in the second half of the year, with a seasonal cycle somewhat similar to CarbonTracker, although averaging about ∼1.5 ppm higher. The validation in the Southern Hemisphere relies on data at the surface and 10 km, with no validation data in the mid troposphere, so it is not possible to fully validate the TES Southern Hemisphere results.
6.4 Comparison to SGP aircraft data

Figure 13 shows comparisons to aircraft data from the Southern Great Plains ARM site. Surface air at the SGP shows a seasonal drawdown arising from nearby winter-wheat (April–May) and later growth of more distant summer crops and grass (June–July) (Fischer et al., 2007; Riley et al., 2009). The aircraft data from 2–4 km and 4–7 km show very similar seasonal patterns at this location so aircraft data between 2–7 km were averaged monthly and compared to TES monthly averages over the spatial region described in Fig. 2. Figure 13 shows the comparison of these data from 2006–2008, and the lower panel shows a correlation of 0.67 between TES and SGP aircraft data and 0.77 correlation between TES and Carbontracker, where the Carbontracker values are selected to match the TES observation area. These correlations do not change when the TES observation operator is applied, however TES shows a high bias when the observation operator is applied, indicating more work is needed on the characterization of the TES bias correction. Since SGP is at one location with a few measurements per month and TES is averaging over most of the United States, it is not surprising that there are some differences between these measurements.

The correlations between TES and SGP are significantly lower than that obtained between TES and Mauna Loa or CONTRAIL data in the Northern Hemisphere. The lower correlation could indicate a problem in TES results over land, or could be because TES is averaging over a good part of the US. Land data present more challenges than ocean, namely an uncertain and variable surface emissivity, and a less certain and more variable surface temperature. It is likely that the less optimal comparison with validation data is a combination of more interference of surface characteristics and more variable carbon dioxide. This dataset is and will be useful for testing improvements to the TES retrieval algorithm.
6.5 Comparison to GLOBALVIEW and surface flasks

Comparisons of TES to GLOBALVIEW data are useful for a statistical validation of TES even though GLOBALVIEW consists of surface site estimates and TES sensitivity peaks in the mid-troposphere. Processed TES data from January, 2006 through September, 2007 are compared to GLOBALVIEW surface values between 35° S and 40° N which includes 24 ocean and 14 land stations. We compare monthly averaged TES values which have at least 20 TES measurements within 830 km of the site in a month (resulting in about a 15° diameter circle centered at the site). Comparison to GLOBALVIEW or in situ flasks yielded nearly identical results within 0.02 correlation, so for simplicity only results compared to GLOBALVIEW are shown. Use of GLOBALVIEW data points with a relative weight of at least 2 (“derived directly from the actual measurements”) resulted in only 4 stations with not much improvement in statistics over using all weights, so all weights are used for comparisons.

Table 3 shows TES and GLOBALVIEW correlations for different subsets of locations; we find that ocean sites have significantly higher correlation than land locations, and the Northern Hemisphere has significantly higher correlation than the Southern Hemisphere. We also find that high altitude sites (>2 km) correlate better with TES than lower altitude sites, likely because at high altitudes the measurement is made closer to the altitude of TES peak sensitivity. As shown in Table 4, offsetting TES ocean targets from GLOBALVIEW by latitude, longitude, or time resulted in a significant reduction of correlation to GLOBALVIEW, validating patterns seen by TES in latitude, longitude, and time.

The mean difference between TES and GLOBALVIEW is 0.1 ppm (TES high) with the bias correction discussed in Sect. 5.5. The expected difference given in Stephens et al. (2007) for 4 km – surface values is −0.7 ppm. However, this bias fluctuates depending on which subset of data is used, so it indicates but does not conclusively show that the TES bias correction is too high. The predicted error for the TES averages (~85 targets per month per GLOBALVIEW site) is 1.9 ppm. A scatter plot of TES ver-
sus GLOBALVIEW is shown in Fig. 14, which shows definite skill for TES, especially considering the TES initial guess and a priori are both set to 380 ppm. The correlation is 0.60, and as discussed above, this correlation decreases if TES is offset from GLOBALVIEW by time, latitude, or longitude.

6.6 Comparison to CarbonTracker

TES is compared to CarbonTracker at the surface and at 500 hPa at GLOBALVIEW ocean locations. Because CarbonTracker spans the surface through 0.1 hPa, the TES observation operator can be applied to CarbonTracker for comparisons to TES. CarbonTracker is interpolated to the TES standard pressure grid (∼65 levels from the surface through 0.1 hPa), the observation operator is applied on the TES standard pressure grid using Eq. (7), and the resultant value is sampled at 511 hPa for comparison to the TES results. For comparisons at the same ocean GLOBALVIEW sites as above, the correlations are 0.62 for TES versus CarbonTracker at the surface and 0.67 for TES versus CarbonTracker w/obs at 500 hPa, indicating a better agreement between TES and CarbonTracker when CarbonTracker is sampled at the TES pressure level. CarbonTracker at 500 hPa shows about 25% less seasonal variability than TES, and CarbonTracker w/obs shows about half the variability of TES in the Northern Hemisphere, as seen in Table 6 and illustrated in Fig. 12. TES is also compared to CarbonTracker at an offset from GLOBALVIEW locations by ±15° latitude or ±30° longitude in Table 5. TES and CarbonTracker correlate ∼0.05 better at GLOBALVIEW locations compared to non-GLOBALVIEW locations. Overall TES compares better to CarbonTracker than to surface sites or AIRS.

6.7 Comparison to AIRS

We compare to AIRS-Chahine CO₂, which is gridded (2×2.5°) monthly data with peak sensitivity at 300 hPa (Olsen, 2009). As seen in Table 3, the correlation between TES and AIRS ranges between 0.16 for Southern Hemisphere ocean (which has very little
seasonal cycle) to 0.53 for Northern Hemisphere ocean, with AIRS seasonal variability less than TES, as seen in Table 6 and Fig. 12.

6.8 Spatial maps from TES, CarbonTracker, GLOBALVIEW, and AIRS

Maps of TES data between 40° S and 45° N are shown for February, April, and September, 2006 (small circles with interpolation) in Fig. 15, with locations and values for GLOBALVIEW surface measurements overplotted (larger circles). For comparison purposes, CarbonTracker (at the surface and 500 hPa) is sampled at TES observation locations and monthly averaged on the same 15° grid. The 500 hPa value shows the CarbonTracker profile mapped to the TES 5 retrieval values, and sampled at 511 hPa. Surface values from CarbonTracker are also shown, which show some correlation with the high values seen by TES over land in Africa, South America, and Asia, suggesting more vertical transport in these locations than included in CarbonTracker. AIRS on a monthly 2×2.5° grid is also shown. High CO₂ values are seen in TES, CarbonTracker, and AIRS data for April, 2007 in the Northern Hemisphere, as expected. September/October is the seasonal minimum of CO₂ in the Northern Hemisphere, and lower values are seen in all 3 datasets in the Northern Hemisphere. In general, TES shows more longitudinal variability than CarbonTracker. Correlations between TES and GLOBALVIEW suggest the longitudinal variations seen by TES are meaningful (see Table 4).

7 Investigating the potential of TES CO₂ in for inverse modeling

We conducted an OSSE to assess the potential utility of the TES data for inverse modeling of CO₂ fluxes. As discussed in Sect. 1, several studies have suggested that satellite observations of CO₂ when averaged on spatial scales of 8°×10°, for example, and on weekly or monthly timescales can provide valuable new constraints on estimates of CO₂ fluxes if the precision of the data is better than about 2.5 ppm. We examine here
the reduction in uncertainty of CO$_2$ flux estimates obtained when simulated unbiased TES data are averaged monthly on spatial scales of 10° × 10°, 15° × 15° and 20° × 30°.

7.1 Inversion configuration

7.1.1 Forward model

We use the GEOS-Chem global chemical transport model (CTM) to simulate a pseudo-atmosphere from which pseudo-observations of CO$_2$ from TES are generated. The GEOS-Chem model uses meteorological fields from the NASA Global Modeling and Assimilation Office (GMAO). We use version v8-01-01 with GEOS-4 meteorological fields at a horizontal resolution of 2° × 2.5° and with 30 vertical sigma levels. The model has multiple separate simulation modes, the most common of which is the O$_x$-NO$_x$-hydrocarbon chemistry mode (Bey et al., 2001). The CO$_2$ simulation mode contains no chemistry, but accounts for CO$_2$ emissions and uptake at the land and marine surface from both anthropogenic and natural sources. The original version of the CO$_2$ simulation is described in Suntharalingam et al. (2003, 2004) but significant improvements have been implemented in conjunction with this work, as described in Nassar et al. (2009).

7.1.2 Inversion methodology

We examine the potential of the TES data to reduce uncertainty in estimates of CO$_2$ fluxes from the 28 land and 11 ocean regions shown in Fig. 16. The ocean regions are the standard TransCom 3 ocean regions (Baker et al., 2006), whereas the land is spatially divided based on AVHRR dominant vegetation types (Hansen et al., 1998, 2000) to obtain the given regions, as described in Nassar et al. (2009). One additional tracer for the Rest of World (ROW) is used to aggregate fluxes from areas not included in any other region such as Greenland/Antarctic ice or small isolated islands.

In our inversion approach, the fluxes used to generate the pseudo-data are defined
as the “truth.” We then use the pseudo-data to sequentially update and thus optimize the flux estimates, starting from an a priori estimate of the fluxes that is different from the truth. We use the maximum a posteriori (MAP) approach described in Jones et al. (2003, 2009), in which we minimize the following cost function

$$J(u) = (\hat{x} - F(u))^T S_{\text{epsilon}} (\hat{x} - F(u)) + (u - u_a)^T S_a^{-1} (u - u_a)$$  \hspace{1cm} (9)$$

where \(\hat{x}\) is the observation vector that consists of the TES CO\(_2\) retrievals at the 511 hPa level, \(u\) is the state vector with elements representing the CO\(_2\) flux from each region, \(u_a\) is the a priori state vector, \(S_{\text{epsilon}}\) is the TES observation error covariance matrix, and \(S_a\) is the a priori covariance matrix for the fluxes. \(F(u)\) is the forward model which reflects the transport of the CO\(_2\) fluxes in the GEOS-Chem model and the TES observation operator (which accounts for the TES sensitivity and a priori profile as described in Sect. 4.3.2). Both the TES retrieval \(\hat{x}\) and the forward model simulation of the observations are expressed with respect to the natural logarithm of the CO\(_2\) volume mixing ratio (VMR). The expression for \(F(u)\) is analogous to Eq. (7)

$$F(u) = x_a + A (\ln[H(u)] - x_a)$$  \hspace{1cm} (10)$$

where \(H(u)\) is the modeled CO\(_2\) profile interpolated onto the TES retrieval grid, \(x_a\) is the TES a priori (given in terms of the logarithm of the CO\(_2\) mixing ratio), and \(A\) is the TES averaging kernel. To minimize possible representation errors in the spatio-temporal averaging of the pseudo-data and the model, the model is first sampled at the location and time (to within 1 h) of each TES global survey observation and then averaged monthly and spatially in bins of 10\(^\circ\)×10\(^\circ\), 15\(^\circ\)×15\(^\circ\), or 20\(^\circ\)×30\(^\circ\). We generate pseudo-data for 2006 and ingest the monthly mean pseudo-data over the entire year to obtain an annual mean estimate of the fluxes.

### 7.2 Inversion results

The results of the inversion analysis are given in Table 7 and Fig. 17. Shown are the ratio of the optimized flux estimates to the truth and the ratio of the a posteriori to
a priori uncertainties for the 40 flux regions and for the three different bin sizes used for averaging the TES data. The differences between the inversions with the different bin sizes are not large. All three inversions indicate that the TES data provide the most constraints on estimates of the tropical fluxes. All three datasets produced the largest error reduction on fluxes from the Southern African Grasslands and the South American Tropical Rain Forest; the ratio of the a posteriori to a priori uncertainty was 0.27 for fluxes from these two regions with the 10°×10° data.

Examination of the uncertainty reduction (the difference between unity and the ratio of the a posteriori to a priori uncertainties) across all the regions indicates that the TES data provide the largest error reduction on the fluxes when averaged on 10°×10° scales. At 10°×10°, 6 regions gave an error ratio less than 0.50, compared to 5 regions with the 20°×30° data. These regions are South American Tropical Rain Forest, Southern Africa Grasslands, South and Central Europe, Northern Africa Grasslands, East Asia Mainland, and South American Wooded Grasslands.

The trace of the inversion resolution matrix is an indication of the number of regions in the 40-element state vector which are constrained independently in the inversion. This is analogous to the DOFs for a profile retrieval. The traces obtained with the 10°×10°, 15°×15°, and 20°×30° data were 14.9, 13.9, and 13.7. We found that at 20°×30° the data provide greater error reduction on the boreal fluxes, whereas the 10°×10° data offered more constraints on the mid-latitude and tropical fluxes.

The greater uncertainty reduction obtained with the 10°×10° averaging is somewhat expected since the monthly mean observation error of the TES data increases from about 1 ppm at 20°×30° to 2 ppm at 10°×10°, whereas the amount of data ingested in the inversion analysis increases by a factor of 6 at 10°×10°. Interestingly, although the 15°×15° averaging (which has a monthly mean observation error of about 1.4 ppm) produced only a modest increase in the DOFs (13.9 compared to 13.7 at 20°×30°), it gives an a posteriori estimate of the fluxes that is closest to the truth. With the 15°×15° averaging there are 19 elements of the 40-element state vector with the smallest residual error, compared to 12 with the 10°×10° data and 9 with the 20°×30° data.
The results presented here suggest that TES CO$_2$ have the potential to provide additional information on the CO$_2$ fluxes. However, it is important to recognize that ability of the OSSE to reliably constrain the true flux estimates reflects the fact that both the model and the pseudo-data were unbiased in the OSSE. If biases in the model and the real data are not properly characterized and accounted for, the inferred flux estimates in the inversion analysis will be biased. Furthermore, although averaging the data reduces the random errors in the measurement, which improves the measurement precision, it could lead to a loss of information associated with atmospheric processes on spatial and temporal scales smaller than that on which the averaging is done. An alternative would be to exploit the individual retrievals without averaging. On the other hand, the large random error in the individual measurements could be an issue for inverse modeling. For example, Wang et al. (2009) showed that a joint inversion analysis of CO and CO$_2$, exploiting the correlations in the model errors for CO and CO$_2$ would provide more constraints on the CO$_2$ fluxes than using only CO$_2$. But a requirement of joint inversion approach, as noted by Wang et al. (2009), is that the measurement error must be smaller than the model error. A more detailed analysis is clearly needed to better assess the potential impact of the spatial and temporal averaging of the data on the inferred flux estimates.

8 Conclusions

Carbon dioxide retrievals from the TES instrument between 40° S and 45° N over 3 yr are shown in comparison to surface data, SGP and CONTRAIL aircraft data, satellite data from AIRS and to the CarbonTracker data assimilation. The peak TES sensitivity is at 511 hPa (~5 km), with about 10% of the sensitivity in the lower troposphere and about 1 degree of freedom total. We find a low bias of 2.1% in TES CO$_2$ which has been corrected using Mauna Loa data at 3.5 km altitude, however the bias correction would be more accurately quantified by comparisons to profile aircraft data at a well-mixed location with values from the surface through ~11 km to cover the range
of TES sensitivity. Maps of TES CO$_2$ show expected latitudinal gradients and seasonal features, with more longitudinal features than seen in CarbonTracker. The characterization of TES sensitivity and errors shows that monthly-averaged TES results show good agreement between the predicted and actual sensitivity and errors, with errors decreasing as predicted as more profiles are averaged. The monthly predicted error for a 15×15° average (with ~80 targets per bin) between 40° S and 45° N is 2.2 ppm.

CO$_2$ from TES, Mauna Loa, CONTRAIL, AIRS, and CarbonTracker in the northern tropical Pacific all show similar seasonal cycles. TES correlates best with the Mauna Loa data, which are collected at 3.5 km, comparable the TES peak sensitivity at 5 km. In the southern Pacific, although all datasets show a yearly increase in CO$_2$, the correlation of TES to the other datasets is much smaller. Comparisons of TES monthly averages to SGP aircraft data over the US shows a correlation of about 0.7, which is significantly less than for N.H. ocean due to a combination of more variability over land (as TES is averaged over a large area) and greater challenges for land retrievals.

At 39 GLOBALVIEW sites, TES is compared to CarbonTracker, AIRS, and GLOBALVIEW. Comparison of TES to GLOBALVIEW surface sites shows a 0.60 correlation at ocean sites and a 0.16 correlation at land sites, with low correlation over land likely related to the sharp gradients seen over land between the surface and free troposphere. Although the troposphere is not expected to completely correlate with the surface, it is significant that the correlations between TES and GLOBALVIEW decrease if the TES data are shifted in latitude, longitude, or time compared to GLOBALVIEW. TES correlates best with CarbonTracker (at 500 hPa with the TES observation operator applied), yielding a 0.67 correlation at ocean sites and 0.36 correlation at land sites. Comparing the variability of the CO$_2$ data at ocean sites shows that TES variability (2.4 ppm) is less than the surface data (3.3 ppm), but significantly more than CarbonTracker (w/obs) (1.3 ppm) or AIRS (1.5 ppm).

An OSSE using simulated TES observations based on GEOS-Chem model output shows that TES data can reduce uncertainty in regional CO$_2$ fluxes when the data are averaged monthly and on various spatial scales. TES data averaged at 10°×10°, for
example, have a total error of about 2.4 ppm and produced a large reduction (of about 70%) in uncertainty of estimates of CO$_2$ fluxes from the South American Tropical Rain Forests, Southern African Grasslands, Northern African Grasslands and Southern and Central Europe. Many of these regions are areas where GLOBALVIEW coverage is relatively sparse. Our results suggest that if biases in the TES CO$_2$ data and the model are properly characterized and accounted for, the data will provide sufficient information to reliably quantify CO$_2$ sources and sinks. Since the TES sensitivity peaks in the middle troposphere, the instrument should offer complementary information to the surface data and, therefore, integrating TES with the surface data should offer valuable new constraints for inverse modeling of carbon fluxes.

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CONTRAIL data were obtained through the World Data Centre for Greenhouse Gases (WDCGG) at http://gaw.kishou.go.jp/wd cg/products/cd-rom/dvd_01/metadata/co2/contributor/200612120102.html (contact Toshinobu Machida).

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Table 1. Spectral windows used for TES CO₂.

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<tr>
<td>1B2</td>
<td>971.660</td>
<td>987.260</td>
</tr>
<tr>
<td>1B2</td>
<td>987.740</td>
<td>990.02</td>
</tr>
<tr>
<td>1B2</td>
<td>1070.000</td>
<td>1073.720</td>
</tr>
<tr>
<td>1B2</td>
<td>1074.200</td>
<td>1074.680</td>
</tr>
<tr>
<td>1B2</td>
<td>1075.280</td>
<td>1080.980</td>
</tr>
<tr>
<td>1B2</td>
<td>1081.520</td>
<td>1085.120</td>
</tr>
<tr>
<td>1B2</td>
<td>1085.780</td>
<td>1104.620</td>
</tr>
<tr>
<td>1B2</td>
<td>1105.160</td>
<td>1117.400</td>
</tr>
</tbody>
</table>

The species included in the forward model were H₂O, CO₂, O₃, HNO₃ for the 2B1 filter and H₂O, CO₂, O₃, CFC-11, CFC-12 for the 1B2 filter.
Table 2. Degrees of freedom for CO₂ in different scenarios.

<table>
<thead>
<tr>
<th></th>
<th>CO₂ alone</th>
<th>+ $T_{ATM}$</th>
<th>+ H₂O</th>
<th>+ clouds, TSUR</th>
</tr>
</thead>
<tbody>
<tr>
<td>v2</td>
<td>1.87</td>
<td>1.00</td>
<td>0.62</td>
<td>0.61</td>
</tr>
<tr>
<td>laser</td>
<td>1.02</td>
<td>0.88</td>
<td>0.72</td>
<td>0.68</td>
</tr>
<tr>
<td>v2+laser</td>
<td>2.08</td>
<td>1.33</td>
<td>1.09</td>
<td>1.04</td>
</tr>
<tr>
<td>Sel. Windows</td>
<td>1.94</td>
<td>1.22</td>
<td>1.01</td>
<td>0.95</td>
</tr>
</tbody>
</table>

Additional retrieval species are added in each column, so the final column retrieves CO₂, atmospheric temperature, water, clouds, and surface temperature. The “v2” window is 670–775 cm⁻¹, the laser windows are 967–990 and 1070–1117, and the selected windows are shown in Table 1. Note that additional windows to improve temperature and water would increase the CO₂ DOFs in a joint retrieval with the upper limit being the “CO₂ alone” column.
Table 3. TES correlation to GLOBALVIEW, CarbonTracker, and AIRS for different subsets.

<table>
<thead>
<tr>
<th></th>
<th>Correlation GLOBALVIEW</th>
<th>Correlation CarbonTracker</th>
<th>Correlation AIRS</th>
<th>GLOBALVIEW station locations used for comparison</th>
</tr>
</thead>
<tbody>
<tr>
<td>N. Hemisphere ocean</td>
<td>0.69</td>
<td>0.69</td>
<td>0.53</td>
<td>BME BMW CHR GMI HAA IZO KEY KUM MID MLO MNM RPB RYO YON GSN AZR PTA TAP</td>
</tr>
<tr>
<td>S. Hemisphere ocean</td>
<td>0.11</td>
<td>0.57</td>
<td>0.16</td>
<td>ASC CPT EIC SEY SMO RTA ASC BKT BME BMW CHR CPT EIC GMI HAA IZO KEY KUM MID MLO MNM RPB RYO SEY SMO YON GSN AZR PTA TAP</td>
</tr>
<tr>
<td>Ocean</td>
<td>0.60</td>
<td>0.67</td>
<td>0.46</td>
<td>Ocean &gt;2 km MLO IZO</td>
</tr>
<tr>
<td>Ocean altitude &gt;2 km</td>
<td>0.83</td>
<td>0.74</td>
<td>0.56</td>
<td>MLO IZO ASK CFA MKN PTA SGP TAP TGC UTA WIS WKT WLG</td>
</tr>
<tr>
<td>Land</td>
<td>0.16</td>
<td>0.36</td>
<td>0.24</td>
<td>Land &gt;2 km ASK CFA MKN PTA SGP TAP TGC UTA WIS WKT WLG</td>
</tr>
<tr>
<td>N. Hemisphere Land</td>
<td>0.35</td>
<td>0.52</td>
<td>0.48</td>
<td>N. Hemisphere Land &gt;2 km ASK GSN PTA SGP TAP TGC UTA WIS WKT WLG</td>
</tr>
<tr>
<td>Land Altitude &gt;2 km</td>
<td>0.51</td>
<td>0.24</td>
<td>0.28</td>
<td>Land Altitude &gt;2 km ASK MKN WLG</td>
</tr>
</tbody>
</table>

Correlations of TES, GLOBALVIEW, CarbonTracker (at 500 hPa with TES observation operator applied), and AIRS (~300 hPa) at subsets of GLOBALVIEW locations. Correlations are higher for ocean versus land, for northern versus Southern Hemisphere; and for higher versus lower altitude surface stations. The highest correlation is for ocean locations with altitude >2 km. Overall, TES correlates best with CarbonTracker.
Table 4. TES correlation to GLOBALVIEW at and offset from GLOBALVIEW locations.

<table>
<thead>
<tr>
<th></th>
<th>Time (±1 month)</th>
<th>Latitude (±15°)</th>
<th>Longitude (±30°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>TES+shift</td>
<td>0.56</td>
<td>0.54</td>
<td>0.47</td>
</tr>
<tr>
<td>Aligned</td>
<td>0.60</td>
<td>0.60</td>
<td>0.60</td>
</tr>
<tr>
<td>TES−shift</td>
<td>0.44</td>
<td>0.44</td>
<td>0.52</td>
</tr>
</tbody>
</table>

This table shows correlation of TES shifted by the indicated amount versus GLOBALVIEW. This shows that TES agrees best with GLOBALVIEW when aligned to the same time, latitude, and longitude. This is for yearly de-trended data.
Table 5. TES and CarbonTracker correlations at and offset from GLOBALVIEW locations.

<table>
<thead>
<tr>
<th></th>
<th>–30 longitude</th>
<th>0</th>
<th>+30 longitude</th>
</tr>
</thead>
<tbody>
<tr>
<td>+15 latitude</td>
<td>0.57</td>
<td>0.61</td>
<td>0.58</td>
</tr>
<tr>
<td>0</td>
<td>0.67</td>
<td>0.67</td>
<td></td>
</tr>
<tr>
<td>–15 latitude</td>
<td>0.59</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Correlations of TES and CarbonTracker w/obs at 500 hPa at and offset from GLOBALVIEW locations for ocean scenes. This suggests that CarbonTracker agrees somewhat better with TES data at GLOBALVIEW locations. Both datasets de-trended by a 2 ppm/yr increase.
Table 6. Variability and mean differences of monthly average data.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>OCEAN</th>
<th>LAND</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Stdev (ppm)</td>
<td>Diff vs. TES (ppm)</td>
</tr>
<tr>
<td>GLOBALVIEW</td>
<td>3.3</td>
<td>0.1</td>
</tr>
<tr>
<td>CarbonTracker-surface</td>
<td>3.2</td>
<td>−0.8</td>
</tr>
<tr>
<td>CarbonTracker 500 hPa</td>
<td>1.5</td>
<td>0.9</td>
</tr>
<tr>
<td>CarbonTracker 500 hPa w/obs</td>
<td>1.3</td>
<td>1.0</td>
</tr>
<tr>
<td>TES (511 hPa)</td>
<td>2.4</td>
<td>−</td>
</tr>
<tr>
<td>AIRS (~300 hPa)</td>
<td>1.5</td>
<td>0.9</td>
</tr>
</tbody>
</table>

Column 1 is the variability of each dataset and column 2 is the mean of (TES minus <dataset>) for data 1/2006 through 9/2007 with all data de-trended at a constant rate of 2 ppm/yr. The first two columns are for GLOBALVIEW ocean locations and the last two are for land locations. TES has a positive bias compared to GLOBALVIEW and CarbonTracker at 500 hPa, but a negative bias compared to CarbonTracker at the surface. TES shows less variability than GLOBALVIEW and CarbonTracker at the surface, but more variability than CarbonTracker at 500 hPa, especially comparing to CarbonTracker with TES observation operator (w/obs).
Table 7. OSSE a posteriori flux estimates compared with the “true” state along with a ratio of the a posteriori error relative to the a priori error for 40 geographic regions. The shaded regions, primarily in the tropics, show regions with the most information added from TES.

<table>
<thead>
<tr>
<th>FLUX REGIONS</th>
<th>10x10 X_post/X_true</th>
<th>15x15 X_post/X_true</th>
<th>20x30 X_post/X_true</th>
<th>Predicted a posteriori error/ a priori error</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 North American Tundra</td>
<td>27.2 1.04 1.00 1.04 0.96 0.97 0.97</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2 North American Boreal Forest</td>
<td>−35.2 1.05 0.89 0.63 0.71 0.79 0.64</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3 Western US and Mexico</td>
<td>−459.3 0.58 1.08 1.15 0.70 0.74 0.75</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4 Central North America</td>
<td>−298.5 0.92 1.11 1.07 0.72 0.79 0.77</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5 North American Mixed Forest</td>
<td>−270.8 1.18 0.87 1.20 0.75 0.80 0.82</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6 Central America and Caribbean</td>
<td>164.1 0.85 1.01 1.28 0.80 0.82 0.84</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>7 South American Tropical Rain Forest</td>
<td>494.0 1.03 0.95 0.94 0.27 0.27 0.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8 South American Coast and Mountains</td>
<td>−190.5 1.03 1.15 0.94 0.96</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>9 South American Wooded Grasslands</td>
<td>−470.9 0.96 1.25 1.26 0.44 0.43 0.51</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>10 Eurasian Tundra</td>
<td>−167.6 1.17 1.04 0.96 0.94 0.95 0.94</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11 Eurasian Boreal Coniferous</td>
<td>−388.0 1.01 1.05 0.94 0.73 0.79 0.69</td>
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<td></td>
<td></td>
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<tr>
<td>12 Eurasian Boreal Deciduous</td>
<td>−215.0 0.94 0.88 1.01 0.67 0.77 0.61</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>13 South and Central Europe</td>
<td>−664.1 1.15 0.91 0.88 0.30 0.33 0.32</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>14 Central Asian Grasslands</td>
<td>−138.0 0.92 1.03 1.16 0.86 0.87 0.88</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15 Central Asian Desert</td>
<td>−39.3 0.93 1.01 1.01 0.93 0.93 0.96</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>16 East Asian Mainland</td>
<td>−87.6 1.10 1.03 1.02 0.41 0.45 0.39</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>17 Japan</td>
<td>−4.8 1.06 1.03 0.93 0.96 0.96 0.97</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>18 Northern African Desert</td>
<td>−69.4 1.08 1.02 0.97 0.89 0.90 0.91</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>19 Northern African Grasslands</td>
<td>−80.7 0.98 1.30 0.85 0.30 0.31 0.33</td>
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<td></td>
<td></td>
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<tr>
<td>20 African Tropical Forest</td>
<td>−249.9 0.87 0.94 1.08 0.63 0.64 0.71</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>21 Southern Africa Grasslands</td>
<td>−792.4 1.02 0.95 0.74 0.27 0.28 0.32</td>
<td></td>
<td></td>
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<tr>
<td>22 Southern African Desert</td>
<td>−109.6 0.97 0.99 1.07 0.97 0.97 0.98</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>23 Middle East</td>
<td>−70.6 1.16 1.01 1.08 0.94 0.95 0.96</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>24 India and Region</td>
<td>−44.6 1.18 0.70 1.03 0.54 0.57 0.58</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>25 Maritime Asia</td>
<td>−61.9 1.25 0.93 1.04 0.69 0.76 0.78</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>26 Australian Forest/Grassland</td>
<td>−112.3 0.90 1.15 1.15 0.86 0.85 0.90</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>27 Australian Desert</td>
<td>−108.8 1.13 0.86 1.17 0.92 0.93 0.94</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>28 New Zealand</td>
<td>−6.9 1.02 1.04 1.08 0.96 0.97 0.97</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>29 Arctic Ocean</td>
<td>−278.3 1.02 1.09 0.98 0.94 0.95 0.95</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>30 North Pacific</td>
<td>−504.4 1.01 1.03 0.91 0.74 0.76 0.75</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>31 Tropical West Pacific</td>
<td>50.2 0.97 0.93 1.00 0.96 0.96 0.97</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>32 Tropical East Pacific</td>
<td>427.4 1.12 1.12 1.00 0.64 0.65 0.67</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>33 South Pacific</td>
<td>−326.7 1.20 0.88 0.92 0.86 0.85 0.87</td>
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<tr>
<td>34 North Atlantic</td>
<td>−201.2 0.90 1.02 0.96 0.92 0.93 0.93</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>35 Tropical Atlantic</td>
<td>114.0 1.17 0.96 0.93 0.94 0.95 0.95</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>36 South Atlantic</td>
<td>−157.7 0.96 1.01 1.17 0.95 0.96 0.96</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>37 Tropical Indian Ocean</td>
<td>114.2 1.07 1.00 1.05 0.92 0.92 0.93</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>38 Southern Indian Ocean</td>
<td>−442.9 0.93 0.90 1.11 0.79 0.78 0.80</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>39 Southern Ocean</td>
<td>−181.6 1.05 0.90 0.86 0.89 0.89 0.91</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>40 Rest of the World (ROW)</td>
<td>−40.1 1.08 1.09 1.12 0.92 0.94 0.95</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Fig. 1. CONTRAIL aircraft data for the Northern Hemisphere (15–30° N) and Southern Hemisphere (15–30° S). The CONTRAIL data show that the seasonal cycle in the Northern Hemisphere is much stronger, although both hemispheres show a similar yearly increases.
Fig. 2. Validation locations: In the Northern Hemisphere, CONTRAIL data (red dots, 13–35° N, ~140° E, 10–11 km) are compared to TES in the same vicinity (blue, 13–35° N, 128–158° E). The same TES data are compared to Mauna Loa observatory (green, 19.5° N, 155° W at 3.4 km). Over land, TES (28.8–44.8° N, 109.8–85.5° W) is compared to aircraft data at the Southern Great Plains (SGP) ARM site in the United States (orange, 36.8° N, –97.5° W, 0.5–5.3 km). In the Southern Hemisphere CONTRAIL data (red dots, 10–30° S, ~150° E, 10–11 km) are compared to TES data from the box (10–30° S, 128–168° E). These are also compared to the Samoa surface site (purple circle, 14° S, 170° W). TES data between 40° S and 45° N are also compared to the GLOBALVIEW dataset (purple +’s).
**Fig. 3.** Radiance change resulting from changes of +10% to water (blue), −1 K to atmospheric temperature (green) and 10 ppm to CO$_2$ (red). The changes are applied to the boundary layer (0–2 km) (top) and to the free troposphere (4–8 km) (bottom). The changes to water and temperature are of the same order as the predicted errors.
Fig. 4. Radiances and Jacobians for the 3 CO$_2$ bands used. The Jacobians show the sensitivity of radiances to changes in CO$_2$ at different altitudes. The red arrow shows the sensitivity of the radiance at 710 cm$^{-1}$ when CO$_2$ at 10 km is changed. The Jacobians have been divided by the radiance noise, so a value of 1 means that the radiance will change by the same amount as the expected radiance noise.
Fig. 5. Averaging kernel rows for an average of ocean (left) and land (right) targets over a multi-year period. The ocean targets, on average, show more sensitivity because the ocean temperature is higher on average.
Fig. 6. Errors for a single target (left) and a 100-target average (right). For the single target, the dominant error is the cross-state error, which results from the propagation of errors from temperature, water, surface temperature, and clouds into CO₂. For the 100-target average, all errors except for self-smoothing, which results from sub-optimal sensitivity, are assumed to add randomly. Self-smoothing is the dominant error for the 100-target average.
Fig. 7. Sensitivity vs. latitude for October, 2006. Since the sensitivity drops off with latitude, only 40° S to 45° N is used for CO₂ retrievals.
Fig. 8. Actual and predicted errors for total error (top panel) and observation error (bottom panel). The actual error is the root mean square difference between TES and in situ data. As predicted, comparisons to in situ data improve as the number of profiles averaged increases. The actual error fits best to an observation error of 12 ppm (about twice the predicted observation error) and a self-smoothing error of 1.1 ppm (as predicted). This fit is shown as a red dashed line in both panels.
Fig. 9. TES results with a 360 ppm initial guess and prior (dashed line). The TES results (red) agree well with Mauna Loa with the TES observation operator (orange), which accounts for TES sensitivity. This validates the TES reported sensitivity, which is captured in the averaging kernel.
Fig. 10. TES (≈5 km, red) is shown compared to the Mauna Loa surface site (3.5 km, purple), CarbonTracker (5 km), AIRS data (≈9 km, blue), and CONTRAIL aircraft data (10–11 km, green) in the Northern Hemisphere (13–35° N). The top panel shows a time series of the different datasets, where the TES initial and a priori values are set to 380 ppm (dashed line). The orange data show the observation operator applied to Mauna Loa, which agrees best with TES data as the TES averaging kernel row sums to about 0.8. The middle panel shows TES – Mauna Loa with TES observation operator, which does not show a trend. The bottom panel shows TES (x-axis) plotted versus the above data.
Fig. 11. TES (~5 km, red) is shown compared to the Samoa surface site (purple), Carbon-Tracker (5 km), AIRS data (~9 km, blue), and CONTRAIL aircraft data (10–11 km, green) in the Southern Hemisphere (10–30° S). The top panel shows a time series of the different datasets, where the TES initial and a priori values are set to 380 ppm (dashed line). The middle panel shows TES – Samoa with TES observation operator. The bottom panel shows TES (x-axis) plotted versus the above data.
Fig. 12. Averages by month for July, 2005 to July, 2008 showing the amplitude and phase of the seasonal cycle in the Northern Hemisphere (top panel) and Southern Hemisphere (bottom panel). The agreement is generally within 2 ppm for all datasets, with Mauna Loa showing the most seasonal variability. TES agrees best with Mauna Loa with the TES observation operator applied, which accounts for TES sensitivity.
**Figure 13.** Monthly averaged TES (~5 km, red) is shown compared to the SGP aircraft data (x’s, monthly average green, 2–7 km) and Carbontracker (grey and black). SGP with the observation operator is influenced by the surface data and affected by seasonal variations in sensitivity. TES compared with SGP with the TES observation operator applied shows a high bias.
Fig. 14. TES plotted versus GLOBALVIEW for TES values within 550 km of GLOBALVIEW sites. The agreement is significant given that TES starts with a uniform 380 ppm prior and initial guess.
Fig. 15. TES (top), CarbonTracker at the surface and 500 hPa with the TES observation operator (middle rows), and AIRS (bottom) for February, April, and September, 2007. The small circles show the values for 15° × 15° × 1 month averages of TES and CarbonTracker sampled at TES observation locations. The AIRS data are shown as 2° × 2.5° monthly averages. The large circles show GLOBALVIEW surface values. Some enhancements over land seen in TES are also seen in CarbonTracker data near the surface. In general TES exhibits more variability than CarbonTracker at 500 hPa. AIRS, TES, and CarbonTracker all show high values in the Northern Hemisphere in April, as expected, and the reverse in September. All color scales are the same.
Fig. 16. The 40 regions used in our inversions are defined as the standard 11 TransCom 3 ocean regions, 28 land regions based on AVHRR definitions of dominant vegetative types, and the Rest of the World (ROW) consisting of mostly Antarctic/Greenland ice and some small isolated islands. Coastal grid boxes can belong to both land and ocean regions.
**Fig. 17.** OSSE uncertainty ratios for the land, ocean and ROW regions at 3 different resolutions (10° × 10°, 15° × 15° and 20° × 30°). Lower ratios indicate a larger error reduction.