Mercury Vapor Air-Surface Exchange Measured by Collocated Micrometeorological and Enclosure Methods – Part II: Bias and Uncertainty Analysis

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Dynamic flux chambers (DFCs) and micrometeorological (MM) methods are extensively deployed for gauging air-surface Hg\textsuperscript{0} gas exchange. However, a systematic evaluation of the precision of the contemporary Hg\textsuperscript{0} flux quantification methods is not available. In this study, the uncertainty in Hg\textsuperscript{0} flux measured by relaxed eddy accumulation (REA) method, aerodynamic gradient method (AGM), modified Bowen-ratio (MBR) method, as well as DFC of traditional (TDFC) and novel (NDFC) designs is assessed using a robust data-set from two field intercomparison campaigns.

The absolute precision in Hg\textsuperscript{0} concentration difference ($\Delta C$) measurements is estimated at 0.064 ng m\textsuperscript{-3} for the gradient-based MBR and AGM system. For the REA system, the parameter is Hg\textsuperscript{0} concentration ($C$) dependent at $0.069 + 0.022C$. During the campaigns, 57\% and 62\% of the individual vertical gradient measurements are found to be significantly different from zero, while for the REA-technique the percentage of significant observations are lower. For the chambers, non-significant fluxes are confined to a few nighttime periods with varying ambient Hg\textsuperscript{0} concentration.

Relative bias for DFC-derived fluxes is estimated to be $\sim \pm 10\%$, and $\sim 85\%$ of the flux bias is within $\pm 2$ ng m\textsuperscript{-2} h\textsuperscript{-1} in absolute term. The DFC flux bias follows a diurnal cycle, which is largely affected by the forced temperature and irradiation bias in the chambers. Due to contrasting prevailing micrometeorological conditions, the relative uncertainty (median) in turbulent exchange parameters differs by nearly a factor of two between the campaigns, while that in $\Delta C$ measurement is fairly consistent. The estimated flux uncertainties for the triad of MM-techniques are 16\%-27\%, 12\%-23\% and 19\%-31\% (interquartile range) for the AGM, MBR and REA method, respectively. This study indicates that flux-gradient based techniques (MBR & AGM) are preferable to REA in quantifying Hg\textsuperscript{0} flux over ecosystems with low vegetation height. A limitation of all Hg\textsuperscript{0} flux measurement systems investigated is their incapability to obtain synchronous samples for the calculation of $\Delta C$.

This reduces the precision of flux quantification, particularly in the MM systems under non-stationarity of ambient Hg\textsuperscript{0} concentration. For future applications, it is recommended to accomplish $\Delta C$-derivation from simultaneous collected samples.
1. Introduction

The volatility of atomic mercury (Hg\(^0\)) adds to the complexity of the element biogeochemical cycle. Mercury differs from other heavy metals in that it continuously goes through deposition and re-emission cycles after it is released into the atmosphere thus exhibiting extensive dynamic cycling among environmental compartments (Schroeder and Munthe, 1998). While assessments of Hg burden in various environmental compartments are rather concordant, the fluxes between them are less well constrained (Selin, 2009). Hg\(^0\) flux measurements in terrestrial ecosystem are predominantly conducted by dynamic flux chambers (DFC) and to a less extent by micrometeorological (MM) methods, which differ in measurement principles and spatial scale of flux footprint (Gustin, 2011). An advantage of the MM-techniques compared to chambers is the measurement under undisturbed conditions. However, this also implies practical disadvantages that Hg\(^0\) has to be detected at ambient level, and that small temporal concentration fluctuations or vertical gradients have to be resolved. A DFC system derives flux from a steady-state mass balance and after deployment there is build-up of an excess (or deficit) of Hg\(^0\) concentration inside the enclosure compared to ambient air. Hg\(^0\) concentration differences between inlet and outlet of a DFC must exceed the system blank to obtain statistical significant fluxes (Eckley et al., 2010). DFCs of different sizes, shapes and operation flow rates yield different Hg\(^0\) fluxes under identical environmental conditions (Wallschläger et al., 1999; Zhang et al., 2002; Eckley et al., 2010). More recently, we designed and deployed a DFC of novel design (NDFC) based on surface wind shear condition (friction velocity) rather than on an artificial fixed flow to account for natural shear conditions (Lin et al., 2012). Nonetheless, implementing a new DFC design prompts for a thorough comparison of in-field collected flux data by the different DFC techniques. It is also important to characterize the effects of
enclosure on the microclimate over diurnal cycles, particularly temperature and radiation balance, that may lead to erroneous flux quantification as observed for other trace gases (Denmead, 2008).

The preferred MM-technique, eddy covariance (EC), a direct flux measurement method without any applications of empirical constants requires a fast response (~10 Hz) gas analyzer and has not been realized for Hg\(^0\). Although newly developed fast instruments for Hg\(^0\) have been tested and validated, their precision needs improvements to perform regular Hg\(^0\)-EC flux measurements (Pierce et al., 2013; Bauer et al., 2014). MM techniques used to quantify Hg\(^0\) (turbulent) flux include relaxed eddy accumulation (REA) and modified Bowen-ratio (MBR), aerodynamic gradient method (AGM). These techniques derive flux from a measured concentration difference (\(\Delta C\)) and MM quantities, where the latter are based on EC measurements. The quality and uncertainty of EC data can be assessed by applying well-established tests and algorithms implemented in open-source software packages designed for processing EC raw data (Aubinet et al., 2012; Fratini and Mauder, 2014). EC data of high quality are typically associated with relative sampling uncertainties less than 20% (Mauder et al., 2013). Giving the challenge in accurate measurement of \(\Delta C\), the precision with which the operational MM-system can resolve small \(\Delta C\) (typically at a few %) (Sommar et al., 2013a) may render a large proportion of flux data to be insignificant at pristine sites (Fritsche et al., 2008). Especially the performance of REA-systems is sensitive to bias between the gas sampling pathways indicating the need to exercise a stringent QA/QC-protocol on the gas sampling and chemical analytical system over time (Moravek et al., 2014; Nemitz et al., 2001).

Most studies that investigated Hg\(^0\) flux did not consider uncertainty and potential bias of the applied techniques, nor did them present uncertainty of the calculated fluxes (Mason, 2009). A limited number of studies show and discuss sampling errors. Smith and Reinfelder (2008) tabulated uncertainties (9%-95%) for individual AGM Hg\(^0\) fluxes over wetlands without information of compartmentalized uncertainties. Marsik et
Meyers et al. (1996) reported ±30% and ±35% mean uncertainties in eddy diffusivity for H$_2$O and CO$_2$ proxy scalars when applying the MBR-method to measure Hg$^0$ flux over forest floor soil and lake. Fritsche et al. (2008) estimated the relative uncertainty for the AGM and MBR method to ~43% and ~14% over grassland. Moreover, there is a lack of detailed comparisons that assess both differences and uncertainties among contemporary MM and DFCs techniques to quantify Hg$^0$ flux under varying conditions. We have recently improved a number of Hg$^0$ flux measurement platforms (Lin et al., 2012; Sommar et al., 2013b; Zhu et al., 2013a) and performed an integrated field comparison of collocated MM (REA, MBR and AGM) and DFC (traditional and novel type) systems. The results are presented in two companion papers.

In Part I, the five systems and their measured fluxes were cross-examined with respect to magnitude, temporal trend and correlation with environmental variables (Zhu et al., 2015). In this Part II, the objective is to investigate the quality of the flux data by quantifying measurement error under varying meteorological conditions. A bottom-up assessment where the uncertainty arising from individual terms in the flux calculation formula is conservatively evaluated and combined by standard Gaussian error propagation (Wolff et al., 2010). We evaluate random and systematic errors in $\Delta C$ by performing in-field extended side-by-side measurements for the REA and gradient-based methods. In addition, we provide theoretical precision requirements for the involved systems to resolve fluxes with regard to varying micrometeorological conditions experienced during the field assessment. Using ambient and DFC internal measured parameters to address for chamber effects as input, empirical flux models are developed to estimate bias in the DFC fluxes. Limitations and sources of uncertainties are discussed in connection with previous relevant studies and future directions for improvements are given as well as aiming to strengthen the technical merits of each technique.
2. Site description, measurements and data processing

The instrumentation set-up, quality control measures and a full site description have been described in the Part I Paper (Zhu et al., 2015). Briefly, two field campaigns were performed in late autumn 2012 (IC #1, bare ploughed soil fetch, November 4th – 24th, DOY 309 - 329) and spring 2013 (IC #2, low-standing wheat canopy, April 16th – 25th, DOY 106 - 115) over agricultural fields inside Yucheng Comprehensive Experimental Station (YCES) located on the North China Plain (36°57′ N, 116°36′ E). The terrain was relatively flat with homogeneous distribution of soil Hg (45.0±3.9 µg kg⁻¹, n=27). IC #1 was conducted over the ploughed bare soil surface using AGM, MBR, TDFC, and NDFC. IC #2 was performed over wheat (height ~0.36 m, leaf area index of 3.4) using REA, AGM, and MBR. All MM measurements were conducted using instrumentation mounted on a ~6.5 m high flux tower. The REA sampling intake (z\text{REA}, 2.96 m a.g.l.) was collocated with upper intake of the gradient system (z₂), while the lower intake (z₁) was at 0.76 m a.g.l. Temperature and humidity sensors (HMP 155A, Vaisala Oy, Finland) housed in radiation shields were positioned at z₂ and z₁ level. The three MM systems were independently operated using separate sets of 2/3-way automated magnetic switching unit (Tekran® 1110) coupled with respective automated Tekran® Model 2537B Hg vapor analyser (Tekran Instruments Corp.). Accumulated up- and down-draft and two-height level air were sampled in sequences of 10-min intervals (two 5-min samples). The TDFC and NDFC were operated in tandem at a flow rate of 15 L min⁻¹ with the inlet and outlet coupled to one 2537B instrument via a four-port switching manifold (Tekran® Model 1115).

Approximately 15% of the measurement periods were dedicated for calibrations, blank testing and other QA/QC-measures. Tests were applied on the fast time (0.1s) series of raw data derived from the OPEC-system (open path eddy covariance) instrumentation for each of the all told 1645 flux (20-min)
measurement periods to assess the turbulence qualitatively and to address the associated size of the MM-technique flux footprint using the Eddypro™ 5.0 flux analysis software package (LI-COR Biosciences Inc.). To indicate periods of limited turbulent mixing, all the individual flux data were flagged using the basic 0-1-2 system scale scheme described in Mauder and Foken (2004), where class 2 indicates a hard flag (low data quality). The data assigned for high (Flag 0) and moderate (Flag 1) turbulence quality (with respect to sensible heat flux) corresponded to 55% and 81% of the flux observations during IC #1 and IC #2 respectively (66% in total). Periods when horizontal wind approached the sampling tower within the immediate ±15º sector of the opposite direction from which the sonic anemometer head (and sampling inlets) was pointing were hard-flagged to account for potentially disturbances of the wind field. This yielded additional 4% of the data classified by Flag 2. The representatives of 20-min fluxes was checked by footprint analysis (Zhu et al., 2015) but occasioned no additional flags since the sampling tower is predominately surrounded by continuous farmlands within ~2 km radius. Hard-flagged data denote periods of greater uncertainty in the turbulent fluxes and the uncertainty quantification itself may become questionable (Mauder et al., 2013). The qualitative information derived from diagnostic flags serves as a guide for further quantitative assessment of uncertainties.

3. Methodology

Error is a single value indicating the difference between an individual measurement and the true quantity being measured. In practice, an observed measurement error is the difference between the observed value and a reference value (Ellison and Williams, 2012). For measurement \( \hat{x} \) of an arbitrary quantity \( \hat{x} \), the observation can be expressed as \( x = \hat{x} + \epsilon_x + \delta_x \), where \( \epsilon_x \) and \( \delta_x \) represent systematic (bias) and random errors, respectively. As far as possible, errors should be traced, and
minimized when possible, and nevertheless accounted for by applying corrections while resulting stochastic uncertainties associated with the precision of a measurement should be estimated and stated (Billesbach, 2011). Measured fluxes are estimates of unknown quantities of air–surface exchange under field conditions and a reference technique for validating the estimates does not exist. Identified flux bias from side-by-side measurement was corrected for while resulting uncertainties associated with the flux measurement was combined by standard Gaussian error propagation.

3.1 Calibration, detection limit and uncertainty of the concentration measurements

Multiple Tekran® 2537 mercury vapor analysers were deployed in this study. For each analyzer, a pre-filtered sample air stream is passed through a gold cartridge that trap Hg by amalgamation, which then is thermo-desorbed and detected by atomic fluorescence spectrophotometry. The instrument utilises two gold cartridges in parallel, with alternating operation modes (sampling and desorbing/analysing in a mercury free Ar stream) on a pre-defined time base of 5 min to allow for continuous operation. The instrument is equipped with an internal permeation source (secondary standard, VICI Metronics Inc., Paulsbo, USA) that can be invoked automatically to perform two-point calibrations with a span value of ~150 pg and a zero-air reference point (exclusively no detectable peak using default integration parameters). The photo-multiplier sensitivity was typically at 6-9×10^6 area unit per ng Hg (response factor). The three Tekran 2537B instruments deployed were operated under the AMNet standard operation procedure (SOP) protocol (NADP, 2011). The internal calibration system (within ±4% repeatability for regular 48 h calibrations of the individual Tekran 2537Bs) was verified prior to each of the field campaigns using syringe injection from a saturated Hg^0 vapor source in a thermostatically controlled water bath. Repeated injections yielded recoveries within ±2% (range: 98-101%) of the expected amount Hg injected.
whereby also taking the temperature difference between the reservoirs into consideration (Brown and Brown, 2008). Consequently, our mass concentration measurements of Hg\textsuperscript{0} are traceable to the accuracy at which Hg\textsuperscript{0} vapor pressure can be gauged. For this purpose, we deployed the commonly used so-called Dumarey equation (Dumarey et al., 1985; Dumarey et al., 2010). The performance of the (A-B) pair of gold cartridges in each of the 2537Bs was evaluated prior to each campaign. In case a significant difference (> 5%) in the A vs. B cartridge response to calibration spans or persistent significant bias (t-test, $P < 0.05$) existed between A and B when monitoring ambient air, the peculiar pair was replaced with a fresh one. Further inter-comparisons indicated that no discernible bias or trends deviating from a 1:1 relationship to proceed.

The uncertainty of concentration measurement depends on the individual uncertainties of the sample volume, the peak integration and field calibration procedure. The sample volume is derived from an internal mass flow controller (MFC, Bronkhorst High-Tech B. V., Ruurlo, Netherlands) and reported exclusively within ±0.01 L of the pre-defined volume. To verify the performance of the MFC, the sampling air flow into the 2537Bs was also measured using an electronic bubble flow meter (Gillibrator, Sensidyne Inc., St. Petersburg, USA). The detector output signal was set in the range 0.15-0.25 V and showed satisfactorily low baseline standard deviations in general of < 80 µV. The default fluorescence peak integration scheme of 2537B is designed for moderate Hg loadings per sampling cycle (i.e. 10-15 pg).

At smaller loadings, this scheme introduces a non-linearly growing relative concentration bias (biased low) with decreasing peak area (Swartzendruber et al., 2009). For one of our applications, the coupling of the REA system with a 2537B yielded sub-optimal Hg mass loadings (typically 2-8 pg per cycle due to the injection of Hg zero-air). To mitigate for this critical effect, the REA-coupled 2537B was operated under a revised scheme of parameters resulting in a slightly longer and fixed integration time (Swartzendruber et
al., 2009). For the remaining 2537Bs (DFCs and gradient sampling system respectively), the integration parameters remained at default level during operation. The 2537B detection limit with this peak integration scheme is at ~0.10 ng m\(^{-3}\).

### 3.2 Derivation of concentration difference detection limit, bias and uncertainty

All the examined flux techniques rely on measurement of Hg\(^0\) concentration differences as shown in Eq. (1)-(5) for TDFC, NDFC, REA, AGM and MBR system, respectively. In this paper, all equation symbols with corresponding units are summarized and explained in the Nomenclature Section.

1. **TDFC**

\[
F_{\text{TDFC}} = \frac{Q}{A} \cdot \frac{(C_{\text{out}} - C_{\text{in}})}{A} = \frac{Q}{A} \cdot \Delta C_{\text{enclosure}}
\]

2. **NDFC**

\[
F_{\text{NDFC}} = \frac{Q}{A} \cdot \frac{k_{\text{max}}(m)}{k_{\text{max}}(a)} = \frac{Q}{A} \cdot \Delta C_{\text{enclosure}} \cdot \left( \frac{4.86 + \frac{3.625 \times 10^6 \cdot u_r}{(z_0 \cdot D_{\text{He-air}})^2}}{1 + 3.911 \times 10^5 \cdot \left(\frac{u_r}{z_0 \cdot D_{\text{He-air}}}\right)^2} \right)
\]

3. **REA**

\[
F_{\text{REA}} = \sum \beta_i \sigma_r \left(C_i - \bar{C}_i\right) = \beta_i \sigma_r \left(\sum_{i} m_i \cdot t_i \cdot Q_i \cdot \alpha_i - \sum_{j} m_j \cdot t_j \cdot Q_j \cdot \alpha_j\right)
\]

4. **AGM**

\[
F_{\text{AGM}} = -K_H \left(u_r, z\right) \frac{\partial C}{\partial z} = -\frac{K_H u_r}{\ln \left(\frac{z_2 - d}{z_1 - d}\right)} \cdot \psi_H (z_2) + \psi_H (z_1) \cdot \frac{C_{\text{in}} - C_{\text{out}}}{\Delta C_{\text{in}}}
\]

5. **MBR**

\[
F_{\text{MBR}} = \frac{w_T}{w_T^T} \cdot \frac{C_{\text{in}} - C_{\text{out}}}{T_{\text{in}} - T_{\text{out}}} = \frac{w_T}{w_T^T} \cdot \frac{\Delta C_{\text{grad}}}{\Delta T_{\text{grad}}}
\]

Since a single 2537B does not have the capability to analyze samples from two channels synchronously, the calculation of concentration difference is based on temporally intermittent concentration measurement. This means that uncertainties in \(\Delta C\) of Eq. (1) – (5) (i.e., \(\Delta C_{\text{enclosure}}\).
\( \Delta C_{\text{REA}} \) and \( \Delta C_{\text{grad.}} \) include a contribution from sampling channels (for enclosures: the chamber blank) as well as from non-stationarity in Hg\(^0\) concentration during the collection of asynchronous samples. The combined uncertainty due to analytical precision and intermittent sampling is expressed as

\[
\delta_{\Delta C_{\text{MM}}} = \pm \sqrt{(\delta_{\Delta C_{\text{MM}}}^{\text{channel}})^2 + (\delta_{\Delta C_{\text{MM}}}^{\text{IS}})^2} \quad \text{and} \quad \delta_{\Delta C_{\text{enclosure}}} = \pm \sqrt{(\delta_{\Delta C_{\text{enclosure}}}^{\text{IS}})^2 + \delta_{\Delta C_{\text{blank}}}^2}
\]

for the MM- and DFC-systems respectively. For the enclosures deployed, system blanks were determined during daytime in the field with the DFCs placed on an acid-cleaned FEP sheet. Our REA-system enables a mode that air is sampled synchronously with both conditional inlets (Sommar et al., 2013b). This referencing mode provides an automated QC-measure to regularly check for gas sampling path bias and to estimate the precision of \( \Delta C_{\text{REA}} \). To investigate and characterize bias and the precision of concentration difference measurements, we performed extended side-by-side measurements with the gradient system and regular periods of reference mode sampling with the REA system during the field experiments. The sign of \( \Delta C \) states the direction of vertical flux derived and therefore its uncertainty determines the limit at which flux can be detected. Detection limits under field conditions was derived based on the standard deviation of the residuals from orthogonal linear regression fitting.

### 3.3 Constraints on Hg\(^0\) analyser resolution for the flux measurement methods

The MM and DFC techniques rely on entirely independent principles. Even at the high air exchange rates (~3.1 and ~2.1 min\(^{-1}\) for TDFC and NDFC) used in this study, there is an inevitable build-up of an excess (or deficit) of Hg\(^0\) concentration inside the enclosure compared to ambient air. The concentration difference to be resolved depends on the magnitude of the flux, but for MM-techniques also on atmospheric stability conditions and measurement height. The method-specific analyser concentration difference resolution (\( \Delta C \)) required to achieve a given uncertainty (\( \delta \)) in the flux measurement under the...
set of atmospheric conditions given during the IC #1 was estimated using the approach of Businger and Delany (1990) modified by Rowe et al. (2011). The analysis is presented as function of the parameters $u_*$ and $\zeta$:

$$\Delta C = \mathbb{R} \cdot |F| \cdot AP_x(\zeta)/u_*$$  \hspace{1cm} (6)

where $|F|$ and $AP_x(\zeta)$ are explained in the Nomenclature Section. For REA with a dead-band of $\pm 0.3 \cdot \sigma_u$, $\beta = 0.45$ was used in this example. Observations of high friction velocities normally resulted in nearly neutral stratification, whereas low winds led to either significant stable or unstable conditions (Fig. 1a). Following Ammann (1998), for typical daytime (unstable) and night-time (stable) conditions respectively, a piecewise logarithmic parameterisation of $u_*$ as a function of $\zeta$ ($\ell(\zeta)$) was applied (dashed lines in the Fig. 1a) to reduce Eq. (6) to being dependent of a single variable: $\Delta C/\mathbb{R} \cdot |F| = AP_x(\zeta)/\ell(\zeta)$. An analogous expression for DFCs, is equal to the ratio $A/Q$ and independent of atmospheric stability. In the Fig. 1b, $\Delta C/\mathbb{R} \cdot |F|$ (h m$^{-1}$) is plotted as a function of stability for the flux measurement techniques inter-compared. For a given flux, it is imperative that the chamber methods have the mildest requirements for Hg$^0$ sensor resolution. On the other hand, the analyser requirements for all MM methods are most stringent at near neutral conditions when the surface boundary layer is well mixed. The intensity of turbulent mixing declines with increasing atmospheric stability ($\zeta$), leading to higher concentration gradients. Among the MM methods, the analyser requirement for gradient methods is least stringent for stable conditions (it should, however, be noted that large flux uncertainties under stable conditions could be encountered with the gradient method (Foken, 2008)), while REA and gradient methods have nearly equivalent precision requirement under significant unstable conditions ($\zeta < -0.1$). With a profile measurement height ratio ($z_2/z_1$) of ~3.9 in this study, the gradient methods are a favourable choice under most conditions as REA requires greater analytical precision. However, flux
measurements over tall vegetation, such as a forest canopy, using gradient relationships become less favourable, e.g. due to that $z_2$ must be chosen quite low according to fetch limitations whereas the recommended minimum height of $z_1$ is confined to a fairly elevated level by issues like the extension of roughness sublayer and internal boundary layers. Over tall vegetation, typically $(z_2 - d)/(z_1 - d) \approx 1.5$ can be achieved (Moravek et al., 2014).

### 3.4 Analysis of flux bias and uncertainty

#### 3.4.1 Dynamic flux chambers

DFC measurement of Hg$^0$ fluxes is potentially prone to a variety of errors. Aspects such as spatial representativeness (Gustin and Lindberg, 2000), chamber design, operation parameters (e.g. flushing flow rate) (Eckley et al., 2010; Lindberg et al., 2002; Lin et al., 2012), fabrication materials (e.g. quartz glass, FEP Teflon film, polycarbonate) (Carpi et al., 2007) and modified microenvironment inside the chamber (e.g. increased temperature) should be considered. The flushing flow rate has been isolated as a key factor that, can force a difference in measured flux up to one order magnitude (Eckley et al., 2010). Other factors including solar radiation, soil temperature and soil moisture are also influential factors of Hg$^0$ flux over soil (Lin et al., 2010). In turn, the modified temperature and radiation balance inside the DFC may lead to an erroneous quantification. In our assessment on the method bias of the TDFC and NDFC techniques, flushing flow rate was set at a fixed value for both DFCs and therefore not considered as a variable. The soil moisture remained largely invariant during the campaign. Therefore, soil temperature ($T_{soil}$) and irradiance ($S$) were the key factors controlling the flux variability during IC#1 (Zhu et al., 2015). We used a polynomial incorporating predictor terms up to quadratic order to fit the DFC flux with corresponding observations of $T_{soil}$ and $S$ inside the DFCs:
Predictive regression models are developed for each of the chamber types (Lin et al., 2010):

\[
\hat{F}_{DFC} = \gamma_0 + \gamma_1 T + \gamma_2 S + \gamma_3 (T_{\text{soil}} \cdot S) + \gamma_4 T_{\text{soil}}^2 + \gamma_5 S^2
\]  

(7)

\[
\hat{F}_{NDFC} = \left[-3.44 - 0.424 T_{\text{soil}} - 0.017 S + 0.003 (T_{\text{soil}} \cdot S) + 0.088 T_{\text{soil}}^2 + 9.02 \times 10^{-5} S^2\right] \frac{k_{\text{mass(a)}}}{k_{\text{mass(m)}}}
\]  

(8)

\[
\hat{F}_{TDFC} = -3.977 - 1.05 T_{\text{soil}} - 0.022 S + 0.003 (T_{\text{soil}} \cdot S) + 0.072 T_{\text{soil}}^2 + 7.214 \times 10^{-5} S^2
\]  

(9)

Overall fits (correlation coefficient, R) of 0.91 and 0.87 were obtained for NDFC and TDFC respectively 

\((p < 0.001)\). Absolute bias (\(\epsilon_{DFC}\)) of chamber-derived flux is estimated using:

\[
\epsilon_{DFC} = \hat{F}_{DFC} - \hat{F}_{N} + \epsilon_{\text{blank}}
\]  

(10)

In turn, as the flux calculated in Eq. (1), the uncertainty associated with TDFC measurements is estimated as:

\[
\delta_{I_{DFC}} = \pm \sqrt{\left(\delta_{\text{enclosure}}^2 + \delta_{\text{blank}}^2\right)} \cdot Q / A
\]  

(11)

Concerning the NDNC approach, the uncertainty in the last term \((k_{\text{mass(a)}}/k_{\text{mass(m)}})\) of Eq. (2) was incorporated into Eq. (11).

3.4.2 Micrometeorological methods

There are several errors in the MM flux measurements, especially for the REA-technique. In general, the sources include source/sink-characteristic (footprint variability), turbulent transport and instrumentation factors (Businger, 1986). Turbulent Hg\(^0\) fluxes determined by Eq. 3 - 5 include parameters derived from OPEC flux, whose precision improves by a factor of \(1/\sqrt{t_{\text{average}}}\) by increasing the flux averaging time \((t_{\text{average}})\). In this work, \(t_{\text{average}} = 20\) min was applied for all methods. For the assessment of \(t_{\text{average}}\), see Sommar et al., 2013b. The estimation of uncertainty in OPEC-derived parameters \((H\) and \(u\)) is based on random sampling errors quantified as the variance of a covariance by the method of
The conventional approach of investigate uncertainties from the bottom up principle was applied.

### 3.4.2.1 REA method

Using error propagation theory on Eq. (3), uncertainties associated with the REA-derived fluxes can be calculated by Eq. (12):

$$\delta_{\varepsilon,\text{REA}} / F_{\text{REA}} = \pm \sqrt{\left(\frac{\delta_{\varepsilon,\text{REA}}}{\sigma_w}\right)^2 + \left(\frac{\delta_{\varepsilon,\text{REA}}}{\Delta C_{\text{REA}}}\right)^2}$$

(12)

However, the first term was demonstrated to give an insignificant contribution to the combined uncertainty (See Section 4.2). Excluding the contribution from $\sigma_w$, the number of independent quantities in Eq. (12) to be propagated for $\delta_{\varepsilon,\text{REA}} / F_{\text{REA}}$ is according to Kramm et al. (1999) described by the Eq. (13):

$$\delta_{\varepsilon,\text{REA}} / F_{\text{REA}} = \pm \sqrt{\left(\frac{\delta_{\varepsilon,\text{REA}}}{\Delta C_{\text{REA}}}\right)^2 + 2\left(\frac{\delta_{\varepsilon,\text{REA}}}{\Delta T_{s,\text{REA}}}\right)^2}$$

(13)

The REA system is potentially affected by lag-time bias and the attenuation of high-frequency concentration fluctuations in the tube flow that leading to an underestimation of turbulent fluxes. These effects were evaluated following Moravek et al. (2013) and the results reported in Sect. 4.2. Theoretically, $\beta$ has negligible bias since any bias in temperature and wind speed is virtually cancelled out during the calculation (Pattey et al., 1992, $\beta_T$ derived from buoyancy heat flux):

$$\beta_T = \frac{wT_s}{\sqrt{\left[\sigma_w \cdot \left(T_s - T_s^\prime\right)\right]^2}} = \frac{wT_s}{\sigma_w \cdot \Delta T_{s,\text{REA}}}$$

(14)

In practice, bias exists due to departures from a zero mean vertical wind speed ($\bar{w}$) during the flux averaging period. The present REA application allowed for the rejection of samples associated with $w$ -fluctuations around zero (“deadband”, DB). Consequently, $C^\uparrow$ is sampled only for $w > w_{DB}$ and $C^\downarrow$ only for $w < -w_{DB}$ (Eq. 3), which also applies for $T_s^\dagger$ and $T_s^\ddagger$ (Eq. 14). A 5-min moving average...
filter combined with a deadband based on a ditto moving standard deviation (\(w_s - 0.3 \cdot \sigma_{w,s} < DB < w_s + 0.3 \cdot \sigma_{w,s}\)) was implemented in the REA program aiming during sampling to alleviate for \(\overline{w}\)-bias from the \(w\) signal. Nevertheless, the effectiveness of various applied filter techniques appears at-large ambiguous (Bowling et al., 1998). To investigate residual bias in the selected conditional sampling scheme, \(\beta_{\tau_s}\) derived on-line was compared with \(\beta_{\tau_s}\) calculated from the a-posteriori known \(w_{20'}\) and \(\sigma_{w,20'}\) using the filter \(w_{20'} - 0.3 \cdot \sigma_{w,20'} < DB < w_{20'} + 0.3 \cdot \sigma_{w,20'}\) to numerically segregate temperature data into up- and downdraft bins representative for \(t_{\text{average}}\). The result is reported in Section 4.2.

### 3.4.2.2 Gradient-based methods

The AGM flux is computed as the product of transfer velocity (\(\nu_{\text{t}}\)) and vertical Hg\(^0\) concentration gradient (\(\Delta C_{\text{grad.}}\)). In Eq. (4), \(\nu_{\text{t}}\) is compounded of multiple independent quantities. Following Wolff et al. (2010), the relative uncertainty in \(F_{\text{AGM}}\) can be calculated according to:

\[
\delta_{\nu_{\text{t}}} / F_{\text{AGM}} = \pm \sqrt{ \left( \delta_{\nu_{\text{t}}} / \nu_{\text{t}} \right)^2 + \left( \delta_{\nu_{\text{t}}} / \nu_{\text{t}} \right)^2 + \left( \delta_{\nu_{\text{t}}} / \nu_{\text{t}} \right)^2 \left( \frac{(\psi_H(z_2) + \psi_H(z_2))}{(\ln(z_2/z_1) - \psi_H(z_2) + \psi_H(z_1))} \right) } \tag{15}
\]

\(\delta_{\nu_{\text{t}}} / F_{\text{AGM}}\) was assessed from extended period of side-by-side measurements (Section 3.2). Friction velocity (\(u_*\)) is derived from OPEC measurements of momentum flux (\(\tau = \rho \cdot u_*^2\)). Assuming insignificant uncertainties in the air density determination, we obtain \(\delta_{u_*} / u_* = \frac{1}{2} \cdot \delta_{\tau} / \tau\) to insert into Eq. (15). For the right-hand compounded term of Eq. (15), we assumed that the uncertainty in \(\psi_H\) is similar to that of the universal function (Foken, 2008), which is generally better than 10%. For near-neutral stability conditions, it becomes confined to a few percent (Garratt and Taylor, 1996). To resolve this, we choose to use a simplistic approach, where \(\delta_{\psi_H} / \psi_H\) is scaled with the aerodynamic stability by intervals (for...
\[ |\varepsilon_2| < 0.1, \quad \delta_{\psi_H}/\psi_H = 0.02, \quad \text{for} \quad |\varepsilon_2| > 0.5, \quad \delta_{\psi_H}/\psi_H = 0.10 \quad \text{and the ranges in-between a linear interpolation was applied.} \]

The relative uncertainty in \( F^{MBR} \) measurements are calculated by:

\[
\delta_{F^{MBR}} / F^{MBR} = \pm \sqrt{(\delta_{H}/H)^2 + (\delta_{\Delta C_{grad.}}/\Delta C_{grad.})^2 + (\delta_{\Delta T_{grad.}}/\Delta T_{grad.})^2}
\]

(16)

Similar to the assessment of \( \delta_{\Delta C_{grad.}} / \Delta C_{grad.} \) discussed in Section 3.2, \( \delta_{\Delta T_{grad.}} / \Delta T_{grad.} \) is derived from collocated duplicate thermocouple measurements of air temperature.

4. Experimental results

The uncertainty in concentration measurements of the three collocated Tekran 2537B was calculated from the uncertainty in volume and calibration measurements. Sample volumes derived from independent techniques are found to be within ±0.5% of the 2537Bs volume readings. The uncertainty of concentration measurement is mainly contributed by field calibrations. The combined uncertainty is estimated to be ±5%.

This compares favourably with the agreement among these 2537B instruments (< ±6%) during side-by-side measurements with a common inlet sampling Hg\(^0\) in ambient air.

4.1 Bias and uncertainty of DFC derived Hg\(^0\) fluxes

Field blanks determined in connection with regular flux measurement periods were consistently low for both DFCs (TDFC: 0.2±0.1 ng m\(^{-2}\) h\(^{-1}\), n=19; NDFC: 0.3±0.2 ng m\(^{-2}\) h\(^{-1}\), n = 32). Bias of DFC-derived flux as estimated using Eq. (8)-(10) was in the ranges of -0.6 to 6.7 and from -7.2 to 10.6 ng m\(^{-2}\) h\(^{-1}\) for TDFC and NDFC, respectively (Fig. 2). The median bias for both DFCs was slightly positive (0.1 and 0.2 ng m\(^{-2}\) h\(^{-1}\) for TDFC and NDFC). In both cases, more than 85% of the flux observations had a bias < 2 ng m\(^{-2}\) h\(^{-1}\) in magnitude. Possible reasons for the data disparity include (1) the difference in the light
transmission properties of the two chamber materials, and (2) the difference in soil temperature inside the chamber. The TDFC was manufactured of quartz glass while the NDFC was assembled by polycarbonate (PC) sheets (Lin et al., 2012; Zhu et al., 2013b; Zhu et al., 2015). Quartz has exceptional transmission properties for UV light down to 250 nm, while PC does not allow transmission of UV light that plays an important role in promoting Hg\textsuperscript{II} photo-reduction in the substrate (Eckley et al., 2010; Lin et al., 2012).

The heating of the soils inside the two chambers was also different (soil temperature difference between inside and outside of the chamber were up to 3.8 and 4.7 °C for TDFC and NDFC) because of the difference in chamber materials, dimensions and air exchange rates (~3.1 and ~2.1 min\textsuperscript{-1} for TDFC and NDFC). Consequently, DFCs flux bias showed diurnal cycles with positive bias in afternoon due to that soil temperature change considerably lags behind that of air temperature (Fig. 3). Discernible negative flux bias in NDFC flux appeared from 10:00 to 11:00 am due to weaker light transmission caused by water condensation that lowered Hg\textsubscript{0} emission. Following Eq. (11), the maximum uncertainty of TDFC-derived flux (\(\delta_{\text{p,src}}\)) was estimated to be ±2.8 ng m\textsuperscript{-2} h\textsuperscript{-1}. For typical daytime conditions (\(\delta_{u}/u_* \leq \pm 5\%\), Section 4.3), \(\delta_{\text{p,src}}\) was within ±2.1 ng m\textsuperscript{-2} h\textsuperscript{-1}, similar to \(\delta_{\text{p,src}}\) (Table 1). For nocturnal conditions, the uncertainty level is similar to the measured fluxes.

4.2 Bias and uncertainty of REA-derived Hg\textsubscript{0} fluxes

The lag time bias due to unsynchronized conditional sampling (Baker et al., 1992) is estimated at ±25 ms as an upper limit based on logged fluctuations of the flow rate in the intake tube upstream the REA segregator valves corresponding to attenuation of Hg\textsubscript{0}-REA flux of at most 2% (Moravek et al., 2013).

Likewise, flux loss due to dampening of sampled high frequency concentration fluctuations in the section is small. The flow regime in the intake line is turbulent (Re ~3500) and the smallest fluctuations in air are...
in fact not sampled since a DB is applied. The insignificant magnitude of these negative biases occasioned no action in form of flux corrections.

The evaluation of the effectiveness of the applied conditional sampling filter (Section 3.4.2.1) is applied on data flagged for high quality turbulence (Flag 0, \( \approx 72\% \) of the IC #2 duration). This procedure yielded an estimate of “unbiased” \( \beta_{r_s} \). It is found that the median of the on-line and “unbiased” \( \beta_{r_s} \) -factor differed significantly (Mann-Whitney U-test, \( n = 378, p < 0.01 \)) with the former higher (0.486 vs. 0.439) (Fig. 4). Accordingly, the on-line derived \( \beta_{r_s} \) tend to overestimate flux by \( \approx 10\% \) on an average (Table 1). The median of resampled \( \beta_{r_s} \) is closer to the value 0.448 (\( -2 < g < 0.06 \)) predicted from the relationship given by Amman and Meixner (2002). The a-posteriori calculated \( \beta_{r_s} \) is used for calculate individual turbulent REA flux for Flag 0 data. A fixed \( \beta_{r_s} \) of 0.45 is implemented for remaining periods (Flag 1 & 2) or if a-posteriori \( \beta_{r_s} \) is outside a \( \pm 0.2 \) interval of the median (Schade and Goldstein, 2001).

The relative uncertainty in \( \sigma_w (\delta_{w}/\sigma_w) \) of Eq. (12) is estimated as an upper limit using \( \delta_w^2/\sigma_w^2 \) (Xu, 2001). According to CSAT-3 specification, the absolute uncertainty of a single measurement of vertical wind (\( \delta_w \)) is 0.5 mm s\(^{-1}\). Concerning class 0 and 1 data, \( \delta_w^2/\sigma_w^2 \) was for \( \approx 98\% \) of the 20-min integrated measurements \( \leq 1\% \). Consequently, Eq. (13) was adopted to assess the relative uncertainty in \( F^{REA} \). In Fig. 5, the argument in the first term (\( H/\delta_h \)) in Eq. (13) segregated into turbulent quality classes is plotted versus the corresponding flux for IC #2. When \( H \) flux changes sign or diminishes to near zero at dawn/dusk and during the night, there is a significant increase in \( \delta_h/H \). Concerning the data classified with high quality and \( |H|> 20 \text{ W m}^{-2} \), the distribution of \( \delta_h/H \) is narrow (9.9 ± 12.7\%, IC #2, Table 1). The result is in agreement with other studies (Walker et al., 2006; Finkelstein and Sims, 2001). In comparison with IC #2, IC #1 included a larger proportion of turbulence data with poor quality (See Fig. 4 in Zhu et al. 2015) contributing to a higher overall uncertainty in \( \delta_h/H \) (Table 1).
The uncertainty and bias in $\Delta C_{\text{REA}}$ was deduced from periods of reference sampling covering a representative span of ambient Hg$^0$ concentrations (~1.5-8.1 ng m$^{-3}$). The asynchronous collected channel data were cross-interpolated to simulate concurrent Hg$^0$ gas analysis of the two channels. This dataset is assessed using orthogonal linear regression assuming equal variances for the channels, which is more appropriate than defining one as independent as in standard least-square methods (Cantrell, 2008). A scatter plot aligns well to a line of slope 1.051 and a non-significant ($p = 0.22$) offset from zero (Fig. 6).

Hence, there exists a moderate bias between the channels, which is corrected in Table 1. Such regular performance tests are very infrequently reported in the REA-literature (Arnts et al., 2013; Hensen et al., 2009; Park et al., 2010; Schade and Goldstein, 2001). Significant and variable REA channel biases were occasionally detected (Nemitz et al., 2001; Schade and Goldstein, 2001). In this study, the time-series of reference sampling covering both day and night period do not reveal any significant diurnal pattern or trend over time to proceed.

Inspection of residuals of the orthogonal fit plotted as a function of sampling time (record number) showed homoscedastic features. In Fig. 7, the residuals that approximately align to a Gaussian distribution are plotted as a function of Hg$^0$ concentration in ambient air. Following Wolff et al. (2010) and Walker et al. (2013), we used the standard deviation of the residuals as a measure of $\delta_{\text{channel}}^{C_{\text{REA}}}$. The absolute uncertainties $\delta_{\text{channel}}^{C_{\text{REA}}}$ were found to be a variant of air concentration and were fitted to a linear function by regression. The resulting function of $\delta_{\text{channel}}^{C_{\text{REA}}} = 0.069 + 0.022C$ was used to predict the $\Delta C_{\text{REA}}$ detection limit for each flux observation and in the uncertainty propagation of Eq. (13) (See Table 1).

Uncertainty due to the intermittent conditional sampling ($\delta_{\text{IS}}^{C_{\text{REA}}}$) was approached by assessing the concentration difference between bias-corrected conditional (10-min) and corresponding 20-min average concentrations as a function of the fractional difference between previous and following same conditional...
line concentrations (Walker et al., 2006). The corresponding median relative uncertainty was 13.7% but the dataset includes transition periods, where individual values raise well over 50%. The calculations of $\delta_{\Delta C,\text{REA}}$ likely represent an upper limit since the estimate of uncertainty due to intermittent sampling includes contribution due to analytical precision.

The last term in Eq. (13) was assessed from the sonic temperature measurement resolution (root mean square) of 0.025 K for standard settings of CSAT-3 (\(\delta_{T_s}\), single measurement). An upper limit of $\delta_{\Delta T_{s,\text{REA}}}/\Delta T_{s,\text{REA}}$ is given by $\frac{\delta_{\Delta T_s}}{\Delta T_{s,\text{REA}} \cdot \sqrt{\frac{2}{m}}}$, where $m$ is the number of measurements per flux averaging period (i.e. $m = 12000$) (Xu, 2001). Due to the bidirectional nature of buoyancy heat flux, when $\Delta T_{s,\text{REA}}$ changes sign or approaches near zero at dawn, dusk, and intermittently during night, $\delta_{\Delta T_{s,\text{REA}}}/\Delta T_{s,\text{REA}}$ attains values above the sub-percent level that it is normally present in. For high turbulence quality segregated data, the $\Delta T_{s,\text{REA}}$ relative uncertainty was calculated to $0.8\pm0.5\%$.

### 4.3 Bias and uncertainty of gradient derived Hg\(^{0}\) fluxes

The primary bias in the MBR and AGM flux is caused by the potential sampling artifact for determining concentration gradient. Extended periods of side-by-side measurements (gas sampling inlets were brought to one height in same lateral proximately as during regular gradient sampling) were conducted. The comparison between the collocated lines used for two level gradient sampling is based on sequential concentration data. For a further investigation, cross-interpolation was used as imputation method to fill up missing values in the time-concentration series. Orthogonal linear regression indicated a bias existed between the sampling lines (Fig. 8), where the longer sampling tube (upper level) is biased low by 4.1%. The remaining scatter (residual) distribution followed a Gaussian distribution and was
homoscedastic with respect to sampling time and concentration. Hence, \( \Delta \text{grad.}_{\text{channel}} \) is largely invariant to \( C \). The absolute uncertainty was estimated to be 0.064 ng m\(^{-3}\) based on the overall standard deviation of the residuals remaining after orthogonal linear regression. The corresponding relative bias for the median ambient Hg\(^0\) concentration during the campaigns is at 2.2%. The uncertainties due to intermittent sampling of the concentration gradient (\( \Delta \text{grad.}_{\text{IS}} \)) were assessed in an analogous way to aforementioned for REA. The fractional uncertainty in \( \Delta C_{\text{grad.}} \) due to non-stationary Hg\(^0\) concentration is at 8.6% (median) with a corresponding median absolute deviation of 7.3%.

Individual \( \delta \tau / \tau \) was estimated (Finkelstein and Sims, 2001) and plotted versus \( u_* \) in Fig. 9. The overall scatter is substantial. However the flag 0 data can favourably be approximated by a power relationship (0.058 \( \cdot \) \( u_*^{0.473} \), \( r=0.89 \)). For the mean \( u_* \) of 0.3 m s\(^{-1}\) during the campaigns, the predicted fractional uncertainty is \( \sim 5\% \) and decreases slightly for the highest wind-forces. For near-neutral stability conditions, \( \delta v_w / \nu_w \) was estimated to 10.9 ± 12.6\% and 6.1 ± 10.2\% for IC #1 and IC #2 (Table 1).

Side-by-side measurements of the HMP 155A sensors deployed for deriving \( \Delta T_{\text{grad.}} \) in Eq. (5) indicated minor scale and offset bias in their performance, which was corrected for calculation. Analysis of residuals indicated that \( \delta \Delta T_{\text{grad.}} / \Delta T_{\text{grad.}} \) is diminutive (~0.4\%) to the other terms in Eq. (16) (Table 1).

### 4.4 Turbulent flux measurements under varying experimental conditions

Based on the \( \Delta C \) detection limit (1\( \sigma \)) derived from side-by-side measurements (gradient method) and reference sampling (REA), ~62\% of the 20-min averaged gradient measurements were above this limit during IC #1, whereas during IC #2 ~57\% and ~55\% of the concentrations difference derived from gradient and REA sampling were above the limit. The empirically derived detection limit for \( \Delta C_{\text{REA}} \) was moderately concentration dependent while that of \( \Delta C_{\text{grad.}} \) is found to be insignificantly variant. Since
Hg\textsuperscript{0} air concentration at this site generally followed pronounced diurnal patterns (Part I, Zhu et al. 2015), the $\Delta C_{\text{REA}}$ detection limit was on an average 10-15\% higher during the peak in the late morning hours compared to the minimum level. Hg\textsuperscript{0} flux observations can be identified as insignificant from zero when the corresponding $\Delta C$ fall below its detection limit. Fig. 10 shows the turbulent flux of REA and MBR time series with data segregated as significant and insignificant according to this analysis for the IC #2 period.

The level of detection limit obtained in this study (0.064 ng m\textsuperscript{-3}) compares favourably with 0.072 ng m\textsuperscript{-3} reported by Converse et al. (2010) using gradient-based MM techniques. Compared to other studies deriving Hg\textsuperscript{0} gas exchange flux from concentration profile measurements (Edwards et al., 2005; Fritsche et al., 2008; Lee et al., 2000; Goodrow et al., 2005), our $\Delta C_{\text{grad}}$ precision (1\sigma) is contrastingly elevated likely due to the generally higher level of ambient Hg\textsuperscript{0} concentration in this study (Zhu et al., 2015). The limited information existing in the literature regarding measurement of Hg\textsuperscript{0} flux by the REA technique (Bash and Miller, 2008; Cobos and Baker, 2002; Bash and Miller, 2009; Olofsson et al., 2005) excludes a rudimentary analysis and discussion of uncertainty and bias associated with conditionally sampled concentration differences.

Table 1 summarizes the uncertainty of MM and DFCs flux methods in our inter-comparison. The relative uncertainties for transfer velocity and sensible heat flux in IC #1 are nearly doubled (on a median basis) compared to that in IC #2 due to its lower turbulence quality. The uncertainty estimates associated with EC sampling errors based on variance analysis of covariance time-series (Finkelstein and Sims, 2001) used in this study are expected somewhat larger than calculations based on a side-by-side comparisons or paired observations (Mauder et al., 2013). However, the latter type of estimate concerning uncertainties in concentration difference measurements is provided here as upper limits. Median $\delta F/\bar{F}$ was slightly
higher for the MBR compared to the AGM technique during IC #1 (~24% vs. ~19%) while the opposite condition was present during IC #2 (~15% vs. ~19%). For comparison of the three MM-techniques during IC #2, the relative flux uncertainty ($\delta F / F$) is slightly higher during night-time (median ~17%, ~20% and ~25% for MBR, AGM and REA techniques). Fig. 11 shows the diurnal pattern of MM-technique $\delta F / F$ during IC #2. A marked maximum is visible for the gradient-based as well as the REA-technique during the hour after sunrise. This period is characterized by a transition in the sign of sensible heat flux and vertical temperature in addition to a generally rapid increase in $\text{Hg}^0$ air concentration while transfer velocities not yet started to increase significantly from night-time low values (generally < 0.10 m s$^{-1}$).

For most of the IC #2 periods $\delta F$ is primarily governed by $\delta_{\Delta C}$ (overall ~60% median contribution for the REA and ~52 - 56% for the gradient techniques). The uncertainties in REA sampling were on an average higher than those during MBR/AGM operation; and the percentage of flux data below the corresponding $\Delta C$ detection limit is slightly larger for REA (Fig. 10). In turn, the turbulent $\text{Hg}^0$ fluxes derived by the MBR (using temperature as proxy scalar) were comparatively more sensitive to varying micrometeorological conditions than the other gradient-based method (median 23.6% vs. 15.0% during IC #1 and IC #2).

5. Discussion

The estimated uncertainty of $\Delta C_{\text{REA}}$ is comparatively greater to the $\Delta C$ in gradient and chamber methods (Table 1). This is a major source that contributes to the greater overall uncertainty in REA-measured flux. One of the difficulties to accurately quantify $\Delta C_{\text{REA}}$ is that the $\text{Hg}^0$ concentration detected by REA apparatus may not truly represent the actual ambient concentration. However, this issue has not been investigated in earlier $\text{Hg}^0$ flux measurement using REA. During our campaign, we carefully investigated the
REA sampling conformity to this criterion. Although the scatter plot of $C_{REAC}^{\text{REA}}$ and $C_{Z_2}$ exhibits relatively good linear trend, the deviation from 1:1 line is significant ($p < 0.01$, Fig. 12).

The REA-system utilizes zero-air injection and is equipped with actuators to suppress pressure differentials to occur in the upstream zone of the fast-response sampling valves that promotes constant flow rate characteristics (Sommar et al., 2013b). This scheme (the effective sampling time per conditional channel is on an average ~39%) yielded substantially lower (~70%) Hg mass loadings per sample cycle (5 min) compared to concentration profile measurements. Furthermore, the conditional sampling volumes on undiluted basis are not static over time since moderate imbalances in up- and down-draft events normally occur during regular REA operation. In addition, the temporal variability of Hg$^0$ in ambient air is pronounced at the site. As mentioned in Section 3.1, the 2537B instrument coupled with REA was operated under a revised set of peak integration parameters to alleviate for low sample loadings to be addressed (Swartzendruber et al., 2009). From the estimation of bivariate kernel densities given in Fig. 12, there appears a tendency of a biased low response from the REA-CVAFS-system in the lowest concentration range ($C_{Z_2} \leq 3$ ng m$^{-3}$). The cluster of higher kernel densities here represents samples with systematic volume differences between the two conditional reservoirs. Therefore, we suggest that REA-system using Hg free air injection application should be operated with sampling cycles of increased duration (sampling volumes). Modifications facilitating QA/QC measures of the REA-system (Arnts et al., 2013) are also prompted for to pin-point the cause of this discrepancy. To address the performance of their Hg$^0$ REA-system, Cobos et al. (2002) used both open and integrated closed path infrared gas analysers to directly measure turbulent fluxes of water vapor by EC and REA respectively and whereby obtain a cross-comparison.
A disadvantage in coupling the flux measurement techniques with a single-channel gas analyser (e.g., Tekran 2537) is the temporally asynchronous samples obtained for the calculation of $\Delta C$. Under the shifting Hg$^0$ concentrations encountered, the asynchronous sampling uncertainties were found in general substantial for all of MM-techniques (Table 1). In some other studies (Edwards et al., 2005; Lee et al., 2000), simulations of the effect of sequential sampling indicated for AGM-derived Hg$^0$ fluxes a minor or non-significant contribution. For the application of the MBR-technique in forest ecosystems, Meyers et al. (1996) reported $\sim$15% relative uncertainty in the calculation of $\Delta C_{\text{grad}}$ due to intermittent sampling. For flux measurements, it is desirable to derive $\Delta C$ from synchronous samples, and therefore a dual-channel Hg$^0$ analyser with alternating pre-concentration of the analyte on a pair of gold traps for each channel (if such an instrument was commercially available) would be ideal.

There are additional sources contributing to the uncertainty and bias in Hg$^0$ flux measurements. For example, the estimation of DFCs flux bias was based on empirical model and therefore the results are subject to the limitation of the regression models. Application of MM techniques relies on the assumption of a non-divergent vertical flux (Loubet et al., 2009). However, the vertical flux measured at a height may differ from the actual flux at the surface as a consequence of either horizontal gradients (advection) or changes in storage (changes in concentration with time). Steen et al. (2009) and Fritsche et al. (2008) noted that inconsistent Hg$^0$ concentration gradients can occasionally occur and impair the surface flux derivation. Analogous, performing multiple-level Hg$^0$ concentration profiling, Edwards et al. (2005) reported large flux divergence to intermittently occur for one (cinnabar-enriched fault zone) out of several sites representing contrasting geological settings of Canada. However, in case of homogeneous substrate settings (comparable Hg content with this study), these author stated the effect of local advection yielding flux divergence to be small. In part I, we assessed that changes in storage had minor effect on the turbulent
fluxes as could be expected given the relative low measurement height and the relative magnitude of surface Hg\textsuperscript{0} efflux during this inter-comparison (Zhu et al. 2015).

6. Conclusions and recommendations

In this paper, five contemporary Hg\textsuperscript{0} flux measurement systems including two types DFCs (novel and traditional designs) and three types MM systems (REA, AGM, and MBR) have been characterized through a detailed measurement error analysis. It was found that the precision in concentration difference measurement poses a critical constraint on obtaining a larger fraction of significant Hg\textsuperscript{0} fluxes using MM methods. In-field determined precision of $\frac{\delta_{\Delta C}}{\Delta C}$ for MM-CVAFS systems in the range 1.8%-2.1% (gradient) and 4.2%-4.4% (REA) based on ambient air median Hg\textsuperscript{0} concentrations during the campaigns. Accordingly, ~38%-43% of the gradient flux data and 45% of the REA flux data were not significantly different from zero. Since the concentration differences were acquired from asynchronous samples, we estimated the corresponding uncertainty caused by the asynchronous measurement in the MM-techniques to be 33%-62% of total uncertainty. Short-term variability in Hg\textsuperscript{0} concentration contributes significantly to the uncertainty level in DFC-derived flux, which rendered a majority of night-time fluxes to be non-significant. The highest DFCs flux bias runs up to ~10% of the Hg\textsuperscript{0} flux but for ~85% of the observations the absolute uncertainty ranged from -2 to 2 ng m\textsuperscript{-2} h\textsuperscript{-1}. The flux bias of NDFC and TDFC methods show a distinct diurnal cycle.

The highest relative median flux uncertainty was observed for REA-technique (24%, IC #2), followed by 24% and 15% for MBR, and 15% and 12% for AGM during IC #1 & #2 respectively. Overall, a higher imprecision in Hg\textsuperscript{0} concentration measurement during REA application indicates technical limitations in accurately isolating conditional samples in our system. The precision requirements for the involved
measurement systems to resolve flux with regard to atmospheric stability and measurement heights obtained in this study provide a guideline for future application. It is indicated that flux-gradient based techniques (MBR & AGM) may well be deployed in favour of a REA-system to quantify Hg\textsubscript{0} air-ecosystem exchange over low vegetation. The incapability to obtain temporally synchronous samples for the calculation of Hg\textsubscript{0} concentration difference in flux measurement impairs the accuracy of MM-derived fluxes under short-term varying concentration of ambient Hg\textsubscript{0}. For future applications especially under non-background field conditions, it is therefore recommended to accomplish $\Delta C$-derivation from simultaneous collected samples.

### Nomenclature

<table>
<thead>
<tr>
<th>Symbols</th>
<th>Explanation</th>
<th>Unit</th>
</tr>
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<tbody>
<tr>
<td>$A$</td>
<td>Dynamic flux chamber footprint</td>
<td>m\textsuperscript{2}</td>
</tr>
<tr>
<td>$AP_x$</td>
<td>Atmospheric parameter for flux measurement method x (*)</td>
<td>h m\textsuperscript{-1}</td>
</tr>
<tr>
<td>$C_z$</td>
<td>Ambient Hg\textsubscript{0} concentration at measurement height $z$ (gradient-based methods)</td>
<td>ng m\textsuperscript{-3}</td>
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<tr>
<td>$C_{out}$</td>
<td>Hg\textsubscript{0} concentration in DFC outlet air</td>
<td>ng m\textsuperscript{-3}</td>
</tr>
<tr>
<td>$C_{in}$</td>
<td>Hg\textsubscript{0} concentration in DFC inlet air</td>
<td>ng m\textsuperscript{-3}</td>
</tr>
<tr>
<td>$c_p$</td>
<td>Specific heat of air at constant pressure</td>
<td>J kg\textsuperscript{-1} K\textsuperscript{-1}</td>
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<tr>
<td>$\Delta C$</td>
<td>Hg\textsubscript{0} concentration difference (non-specific)</td>
<td>ng m\textsuperscript{-3}</td>
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<tr>
<td>$\Delta C_{REA}$</td>
<td>Method-specific analyser concentration difference resolution</td>
<td>ng m\textsuperscript{-3}</td>
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<td>$\Delta C_{grad.}$</td>
<td>Vertical Hg\textsubscript{0} concentration gradient</td>
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<td>Time-averaged Hg\textsubscript{0} concentration difference between conditional samples ($\Delta C_{REA} = C^\uparrow - C^\downarrow$)</td>
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<tr>
<td>$\Delta C_{enclosure}$</td>
<td>Difference in Hg\textsubscript{0} concentration between DFC outlet and inlet air</td>
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<td>$\Delta C_{blank}$</td>
<td>Difference in Hg\textsubscript{0} concentration between DFC outlet and inlet air when measuring DFC blank from an inert surface</td>
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<td>$C^{\uparrow\downarrow}$</td>
<td>Conditionally sampled Hg\textsubscript{0} concentration for updraft/downdraft air parcels (corrected for dilution by zero air injection) measured at height $z$</td>
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</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
<td>Unit</td>
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<tr>
<td>$C^{REA}$</td>
<td>Average Hg$^0$ concentration in accumulated up- and down-drafts measured at height $z$</td>
<td>ng m$^{-3}$</td>
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<tr>
<td>$d$</td>
<td>Zero plane displacement height</td>
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<td>$D_{Hg^0,\text{air}}$</td>
<td>Hg$^0$ diffusivity in air</td>
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<td>$f_w$</td>
<td>Similarity function for the standard deviation of vertical wind velocity</td>
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<td>$F^{TDFC}$</td>
<td>Hg$^0$ flux gauged by the traditional DFC (TDFC) method</td>
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</tr>
<tr>
<td>$F^{NDFC}$</td>
<td>Hg$^0$ flux gauged by the novel DFC (NDFC) method</td>
<td>ng m$^{-2}$ h$^{-1}$</td>
</tr>
<tr>
<td>$F^{REA}</td>
<td>_z$</td>
<td>Turbulent Hg$^0$ flux gauged by the REA method (at measurement height $z$)</td>
</tr>
<tr>
<td>$F^{MBR}$</td>
<td>Turbulent Hg$^0$ flux gauged by the MBR method</td>
<td>ng m$^{-2}$ h$^{-1}$</td>
</tr>
<tr>
<td>$F^{AGM}$</td>
<td>Turbulent Hg$^0$ flux gauged by AGM measurements</td>
<td>ng m$^{-2}$ h$^{-1}$</td>
</tr>
<tr>
<td>$\hat{F}^{DFC}$</td>
<td>Predicted Hg$^0$ DFC flux from empirical model using chamber internal environmental variables as input</td>
<td>ng m$^{-2}$ h$^{-1}$</td>
</tr>
<tr>
<td>$\hat{F}^{N}$</td>
<td>Predicted Hg$^0$ DFC flux from empirical model using ambient environmental variables as input</td>
<td>ng m$^{-2}$ h$^{-1}$</td>
</tr>
<tr>
<td>$</td>
<td>F</td>
<td>$</td>
</tr>
<tr>
<td>$H$</td>
<td>Sensible heat flux ($H = \rho \cdot c_p \cdot \overline{w \cdot T}$)</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$H_s$</td>
<td>Buoyancy heat flux ($\rho \cdot c_p \cdot \overline{w \cdot T_s}$)</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>$k_{\text{mass}( a )}$</td>
<td>Overall mass transfer coefficient under atmospheric condition</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$k_{\text{mass}( m )}$</td>
<td>Overall mass transfer coefficient in the NDFC</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$K_H$</td>
<td>Turbulent diffusion coefficient of sensible heat</td>
<td>m$^2$ s$^{-1}$</td>
</tr>
<tr>
<td>$L$</td>
<td>Monin-Obukhov length</td>
<td>m</td>
</tr>
<tr>
<td>$m_i^{z/4}$</td>
<td>Mass of Hg$^0$ collected in accumulated up-/down-draft sample $i$</td>
<td>pg</td>
</tr>
<tr>
<td>$Q$</td>
<td>DFC flushing flow rate</td>
<td>m$^3$ h$^{-1}$</td>
</tr>
<tr>
<td>$Q_i^{z/4}$</td>
<td>Flow rate through the up-/down-draft channels for sample $i$</td>
<td>L min$^{-1}$</td>
</tr>
<tr>
<td>$\mathbb{R}$</td>
<td>Uncertainty level in the flux measurement</td>
<td>–</td>
</tr>
<tr>
<td>$Re$</td>
<td>Reynolds number</td>
<td>–</td>
</tr>
<tr>
<td>$S$</td>
<td>Irradiance</td>
<td>W m$^{-2}$</td>
</tr>
<tr>
<td>Variable</td>
<td>Definition</td>
<td>Unit</td>
</tr>
<tr>
<td>----------</td>
<td>------------</td>
<td>------</td>
</tr>
<tr>
<td>$T_i$</td>
<td>Time duration of up-/down-draft sample $i$</td>
<td>min</td>
</tr>
<tr>
<td>$T_z$</td>
<td>Air temperature at height $z$</td>
<td>K</td>
</tr>
<tr>
<td>$T_s$</td>
<td>Sonic air temperature</td>
<td>K</td>
</tr>
<tr>
<td>$T_z^{\uparrow/\downarrow}$</td>
<td>Conditionally sampled $T_s$ for updraft/downdraft air parcels</td>
<td>K</td>
</tr>
<tr>
<td>$\Delta T_{s,REA}$</td>
<td>Time-averaged $T_s$ difference between conditional samples</td>
<td>K</td>
</tr>
<tr>
<td>$\Delta T_{s,REA} = T_s^{\uparrow} - T_s^{\downarrow}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$T_{soil}$</td>
<td>Surface soil temperature</td>
<td>°C</td>
</tr>
<tr>
<td>$\Delta T_{\text{grad.}}$</td>
<td>Vertical air temperature gradient</td>
<td>K</td>
</tr>
<tr>
<td>$u_s$</td>
<td>Friction velocity</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$w$</td>
<td>Vertical component of the wind velocity</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$W_{DB}$</td>
<td>Vertical wind deadband threshold for conditional sampling</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$\overline{wT'}$</td>
<td>Kinematic heat flux</td>
<td>K m s$^{-1}$</td>
</tr>
<tr>
<td>$w_{x'}$</td>
<td>$w$ averaged over time interval $x'$ ( $x' = 5$ or $20$ min)</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$z$</td>
<td>Sampling height (above ground level)</td>
<td>m</td>
</tr>
<tr>
<td>$z_0$</td>
<td>Surface roughness height</td>
<td>m</td>
</tr>
<tr>
<td>$\alpha_i^{\uparrow/\downarrow}$</td>
<td>Fraction of total time the up- or down-draft isolation valves were activated during sample $i$</td>
<td>%</td>
</tr>
<tr>
<td>$\beta_i$</td>
<td>Relaxation coefficient used in REA method (derived for generic scalar $s$, in this work $\beta_i$ was used).</td>
<td>–</td>
</tr>
<tr>
<td>$\gamma$</td>
<td>Dimensionless constant</td>
<td>–</td>
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<tr>
<td>$\delta_x$</td>
<td>Uncertainty for specific parameter or flux measurement method “$x$”</td>
<td>Follows the units of “$x$”</td>
</tr>
<tr>
<td>$\delta_{\Delta C_{\text{MM}}}$</td>
<td>Uncertainty in concentration difference measurement for MM (REA or gradient) flux methods: $\delta_{\Delta C_{\text{MM}}} = \sqrt{\left(\delta_{\Delta C_{\text{MM}}}^{\text{channel}}\right)^2 + \left(\delta_{\Delta C_{\text{MM}}}^{\text{IS}}\right)^2}$</td>
<td>ng m$^{-3}$</td>
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<tr>
<td>$\delta_{\Delta C_{\text{MM}}}^{\text{channel}}$</td>
<td>Uncertainty in concentration difference measurement due to gas sampling channels for MM (REA or gradient) flux methods</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\delta_{\Delta C_{\text{MM}}}^{\text{IS}}$</td>
<td>Uncertainty in concentration difference measurement due to intermittent sampling for MM (REA or gradient) flux methods</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
<td>Unit</td>
</tr>
<tr>
<td>--------</td>
<td>-------------</td>
<td>------</td>
</tr>
<tr>
<td>$\delta_{\Delta C_{\text{enclosure}}}$</td>
<td>Combined uncertainty in $\Delta C_{\text{enclosure}}$ due to intermittent sampling of DFC inlet and outlet air as well as DFC blank determination:</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\delta_{\Delta C_{\text{enclosure}}}^{\text{IS}}$</td>
<td>Uncertainty in $\Delta C_{\text{enclosure}}$ due to intermittent sampling of DFC inlet and outlet air</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\delta_{\Delta C_{\text{blank}}}$</td>
<td>Uncertainty in the DFC blank measurement</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\varepsilon_x$</td>
<td>Bias for specific parameter or flux measurement method “$x$”</td>
<td>–</td>
</tr>
<tr>
<td>$\zeta$</td>
<td>Atmospheric stability parameter: $\zeta = (z - d)/L$</td>
<td>–</td>
</tr>
<tr>
<td>$\kappa$</td>
<td>von Kármán constant</td>
<td>–</td>
</tr>
<tr>
<td>$\nu_t$</td>
<td>Transfer velocity (used in the AGM technique)</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$\sigma_w$</td>
<td>Standard deviation of $w$</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$\overline{\sigma_{w,x'}}$</td>
<td>$\sigma_w$ averaged over time interval $x'$ ($x' = 5$ or $20$ min)</td>
<td>m s$^{-1}$</td>
</tr>
<tr>
<td>$\rho$</td>
<td>Air density</td>
<td>kg m$^{-3}$</td>
</tr>
<tr>
<td>$\tau$</td>
<td>Momentum flux</td>
<td>kg m$^{-1}$ s$^{-2}$</td>
</tr>
<tr>
<td>$\psi_H$</td>
<td>Integrated universal function for heat</td>
<td>–</td>
</tr>
</tbody>
</table>

Notes: (*) The “atmosphere parameter” can be specified as $4/[5 \cdot \beta_s \cdot f_w (\zeta_s)]$ and $\left[ \ln \left( \frac{z_2 - d}{z_1 - d} \right) - \psi_H (\zeta_2) + \psi_H (\zeta_1) \right]/\kappa$ for REA and gradient methods respectively, where the similarity functions of $\sigma_w (f_w (\zeta))$ and $\psi_H (\zeta)$ were adopted from Rowe et al. (2011) and Businger et al. (1971) respectively.

**Acknowledgements**

This research was financially supported by “973 Program” (2013CB430002), National Science Foundation of China (41030752), Chinese Academy of Sciences through an instrument development program (YZ200910), and the State Key Laboratory of Environmental Geochemistry. We would like
to express our gratitude to the staff from Yucheng Comprehensive Experimental Station, Chinese Academy of Sciences for sampling and logistical assistance.

References


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### Table 1: Estimated Hg⁰ flux bias and uncertainties of inter-compared DFCs and MM flux measurement techniques

<table>
<thead>
<tr>
<th>Methods</th>
<th>Sources of errors</th>
<th>Flux bias</th>
<th>Flux uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>REA</td>
<td>Inadequacy of on-line filtering the ( \vec{w} )-signal from ( \vec{w} )-bias</td>
<td>Overestimated: 9.7% ± 14.5%</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sensor separation, lag time and smearing of conditionally sampled eddies</td>
<td>Underestimated &lt;2%</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Sensible heat flux measurement</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Conditional sampling channels</td>
<td>Overestimated: 5.1%</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Intermittent conditional sampling</td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Conditional sampled sonic temperature</td>
<td></td>
<td></td>
</tr>
<tr>
<td>MBR</td>
<td>Concentration gradient sampling</td>
<td>Underestimated: 4.1%</td>
<td>7.2 ± 6.2%</td>
</tr>
<tr>
<td></td>
<td>Intermittent sampling of conc. gradient</td>
<td>4.6 ± 11.3%</td>
<td>4.6 ± 12.3%</td>
</tr>
<tr>
<td></td>
<td>Sensible heat flux</td>
<td>18.0 ± 49.7%</td>
<td>9.9 ± 12.7%</td>
</tr>
<tr>
<td></td>
<td>Temperature gradient</td>
<td>≤ 0.4%</td>
<td>≤ 0.4%</td>
</tr>
<tr>
<td>AGM</td>
<td>Concentration gradient sampling</td>
<td>Underestimated: 4.1%</td>
<td>7.2 ± 6.2%</td>
</tr>
<tr>
<td></td>
<td>Intermittent sampling of conc. gradient</td>
<td>4.6 ± 11.3%</td>
<td>4.6 ± 12.3%</td>
</tr>
<tr>
<td></td>
<td>Friction velocity</td>
<td>9.1 ± 10.6%</td>
<td>5.5 ± 5.6%</td>
</tr>
<tr>
<td></td>
<td>Transfer velocity</td>
<td>10.9 ± 12.6%</td>
<td>6.1 ± 10.2%</td>
</tr>
<tr>
<td>NDFC</td>
<td>Micro-environmental effect</td>
<td>-7.2 - 10.6 ng m⁻² h⁻¹</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Intermittent sampling</td>
<td>2.1 ng m⁻² h⁻¹</td>
<td></td>
</tr>
<tr>
<td>TDFC</td>
<td>Micro-environmental effect</td>
<td>-0.6 - 6.7 ng m⁻² h⁻¹</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Intermittent sampling</td>
<td>2.8 ng m⁻² h⁻¹</td>
<td></td>
</tr>
</tbody>
</table>

Notes: For MM techniques, bias and uncertainties are given as fractional values (percent) of the flux representing the median ± 1.48・IQR, while for the enclosure techniques the absolute values are given.
Fig. 1. (a) Upper panel: Lin-log scatter plot of observed friction velocity ($u_*$) versus aerodynamic stability ($\zeta = (z - d)/L$) during the IC #1. The dashed lines indicate the parameterisation $u_* = \ell(\zeta)$ used for calculations of analyser resolution requirements for the MM-techniques; (b) Lower panel: comparison of the required sensor resolution (expressed as $\Delta F = \left[ \frac{\Delta F}{F} \right]$) as a function of stability for REA, gradient-based and enclosure methods (double logarithmic plot).

Fig. 2. Frequency distribution of DFCs flux bias ($\epsilon_{DFC}$) for TDFC and NDFC methods during IC #1.

Fig. 3. Box-whisker plots of diurnal flux bias measured with two DFCs. The box boundaries represent 25th, and 75th percentiles from bottom to top, and whiskers indicate 10th and 90th percentiles of Hg$^0$ flux. Line in the box and plots out of the whiskers indicate mean and bias threshold.

Fig. 4. Scatter plot of $\beta_T$-factor derived from actual REA sampling (filled blue circles) and from a posteriori off-line synthesis (filled yellow circles) versus buoyancy heat flux. The inlaid line (magenta-colored) represents the predicted $\beta_T$ (0.448) for a dynamic deadband discrimination factor of 0.3 (Ammann and Meixner, 2002).

Fig. 5. Scatter plot of fractional uncertainty in sensible heat flux ($\delta_H/H$) segregated into turbulence quality classes (Mauder and Foken, 2004) versus the corresponding flux during IC #2.

Fig. 6. Results from conditional channel inter-comparison using REA reference sampling mode (slope: 1.051, intercept: -0.012). The 1:1 slope was inlaid with the orthogonal linear fit.

Fig. 7. Histogram of residuals obtained after correcting the channel data for bias with orthogonal linear regression (right). Scatterplot of residuals versus Hg$^0$ concentration (indicated by the predicted concentration of the downdraft channel). The blue lines (uncertainty range around zero) are derived from linear regression of the moduli of residuals.
Fig. 8. Scatter plot of concentration from lower and upper level sampling line during side-by-side measurement. The linear fit derives from orthogonal regression. The 1:1-relationship and 95% prediction intervals are indicated by dashed lines (light blue and red colour respectively).

Fig. 9. Relationship between fractional uncertainty in momentum flux ($\tau$) and friction velocity ($u_\tau = \sqrt{\tau/\rho}$) for turbulence quality segregated data.

Fig. 10. Turbulent Hg$^0$ fluxes measured by the REA (upper panel) and the MBR (lower panel) technique during the second inter-comparison campaign. Error bars denote flux uncertainties derived from the analysis. The open grey circles represent Hg$^0$ fluxes that are made up of $\Delta C_{REA}$ and $\Delta C_{grad}$, falling below their respective 1-$\sigma$ detection limit.

Fig. 11. Box-whisker plots of the hourly fractional flux bias ($\delta_F$/$F$) estimated for MM-techniques inter-compared during IC #2. Boxes encompass the interquartile range (IQR, 25th to 75th quantiles) and the horizontal line within the median value. The length of a whisker is 1.5 times of IQR.

Fig. 12. Linear regression of the Hg$^0$ concentrations measured by the REA system ($C^{REA}$) versus the concentrations measured by the concentration gradient upper intake ($C_{Z2}$) at the same height (2.96 m). Fitting functions are shown for both orthogonal (black solid line) and standard (violet solid line) linear regression. The scatterplot includes quantile density contours based on a bivariate kernel density estimation.
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