The impact of parameterising light penetration into snow on the photochemical production of NO\textsubscript{x} and OH radicals in snow

H. G. Chan\textsuperscript{1,2}, M. D. King\textsuperscript{2}, and M. M. Frey\textsuperscript{1}

\textsuperscript{1}British Antarctic Survey, Natural Environment Research Council, Cambridge, CB3 0ET, UK
\textsuperscript{2}Department of Earth Sciences, Royal Holloway University of London, Egham, Surrey, TW20 0EX, UK

Correspondence to: H. G. Chan (hohan47@bas.ac.uk)
Abstract

Snow photochemical processes drive production of chemical trace gases in snowpacks, including nitrogen oxides (NO and NO$_2$ = NO + NO$_2$), and hydrogen oxide radical (HO$_x$ radicals in snowpacks = OH + HO$_2$), which are then released to the lower atmosphere. Coupled atmosphere–snow modelling of these processes on global scales requires simple parameterisations of actinic flux in snow to reduce computational cost. The disagreement between a physical radiative transfer (RT) method and a method parameterisation based upon the $e$-folding depth of light in actinic flux in snow is evaluated. In particular for the photolysis of the nitrate anion (NO$_3^-$), the nitrite anion (NO$_2^-$) and hydrogen peroxide (H$_2$O$_2$) within snow and photolysis of gas-phase in snow and nitrogen dioxide (NO$_2$) within the snowpack interstitial air are considered.

The emission flux from the snowpack is estimated as the product of the depth-integrated photolysis rate coefficient, $v$, and the concentration of photolysis precursors in the snow. The depth-integrated photolysis rate coefficient, $v$ is calculated (a) explicitly with a physical radiative transfer an RT model (TUV), $v_{TUV}$ and (b) with a simple parameterisation based on $e$-folding depth, $v_{ze}$. The metric for the evaluation is based upon the deviation of the ratio of depth-integrated photolysis rate coefficient determined by the two methods, $\frac{v_{TUV}}{v_{ze}}$, from unity. The disagreement in depth-integrated photolysis rate between the RT model and $e$-folding depth parameterisation ratio depends primarily on the position of the peak in the photolysis action spectrum of chemical species, solar zenith angle and optical physical properties of the snowpack, (i.e. strong dependence on the light scattering cross-section and a weak dependence on the mass-ratio of light absorbing impurity (black carbon) and density). For i.e. black carbon and HULIS) with a weak dependence on density. For the photolysis of NO$_2$, the NO$_2^-$ anion, the NO$_3^-$ anion and H$_2$O$_2$ the ratio $\frac{v_{TUV}}{v_{ze}}$ varies within the range of 0.82–1.35, 0.88–1.28 and 0.92, 0.93–1.27 and 0.91–1.28 respectively. The $e$-folding depth parameterisation underestimates for small solar zenith angles and overestimates at solar zenith angles around 60° compared to the RT method. A simple algorithm has been developed to improve the parameterisation which reduces the ratio $\frac{v_{TUV}}{v_{ze}}$ to 0.97–1.02,
0.99–1.02 and 0.99–1.03 and 0.98–1.06 for photolysis of NO₂, the NO₂⁻ anion, the NO₃⁻ anion and H₂O₂ respectively. The e-folding depth parameterisation may give acceptable results for the photolysis of the NO₃⁻ anion and H₂O₂ in cold polar snow with large solar zenith angles, but can be improved by a correction based on solar zenith angle and for cloudy skies.

1 Introduction

Field and laboratory experiments over the past two decades have provided evidence that photochemical reactions occurring within snow lead to the emission of various gaseous compounds from the snowpack (e.g. Jacobi et al., 2004; Jones et al., 2000; Beine et al., 2002, 2006; Dibb et al., 2002; Simpson et al., 2002) and production of radicals, e.g. OH) hydroxyl radical (OH), within the snowpack (e.g. Mauldin et al., 2001; Chen et al., 2004; Sjostedt et al., 2005; France et al., 2011). The porous structure of snowpacks allows the exchange of gases and particles with the atmosphere and the incorporation of gas and particles from atmosphere on and in the snow surface. The exchange between snowpack and overlying atmosphere depends on dry and wet deposition, transport (including wind-pumping and diffusion) and snow microphysics (e.g. Bartels-Rausch et al., 2014). Thus snow can act as both a source and a sink of atmospheric chemicals (Fuhrer et al., 1996; Sumner et al., 2002; Honrath et al., 1999) chemical species as summarised in Bartels-Rausch et al., 2014 and Grannas et al., 2007. Photochemistry in the snowpack needs to be fully understood because: (1) emitted photolysis products play an important role in determining the oxidizing capacity of the lower atmosphere, e.g. concentration of O₃, HOₓ, H₂O₂, and (2) chemicals to be chemical preserved in ice cores, and used as paleoclimate indicators or paleo-climate proxies, may be altered through reactions with OH radicals or photolysed by solar radiation. Thus not a proxy for past climate without correction (Hutterli et al., 2003) photolysis or physical uptake and release (Wolff and Bales, 1996).
The photolysis lifetime of a chemical species in the snowpack is the reciprocal of the photolysis rate coefficient (also known as photodissociation rate coefficient), $J$, which is dependent on the intensity of the actinic flux (also known as spherical or point irradiance; hereafter known as the actinic flux) in the snowpack, $I$, the quantum yield of the photolysis reaction, $\Phi$, and absorption cross-section of the photolysing species, $\sigma$.

$$J(\theta, z, T) = \int \sigma(\lambda, T) \Phi(\lambda, T) I(\theta, z, \lambda) \, d\lambda$$

(1)

where $\theta$ is solar zenith angle, $z$ is the depth into the snowpack, $\lambda$ is the wavelength of the incident solar radiation, and $T$ is the temperature of the snowpack.

Under clear sky conditions, a homogeneous snowpack can be separated into two optical layers based on the propagation of actinic flux from the atmosphere to deep within the snow: the near-surface layer is, i.e. the top few centimetres of the snowpack, where direct solar radiation is converted into diffuse radiation. Below the near-surface layer the solar radiation within the snowpack is all in the asymptotic zone where all solar radiation is diffuse and will decrease exponentially with depth (Warren, 1982).

The relationship between actinic flux (and the photolysis rate coefficient) and depth in the snowpack is complex near the surface of the snowpack due to rapidly changing contributions from both direct and diffuse radiation. Enhancement or attenuation of actinic flux in the near-surface layer compared to above the snow is dependent on the solar zenith angle, as shown in (Fig. 1 and by others (Fig. 4 in Lee-Taylor and Madronich, 2002). Snowpack is a very scattering and low absorption environment for UV-visible photons with individual snow grains tending to forward scatter photons. The direct radiation of an overhead sun will be diffused in the top few cm in the snowpack leading to an enhancement in the actinic flux as shown in Fig. 1 (Warren, 1982). The enhancement in actinic flux compared to above the snow occurs for solar zenith angles $< 50^\circ$. For solar zenith angles $\sim 50^\circ$ actinic flux will decrease almost exponentially with depth (Wiscombe and Warren, 1980). For direct radiation from a low sun (large solar zenith angle, i.e. $> 50^\circ$) there is a larger probability that the photons will be scattered upwards and out of the snowpack, leading to a rapid decrease in actinic flux with depth in the first few cm of the snowpack i.e. decaying faster than...
Illumination of a snowpack with an solar zenith angle \( \sim 50^\circ \) will have an almost exponential decay of actinic flux with depth (Wiscombe and Warren, 1980, Warren, 1982).

Below the near-surface layer is the “asymptotic zone”, in which the actinic flux is effectively diffuse radiation and decays exponentially according to the Beer–Lambert law (providing the snowpack is semi-infinite, i.e. the albedo of the surface underlying the snow does not affect the calculation of the actinic flux within the snowpack an the radiation decreases exponentially according to the Beer–Lambert law (providing the snowpack is semi-infinite) as 3-4 e-folding depths).

\[
I(z, \lambda) = I(z', \lambda) e^{-\frac{z-z'}{z_e(\lambda)}} e^{-\frac{z-z_0}{z_e(\lambda)}}
\]  
(2)

where \( I(z) \sim I_0 \) is the actinic flux at a depth \( z \), in the snowpack, \( I(z') \) is the actinic flux at a shallower depth, \( z' \), reference depth \( z_0 \) within the asymptotic zone, and \( z_e(\lambda) \) is the asymptotic e-folding depth, which is the depth of snow that actinic flux at which \( I \) has decayed to \( 1/e \), \( \sim 37\% \) of its incident value reference value, \( I_0 \).

Radiative-transfer (RT) models, such as the TUV-snow (Lee-Taylor and Madronich, 2002), were developed to capture the non-exponential attenuation of radiation near the surface of the snowpack. However, running a radiative-transfer model is a time consuming step within some complex models such as 3-D chemical transport model large scale (e.g. 3D) chemical transport models or global climate model models so photolysis rate coefficients in the snowpack, \( J \), are often parameterised with e-folding depth (e.g. Thomas et al., 2011), i.e.

\[
J_{z_e}(\theta, z) = J_0(\theta, z_0) e^{-\frac{z-z_0}{z_e(\lambda)}}
\]  
(3)

where \( J_{z_e}(\theta, z) \) is the parameterised photolysis rate coefficient at depth \( z \), \( J(\theta, z_0) \sim J_0 \) is the photolysis rate coefficient at the surface of the snowpack at solar zenith angle, \( \theta \), and \( z_e \) is the e-folding depth of the snowpack. The aim of this paper is to investigate the accuracy of the e-folding depth parameterisation (Eq. 3) relative to a value of \( J \) calculated using
a precise physically explicit RT model and Eq. (1). The metric to compare the two models is the depth-integrated photolysis rate coefficient (also known as the transfer-velocity, France et al., 2007), which may be considered approximately proportional to the flux of potential gaseous photo-produced compounds from the snowpack. The transfer velocity depth-integrated photolysis rate coefficient, \( v \), is calculated (Simpson et al., 2002) by as

\[
v(\theta) = \int J(\theta, z) \, dz
\]

(4)

The depth-integrated production rates of a chemical species \( B \) from the photolysis of a chemical species \( A \), \( F_B(\theta) \), is the product of concentration of \( A \), \([A]\), and the transfer velocity of \( B \), \( v_B \), depth-integrated photolysis rate coefficient, \( v_A \), assuming the concentration of \( A \) is constant with depth.

\[
F_B(\theta) = [A] \, v_{BA}(\theta)
\]

(5)

The photolysis of chemicals within snow is important. Photolytic destruction of the nitrate anions (For example, the photolysis of the nitrate anion, \( \text{NO}_3^- \)) within the snowpack, one of the most studied snow photolysis reactions, is important and has therefore been studied extensively in the past. It leads to emission of nitrogen oxides (\( \text{NO}_x = \text{NO} + \text{NO}_2 \)) to the atmosphere. The ratio of the atmospheric \([\text{NO}_2] : [\text{NO}]\) has an indirect impact on the regional energy balance and climate via altering the steady-state mixing ratio of ozone in the troposphere. The following reactions summarise the main channels of \( \text{NO}_x \) production from \( \text{NO}_3^- \) photolysis in snowpack. The quantum yield and absorption cross-section of all the chemical species used in this study are listed in Table 1.

\[
\text{NO}_3^- + h\nu \rightarrow \text{NO}_2 + \text{O}^- , \lambda_{act\,peak} = 321 \, \text{nm} \tag{R1}
\]

\[
\text{NO}_3^- + h\nu \rightarrow \text{NO}_2^- + \text{O}(^3\text{P}) , \lambda_{act\,peak} = 321 \, \text{nm} \tag{R2}
\]

\[
\text{NO}_2^- + h\nu \rightarrow \text{NO} + \text{O}^- , \lambda_{act\,peak} = 345 \, \text{nm} \tag{R3}
\]
where $hν$ represents a photon. Snowpack is a porous medium in which gas-phase reactions can occur within the interstitial air. Gaseous nitrogen dioxide ($\text{NO}_2$) has a large quantum yield and its absorption action spectrum peak is in the visible wavelengths. Visible UV-A wavelengths, around 375 nm. Long wavelength UV light penetrates deeper into the snowpack than UV, therefore, shorter wavelength UV. Therefore, $\text{NO}_2$ is photo-labile within photolyses within the snowpack and may produce ozone (Reactions [R4] and [R5]).

$$\text{NO}_2 + hν \rightarrow \text{NO} + O(3P), \lambda_{\text{act peak}} = 375 \text{ nm}$$ (R4)

$$O(3P) + O_2 + M \rightarrow O_3 + M$$ (R5)

Studies have also demonstrated that photolysis of the nitrate anion ($\text{NO}_3^-$) and the nitrite anion ($\text{NO}_2^-$) in snow and ice contribute to the formation of OH radicals within the snowpack (Dubowski et al., 2001, 2002; Cotter et al., 2003; Chu and Anastasio, 2003; Jacobi and Hilker, 2007; Anastasio and Chu, 2008) through reaction of oxygen radical anion ($O^-$) with water (Reaction [R6]).

$$O^- + H_2O \rightarrow OH + OH^-$$ (R6)

In the presence of oxygen, formation of the OH radical may create a radical-initiated oxidizing medium allowing oxidation of organic chemicals to emit species such as formaldehyde, acetaldehyde or organic halogen halogens to the lower atmosphere (France et al., 2010 and references McNeill et al., 2012). Another source of OH radicals in the snowpack is photolysis of hydrogen peroxide ($\text{H}_2\text{O}_2$) (Chu and Anastasio, 2005, 2007a)

$$\text{H}_2\text{O}_2 + hν \rightarrow 2\text{OH}, \lambda_{\text{act peak}} = 321 \text{ nm}$$ (R7)
The ratio of the transfer velocities, $Q = \frac{v_{TUV}}{v_{o_{2}}}$, determined from the two methods (- the RT model and $e$-folding depth parameterisation and radiative transfer calculation) of four widely studied snow photolysis reactions of the nitrate anion, the nitrite anion, nitrogen dioxide and hydrogen peroxide. Reactions (R1)–(R4) were calculated for the photolysis of $\text{NO}_3^-$, $\text{NO}_2^-$, $\text{NO}_2$ and $\text{H}_2\text{O}_2$ in snow. Reactions rate coefficients for reactions R1–R4 and (R7), will be, were determined for hypothetical snowpacks with different physical and optical properties and under different environmental conditions, e.g. total column ozone.

2 Modelling procedure

Studies were performed with seven hypothetical homogeneous snowpacks that were defined by their physical and optical properties. All values of the optical and physical parameters used in this work are shown. Defined in this study were based on three different types of snow - cold polar, wind-packed and melting snow (Table 2, Marks and King, 2014). The snowpacks are assumed to be semi-infinite.

Sensitivity tests calculating $Q$ were run against the following parameters - Base Case: a typical cold polar snowpack Case 1: the density of the snowpack was varied, Case 2: the scattering cross-section was varied, Case 3: the black carbon (BC) mass ratio was varied, Case 4: the HUmid Like Substances (HULIS) mass ratio was varied, Case 5: the mass ratio with both BC and HULIS was varied, Case 6: the asymmetry factor was varied, and, Case 7: the total column ozone was varied. Values for these parameters, listed in Table 3, were chosen based on previous field measurements made in various geographic locations and conditions (Grenfell et al., 1994; Beaglehole et al., 1998; King and Simpson, 2001; Fisher et al., 2005, France). The snowpacks are assumed to be semi-infinite, i.e. the albedo of the surface underlying the snow does not affect the calculation of the actinic flux within the snowpack. The density, $\rho$, of natural snowpacks typically varies between
Grenfell et al., 1994; Beaglehole et al., 1998; King and Simpson, 2001; Fisher et al., 2005; France et al., 2010; Marks and King, 2014).

In Case 1 - snow densities were varied in the range observed typically in natural snowpack of 0.2 to 0.6 g cm\(^{-3}\) (Marks and King, 2014 and references), therefore values within this range were used to represent the natural variability in snowpack density.

In Case 2-5, the scattering cross-section and mass ratio of light absorbing impurities of the snowpack were varied. Both of which have an impact on the propagation of actinic flux within the snowpack. The reciprocal of the e-folding depth, \(z_e\), is the asymptotic flux extinction coefficient, \(\kappa_{\text{ext}}\), which is the sum of the scattering, \(r_{\text{scatt}}\), and absorption coefficients, \(\mu\) (Lee-Taylor and Madronich, 2002). The scattering and absorption coefficients refer to describe the attenuation per unit length and both are density dependent (Lee-Taylor and Madronich, 2002). For general use, the following scattering, \(\sigma_{\text{scatt}}\), and absorption, \(\sigma_{\text{abs}}\), cross-sections are introduced

\[ \sigma_{\text{ext}} = \sigma_{\text{scatt}} + \sigma_{\text{abs}} \]  \hspace{1cm} (6)

where \(\sigma_{\text{ext}} = \kappa_{\text{ext}}/\rho\) is the extinction cross-section, \(\sigma_{\text{scatt}} = r_{\text{scatt}}/\rho\), the scattering cross-section of snow, and \(\sigma_{\text{abs}} = \mu/\rho\), the absorption cross-section of snow and light absorbing impurities.

\[ \sigma_{\text{abs}} = \sigma_{\text{ice abs}} + \sigma^+ \]

The values of \(\sigma_{\text{scatt}}\) were selected to cover a wide range of snow types (Table 2). The values of the scattering cross-section are assumed to be independent of wavelength (Lee-Taylor and Madronich, 2002).

The absorption cross-section of snowpack is due to wavelength dependent absorption by ice, \(\sigma_{\text{ice abs}}\), and light absorbing impurities, \(\sigma^+\). Warren et al. (2006) identified, such as black carbon and HULIS.

\[ \sigma_{\text{abs}} = \sigma_{\text{ice abs}} + \sigma^+ \] \hspace{1cm} (7)
Warren et al. (2006) showed that black carbon (BC) can dominate the absorption in snow as it is a factor of $\sim 50$ times more efficient at light absorption than mineral dust particles of the same mass, so in this study. Thus in sensitivity test - Case 3, black carbon is considered to be the only light-absorbing impurity considered in the work presented here. For the work presented here the light absorption cross-section of black carbon, $\sigma_{\text{BC}}^+$, is assumed to be wavelength independent and equal to $\sim 10 \text{ m}^2\text{g}^{-1}$ (France et al. 2010; Lee-Taylor and Madronich 2002). To account for all pollution scenarios, from clean to dirty, the mass-ratio of black carbon is varied from 4 to 128 ng g$^{-1}$, these are the mass-ratios likely to be found in coastal Antarctica snow to cover the concentration range typically measured in coastal (Beaglehole et al. 1998) or snow near polar station (?) and heavily polluted snow respectively. The values were chosen to cover a wide range of snow types, such as cold polar, which has a relatively large values of $\sigma_{\text{scatt}}$, windpacked snow, which has a mid-range value of $\sigma_{\text{scatt}}$, and melting or wet snow would have a relatively small value of $\sigma_{\text{scatt}}$. The scattering, Antarctica near research stations (Zatko et al. 2013) or in mid-latitude snow. Other common pollutants found in snow samples include HULIS, which represent an important fraction of biomass-buring, biogenic and marine aerosol etc. (e.g. Voisin et al. 2012). HULIS absorb most effectively in the UV region of the solar spectrum and the absorption cross-section values are assumed to be independent of wavelength (Lee-Taylor and Madronich 2002).

The effect of ozone column on the transfer velocity ratio was also explored as Stratospheric ozone is responsible for filtering out high frequency solar radiation such as UV-B and UV-C from reaching Earth’s surface. A typical measurement of column ozone in Antarctica (also the global average, Kroon et al. 2008) is about 300 DU (Frey et al. 2013) but can be as low as 200 DU in the Antarctic hole. The column amount of ozone generally increases from the tropics to the mid-latitude. Therefore, three different values of total ozone column, 200, 300 and 400 DU, were chosen to cover the seasonal and spatial variability decreases towards the visible (Hoffer et al. 2006). Concentrations of HULIS measured in polar snow vary between 1 to 1000 ng g$^{-1}$ and depend on the measurement method (Voisin et al. 2012, ?), which is taken into account by the range of values used in
Case 4. In natural snow, it is rare that HULIS would be the only light absorbing impurity within snow as shown in France et al. (2011) and France and King (2012) therefore, in Case 5 a combination of both black carbon and HULIS were used and varied.

The asymmetry factor, $g$, is the average cosine of the scattering angle and is a measure of the preferred scattering direction. Sensitivity tests were run with two different values of $g$ of 0.89 and 0.86 as discussed by Marks and King (2014) and Libois et al. (2014) respectively. Both selected values are close to 1, i.e. indicating light scattering by snow grains is dominated by forward scattering.

Within Case 7, column ozone values were varied to cover the seasonal and spatial variability observed above the polar regions. The effect of column ozone on the depth-integrated photolysis rate coefficient ratio was explored as downwelling UV radiation is very sensitive to stratospheric ozone absorption and the attenuation is a strong function of wavelength. Typical value of column ozone in Antarctica (also the global average, Kroon et al., 2008) is about 300 DU but can be as low as 150 DU in the Antarctic O$_3$ hole (Kramarova et al., 2014). Column ozone generally increases from the tropics to the mid-latitude. Therefore, three different values of total column ozone, 200, 300 and 400 DU.

2.1 RT method: radiative-transfer model, TUV

The attenuation of actinic flux with depth was calculated by a coupled atmosphere–snow radiative-transfer model, TUV 4.4, using an 8-stream DISORT model. The optical properties of the snow are controlled by the variables $g$, $\sigma_{\text{scatt}}$, and $\sigma_{\text{abs}}$ and 8-stream DISORT model (Lee-Taylor and Madronich, 2002). The model treats the snow as a weakly absorbing but very scattering homogenous layer with its optical properties described by the variables $g$, $\sigma_{\text{scatt}}$, and $\sigma_{\text{abs}}$. The snowpacks were modelled as described in detail in Lee-Taylor and Madronich (2002) except the optical constants of ice were absorption cross-section of ice was updated to values given by Warren and Brandt (2003). The TUV model configuration in this study used 110 snowpack layers with 1 cm spacing in the top 1 cm and 1 cm interval spacing for the rest of the 1 m snowpack and 72 atmospheric layers with 1 m spacing for the first 10 m above snowpack surface then 10 m intervals until 100 m, 100 m interval up
to 1 km, 1 km intervals up to 10 km and 2 km intervals up to 80 km, with no atmospheric loading of aerosol and clear sky assumed clear sky conditions.

Values of the Photolysis photolysis rate coefficient, $J$, for Reactions \{R1\} reactions [R1–\{R4\} and [R7]] R4 and [R7] were calculated by TUV using Eq. (1). The absorption cross-section of the chromophores in ice environment is the ice phase are assumed to be the same as the aqueous environment phase and are listed with temperature dependent quantum yields for reactions used in this study in (Table 1). Photolysis rate coefficients calculated with the TUV are referred to as the “RT method”.

2.2 $z_e$ method: $e$-folding depth

The $e$-folding depths, $z_e$, for the snowpacks described in Table 3 were calculated by fitting Eq. (2) to an actinic flux depth profile through snowpack obtained from TUV with an a vertical resolution of 1 cm from 20 cm below the snowpack surface, where. At this depth radiation is effectively all diffuse and decays exponentially with depth (asymptotic zone); to near the bottom of the 1 thick snowpack. Field measurements of $e$-folding depth are measured have been previously carried out over similar depths in the snowpack (e.g. France and King, 2012).

Values of $z_e$ were determined for three wavelengths ($\lambda = 321, 345$ and $375$ nm) and at seven different solar zenith angles (0, 36.9, 53.1, 66.4, 78.5, 80 and 90°). These wavelengths were chosen as they represent the peak of the photolysis action spectrum for each chemical species. The quantum yield and absorption cross-section of the anion and \{Anastasio and Chu, 2008\}, the anion (Chu and Anastasio, 2007a) and gas phase (Topaloglou et al., 2005) respectively, assuming that the ice environment of the anion, the anion and are similar to that of aqueous environment. (Table 1). The photolysis rate coefficients were approximated by scaling the surface photolysis rate coefficient calculated by the RT method (TUV model) with the average $e$-folding depth, $z_e$, over seven solar zenith angles at a wavelength that is near the peak of the action spectrum of the chemical species species (as shown in Eq. 3). For parameterisation of
photolysis rate coefficient of \textit{example in the case of} NO$_3^-$ photolysis:

\begin{equation}
J_{\text{ze,NO}_3^-}(\theta,z) = J_{\text{NO}_3^-}(\theta,z_0) e^{-\frac{z-z_0}{z\text{e}(\lambda=321\text{ nm})}}
\end{equation}

Where \(J_{\text{ze,NO}_3^-}(\theta,z)\) is the parameterised photolysis rate coefficient at depth \(z\), \(J_{\text{NO}_3^-}(\theta,z_0)\) is the \textit{surface}–photolysis rate coefficient of an NO$_3^-$ anion at the surface obtained by the RT method (TUV model), and \(z\text{e}(\lambda=321\text{ nm})\) is the \(e\)-folding depth, \(z\text{e}\), at a wavelength of 321 nm. For clarity, this \(e\)-folding depth parameterisation is called the “\(z\text{e}\) method”.

\subsection*{2.3 Ratio of transfer velocities by the two methods, \(Q\), depth-integrated photolysis rate coefficients}

To determinate the accuracy of the \(z\text{e}\) method relative to the RT method the ratio of transfer velocities \((v(\theta) = \int J(\theta,z) \, dz\), see Eq. 5\) were depth-integrated photolysis rate coefficients, \(Q\), was determined. The \(Q\) ratio is defined as depth-integrated photolysis rate coefficient calculated with the RT method and over the depth-integrated photolysis rate coefficients estimated by the \(z\text{e}\) method is determined. The ratio of transfer velocities for the production of NO$_2$ from photolysis (Reaction R1) is given by

\begin{equation}
Q = \frac{v_{\text{TUV,NO}_2}}{v_{\text{ze,NO}_2}} = \frac{\int J_{\text{NO}_3^- \rightarrow \text{NO}_2}(z) \, dz}{J_{\text{NO}_3^- \rightarrow \text{NO}_2}(z_0) \int e^{-\frac{z-z_0}{z\text{e}(\lambda=321\text{ nm})}} \, dz}
\end{equation}

where \(J_{\text{ze,NO}_3^- \rightarrow \text{NO}_2}(z_0)\) is the photolysis rate coefficient \textit{for NO}_3^- \textit{photolysis} at the surface of the snowpack. For Reactions (R3), (R4) and (R7), the surface photolysis rate coefficient \textit{coefficients} were scaled with \(e^{-\frac{z-z_0}{z\text{e}}}\) with \(e\)-folding depth at 345, 375 and 321 nm respectively \textit{for each depth} \(z\).
3 Results and discussion

The study evaluates the accuracy of parameterisation of transfer velocity photolysis rate coefficient to variation in solar zenith angle, different chemical-species photolysis precursors, snowpack properties and environment conditions i.e. total column ozone. Correction factors were also found for each different species to improve the performance of the $z_e$ method.

3.1 The response of $e$-folding depth to solar zenith angle and wavelength

Our results agreed with previous studies that the attenuation of radiation within snow Radiation in the asymptotic layer, i.e. below the first few centimetres, the asymptotic layer in of the snow surface (Fig. 1 has been demonstrated to decay), decreases exponentially with depth (Warren and Wiscombe 1980; Marks and King 2014; Fisher et al. 2005; King and Simpson 2001). No significant difference between $z_e(\lambda)$ calculated at seven different as observed previously at various polar and non-polar sites (Warren and Wiscombe 1980; Marks and King 2014; Fisher et al. 2005; King and Simpson 2001).

Table 3 lists the average $e$-folding depth across seven solar zenith angles (as listed in Sect. 2.2) for all snowpacks and the three chosen for all Cases. For the Base Case, Cases 1-3, 6 & 7, the $e$-folding depths listed are not only averaged across solar zenith angles but also across three wavelengths (321, 345, & 375 nm).

There are no significant differences between the calculated $e$-folding depths, across different solar zenith angles or across the three wavelengths of which the variation coefficients are between 0.002 and 2%. For snowpacks in Case 4 and 5, the $e$-folding depths were at a single wavelength (321 nm) only and the variation coefficients are ranging from 0.007-0.16 %. Figure 2 shows how $e$-folding depth varies with wavelength and the physical and optical properties of snowpack. Increasing the density, black carbon mass ratio, HULIS mass ratio or scattering cross-section of the snowpack. At all wavelengths, the $e$-folding depth decreases with increasing snow density and increasing the mass ratio of the black carbon increased the absorption of incident radiation. Increasing the
scattering Absorption of HULIS is wavelength dependent, i.e. increasing mass ratio of HULIS only increases absorption of UV and near-UV radiation. However, the absorption of the incident radiation in the visible wavelengths are independent of the mass ratio of HULIS. Increasing the scattering cross-section increased the reflectance of the snowpack. Therefore, a shorter also leads to a decrease in e-folding depth as the black carbon mass ratio or.

Scattering of photon typically occurs at the air-ice interface of a snow grain and absorption occurs within the snow grain. A denser snowpack implies more scattering or absorption events per unit length. A larger scattering cross-section increases. At all wavelengths, the will typically reduce the path length of a photon through the snowpack and reduce the possibility for absorption by ice or light absorbing impurities. Therefore, increases in density, light absorbing impurities and scattering cross-section result in a smaller e-folding depth decreases with increasing snowpack density.

3.2 Variation of $Q$, ratio of transfer–velocities depth-integrated photolysis rate coefficients

Transfer velocities Depth-integrated photolysis rate coefficients of the four chemical species (NO$_3^-$ anion, NO$_2^-$ anion, H$_2$O$_2$ and NO$_2^-$) were calculated by either the RT method or and the $z_e$ method. To evaluate the accuracy of the approximation by the $z_e$ method, the ratio $Q$, $\frac{v_{\text{UV}}}{v_{z_e}}$, using Eq. 9, is calculated and considered independently.

3.2.1 Variation with solar zenith angle

When the solar zenith angle is between 0 to 37°, using the $z_e$ method leads to a depth-integrated photolysis rate coefficient ratio, $Q$, of up to 1.35 (Fig. 3). The underestimation of the $z_e$ method at small solar zenith angles is due to the enhancement of actinic flux compared to above surface in the near-surface layer being considered in the RT method but being neglected in the $z_e$ method. For solar zenith angles between around 50° and 85 larger than 80° the value of $Q$ is close to unity, suggesting the $z_e$
method may be a good approximation for these solar zenith angles. Wiscombe and Warren (1980) suggested that direct radiation solar illumination around a solar zenith angle of 50° was effectively the same as diffuse illumination. The actinic flux—depth profile of a snowpack illuminated by diffuse actinic flux has no near-surface region and light within the snowpack decays diffuse radiation, which deceases exponentially with depth from the snow surface. At large solar zenith angles (> 80°) there is little direct solar radiation relative to diffuse radiation illuminating the snowpack and the snowpack is effectively illuminated by diffuse radiation, thus the difference between the two methods is small. Between the solar zenith angles of ∼ 66–75°, i.e. minimum values of $Q$ in Fig. 3, the direct radiation entering the snowpack may be potentially scattered out of the snowpack, resulting in an actinic flux—depth profile in snow that initially decays quicker due to the strong forward scattering property of snow. Hence, the actinic flux attenuates at a quicker rate than the e-folding depth in the near-surface zone. In Fig. 3, the purple lines (corresponding to a large solar zenith angle) show that the and the $z_e$ method overestimates relative to the RT method. At very large solar zenith angles (> 85°) there is little direct solar radiation relative to diffuse radiation illuminating the snowpack and the snowpack is effectively illuminated by diffuse radiation, thus the difference between the two methods is small over estimates the intensity of solar radiation in the snowpack.

In reality, only high-altitude glaciers in the tropics, such as those found in the Himalayas or Andes, would experience the overhead sun or small solar zenith angles in the summer. From Fig. 3, a solar zenith angle between 0 to 38° in the polar regions, where snow emission can dominate boundary layer chemistry (e.g. Davis et al., 2004), solar zenith angles vary between 42.8°, using (Antarctic/Arctic Circle) to 66.5° (at the pole) at summer solstice and close to or greater than 90° during winter solstice for Antarctic/Arctic Circle. Within this solar zenith angle range, the $z_e$ method to estimate is most likely to yield small overestimates of fluxes and photochemical production rate can result in a 10–35% underestimation. Anthropogenic pollution at medium latitudes is generally high, Yasunari et al. (2010) has estimated 26–68.2 of black carbon in the 2 surface snow layer on Himalayan glacier.
Despite direct overhead sun only available near the equator, small “effective” solar zenith angles can be achieved in mountainous sloping snow covered terrain, as shown in Fig. [4]. The “effective” solar zenith angle, $\theta_{\text{eff}}$, on a snow covered slope is the difference between the solar zenith angle normal to a horizontal surface, $\theta_{\text{dir}}$, and the angle of the slope, $\phi$. Therefore, the $z_e$ method might lead to underestimation of depth-integrated production rates on snow-covered mountains.

In the remote regions of the planet away from pollution sources, i.e. the polar regions, snow emission can dominate boundary layer chemistry ([Davis et al., 2004]). The polar regions may have a minimum solar zenith angle between 42.8 (Antarctic/Arctic Circle) to 66.5 (at the pole) at summer solstice and have zenith angles close to or greater than 90° during winter solstice for Antarctic/Arctic Circle. Within this solar zenith angle range, the $z_e$ method is most likely to yield small overestimates of fluxes, photochemical production rate.

### 3.2.2 Variation with chemical species and total column ozone

The value of the ratio $\frac{Q}{z_e}$ for the photolysis of the NO$_3^-$ anion and H$_2$O$_2$ are very similar in terms of their response to changing solar zenith angle. The magnitude of the disagreement between the two methods, is up to 27% underestimation (Fig. 3a & b). The maximum and minimum values of $Q$ is $\sim$1.27 (underestimation of solar radiation by $z_e$ method), at direct overhead sun and overestimated by 8% at large zenith angles, and $\sim$0.92 (overestimation of solar radiation by $z_e$ method), at solar zenith angles between $\sim$66-70°. The disagreement between the two methods for the photolysis of the NO$_2^-$ anion is slightly larger, the ratio $Q$ ranging between 0.88–1.28 (Fig. 3c). The approximation with $z_e$ method is the most inaccurate for the photolysis of NO$_2$ within snowpack interstitial air, up to 35% underestimation and 18% overestimation, as shown in having $Q$ values range between 0.82 and 1.35 (Fig. 3d).

The solar spectrum is strongly modulated by atmospheric absorption and scattering. The NO$_3^-$ anion and H$_2$O$_2$ have the peak of their action spectrum in the UV-B while the NO$_2^-$ anion and NO$_2$ have a peak in near-UV and visible wavelengths respectively. Solar radiation in the UV region is less intense and more diffuse relative to the UV-A and visible radiation.
at the snow surface as 1) the ozone layer absorbs strongly in the UV-B & C while relatively weakly in the near-UV and almost negligible UV-A and almost negligibly in the visible region. and 2) the Rayleigh scattering of photons by air molecules increases as the wavelength decreases. Therefore, solar radiation in the near-UV region, reaches the surface, less intense and more diffuse relative to visible radiation. The larger deviations in $Q$ between the two methods for the anion and is due to their wider action spectrum and peak in near-UV and visible wavelengths while the anion and have the peak of the action spectrum in the UV-B, which is more diffuse and hence the attenuation of the radiation. The actinic flux attenuation profile with depth, in snow, of more diffused actinic flux can be better approximated by the $e$-folding depth.

Three different values of total ozone column, 200, 300 and 400 DU were used to represent seasonal and latitudinal variation. The anion and, therefore, the $z_e$ method provides a better estimation of photolysis rate coefficient profile for NO$_3^-$ and H$_2$O$_2$, the chemical species have peak in UV-B, their compared to NO$_2^-$ and NO$_2$. The wavelength of the peak in the action spectrum of a chemical species also has an impact on its response to changes in column ozone concentration (Case 7) in terms of photolysis rate coefficient. The surface photolysis rate coefficients for NO$_3^-$ and H$_2$O$_2$ are more sensitive to the change in ozone column changes in column ozone, due to their action spectrum peak in the UV-B region, compared to species that have their peak in near-UV and visible wavelengths UV-A, such as the NO$_2^-$ anion and NO$_2$. The surface values of $J_{NO3^-}$ (Fig. 5a) and $J_{H2O2}$ have increased by $\sim 20\%$ when total ozone column decreased from 300 to 200 DU while surface values of $J_{NO2^-}$ and $J_{NO2}$ only raised (Fig. 5b) only increased by approximately 6 and 0.9\% respectively. When total ozone column increased from 300 to 400 DU, surface values of $J_{NO3^-}$ and $J_{H2O2}$ dropped approximately by $\sim 14\%$ whereas surface values of $J_{NO2^-}$ and $J_{NO2}$ only decreased by $\sim 5\%$ and 0.6\% respectively.

Despite the value of the photolysis rate coefficient varying with values of different column ozone, especially for the NO$_3^-$ anion and H$_2$O$_2$, the propagation of radiation throughout the snowpack was not affected by the column ozone, i.e. the value of $Q$ was un-changed by changing the ozone column and the $z_e$ method is not sensitive to ozone column values.
3.2.3 Variation with snow physical and optical properties

Density (Case 1), scattering cross-section (Case 2), light absorbing impurities (Case 3-5) and asymmetry factor (Case 6) were considered as the four varying physical properties of the snowpack in this study. Figure 3 highlights three results: The $z_e$ method underestimates the photolysis at small and large solar zenith angles for clean snowpacks with low scattering cross-section. Secondly, the snowpack in terms of various physical properties of the snowpacks: First, snow density has a small effect on the ability of the $z_e$ method to reproduce the results of RT method. Thirdly, how the value significantly for relatively clean snowpacks and snowpacks with low scattering cross-section at small and large solar zenith angles. Thirdly, changes of $Q$ changes with increasing mass ratio of light absorbing impurities depends on chemical depend on the chemical species being photolysed.

All three of these effects depend on either the ratio of direct to diffuse radiation in the top of the snowpack or the conversion of direct solar radiation to diffuse solar radiation in the few cm near-surface layer of the snowpack. Clean snowpacks with low values of the scattering cross-section tend to have a maxima in

With regard to the density of the snowpack, the photolysis rate coefficient maxima are at a deeper depth for snowpacks with lower density. That is the path length of the photon is longer for a less dense snowpacks. However, for the range of density values found in natural snow (Case 1, $\rho = 0.2-0.6 \text{ g cm}^{-3}$) the difference in the photolysis rate coefficient depth profile as shown in Fig. 3. The $Q$ ratio is very small, on the order of $\sim 3.5\%$ (red symbols and lines in Fig. 3).

Scattering cross-section of the snowpack: Lower values of the scattering cross-section implies longer path length of the photon is longer between individual scattering events in a clean snowpack with a small. Hence, the maximum photolysis rate coefficient tend to occur deeper into the snowpacks, as shown in blue in Fig. 6 (Scatt2, i.e. melting snow), compared with snowpacks that have a larger scattering cross-section - (magenta in Fig. 6, BaseC, i.e. cold polar snow). Thus for snowpacks with a small scattering cross-section the
agreement between the RT and $z_e$ methods is likely to be poor as the $z_e$ method will not
capture the behaviour in the near-surface layer accurately. A similar argument can be used
for the lowering of the density of the snowpack.

The light absorbing impurities in the snowpack: The propagation of actinic flux and the
vertical variation of photolysis rate coefficient within snowpack is dominated by scattering
when light absorbing impurity contents are low and therefore the absorption properties of
the impurity become unimportant, i.e. there is no difference between the value of $Q$ for
snowpack BC0.18 and HULIS1 listed in Table 3. In Case 3, absorption due to black carbon,
the variation of $Q$ with the mass ratio of light absorbing impurity is similar solar zenith
angle is approximately the same for the photolysis of the $\text{NO}_3^-$ anion and ($\lambda \sim 321 \text{ nm}$),
$\text{H}_2\text{O}_2$ but is different for the ($\lambda \sim 321 \text{ nm}$), $\text{NO}_2^-$ ($\lambda \sim 345 \text{ nm}$) and $\text{NO}_2$($\lambda \sim 375 \text{ nm}$). Except
for heavily polluted snow, e.g. snowpack BC128 ($\rho = 0.4 \text{ g cm}^{-3}$, $[\text{BC}] = 128 \text{ ng (C) g}^{-1}$
and $\sigma_{\text{scatt}} = 25 \text{ m}^2 \text{ kg}^{-1}$), that the ratio $Q$ for photolysis of the $\text{NO}_2^-$ anion and $\text{NO}_2$ is
deviated from snowpacks with lower black carbon mass ratio slightly ($\sim 3\%$ and $\sim 3.5\%$
respectively). In Fig. 6, black lines representing the extreme polluted case - BC128, the
photolysis rate coefficient calculated by the two methods matches at around 2 cm depth for
the $\text{NO}_3^-$ anion, but $\sim 4$ and $\sim 5$ cm for the $\text{NO}_2^-$ and $\text{NO}_2$ respectively. The latter two com-
ounds have the peak of their action spectrum at larger wavelengths relative to the $\text{NO}_3^-$
anion and $\text{H}_2\text{O}_2$ as discussed in Section 3.2.2. The direct to diffuse ratio of the incident solar
radiation in the snowpack increases with wavelength around 300–400 nm and will increase
the difference between the photolysis rate coefficient-depth profile calculated by the $z_e$ and
RT methods especially in the top few cm of the snowpack. Thus photolysis of compound
with a peak in their action spectrum at larger wavelengths will be poor reproduced by-

In Case 4, the absorption due to HULIS is considerable. A mass-ratio of 100 ng g$^{-1}$ of
HULIS in the snowpack will reduce the photolysis of $\text{NO}_3^-$ anion and $\text{H}_2\text{O}_2$ much more
than the photolysis of $\text{NO}_2^-$ and $\text{NO}_2$ as HULIS absorption cross-section increases with
decreasing wavelengths. The absorption cross-section due to 1, 8, 17 & 1000 ng g$^{-1}$ of
HULIS are equivalent to 0.18, 1.4, 3.0 & 177 ng(C) g$^{-1}$ of black carbon at 321 nm, but
only equivalent to 0.11, 0.87, 1.85 & 109 ng(C) g$^{-1}$ of black carbon at 345 nm and 0.06,
0.50, 1.05 & 62.0 ng(C) g$^{-1}$ of black carbon at 375 nm. If the light absorption by impurities in a snowpack is dominated by black carbon then the value of e-folding depth in the $z_e$ method relative to the RT method UV-B & A will be similar. However, if the light absorption in the snow is dominated by HULIS (or even dust) then strictly a different e-folding depth is needed for each wavelength that is characteristic of the photolysis of the species of interest.

3.2.4 Variation with asymmetry factor

Asymmetry factor of the snowpack: Libois et al. (2014) recently suggested that the value of the asymmetry parameter, $g$, be changed from $g = 0.89$ to should be $g = 0.86$ due to non-spherical grains observed in the laboratory and in the field in Antarctica and French Alps. The e-folding depth is sensitive to the value of the asymmetry factor as shown by Libois et al. (2013). Reducing the asymmetry factor from 0.89 to 0.86, reduces the tendency of photon being forward scattered and hence the e-folding depth is reduced by $\sim 11\%$. The reduction in photolysis rate coefficient is also $\sim 11\%$. Nevertheless, there are no significant relative differences between the RT and $z_e$ methods for changing $g$. The parameterisation with e-folding depth generated a similar approximation of photolysis rate coefficient for either of the two $g$ values. The other properties of the snowpacks were unchanged.

3.3 Parameterisation correction

The difference in the transfer velocity depth-integrated photolysis rate coefficient, $v$, between the $z_e$ method and RT method can be minimised by applying a correction factor, $EC(\theta)$, as a function of the solar zenith angle. The correction factor, $C(\theta)$, was computed by fitting an a quadratic equation to the plot of transfer velocity ratio depth-integrated photolysis rate coefficient ratio, $Q$ (Eq. 9), of each reaction as a function of solar zenith angle. The fitting is categorised into two types of snow – (1) windpack and cold polar snow (2) melting and clean snow. Formulation of the correction factor, $C$, is shown in Eq. (10) and the coefficients $(a, b, c)$ of the quadratic equation are listed in Tables 4 and 5 for windpack and melting “windpack and cold polar” and “melting and clean” snow respectively. The transfer velocity
depth-integrated photolysis rate coefficient approximated by the \( z_e \) method at a particular solar zenith angle can then be corrected by multiplying by the correction factor, \( C(\theta) \) at that particular solar zenith angle as shown in Eq. (11).

\[
C(\theta) = a \cos^2(\theta) + b \cos(\theta) + c
\]

\[
v_{ze}^{Corr}(\theta) = C(\theta)v_{ze}(\theta)
\]

where \( C(\theta) \) is the correction factor at a particular solar zenith angle, \( a, b, c \) are the coefficients of the quadric equation, \( v_{ze} \) is the transfer velocities depth-integrated photolysis rate coefficients approximated by \( z_e \) method and \( v_{ze}^{Corr} \) is the corrected transfer velocity depth-integrated photolysis rate coefficient \( v_{ze} \).

Snowpacks with a large \( e \)-folding depth, i.e. \( > 30 \) cm, e.g. either have small scattering cross-section or contain small amount of light absorbing impurities, are suggested to apply correction factors for “melting and clean snow” when solar zenith angles are smaller than 50° and larger than 80° to reduce the error by 10–30%. For snowpacks that have an \( e \)-folding depth smaller than \( \sim 30 \) cm should apply correction factors for “windpack and cold polar snow” when solar zenith angles are smaller than 30° or between 60–70°, which could reduce the error by up to 15%.

The correction was evaluated by comparing transfer velocities the depth-integrated photolysis rate coefficients computed by the RT method, \( v_{TUV} \), to transfer velocity approximated by depth-integrated photolysis rate coefficient approximated by the \( z_e \) method, \( v_{ze} \), and the corrected transfer velocity depth-integrated photolysis rate coefficient by \( z_e \) method, \( v_{ze}^{Corr} \), for all four species at twenty different solar zenith angles of snowpack Standard (\( \rho = 0.4 \), \( BC = 4 \) and \( \sigma_{scatt} = 25 \)) using general snowpack correction factor and snowpack BaseC (Table 3) using “windpack and cold polar” snowpack correction factors and results are shown in Fig 7. For evaluating the “melting and clean” snowpack correction factors, snowpack Scatt2 (\( \rho = 0.4 \), \( BC = 4 \) and \( \sigma_{scatt} = 2 \)) using melting snowpack correction factor. Table 3 was used and results are shown in Fig. 8. The corrections factors for the \( \text{NO}_3^- \) photolysis rate coefficient were also tested against snowpacks HULIS1, HULIS8 and Comb (Table 3) too.
The correlation between $v_{ze}$ and $v_{ze}^{\text{Corr}}$ with $v_{TUV}$ is described by square of correlation coefficients, $R^2$, and is listed in Table 4 and 5 for Standard and Scatt2 snowpack “windpack and cold polar” and “melting and clean” snowpacks correction factors respectively. The approximation of transfer velocity depth-integrated photolysis rate coefficient has improved significantly with the correction factor, especially for the melting snowpack, 1) the melting and clean snowpack, 2) photolysis of the NO$^-$ anion and 3) NO$_2$ and at small solar zenith angles, as shown in Figs. 7 and 8.

There are many factors that might have an impact on the disagreement between the two methods not taken into account in this study. Unrealistic atmospheric conditions, such as clear sky were assumed. Cloudy skies are not taken into account. However, cloud converts direct radiation into diffuse radiation. Under a very thick cloudy sky all radiation reaching the ground will be diffused and the decay of actinic flux within the snowpack would be exponential. Therefore, on a cloudy day the $z_e$ method would provide a very good approximation of actinic flux profile and photolysis rate coefficient within snowpack even without correction.

Other assumptions have also been made on snowpack properties i.e. assuming homogeneous single layer snowpack, black carbon or HULIS as the only absorber other than ice and constant vertical chemical concentration profile. Geographic location and weather conditions may have major influence on the number of layers within snowpack and the distribution of their physical and optical properties. Other common absorbers such as dust and humic-like substances (HULIS) may have a much stronger wavelength dependence across the UV and near-visible (France et al., 2012; Reay et al., 2012). Last, but not least, many field campaigns e.g. Frey et al. (2009); France et al. (2011) had recorded field observations on the Antarctic Plateau (Frey et al. (2009); France et al. (2011)), show there is a much higher nitrate anion concentration in the top few centimetres of the snowpack, the region of the snowpack where the solar radiation attenuation is often non-exponential, than deeper into the snowpack, causing a potentially larger error estimating depth-integrated production rates from $z_e$ method.
4 Conclusions

The parameterisation of snowpack actinic flux with based on the e-folding depth – the $z_e$ method, which approximates the actinic flux profile by an exponential function, may lead to under/overestimation of depth-integrated photolysis rates compared to the RT (radiative transfer) method. The deviation depends on the chemical species, solar zenith angle and properties of the snowpack. The $z_e$ method is most likely to provide a poor estimation of depth-integrated photolysis rate under three-four conditions: (1) when solar zenith angle or effective solar zenith angle is small ($\theta < 37^\circ$), (2) the chemical species of interest has an action spectrum peak near or in the visible wavelength, and, such as $\text{NO}_2^-$ and $\text{NO}_2$ (3) melting snowpack, which has a small value of scattering cross-section, and (4) clean snowpack, which has a small absorption cross-section due to low impurity content.

The discrepancy between the $z_e$ and RT method can be improved with a correction factor, $C$, by applying the correction factors, $C(\theta)$, especially for “melting” snowpack and clean snowpack (i.e. snowpacks have an e-folding depth larger than $\sim 30 \text{ cm}$), of which the ratio of depth-integrated photolysis rate coefficient between the two methods, $Q$, has reduced from 0.82–1.35 to 0.97–1.02 for photolysis of $\text{NO}_2$, from 0.88–1.28 to 0.99–1.02 for photolysis of the $\text{NO}_2^-$ anion and from 0.92, from 0.93–1.27 to 0.99–1.01–0.03 for photolysis of the $\text{NO}_3^-$ anion and from 0.91–1.28 to 0.98–1.06 for $\text{H}_2\text{O}_2$.

Within the polar circles, solar zenith angles larger than 42.8° are the norm, the simple $z_e$ method provides an acceptable estimation (10–16% underestimation compare to radiative transfer model). However, if the site of interest is a tropical glacier or low latitude, which may experiences small solar zenith angle, on a slope, or slope snowpack, or a site with a small effective solar zenith angle, or wet snow, correction using the correction factor or moderately to heavily polluted (e.g. e-folding depth smaller than 30 cm) then correction factors, $C$, as listed in Tables 4 and 5) is advised. should be applied to reduce error up to 15%. Correction factors, $C$, listed in Table 5 should be
applied when the snowpack is clean, wet or melting (e.g. \(e\)-folding depth larger than 31 cm) to reduce the difference by up to 30%.

The values of \(e\)-folding depth used in some of the previous modelling studies were broadly based on field measurements (Thomas et al., 2011; Simpson et al., 2002). Recently research groups have started to develop new algorithms to estimate optical properties of snowpack, such as grain size and mass-ratio of pollutants, from satellite measurements (Zege et al., 2011; Malinka, 2014; Khokanovsky, 2015). These measurements and algorithms can be integrated into large scale chemical transport models in the future to estimate \(e\)-folding depth and photolysis rate coefficient for wide inaccessible areas.

An important approximation of the \(e\)-folding depth (\(z_e\)) method is that snowpack is optically thick, i.e. assuming the snowpacks are semi-infinite. For shallow snowpacks the exact RT method should be used. It is unlikely a robust simple parameterization could be developed to correct the \(z_e\) method for shallow snowpacks over a range of light absorbing snowpack, solar zenith angles and underlying terrains for the thin snowpack, i.e. soil or sea ice. For shallow snowpacks (< 2-3 \(e\)-folding depths) the RT method is recommended.

Acknowledgements. H. G. Chan is funded by the Natural Environment Research Council through Doctoral Studentship NE/L501633/1.

References


Optical properties of the snowpacks used in the sensitivity test within this study.

**Table 1.** Reference for quantum yield, $\Phi$, used for Reactions (R1)–(R4) and (R7) and absorption cross-section, $\sigma$, of the NO$_3^-$ anion, the NO$_2^-$ anion, H$_2$O$_2$, and NO$_2$.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Reference for $\Phi$</th>
<th>Quantum yield, $\Phi$ at 258 K</th>
<th>$\lambda_{act,peak}$, nm</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>Chu and Anastasio (2003)</td>
<td>0.00338</td>
<td>321</td>
</tr>
<tr>
<td>R2</td>
<td>Warneck and Wurzinger (1988)</td>
<td>0.00110</td>
<td>321</td>
</tr>
<tr>
<td>R3</td>
<td>Chu and Anastasio (2007a)</td>
<td>0.12066*</td>
<td>345</td>
</tr>
<tr>
<td>R4</td>
<td>Gardner et al. (1987)</td>
<td>0.97900</td>
<td>375</td>
</tr>
<tr>
<td>R7</td>
<td>Chu and Anastasio (2005)</td>
<td>0.68300</td>
<td>321</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Species</th>
<th>Reference for $\sigma$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO$_3^-$</td>
<td>Chu and Anastasio (2003)</td>
</tr>
<tr>
<td>NO$_2^-$</td>
<td>Chu and Anastasio (2007a)</td>
</tr>
<tr>
<td>NO$_2$</td>
<td>DeMore et al. (1997)</td>
</tr>
<tr>
<td>H$_2$O$_2$</td>
<td>Chu and Anastasio (2005)</td>
</tr>
</tbody>
</table>

* Quantum yield at $\lambda = 345$ nm, the photochemical action spectrum peak of the NO$_2^-$ anion.
Table 2. Parameterisation—correction for “general” snowpacks: Properties of snow type studied. Optical and physical properties are based on work by [Marks and King (2014)](#) there within.

<table>
<thead>
<tr>
<th>Species—Snow type</th>
<th>$\alpha \rho$</th>
<th>$b \sigma_{\text{scatt}}$</th>
<th>$R^2$, $v_{ze}^2$, $v_{ze}^{\text{Corr}}$ cm$^2$ kg$^{-1}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cold polar snow</td>
<td>0.469—0.2–0.6</td>
<td>$-0.327$ 0.995 0.9788 0.9996 15–25</td>
<td></td>
</tr>
<tr>
<td>Wind-packed snow</td>
<td>0.2–0.6</td>
<td>0.9758 0.99985–10</td>
<td></td>
</tr>
<tr>
<td>Melting snow</td>
<td>0.494 0.2–0.6</td>
<td>$-0.345$ 0.980 0.9749 1.0000 0.2–2</td>
<td></td>
</tr>
<tr>
<td>0.758—0.495 0.941 0.9435 0.9995—</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 3. Optical properties of the snowpacks used.

<table>
<thead>
<tr>
<th></th>
<th>ρ</th>
<th>[BC]</th>
<th>σ_{scatt}</th>
<th>O_3 col.</th>
<th>g</th>
<th>z_e *</th>
<th>designation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>g cm^{-3}</td>
<td>ng(C) g^{-1}</td>
<td>m^2 kg^{-1}</td>
<td>DU</td>
<td></td>
<td>cm^{-1}</td>
<td></td>
</tr>
<tr>
<td>Base Case</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>13.3</td>
<td>BaseC</td>
</tr>
<tr>
<td>Case 1</td>
<td>0.2</td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>25.2</td>
<td>Den0.2</td>
</tr>
<tr>
<td>Density of snowpack</td>
<td>0.6</td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>9.1</td>
<td>Den0.6</td>
</tr>
<tr>
<td>Case 2</td>
<td>0.4</td>
<td>4.0</td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>35.3</td>
<td>Scatt2</td>
</tr>
<tr>
<td>Scattering cross-section</td>
<td>0.4</td>
<td>4.0</td>
<td>7</td>
<td>300</td>
<td>0.89</td>
<td>24.4</td>
<td>Scatt7</td>
</tr>
<tr>
<td>Case 3</td>
<td>0.4</td>
<td>0.18</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>36.9</td>
<td>BC0.18</td>
</tr>
<tr>
<td>Black carbon content</td>
<td>0.4</td>
<td>32.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>4.9</td>
<td>BC32</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>128.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>2.5</td>
<td>BC128</td>
</tr>
<tr>
<td>Case 6, g</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>300</td>
<td>0.86</td>
<td>12.0</td>
<td>g0.86</td>
</tr>
<tr>
<td>Case 7</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>200</td>
<td>0.89</td>
<td>13.3</td>
<td>O_3200</td>
</tr>
<tr>
<td>Ozone column</td>
<td>0.4</td>
<td>4.0</td>
<td>25</td>
<td>400</td>
<td>0.89</td>
<td>13.3</td>
<td>O_3400</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th></th>
<th>ρ</th>
<th>[HULIS]</th>
<th>σ_{scatt}</th>
<th>O_3 col.</th>
<th>g</th>
<th>z_e *</th>
<th>designation</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>g cm^{-3}</td>
<td>ng g^{-1}</td>
<td>m^2 kg^{-1}</td>
<td>DU</td>
<td></td>
<td>cm^{-1}</td>
<td></td>
</tr>
<tr>
<td>Case 4</td>
<td>0.4</td>
<td>1.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>36.9</td>
<td>HULIS1</td>
</tr>
<tr>
<td>HULIS content</td>
<td>0.4</td>
<td>8.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>22.0</td>
<td>HULIS8</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>17.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>15.3</td>
<td>HULIS17</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>1000.0</td>
<td>25</td>
<td>300</td>
<td>0.89</td>
<td>2.06</td>
<td>HU1000</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>17.0</td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>37.0</td>
<td>HU17S2</td>
</tr>
<tr>
<td></td>
<td>0.4</td>
<td>1000.0</td>
<td>2</td>
<td>300</td>
<td>0.89</td>
<td>7.3</td>
<td>HU1000S2</td>
</tr>
<tr>
<td>Case 5</td>
<td>[BC] + [HULIS]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Combined</td>
<td>0.4</td>
<td>0.6 + 8</td>
<td>7</td>
<td>300</td>
<td>0.89</td>
<td>30.6</td>
<td>Comb</td>
</tr>
</tbody>
</table>

* For Case 1-2 & 4-6, the reported e-folding depth, z_e, is the average of e-folding depth at 321, 345 and 375 nm. For Case 3 & 7, z_e is the e-folding depth at 321 nm.
Table 4. Parameterisation correction for “meltingcold polar & coastal” snowpacksnowpacks. Species $a, b, c$, $R^2$, $v_{ze}, v_{ze}^\text{Corr}$. Values of the correlation coefficient were calculated for two different snowpacks (BaseC, $v_{ze}, v_{ze}^\text{Corr}$: $R^2, 0.543 - 0.378, 1.110 0.9004, 1.0000, 0.8503, 0.9934, 0.565 - 0.394, 1.066 0.8883, 1.0000, 0.868 - 0.565, 1.062 0.8352, 0.9995 HULIS8 and Comb) with and without applying the correction factors.

<table>
<thead>
<tr>
<th>Species</th>
<th>$a$</th>
<th>$b$</th>
<th>$c$</th>
<th>$R^2, v_{ze}$</th>
<th>$R^2, v_{ze}^\text{Corr}$</th>
<th>$R^2, v_{ze}$</th>
<th>$R^2, v_{ze}^\text{Corr}$</th>
<th>$R^2, v_{ze}$</th>
<th>$R^2, v_{ze}^\text{Corr}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO$_3^-$</td>
<td>0.452</td>
<td>-0.320</td>
<td>1.000</td>
<td>0.9788</td>
<td>0.9996</td>
<td>0.9862</td>
<td>0.9971</td>
<td>0.9468</td>
<td>0.9927</td>
</tr>
<tr>
<td>H$_2$O$_2$</td>
<td>0.485</td>
<td>-0.334</td>
<td>0.989</td>
<td>0.9758</td>
<td>0.9998</td>
<td>0.9749</td>
<td>1.0000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2^-$</td>
<td>0.494</td>
<td>-0.345</td>
<td>0.980</td>
<td>0.9749</td>
<td>1.0000</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2$</td>
<td>0.758</td>
<td>-0.495</td>
<td>0.941</td>
<td>0.9435</td>
<td>0.9995</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 5. Notation: Parameterisation correction for “melting & clean” snowpack. Values of the correlation coefficient were calculated for two different snowpacks (Scatt2, HULIS1 and Comb) with and without applying the correction factors.

- Absorption cross-section by species $\sigma_{\text{ice}}$
- Absorption cross-section by ice $\mu_{\text{abs}}$
- Absorption cross-section by impurities $I$
- Actinic flux $z_e$
- Asymptotic $e$-folding depth $g$
- Asymmetry factor dimensionless $BC$
- Black carbon $c$
- Correction factor for transfer velocity dimensionless $\rho$
- Density of snowpack $\kappa_{\text{ext}}$
- Extinction coefficient $\sigma_{\text{ext}}$
- Extinction cross-section $J$
- Photolysis rate constant $F$
- Photochemical production rate $\Phi$
- Quantum yield dimensionless $Q$
- Quotient, ratio of transfer velocity dimensionless $Q$
- Scattering cross-section $\theta$
- Solar zenith angle degree $\theta$
- Total absorption cross-section $\sigma_{\text{abs}}$
- Transfer velocity $v$
- Wavelength $\lambda$

<table>
<thead>
<tr>
<th>Species</th>
<th>$a$</th>
<th>$b$</th>
<th>$c$</th>
<th>BaseC $R^2$, $v_{z_e}$</th>
<th>$v_{z_e}^{\text{Corr}}$</th>
<th>HULIS1 $R^2$, $v_{z_e}^{\text{Corr}}$</th>
<th>Comb $R^2$, $v_{z_e}^{\text{Corr}}$</th>
<th>$R^2$, $v_{z_e}^{\text{Corr}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NO$_3^-$</td>
<td>0.523</td>
<td>-0.384</td>
<td>1.146</td>
<td>0.9004</td>
<td>0.9996</td>
<td>0.8742</td>
<td>0.9991</td>
<td>0.9481</td>
</tr>
<tr>
<td>H$_2$O$_2$</td>
<td>0.550</td>
<td>-0.378</td>
<td>1.107</td>
<td>0.8503</td>
<td>0.9934</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2^-$</td>
<td>0.565</td>
<td>-0.394</td>
<td>1.106</td>
<td>0.8883</td>
<td>1.0000</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NO$_2$</td>
<td>0.868</td>
<td>-0.565</td>
<td>1.062</td>
<td>0.8352</td>
<td>0.9995</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Figure 1. Depth profile within a “typical” snowpack ‘cold polar snow’ (Base Case: $\rho = 0.4$ g cm$^{-3}$, $[\text{BC}] = 4$ ng(C) g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$) of actinic flux, $I$, at $\lambda = 451$ nm at different solar zenith angles $\theta$. Squares: $\theta = 0^\circ$, circles: $\theta = 52.1^\circ$, diamonds: $\theta = 80.5^\circ$, plus: $\theta = 85.3^\circ$. 
Figure 2. Dependence of the e-folding depth, $z_e$, as a function of wavelength and dependence on (a) snow density of snowpack, $\rho$. Blue, magenta and green: $\rho=0.2$, $0.4$ and $0.6$ respectively. (Case 1); (b) Absorption scattering cross-section, $\sigma_{\text{scatt}}$. (Case 2); (c) absorption due to black carbon, $\sigma_{\text{abs}}$. Magenta [BC], and cyan: 0.4 (Case 3); (d) absorption due to HULIS, 3.2 [HULIS]. (Case 4): Values of e-folding depth decrease as values of density, black carbon mass ratio and 12.8 respectively. (e) Scattering scattering cross-section $\sigma_{\text{scatt}}$ increase across wavelengths between 300–600 nm. Black For snowpacks containing black carbon as the only absorber other than ice, mint green the change in e-folding depths are not sensitive to wavelength in the UV and magenta: 2 near-UV. However, 7 and 25 respectively for snowpacks contain i.e. HULIS the change in e-folding depth is sensitive to wavelength.
**Figure 3.** The ratio of depth-integrated photolysis rate coefficient, $Q = \frac{v_{TUV}}{v_{ze}}$, for the two different methods as a function of solar zenith angle, $\theta$. a) NO$_3^-$ anion; b) H$_2$O$_2$; c) NO$_2^-$ anion; d) NO$_2$; Magenta: BaseC snowpack ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4 ng(C) g$^{-1}$ and $\sigma_{scatt} = 25$ m$^2$ kg$^{-1}$);
Figure 4. The effective solar zenith angle, $\theta_{\text{eff}}$, is the same as the solar zenith angle of direct solar radiation, $\theta_{\text{dir}}$, on a flat surface (left). However, on a surface that has an incline (right) the effective solar angle, $\theta_{\text{eff}}$, is the difference of the direct solar zenith angle and the angle of the surface, $\phi$, and typically smaller.
Figure 5. The effect of different column ozone amount on the photolysis rate coefficient of a) $\text{NO}_3^-$ and b) $\text{NO}_2$ at 3 selected solar zenith angles ($0^\circ$, $66^\circ$ and $85^\circ$).
Figure 6. Photolysis rate coefficient for the NO$_3^-$ anion (LH panselsa & d), the NO$_2^-$ anion (middle panelsb & e) and NO$_2$ (RH panelssc & f) computed by TUV (solid line) and $z_e$ method (dashed line) at two different solar zenith angles, $\theta$, at 0° (top row) and 66° (bottom row). Maximum and minimum depth-integrated photolysis rate coefficient ratio occurred at $\theta = 0^\circ$ the transfer velocity ratio is maximum while minimum transfer velocity ratio when and $\theta = \sim 66^\circ$ respectively. Blue is the “melting snow”, Scatt2, ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4 ng(C) g$^{-1}$ and $\sigma_{\text{scatt}} = 2$ m$^2$ kg$^{-1}$); red-Black is the “standard heavily black carbon polluted snow”, StandardBC128, ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4128 ng(C) g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$); and black Magenta is the “heavily polluted BaseC snow”, BC128BaseC, ($\rho = 0.4$ g cm$^{-3}$, [BC] = 4284 ng(C) g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$); and Green is the “HULIS polluted snow” HULIS8 ($\rho = 0.4$ g cm$^{-3}$, [HULIS] = 8 ng g$^{-1}$ and $\sigma_{\text{scatt}} = 25$ m$^2$ kg$^{-1}$).

Surface (depth = 0 cm) values of photolysis rate coefficient from “RT method” and “$z_e$ method” are the same (see Eq. (8) for calculation of $J_{\text{TUV}}$). The deviation between the two methods was the largest for “melting snowpack”, especially for small solar zenith angles, and the the $z_e$ method provided the best estimation compare with RT method with the “heavily polluted” snowpack.
Figure 7. Transfer velocity—Depth-integrated photolysis rate coefficient at various solar zenith angles for different species within snowpack Standard BaseC, \( \rho = 0.4 \, \text{g cm}^{-3} \), \([\text{BC}] = 4 \, \text{ng(C)} \, \text{g}^{-1}\) and \(\sigma_{\text{scatt}} = 25 \, \text{m}^2 \, \text{kg}^{-1}\). Top left: transfer velocity—a) depth-integrated photolysis rate coefficient of the \(\text{NO}_3^-\) anion; top right: transfer velocity—b) depth-integrated photolysis rate coefficient of \(\text{H}_2\text{O}_2\); bottom left: transfer velocity—c) depth-integrated photolysis rate coefficient of the \(\text{NO}_2^-\) anion; bottom right: transfer velocity—d) depth-integrated photolysis rate coefficient of \(\text{NO}_2\); blue circle — \(v_{\text{TUV}}\), computed by TUV; green cross — \(v_{\text{ze}}\), calculated by e-folding depth method; pink diamond — \(v_{\text{ze}}^{\text{corr}}\), corrected \(v_{\text{ze}}\) by coefficients listed in Table 4. The simple \(z_e\) method provided a good match to the RT method at large solar zenith angles. At small solar zenith angles, the parameterisation with \(z_e\) were improved by applying the correction factors.
Figure 8. Transfer velocity—Depth-integrated photolysis rate coefficient at various solar zenith angle for different species within snowpack Scatt2, \((\rho = 0.4 \text{ g cm}^{-3}, [\text{BC}] = 4 \text{ ng(C) g}^{-1} \text{ and } \sigma_{\text{scatt}} = 2 \text{ m}^2 \text{ kg}^{-1})\). Top left: transfer velocity—a) depth-integrated photolysis rate coefficient of the \(\text{NO}_3^-\) anion; top right: transfer velocity—b) depth-integrated photolysis rate coefficient of \(\text{H}_2\text{O}_2\); bottom left: transfer velocity—c) depth-integrated photolysis rate coefficient of the \(\text{NO}_2^-\) anion; bottom right: transfer velocity—d) depth-integrated photolysis rate coefficient of \(\text{NO}_2\); blue circle — \(v_{\text{TUV}}\), computed by TUV; green cross — \(v_{\text{ze}}\), calculated by \(e\)-folding depth method; 

\textbf{Pink Red} diamond — \(v_{\text{ze}}^\text{corr}\), corrected \(v_{\text{ze}}\) by coefficients listed in Table 5. The \(R^2\) between the precise RT method and \(z_e\) parameterisation has improved significantly after applying the correction factors.
Appendix A: **Notation**
<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\sigma$</td>
<td>Absorption cross-section of chemical species</td>
<td>cm$^2$ molecule$^{-1}$</td>
</tr>
<tr>
<td>$\sigma_{\text{ice}}$</td>
<td>Absorption cross-section of ice</td>
<td>cm$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$\mu_{\text{abs}}$</td>
<td>Absorption coefficient</td>
<td>m$^{-1}$</td>
</tr>
<tr>
<td>$\sigma^+$</td>
<td>Absorption cross-section per mass of impurities</td>
<td>cm$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$I$</td>
<td>Actinic flux</td>
<td>quanta cm$^{-2}$ s$^{-1}$ nm$^{-1}$</td>
</tr>
<tr>
<td>$z_e$</td>
<td>Asymptotic $e$-folding depth</td>
<td>cm</td>
</tr>
<tr>
<td>$g$</td>
<td>Asymmetry factor</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$c$</td>
<td>Correction factor for depth-integrated photolysis rate coefficient</td>
<td>g cm$^{-3}$</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Density of snowpack</td>
<td>m$^{-1}$</td>
</tr>
<tr>
<td>$\rho_{\text{ext}}$</td>
<td>Extinction coefficient</td>
<td>g cm$^{-3}$</td>
</tr>
<tr>
<td>$\sigma_{\text{ext}}$</td>
<td>Extinction cross-section</td>
<td>m$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$J$</td>
<td>Photolysis rate constant</td>
<td>s$^{-1}$</td>
</tr>
<tr>
<td>$F$</td>
<td>Photochemical production rate</td>
<td>$\mu$mol cm$^{-2}$ s$^{-1}$</td>
</tr>
<tr>
<td>$\Phi$</td>
<td>Quantum yield</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$Q$</td>
<td>Quotient, ratio of depth-integrated photolysis rate coefficient</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$r_{\text{scatt}}$</td>
<td>Scattering coefficient</td>
<td>m$^{-1}$</td>
</tr>
<tr>
<td>$\sigma_{\text{scatt}}$</td>
<td>Scattering cross-section</td>
<td>m$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$\theta$</td>
<td>Solar zenith angle</td>
<td>degree</td>
</tr>
<tr>
<td>$\sigma_{\text{abs}}$</td>
<td>Total absorption cross-section</td>
<td>cm$^2$ kg$^{-1}$</td>
</tr>
<tr>
<td>$\nu$</td>
<td>depth-integrated photolysis rate coefficient</td>
<td>cm s$^{-1}$</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>Wavelength</td>
<td>nm</td>
</tr>
</tbody>
</table>