

1 **Competition between water uptake and ice nucleation by**  
2 **glassy organic aerosol particles**

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4 **T. Berkemeier<sup>1,2,\*</sup>, M. Shiraiwa<sup>1</sup>, U. Pöschl<sup>1</sup> and T. Koop<sup>2,\*</sup>**

5 [1] Multiphase Chemistry Department, Max Planck Institute for Chemistry, Mainz, Germany

6 [2] Faculty of Chemistry, Bielefeld University, Bielefeld, Germany

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8 Correspondence to: T. Berkemeier ([t.berkemeier@mpic.de](mailto:t.berkemeier@mpic.de))

9 T. Koop ([thomas.koop@uni-bielefeld.de](mailto:thomas.koop@uni-bielefeld.de))

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14 **Abstract**

15 Organic aerosol particles play a key role in climate by serving as nuclei for clouds and  
16 precipitation. Their sources and composition are highly variable, and their phase state ranges  
17 from liquid to solid under atmospheric conditions, affecting the pathway of activation to cloud  
18 droplets and ice crystals. Due to slow diffusion of water in the particle phase, organic  
19 particles may deviate in phase and morphology from their thermodynamic equilibrium state,  
20 hampering the prediction of their influence on cloud formation. We overcome this problem by  
21 combining a novel semi-empirical method for estimation of water diffusivity with a kinetic  
22 flux model that explicitly treats water diffusion. We estimate timescales for particle  
23 deliquescence as well as various ice nucleation pathways for a wide variety of organic  
24 substances, including secondary organic aerosol (SOA) from the oxidation of isoprene,  $\alpha$ -  
25 pinene, naphthalene, and dodecane. The simulations show that in typical atmospheric  
26 updrafts, glassy states and solid/liquid core-shell morphologies can persist for long enough  
27 that heterogeneous ice nucleation in the deposition and immersion mode can dominate over  
28 homogeneous ice nucleation. Such competition depends strongly on ambient temperature and  
29 relative humidity as well as humidification rates and particle sizes. Reflecting difference in  
30 glass transition temperature, hygroscopicity and atomic O/C ratio of SOA, naphthalene SOA  
31 particles have the highest potential to act as heterogeneous ice nuclei. Our findings  
32 demonstrate that kinetic limitations of water diffusion into organic aerosol particles are likely  
33 to be encountered under atmospheric conditions and can strongly affect ice nucleation  
34 pathways. For the incorporation of ice nucleation by organic aerosol particles into  
35 atmospheric models, our results demonstrate a demand for model formalisms that account for  
36 the effects of molecular diffusion and describe ice nucleation onsets not only as a function of  
37 temperature and relative humidity, but also include updraft velocity, particle size and  
38 composition.

## 39 1 Introduction

40 Atmospheric aerosol particles influence climate through affecting the earth's radiation budget  
41 directly by scattering and absorbing light, and indirectly by acting as nuclei for cloud droplets  
42 and ice crystals (Yu et al., 2006; Andreae and Rosenfeld, 2008; IPCC, 2013). Ice nucleation is  
43 an important pathway for high-altitude cirrus cloud formation and it occurs either  
44 homogeneously in liquid aerosol particles or heterogeneously in the presence of active ice  
45 nuclei (IN), which are solid particles that facilitate nucleation. Homogeneous ice nucleation  
46 generally requires high supersaturations in aqueous aerosol droplets, occurring at ice  
47 saturation ratios of  $S_{\text{ice}} \geq 1.4$  (Koop et al., 2000). Only a small fraction of atmospheric aerosol  
48 particles act as IN below this homogeneous ice nucleation threshold (DeMott et al., 2003;  
49 Cziczo et al., 2013). Heterogeneous ice nucleation can occur via several pathways such as  
50 deposition nucleation, i.e. deposition of gaseous water molecules to form crystalline ice on a  
51 solid IN, or immersion freezing, which describes nucleation induced by IN immersed in  
52 supercooled aqueous droplets (Pruppacher and Klett, 1997; Hoose and Möhler, 2012).

53 Organic aerosol particles are ubiquitous and abundant in the atmosphere, but traditionally are  
54 not referred to as effective IN when compared to dust or biological particles (see Hoose and  
55 Möhler (2012) and references therein). More recently, however, several laboratory studies  
56 have shown that glassy organic particles can act as IN at low-temperature cirrus conditions in  
57 the deposition mode or at slightly elevated temperatures in the immersion mode (Murray et  
58 al., 2010; Wagner et al., 2012; Wang et al., 2012; Wilson et al., 2012; Baustian et al., 2013;  
59 Schill et al., 2014), in agreement with inferences from field data (Froyd et al., 2010; Knopf et  
60 al., 2010; Knopf et al., 2014). This IN ability has been observed for a number of different  
61 types of particles composed of pure organic substances such as simple sugars and acids  
62 (Murray et al., 2010; Wagner et al., 2012; Wilson et al., 2012; Baustian et al., 2013) and  
63 biomass burning marker compounds (Wagner et al., 2012; Wilson et al., 2012), for (phase-  
64 separated) organic-inorganic mixtures (Wagner et al., 2012; Wilson et al., 2012; Baustian et  
65 al., 2013; Schill and Tolbert, 2013), as well as for SOA particles derived from aromatic VOCs  
66 (Wang et al., 2012) or emerging from aqueous phase reactions (Schill et al., 2014). It has also  
67 been proposed recently that formation of highly porous structures upon atmospheric freeze-  
68 drying could enhance the IN ability of organic aerosol particles (Adler et al., 2013).

69 These observations suggest a connection between particle phase state and the resulting  
70 predominant ice nucleation pathway (Murray et al., 2010). Organic aerosol particles can adopt

71 liquid, semisolid or solid states, or may even exhibit mixed phases, depending on composition  
72 and ambient conditions (Mikhailov et al., 2009; Koop et al., 2011; Vaden et al., 2011; Kuwata  
73 and Martin, 2012; Perraud et al., 2012; Song et al., 2012; You et al., 2012; Renbaum-Wolff et  
74 al., 2013; Kidd et al., 2014). SOA particles are expected to be liquid at high temperature and  
75 high humidity, but are very likely to exhibit a highly viscous semisolid or even glassy state at  
76 low temperature and low humidity (Virtanen et al., 2010; Saukko et al., 2012; Renbaum-  
77 Wolff et al., 2013; Shiraiwa et al., 2013a). For example, typical  $\alpha$ -pinene derived secondary  
78 organic aerosol particles are expected to be in a glassy state below about 260 K at 30 %  
79 relative humidity, whereas at a higher humidity of 80 %, such glass transition is expected at  
80 approximately 215 K (Koop et al., 2011). Glassy states are characterized by viscosities greater  
81 than  $10^{12}$  Pa s, corresponding to diffusion time scales within these particles that can exceed  
82 days or even years (Shiraiwa et al., 2011; Koop et al., 2011; Zhou et al., 2013). Water uptake  
83 into glassy aerosols has been shown to occur slowly and to proceed gradually with increasing  
84 relative humidity (Mikhailov et al., 2009; Tong et al., 2011; Zobrist et al., 2011; Bones et al.,  
85 2012; Price et al., 2014).

86 Hence, several competing processes can occur in glassy organic aerosol particles during  
87 updraft of an air parcel: Heterogeneous ice nucleation in the deposition mode onto the glassy  
88 solid aerosol surface; diffusion of water into the particle, inducing a gradual phase transition  
89 towards the liquid state; and immersion freezing during the transition between both states. In  
90 order to determine those atmospheric conditions at which one of these processes dominates,  
91 we employ a numerical aerosol diffusion model based on the kinetic multi-layer model for  
92 gas-particle interactions in aerosols and clouds (KM-GAP), which explicitly treats mass  
93 transport of water molecules in the gas and particle phases (Shiraiwa et al., 2012). Due to  
94 experimental constraints associated with very long observation times, parameterizations for  
95 water diffusivity in glassy organic material are sparse and hence are only known for a few  
96 model compounds. Therefore, water diffusivity in SOA materials from various biogenic and  
97 anthropogenic precursors are deduced from water diffusivity parameterizations of model  
98 compounds using a semi-empirical physico-chemical model of water diffusion in glass-  
99 forming aqueous organics.

100

## 101 2 Modelling approach

### 102 2.1 Numerical diffusion model

103 The numerical diffusion model employed in this study is based on the kinetic multi-layer  
104 model for gas-particle interactions in aerosols and clouds, KM-GAP (Shiraiwa et al., 2012).  
105 KM-GAP consists of multiple model compartments and layers, respectively: gas phase, near-  
106 surface gas phase, sorption layer, surface layer, near-surface bulk, and a number of  $n$  bulk  
107 layers (cf. Fig. S1 in the supplementary material). The following processes are considered in  
108 KM-GAP: gas phase diffusion, gas-surface transport, surface-bulk transport, and bulk  
109 diffusion. The bulk layers can either grow or shrink in response to mass transport. The initial  
110 bulk layer sizes are chosen small enough to ensure numerical convergence (usually 100-750  
111 layers), but are not allowed to fall below the molecular length scale ( $\sim 0.3$  nm).

112 The model was complemented by modules predicting homogeneous ice nucleation as a  
113 function of water activity according to Koop et al. (2000), heterogeneous ice nucleation at a  
114 pre-defined ice supersaturation level, and it considers Kelvin effects. Moreover, a few further  
115 conceptual changes have been introduced to the original KM-GAP, including a more explicit  
116 treatment of gas diffusion, composition-based bulk diffusion and a mechanism of surface-to-  
117 bulk transport facilitated by surface-adsorbed water, as detailed in the following sections.  
118 Parameterizations of composition-dependent density, water activity and bulk diffusivity for  
119 the sucrose/water system have been adopted from Zobrist et al. (2011). A detailed description  
120 of the gas diffusion scheme and a list of all employed parameterizations are provided as  
121 supplementary material.

122 In this study, the model is used to simulate an atmospheric updraft situation by following a  
123 preselected trajectory in temperature, relative humidity and pressure. It tracks the chemical  
124 composition of an amorphous aerosol particle as a function of time and depth below the  
125 particle surface in discretized layers, providing concentration profiles of water and organics at  
126 any given time. The equilibrium composition is calculated through a water activity  
127 parameterization that translates ambient relative humidity into equilibrium mass fractions of  
128 the bulk constituents. Mass fluxes from the far-surface into the near-surface gas phase, onto  
129 the particle surface, into as well as between bulk layers are coupled in flux-based differential  
130 equations, which are solved with an ordinary differential equation solver using Matlab  
131 software (ode23tb).

## 132 2.1.1 Ice nucleation modules

133 Besides water diffusion, the model is able to simulate ice nucleation and growth. However,  
134 the initial numerical solution of the differential equations treats merely water uptake into the  
135 particle. The model registers an ice nucleation event when all necessary conditions in ambient  
136 relative humidity and water activity are satisfied. From this point onwards, the model  
137 simulates ice crystal growth by deposition of water molecules from the gas phase.

138 For homogeneous ice nucleation, a stochastic approach based on classical nucleation theory  
139 has been chosen. An ice nucleation event is triggered when the probability of the particle  
140 being liquid ( $P_{\text{liq}}$ ) falls below 50 %.  $P_{\text{liq}}$  is the product of the individual probabilities in all  $n$   
141 layers, using the homogeneous nucleation rate coefficient for each layer  $J_{\text{hom},n}$  as  
142 parameterized by Koop et al. (2000). The nucleation rate then translates into  $P_{\text{liq}}$  by  
143 multiplication with layer volume  $V_n$  and (numerical) integration time step  $dt$ :

$$P_{\text{liq,tot}}(t) = \int_{t_0}^t \prod_{n=1}^L (1 - J_{\text{hom},n}(t) \cdot V_n(t)) dt \quad (1)$$

144 Heterogeneous nucleation is assumed to occur once a certain freezing threshold is exceeded.  
145 In this work, we distinguish between heterogeneous ice nucleation thresholds for sucrose and  
146 SOA, which have been shown to occur at different ice supersaturations, as summarized by  
147 Schill et al. (2014). For sucrose, we apply a linear fit to nucleation data from Baustian et al.  
148 (2013), whereas for SOA we fit the nucleation data of naphthalene SOA from Wang et al.  
149 (2012) and those of aqSOA from Schill et al. (2014). The fit results are shown in Fig. A1 in  
150 Appendix A.

151 To distinguish between deposition and immersion freezing, additional criteria are employed.  
152 For deposition nucleation, the necessary condition is solidness of the outermost layer of the  
153 particle, requiring the water activity to be below the quasi-equilibrium glass transition point.  
154 In case of immersion mode nucleation, a 1 nm thick region in the near-surface bulk is  
155 required to be entirely liquefied before nucleation can occur in the immersion mode. For this  
156 purpose, a 2 nm thick region below the particle surface is finely resolved by multiple bulk  
157 layers (cf. Fig. S1).

## 158 2.1.2 Bulk diffusion and bulk layer mixing

159 Bulk diffusion of water is treated as kinetic flux  $J_{bk,bk\pm 1}$  from one bulk layer ( $bk$ ) to the next  
160 ( $bk\pm 1$ ). Because layer thickness is not allowed to fall below molecular resolution,  
161 concentrations in adjacent layers can differ significantly. As in Zobrist et al. (2011), this  
162 heterogeneity is accounted for with a virtual mixing scheme for the determination of bulk  
163 diffusivities between layers. In this scheme, the composition of a mixture of two subsequent  
164 bulk layers is determined and the bulk diffusion coefficient calculated according to the  
165 effective composition along the diffusion path. Scenarios with very low diffusivities and  
166 hence steep concentration gradients thus lead to situations in which a liquefied layer (high  
167 bulk diffusivity of water,  $D_{H_2O}$ ) “softens” the subsequent glassy layer (low  $D_{H_2O}$ ), facilitating  
168 further diffusion. Such a process can be seen analogously to a dissolution process, in which  
169 the glassy matrix dissolves into nearby water-rich regions.

170 Diffusion of the organic matrix has been neglected for this study, because the organic  
171 molecules investigated here can be expected to diffuse much slower than water molecules.  
172 Also, in the glassy state, the organic molecules diffuse on a much longer timescale compared  
173 to the experimental time scale of minutes to hours [cf. Shiraiwa et al. (2011), Koop et al.  
174 (2011)].

## 175 2.1.3 Surface monolayers and surface softening

176 The original KM-GAP uses a double monolayer approach to describe the particle surface,  
177 comprising a sorption layer and a quasi-static surface layer. In this study the quasi-static  
178 surface layer was replaced by a near-surface volume layer similar to that used in Shiraiwa et  
179 al. (2013a), which is more suitable for systems with low diffusivity.

180 Surface-adsorbed water can lead to softening of the solid surface (Koop et al., 2011), thereby  
181 facilitating exchange between surface and first near-surface bulk layer. In the model, this is  
182 accounted for by introducing a surface softening scheme that estimates the surface-to-bulk  
183 transport rate by mixing a hypothetical water monolayer with a hypothetical bulk monolayer  
184 containing water and bulk material. Using the momentary molar fractions of water ( $x_{b1,H_2O}$ )  
185 and organics ( $x_{b1,org}$ ) of the near-surface bulk layer, the effective surface coverages of water  
186 ( $\theta_{ss,H_2O}$ ) and organics ( $\theta_{ss,org}$ ) at the surface bulk layer can be described as:

$$\theta_{ss,i} = \frac{x_{b1,i} \cdot \sigma_i}{x_{b1,org} \cdot \sigma_{org} + x_{b1,H2O} \cdot \sigma_{H2O}} \quad (2)$$

187 where  $\sigma_i$  is the molecular cross section of species  $i$  [i.e. water (H<sub>2</sub>O) or organics (org)],  
 188 respectively. The weight fraction of organics in the “softened” surface is then given by:

$$w_{ss,org,mix} = \frac{\frac{\theta_{ss,org}}{\sigma_{org}} \cdot M_{org}}{\frac{\theta_{ss,org}}{\sigma_{org}} \cdot M_{org} + \left(\frac{\theta_{ss,H2O} + 1}{\sigma_{H2O}}\right) \cdot M_{H2O}} \quad (3)$$

189 where  $M_{org}$  and  $M_{H2O}$  are the molar mass of organics and water. This process facilitates the  
 190 initial water uptake into a glassy particle and leads (in most cases) to a sub-surface layer that  
 191 is in equilibrium with the surrounding gas phase. In the temperature range relevant for  
 192 immersion freezing, liquefaction of the surface was always obtained at the quasi-equilibrium  
 193 glass transition point due to the surface softening mechanism. At lower temperatures however  
 194 (deposition regime), the particle surface was not always in quasi-equilibrium with ambient  
 195 humidity.

196

## 197 **2.2 Estimation of water diffusivity in SOA**

198 For model systems other than sucrose/water, no direct parameterization of water diffusivity in  
 199 the full atmospherically relevant temperature and composition range is available to date. For  
 200 compounds chemically similar to sucrose (i.e. organic polyols and acids), we present a  
 201 scheme that enables estimation of bulk diffusivity data from glass transition and  
 202 hygroscopicity data. Bulk diffusivity of water is parameterized using a Vogel-Fulcher-  
 203 Tamman (VFT) approach (Vogel, 1921; Fulcher, 1925; Tamman and Hesse, 1926). The  
 204 estimation scheme utilizes the structure of the VFT equation, Eq. (S9), and the physical  
 205 interpretation of its parameters. The method can be described by the following set of  
 206 assumptions:

- 207 1. Two similar organic substances act similar in the way they approach the glass  
 208 transition and thus have a similar fragility:  $B_{org,1} \approx B_{org,2}$ .
- 209 2. The same two substances have a similar diffusion coefficient in the high temperature  
 210 limit:  $A_{org,1} \approx A_{org,2}$ .

211 3. A difference in glass transition temperatures between the two substances indicates a  
212 difference in Vogel temperatures of same direction and (relative) magnitude

$$\frac{T_{0,\text{org},1}}{T_{0,\text{org},2}} \approx \frac{T_{g,\text{org},1}}{T_{g,\text{org},2}} \quad (4)$$

213 Thus, diffusivities within an organic substance can be estimated by knowledge of its glass  
214 transition curve relative to a known standard with similar chemical functionality. This  
215 approach requires knowledge of three parameters for inferring water diffusivity over the full  
216 temperature and composition range: the hygroscopicity coefficient  $\kappa_{\text{org}}$ , the glass transition  
217 temperature of the pure organic  $T_{g,\text{org}}$  and the Gordon-Taylor coefficient  $k_{\text{GT}}$  of the aqueous  
218 organic mixture. For justification, more information on this procedure and a description of  
219 how the required input parameters are obtained, see Appendix A. For validation of the  
220 estimation scheme, we provide applications to literature ice nucleation experiments in  
221 Appendix B.

## 222 3 Results and discussion

### 223 3.1 Particle Morphology

224 We investigate ice nucleation in glassy organic aerosols induced by changing ambient  
225 conditions during the updraft of an air parcel. In updraft events, adiabatic cooling leads to a  
226 decrease in temperature and a corresponding increase of relative humidity (RH).  
227 Humidification of air leads to water uptake into the particle phase, causing a humidity-  
228 induced phase transition that for glassy aerosol particles has been termed *amorphous*  
229 *deliquescence* (Mikhailov et al., 2009). This process is often kinetically limited by diffusion  
230 of water in the particle phase (Zobrist et al., 2011), so that a particle can be out of equilibrium  
231 when the time scale of humidification is shorter than that of diffusion.

232 Amorphous deliquescence is a self-accelerating process since water acts as a plasticizer in the  
233 organic matrix (Mikhailov et al., 2009; Zobrist et al., 2011): Water molecules taken up by the  
234 particle reduce the particle's viscosity and, hence, increase bulk diffusivity locally, thus  
235 accelerating the uptake of further molecules. The microphysical consequences of this  
236 mechanism are illustrated in Fig. 1, which shows the temporal evolution of particle  
237 morphology of a glassy organic aerosol particle exposed to a gradual increase in relative  
238 humidity (simulated atmospheric updraft, see also Movie S1). The quasi-equilibrium glass  
239 transition of the aqueous organic,  $RH_g$ , is shown in grey. With “quasi-equilibrium glass  
240 transition“, we denote the conditions under which a binary organic-water system would  
241 undergo amorphous deliquescence when humidification occurs sufficiently slow so that  
242 equilibrium between ambient RH and water activity is always maintained. Humidification  
243 may be fast enough to cause a difference in phase state from equilibrium: Water activity,  
244 colour-coded from dark blue (low water activity) to light blue (high water activity), trails  
245 behind ambient RH due to kinetic limitations in water diffusivity (Koop et al., 2011). Note  
246 that when using a constant  $D_{H_2O}$ , diffusion gradients appear less pronounced (cf. Fig. S2 and  
247 Movie S2). Hence, self-accelerating water diffusion leads to a sharpening of the diffusion  
248 gradient that can be close to the molecular length scale (Zobrist et al., 2011).

249 Several morphological stages can be distinguished during the humidification process in Fig. 1.  
250 Starting from a homogeneous, glassy particle (1), an increase in RH first leads to liquefaction  
251 of a thin outer layer and emergence of a core-shell morphology (2). This liquid outer layer  
252 grows in equilibrium with ambient relative humidity and also extends towards the particle

253 centre by diffusion of water into the glassy organic matrix (3), leading to shrinkage of the  
254 residual glassy core until the particle is fully deliquesced (4). Thus, during the continuous  
255 amorphous deliquescence process two characteristic instants can be distinguished, each  
256 occurring at a different humidity: We define the *Partial Deliquescence Relative Humidity*  
257 (PDRH) as the point where a thin aqueous outer shell of the particle is homogeneously mixed  
258 and the shell's water activity is larger than that of the quasi-equilibrium glass transition. In  
259 this study we set the thickness of this surface shell to 1 nm, corresponding to about 5  
260 monolayers of water. We define the *Full Deliquescence Relative Humidity* (FDRH) as the  
261 point where its water activity corresponds to that of a liquid (i.e. it is larger than that of the  
262 quasi-equilibrium glass transition) and the water activity gradient from the surface to the  
263 particle core is less than 5 %. Note that in the case of a sufficiently slow updraft, both PDRH  
264 and FDRH would occur at  $RH_g$ . In fact, the KM-GAP simulations suggest that, with updraft  
265 velocities typical for atmospheric conditions (e.g.  $0.01 - 10 \text{ m s}^{-1}$ ), PDRH often coincides  
266 with  $RH_g$ . In contrast, FDRH often extends far into the liquid region of the phase diagram,  
267 indicating the importance of kinetic limitations and implying that particles can contain glassy  
268 cores even at relative humidities above  $RH_g$  due to slow water diffusion.

### 269 **3.2 Ice nucleation regimes**

270 Next, we investigate by kinetic model simulations the competition between amorphous  
271 deliquescence and ice nucleation during an atmospheric updraft. For our initial calculations  
272 we use sucrose as a proxy for organic aerosols since detailed physico-chemical  
273 parameterizations for water diffusivity, the RH-dependent equilibrium composition as well as  
274 glass transition data are available (Zobrist et al., 2011). The heterogeneous ice nucleation  
275 onset ( $RH_{\text{het}}$ ) for sucrose was obtained from ice nucleation experiments by Baustian et al.  
276 (2013) and is shown as brown dashed lines in Fig. 2. Here we use the ice saturation ratio  $S_{\text{ice}}$   
277 as an indicator of humidity because it scales with RH according to  $S_{\text{ice}} = p_{\text{liq},0}(T) / p_{\text{ice}}(T) \cdot \text{RH}$ ,  
278 but is also a more direct indicator of the supersaturation of ice.

279 Figure 2A shows results obtained with KM-GAP simulating the updraft of 100 nm sucrose  
280 particles for a wide range of temperatures. Each simulated trajectory started at ice saturation  
281 ( $S_{\text{ice}} = 1$ ), as is often the case for cloud chamber or environmental cell experiments (Murray et  
282 al., 2010; Wang et al., 2012). Temperature was decreased so that the resulting humidification

283 rate was constant at  $1 \text{ \% RH min}^{-1}$ , corresponding to an atmospheric updraft of about  $0.2 \text{ m s}^{-1}$ ,  
284  $^1$ , typical of atmospheric gravity waves (Jensen et al., 2005).

285 As expected FDRH of sucrose particles, indicated by the red solid line, occurs significantly  
286 above  $\text{RH}_g$  at all temperatures. The intersection of  $\text{RH}_{\text{het}}$  with  $\text{RH}_g$  defines the upper  
287 temperature limit for deposition nucleation. Below this temperature, a sucrose particle is a  
288 glassy solid when  $\text{RH}_{\text{het}}$  is reached, and hence deposition ice nucleation may occur. Above  
289 this temperature, the particle is partially deliquesced when approaching  $\text{RH}_{\text{het}}$  and the glassy  
290 core of the particle may act as an IN for immersion freezing. The upper limit of the immersion  
291 freezing regime is given by the intersection of  $\text{RH}_{\text{het}}$  with the FDRH line. Above this  
292 temperature, particles are already fully deliquesced once  $\text{RH}_{\text{het}}$  is reached. Hence, these  
293 particles do not nucleate ice heterogeneously and freeze only at the homogeneous ice  
294 nucleation limit (green dashed line; Koop et al., 2000). Finally at  $\sim 232 \text{ K}$ , the homogeneous  
295 ice nucleation limit coincides with water saturation (solid black line) and above this  
296 temperature the aerosol particles activate into cloud droplets consisting of supercooled water,  
297 thus representing the upper limit of the homogeneous ice nucleation regime.

298 The delay between the nominal quasi-equilibrium glass transition  $\text{RH}_g$  and the actual full  
299 deliquescence at FDRH is governed by the competition between humidification rate  
300 (synonymous to updraft velocity) and timescale for water diffusion within the particle bulk.  
301 FDRH will shift towards higher relative humidities when higher humidification rates are  
302 employed, as shown in Fig. 2B. For example, increasing the rate of humidification to  $10 \text{ \%}$   
303  $\text{RH min}^{-1}$ , a value corresponding to an updraft velocity of about  $2 \text{ m s}^{-1}$  and commonly  
304 reached in convective updrafts (Jensen et al., 2005), shifts the FDRH line upwards (solid dark  
305 blue line) and thus its intersection with the  $\text{RH}_{\text{het}}$  line towards higher temperatures.  
306 Accordingly, decreasing the updraft velocity to  $0.02 \text{ m s}^{-1}$ , a value found in large-scale,  
307 synoptic updrafts (Jensen et al., 2005), leads to FDRH (solid light blue line) much closer to  
308 the quasi-equilibrium glass transition  $\text{RH}_g$ . Moreover, an increase in particle size delays the  
309 deliquescence process (indicated by the solid purple line), since it increases the timescale of  
310 diffusion. The range of the immersion freezing regime thus strongly depends on ambient  
311 conditions and is extended towards higher temperatures in fast updrafts and for large particles.  
312 Laboratory ice nucleation measurements with sucrose particles (Baustian et al., 2013) are  
313 used to validate our model calculations of ice nucleation regimes in Fig. 2C. Baustian et al.  
314 used optical microscopy in conjunction with a cold stage to detect ice nucleation on glassy

315 sucrose particles (4  $\mu\text{m}$  diameter) during humidification (1 % RH  $\text{min}^{-1}$ ), leading to the  
316 nucleation onsets shown in Fig. 2C (brown markers). A range of simulations mimicking the  
317 experimental conditions at different starting temperatures leads to a continuous FDRH curve  
318 (solid blue line) over the entire temperature range. For details on the calculations see  
319 Appendix B. The modelled FDRH curve correctly confines the region below which  
320 heterogeneous ice nucleation is observed in the experiments. Based on our calculations, the  
321 experimental data points below  $\text{RH}_g$  (full brown circles) can be assigned to the deposition  
322 nucleation regime, whereas points between  $\text{RH}_g$  and FDRH (open brown circles) can be  
323 assigned to immersion freezing. Additional analyses for validation have been performed for  
324 other types of organic particles (Figs. B1 and B2).

### 325 **3.3 Biogenic and anthropogenic SOA**

326 In order to apply our kinetic model to ice nucleation in secondary organic aerosol (SOA),  
327 estimates of  $D_{\text{H}_2\text{O}}$  in SOA material have been inferred. Four major SOA precursors were  
328 chosen to represent biogenic and anthropogenic origin, respectively:  $\alpha$ -pinene and isoprene,  
329 as well as naphthalene and dodecane. Each of these SOA is represented by a choice of marker  
330 compounds taken from the literature (cf. Table S1). Water diffusivities are estimated utilizing  
331 the scheme described in Sect. 2.2. The heterogeneous ice nucleation onset ( $\text{RH}_{\text{het}}$ , brown  
332 dashed line) for SOA was obtained from laboratory measurements by Wang et al. (2012) and  
333 Schill et al. (2014) as derived in Fig. A1. Hygroscopicities of the various SOA were taken  
334 from Lambe et al. (2011), who suggested that  $\kappa_{\text{org}}$  can be parameterized independently of SOA  
335 type as function of O/C ratio. In all simulations, particles of 100 nm diameter were humidified  
336 at a rate of 1 % RH  $\text{min}^{-1}$ .

337 Figure 3A shows the simulation results of FDRH for all four precursor types. Naphthalene  
338 SOA is observed to be fully deliquesced latest due to the high estimated glass transition  
339 temperature and low hygroscopicity (cf. Table A1), followed by  $\alpha$ -pinene and isoprene.  
340 Dodecane SOA showed the earliest deliquescence, reflecting the low glass transition  
341 temperature of pure dodecane SOA of  $\sim 210$  K. By comparison of FDRH with measured  $\text{RH}_{\text{het}}$   
342 on SOA, compound-specific upper temperature limits for heterogeneous ice nucleation on  
343 SOA particles can be determined (arrows on x-axis, values are given in Table S2).  
344 Uncertainty estimates for FDRH and  $\text{RH}_g$  of all four precursors classes are given in Fig. S4.

345 For the calculations in Fig. 3A, we chose an average oxidation state typically observed for  
346 SOA from the respective precursor. The atomic oxygen to carbon ratio (O/C) increases upon  
347 chemical ageing, thereby affecting hygroscopicity (Lambe et al., 2011) and glass transition  
348 temperature (Fig. A2). The resulting effects of chemical ageing on modelled FDRH are  
349 shown exemplarily for  $\alpha$ -pinene and dodecane SOA in Fig. 3B and C, respectively. For  $\alpha$ -  
350 pinene SOA (B), a higher O/C results in hardening of the organic material with ageing,  
351 leading to a FDRH increase, whereas for dodecane SOA (C) a higher O/C results in softening,  
352 thus leading to earlier deliquescence and a FDRH decrease.

353 The observed effects can be explained by the competition between a simultaneous increase of  
354 hygroscopicity with O/C and an increasing glass transition temperature of the pure organic  
355 matrix due to stronger molecular interactions in the highly oxidized organic material. A  
356 higher glass transition value enhances the rigidity of the pure organic matrix, whereas a  
357 higher hygroscopicity enhances the amount of water taken up by the aqueous organic mixture  
358 at a given humidity and thus its plasticizing effect.

359 Figure 4 illustrates this competition by displaying estimated characteristic timescales of water  
360 diffusion in 100 nm diameter SOA particles at 220 K as a function of hygroscopicity ( $\kappa_{\text{org}}$ )  
361 and glass transition temperature of the pure organic matrix ( $T_{\text{g,org}}$ ). Dotted contour lines show  
362 characteristic mass transport times associated with the diffusion coefficient  $D_{\text{H}_2\text{O}}$  (Shiraiwa et  
363 al., 2011). Coloured oval shapes indicate estimated ranges of  $\kappa_{\text{org}}$  and  $T_{\text{g,org}}$  for the four SOA  
364 precursor classes, for three different oxidation states each (cf. Table A1). The arrows pointing  
365 from the lowest to the highest oxidation state reveal that both  $\kappa_{\text{org}}$  and  $T_{\text{g,org}}$  increase with O/C.  
366 The slope of these arrows when compared to the slope of the contour lines indicates whether a  
367 compound undergoes hardening (steeper slope) or softening (shallower slope) during the  
368 ageing process. Apparently, both biogenic SOA types undergo hardening upon ageing,  
369 whereas the two anthropogenic SOA types undergo softening, with the strongest effects for  
370 pinene and dodecane SOA.

371 The area between 1 s and 1 h represents the time scale of atmospheric updraft processes. For  
372 SOA in this range, diffusion processes occur on the same time scales as typical air parcel  
373 updrafts and the predominant cloud formation process depends strongly on atmospheric  
374 conditions. All four SOA types fall within or beneath this range, indicating the importance of  
375 the actual updraft velocity for ice nucleation on glassy aerosols. But it is also obvious that

376 SOA particles from naphthalene are most likely to be subject to kinetic effects and may thus  
377 act as IN.

### 378 **3.4 Model uncertainties**

379 The model results presented in this study are subject to various types of uncertainty. Among  
380 these are uncertainties arising from model assumptions such as the validity of first-order  
381 Fickian diffusion and the applied schemes for bulk mixing and surface softening (Sects. 2.1.2  
382 and 2.1.3). At present there is a lack of fundamental chemical and physical knowledge for  
383 describing these processes in aqueous binary or multicomponent systems. We note, however,  
384 that the approach taken here is in agreement with the sparse data on water diffusivities in  
385 aqueous organic systems (Zobrist et al., 2011; Shiraiwa et al., 2013b; Lienhard et al., 2014;  
386 Price et al., 2014). Model results obtained for aqueous sucrose (Fig. 2) are expected to be  
387 reliable because the thermodynamic and kinetic parameters of this benchmark system are well  
388 studied and agree within the literature (e.g. Zobrist et al., 2011; Price et al., 2014); on the  
389 other hand, model results obtained for SOA (Fig. 3) are subject to larger uncertainties as  
390 detailed in the following.

391 The model neglects liquid-liquid phase separation in the aqueous organic phase (You et al.,  
392 2014) by assuming that all SOA components are miscible with water over the entire  
393 concentration and temperature range. We note that for SOA types that typically show only  
394 low O/C ratios (e.g. SOA from long chain aliphatic precursors such as dodecane), insoluble  
395 fractions may become important for ice nucleation (see discussion in Sect. B2).

396 Volatilization of organic material has not been included in the calculations presented above  
397 since vapour pressures of typical SOA marker compounds are low under the low temperature  
398 conditions employed in this study (Huisman et al., 2013; O'Meara et al., 2014).

399 Self-diffusion of SOA material has been neglected as diffusion time scales of large organic  
400 molecules exceed those of small guest molecules in the SOA matrix by orders of magnitudes  
401 (Koop et al., 2011; Shiraiwa et al., 2011).

402 Minor model uncertainty comes from parameters determining the volume concentration of  
403 organic molecules at a given organic mass fraction, i.e. average molar mass  $M_{\text{org}}$  of the  
404 organics and density of the aqueous organic mixture (cf. Table S3). Variation by  $100 \text{ g mol}^{-1}$   
405 in  $M_{\text{org}}$  showed no effect on model results, varying  $\rho_{\text{org}}$  by  $0.1 \text{ g cm}^{-3}$  showed only a slight  
406 influence on aerosol deliquescence humidity on the order of 1 % RH.

407 The arguably largest source of uncertainty is insufficient knowledge of the thermodynamic  
408 input parameters required for the diffusivity estimation scheme ( $\kappa_{\text{org}}$ ,  $T_{\text{g,org}}$ ,  $k_{\text{GT}}$ , cf. Appendix  
409 A). In addition to the general assumptions made in that scheme and the uncertainties in the  
410 sucrose parameterization used within the diffusivity estimation scheme, uncertainties in input  
411 parameters propagate into an uncertainty in  $D_{\text{H}_2\text{O}}$ , which we assess in Figs. S4 and S6. Figure  
412 S4 shows the uncertainty for each specific SOA precursor and a particular O/C ratio by  
413 propagating the maximum deviation estimates in  $\kappa_{\text{org}}$  and  $T_{\text{g,org}}$  given in Table A1. Figure S6  
414 shows the full uncertainty towards single model input parameters irrespective of precursor or  
415 oxidation state. Among these,  $\kappa_{\text{org}}$  seems to be the largest source of uncertainty as the model  
416 results are sensitive towards  $\kappa_{\text{org}}$  and its numerical value subject to a rather large variability  
417 for atmospherically relevant organic substances (Koop et al., 2011; Lambe et al., 2011;  
418 Rickards et al., 2013). Due to lack of consistent experimental data, a constant  $\kappa_{\text{org}}$  is used in  
419 this study to parameterize hygroscopicity over the entire concentration and temperature range.

420 Thus, laboratory experiments that directly probe diffusivity within SOA at room temperature  
421 and also at low temperature are highly desirable, as it has been done for sucrose and few other  
422 single-compound proxies (Tong et al., 2011; Zobrist et al., 2011; Bones et al., 2012; Lienhard  
423 et al., 2014; Price et al., 2014). Moreover, experiment-based water activity parameterizations  
424 over a large temperature range are needed, because at least some water-soluble organic  
425 oligomers/polymers show a strong temperature dependence of water activity for aqueous  
426 mixtures of constant composition (Zobrist et al., 2003). Both such improvements would  
427 reduce the model uncertainty in future modelling studies substantially.

428 Another type of uncertainty arises from uncertainty in heterogeneous ice nucleation onsets.  
429 To date, little is known about the exact microphysical mechanism by which amorphous  
430 organics nucleate ice heterogeneously (Wagner et al., 2012; Marcolli, 2014; Schill et al.,  
431 2014). Reported ice nucleation onsets of glassy particles span wide ranges and are most likely  
432 substance or substance class-specific (Wilson et al., 2012; Schill et al., 2014). Thus, further  
433 laboratory experiments are needed that reveal details on the ice nucleation mechanism and  
434 that allow predictions of ice nucleation ability for a wide variety of substances.

435

#### 436 **4 Atmospheric implications of glassy organic IN**

437 Organic aerosols can induce cloud formation via many different pathways depending on  
438 ambient conditions and composition. At high temperature and high humidity, liquid organic  
439 particles can act as cloud condensation nuclei (CCN). At lower temperatures, they facilitate  
440 formation of ice crystals. Figure 5 summarizes how the phase state and morphology of  
441 atmospheric organic aerosol particles may vary upon changes in ambient relative humidity  
442 (humidity-induced phase transitions). Upon humidifying, the phase state changes from  
443 amorphous solid (glassy) over a partially-deliquesced state with a solid core residual coated  
444 by a liquid shell to a fully-deliquesced liquid. Upon drying the transition may occur via an  
445 inverse core-shell morphology, i.e. a liquid coated by a solid shell. Consequently, the particle  
446 phase state determines the active ice nucleation pathway: Glassy solids can nucleate ice in the  
447 deposition mode, partially deliquesced particles with core-shell morphologies may act as IN  
448 in the immersion mode and liquid particles nucleate ice homogeneously, at significantly  
449 higher ice supersaturation.

450 From the SOA types investigated in this study, aromatic SOA or highly aged  $\alpha$ -pinene SOA  
451 may persist in a glassy state to the highest temperatures and humidities and may thus facilitate  
452 heterogeneous ice nucleation at temperatures of up to 225 K. Below 210 K, SOA from all  
453 precursors are expected to be in the glassy state required for heterogeneous ice nucleation.  
454 Our microphysical simulations suggest a potential anthropogenic influence of IN from  
455 emission of aromatic VOCs and by providing high oxidative capacities in urban areas leading  
456 to an increase of ice nucleation in and on glassy organic particles.

457 Compared to typical atmospheric IN such as dust, soot and biological particles, glassy organic  
458 particles require temperatures below  $\sim 230$  K to nucleate ice heterogeneously (Hoose and  
459 Möhler, 2012). This restriction confines their atmospheric activity range to the upper  
460 troposphere – lower stratosphere region since the glassy state is prevalent only up to  
461 temperatures of about 200 – 240 K under typical atmospheric humidities ( $S_{\text{ice}} \approx 1$ ), depending  
462 on composition.

463 In this study we show a strong interplay between diffusion time scales in the atmosphere and  
464 atmospheric updraft speeds: the stronger the updraft and the larger the particle size, the more  
465 kinetic limitations delay the liquefaction of glassy particles. These findings also imply that an  
466 ice nucleation onset determined in laboratory studies needs to be interpreted carefully in order  
467 to apply it to realistic atmospheric parameters, i.e. humidification rate, particle size and

468 starting humidity. Kinetic limitations are already pronounced at the smallest atmospherically  
469 relevant updraft velocities of  $0.02 \text{ m s}^{-1}$ . When humidification is fast (e.g. in convective  
470 updrafts), the glassy state may persist well above its quasi-equilibrium boundaries. Our  
471 simulations on sucrose and SOA particles suggest a shift of humidity-induced glass transition  
472 to higher temperatures by about 5 K when updraft velocities are increased by a factor of 10.  
473 Also, the history of an organic particle has effects on its water uptake properties: Particles that  
474 were equilibrated at lower humidity are expected to deliquesce at higher ice supersaturation.  
475 In situations where particles are both, equilibrated in dry air ( $S_{\text{ice}} < 0.9$ ) and elevated quickly,  
476 upper temperature limits for immersion freezing on glassy organics might reach much higher  
477 values than the conservative estimates given in this study. Thus, also ice nucleation in mid-  
478 altitude clouds may be affected by this heterogeneous ice nucleation pathway.

479 This study outlines the basic physico-chemical relations and makes a first attempt in  
480 quantifying temperature limits for heterogeneous ice nucleation by four generic types of SOA,  
481 but further laboratory and modelling studies are needed to provide a comprehensive set of  
482 parameterizations to be used in atmospheric models. To assess the global importance of ice  
483 nucleation by SOA particles and to quantify the associated aerosol effects on climate, studies  
484 with large scale computational models are needed. As small scale kinetic processes cannot be  
485 treated explicitly in these kinds of models, parameterizations are required that include  
486 dependencies upon temperature, relative humidity, updraft velocity, particle size and  
487 composition.

488 **Appendix A: Details on the estimation of bulk diffusivities from glass transition**  
489 **and hygroscopicity data**

490 **A.1. Justification of the method**

491 Even though the estimation scheme described in Sect. 2.2 represents a rather crude estimation  
492 of water diffusivities, it builds on basic physical principals: In solutions of chemically similar  
493 organic substances (like the mixture of highly functionalized organic species in SOA), the  
494 types of molecular interactions are mostly hydrogen bonds and dispersion interactions,  
495 irrespective of the actual composition. Differences in diffusive properties are to a substantial  
496 degree due to factors such as molar mass and shape, both of which directly affect the glass  
497 transition temperature (Koop et al., 2011). The way by which the glass transition is  
498 approached is not affected strongly by the substance type, as all organic compounds relevant  
499 for SOA are *fragile* glass-formers (Angell, 1985). The proposed method is consistent with the  
500 following previous studies:

501 Rampp et al. (2000) used NMR spectroscopy to determine water diffusion coefficients in  
502 different carbohydrate matrices (sucrose, allosucrose, leucrose, trehalose) and fitted VFT  
503 parameters to the temperature and concentration-dependent data sets. Overall, similar VFT  
504 parameters  $A$  and  $B$  were found for these chemically similar substances, even though  $D_{\text{H}_2\text{O}}$   
505 seemed to depend strongly on organic mass fraction, thus supporting assumptions 1 and 2  
506 above. The observed concentration dependence was described almost exclusively by a change  
507 in  $T_0$ , with only small trends in  $A$  and minor variation in  $B$ , possibly due to experimental error,  
508 thus supporting assumption 3.

509 Angell (1997) investigated the correlation of Kauzmann temperatures  $T_k$  with Vogel  
510 temperatures  $T_0$  and found their ratio to be close to unity. The ratio of  $T_g$  to  $T_0$  has been shown  
511 to be confined to a narrow range between  $1.07 < T_g/T_0 < 1.82$  for a wide variety of strongly  
512 different substances. This ratio seems to be correlated in magnitude to the substances fragility  
513 (i.e. VFT parameter  $B$ ), with high fragilities implying high  $T_g/T_0$  ratios. Reversely the  
514 assumption of similar fragilities (assumption 2) directly points towards similar  $T_g/T_0$  ratios  
515 (assumption 3). Accordingly, deducing Vogel temperatures  $T_0$  from glass transition properties  
516 seems reasonable.

## 517 **A.2. Estimation of glass transition temperatures $T_{g,org}$**

518 The proposed estimation scheme enables the prediction of bulk diffusion coefficients only  
519 from knowledge of glass transition values for the desired RH range. The glass transition curve  
520 can be described by three parameters: the glass transition temperature of the pure molecular  
521 compound  $T_{g,org}$ ; the Gordon-Taylor constant  $k_{GT}$  of the aqueous organic mixture; and the  
522 hygroscopicity  $\kappa_{org}$  for translating composition into water activity.  $T_{g,org}$  exhibits a linear  
523 correlation with melting point  $T_m$ , also known as the Boyer-Beaman rule (Koop et al., 2011).  
524  $T_m$  can be estimated by group contribution models with knowledge of its chemical structure.  
525 We use the melting point prediction model of UPPER (Unified Physical Property Estimating  
526 Relationships) as presented by Jain et al. (Jain and Yalkowsky, 2006; Jain et al., 2004).

527 Table S1 shows our choice of marker substances for four different types of SOA along with  
528 molar mass, melting points predicted with UPPER and predicted glass transition values based  
529 on the Boyer-Beaman rule. The SOA groups were chosen to include SOA from the most  
530 commonly studied precursors and are derived from one specified precursor substance each.  
531 The groups “ $\alpha$ -Pinene” and “Isoprene” represent SOA from biogenic origin, whereas  
532 “Naphthalene” and “Dodecane” are our choice for precursors of anthropogenic origin.

533 The group “ $\alpha$ -Pinene” contains compounds characteristic for photooxidation and ozonolysis  
534 of the biogenic SOA precursor  $\alpha$ -pinene, which has been chosen as proxy for the different  
535 monoterpene VOCs responsible for biogenic SOA formation. The list contains compounds  
536 with the highest yields according to MCM-based simulations of Shilling et al. (2009) as well  
537 as of Zuend and Seinfeld (2012), who also included two dimer substances. Furthermore, we  
538 included 3-MBTCA, a highly oxidized pinene derivative found in ambient samples  
539 (Szmigielski et al., 2007) as well as terpenylic acid, a tracer for rather fresh SOA, along with  
540 two of its derivatives (Claeys et al., 2009).

541 The group “Isoprene” contains isoprene-derived compounds found in ambient and laboratory  
542 aerosol as suggested by Surratt et al. (2006) and references therein. These authors also  
543 proposed a high contribution of esterification products with 2-methylglyceric acid as  
544 monomeric unit to SOA mass. Table S1 lists these oligomers up to the tetramer level, where  
545 predicted glass transition values start to level off.

546 The group “Naphthalene” represents typical products originating from the oxidation of  
547 anthropogenic aromatic precursors. Note that for highly functionalized aromatic compounds,

548 UPPER predicts unusually high values for  $T_m$ , which are inconsistent with observations. For  
549 example, phthalic acid melts under decomposition (presumably anhydrate formation) at 403 K  
550 (Lide, 2005), whereas UPPER suggests a melting point of about 539 K. For this reason, we  
551 used only those naphthalene oxidation products for which literature melting points are known,  
552 such as the substances given in Saukko et al. (2012) and a number of compounds listed in  
553 Kautzman et al. (2010). Note that for the same reason we did not include oligomerization  
554 products to the “Naphthalene” group. Oligomerization is however also expected for aromatic  
555 SOA, shown e.g. by Kalberer et al. (2004), which would lead to higher  $T_{g,org}$  (Koop et al.,  
556 2011). For these reasons, our estimates for aromatic SOA materials may be regarded as a  
557 conservative estimate.

558 The group “Dodecane” in Table S1 lists oxidized organics derived from the C12 straight  
559 chain alkane to represent the family of similar compounds originating from aliphatic VOCs of  
560 anthropogenic origin. The list is a selection from the comprehensive chemical mechanism in  
561 Yee et al. (2012) and three compounds from those suggested by Zhang et al. (2014).

562 The resulting glass transition values are presented in Fig. A2 as a function of atomic O/C ratio  
563 and a clear positive correlation is observed within each group of compounds. Such a  
564 correlation between  $T_{g,org}$  and O/C has been supported by recent  $T_g$  measurements of mixtures  
565 of  $\alpha$ -pinene derived oxidation compounds (Dette et al., 2014). In Fig. A2, the solid lines are  
566 obtained by linear regressions of the glass transition values using a bisquare weighting  
567 function and shaded areas are confidence intervals at the  $1\sigma$  level. The chosen marker  
568 compounds occupy compound-specific ranges of O/C values, which is in part due to a  
569 different carbon number in the precursor molecule. To estimate a value characteristic for a  
570 mixture of the single compounds, we choose three values of O/C ratios that are typical for the  
571 respective group and take at each of those values the corresponding  $T_{g,org}$  that arises from the  
572 linear fit. The errors are then given by the extension of confidence bands at each point. The  
573 results are shown in Table A1.

574

### 575 **A.3. Estimation of Gordon-Taylor constants $k_{GT}$**

576 Gordon-Taylor constants are necessary to estimate the glass transition temperatures of  
577 compound mixtures. Zobrist et al. (2008) determined Gordon-Taylor constants for a variety of  
578 atmospherically relevant substances and SOA proxies. However, data are sparse when  
579 compared to the wide structural variety of compounds in SOA and no clear correlation can be

580 drawn from the molecular structure. For this reason, Koop et al. (2011) recommended the  
581 usage of a mean Gordon-Taylor constant of  $k_{GT} = 2.5 \pm 1$  (cf. Table A1). Figure S6 shows the  
582 temperature dependence of FDRH in calculations similar to Figs. 2 and 3, this time using the  
583 best guess parameters recommended in Koop et al. (2011). The uncertainty in FDRH that  
584 arises from the given input parameter ranges is shown (grey shaded), but also the specific  
585 uncertainty from varying  $k_{GT}$  between 1.5 and 3.5 is highlighted (orange shaded).

586

#### 587 **A.4. Estimation of hygroscopicities $\kappa_{org}$**

588 The hygroscopicity of a compound can be expressed by a single parameter  $\kappa_{org}$ , which is  
589 strongly correlated to its degree of oxidation (Petters and Kreidenweis, 2007; Lambe et al.,  
590 2011). A typical value for  $\kappa_{org}$  in biogenic SOA particles collected in pristine rainforest  
591 environments is 0.1 (Gunthe et al., 2009), which was also used by Koop et al. (2011) for their  
592 estimation of glass transition values in biogenic SOA.

593 For estimation of  $\kappa_{org}$ , we use the parameterization of Lambe et al. (2011) that correlates the  
594 O/C ratio of secondary organic material to its hygroscopicity, Eq. (A1).

$$\kappa_{org} = (0.18 \pm 0.04) * O/C + 0.03 \quad (A1)$$

595 Each SOA precursor class is assigned a typical O/C value from previous investigations of  
596 marker compounds (cf. Fig A2) and results are shown in Table A1. With the knowledge of  
597  $T_{g,org}$ ,  $k_{GT}$  and  $\kappa_{org}$ , the entire glass transition curves for the four SOA types can be calculated,  
598 as visualized in Fig. S4. Dashed lines and grey shaded areas indicate ranges of uncertainty.

599

#### 600 **A.5. Evaluation of the method**

601 For evaluation of the performance of the diffusivity estimation scheme, we compare estimated  
602 diffusivity values with values obtained in experiments by Price et al. (2014). In these  
603 experiments, D<sub>2</sub>O-H<sub>2</sub>O exchange in an organic matrix at constant temperature and humidity is  
604 investigated by Raman spectroscopy. Figure S3 shows the experimentally determined  $D_{H_2O}$   
605 values for sucrose and levoglucosan in Price et al. (blue and red markers) as well as the  $D_{H_2O}$   
606 parameterization from Zobrist et al. (2011) (blue solid line).  $D_{H_2O}$  in levoglucosan has also  
607 been estimated with the diffusivity estimation scheme (red solid line), utilizing input  
608 parameters from Zobrist et al. (2008) ( $T_{g,org} = 283.6$  K,  $k_{GT} = 5.2$ ). Water activity has been

609 parameterized using the parameters in Table S4. Experimental and estimated values coincide  
610 for the highest and lowest water activities but differ under medium conditions due to the  
611 different curvature of the base parameterization from Zobrist et al. that underlies all  
612 calculations. However, diffusivities differ only within at most two orders of magnitude, which  
613 is a considerably small deviation compared to the large set of approximations made here and  
614 the difference between experimental techniques.

615 Figure S3 also shows the ranges of estimated diffusivity coefficients  $D_{\text{H}_2\text{O}}$  for two types of  $\alpha$ -  
616 pinene SOA: Fresh  $\alpha$ -pinene SOA (O/C = 0.3, orange dashed line) and aged  $\alpha$ -pinene SOA  
617 (O/C = 0.7, green dashed line). Dark shadings confined by dotted lines indicate the range of  
618 uncertainty at a fixed O/C, corresponding to the input uncertainties used for Figure S4. Light  
619 shadings illustrate how an uncertainty in O/C of  $\pm 0.1$  translates into uncertainty in  $D_{\text{H}_2\text{O}}$  and  
620 thus accounts for the natural variability within SOA as complex mixture.

## 621 **Appendix B: Application of the model to ice nucleation experiments in the** 622 **literature**

623

### 624 **B.1. Sucrose experiments**

625 Baustian et al. (2013) investigated sucrose particles deposited on a quartz substrate and  
626 humidified inside an experimental flow cell. After cooling and drying below the glass  
627 transition, particles with an average diameter of 4  $\mu\text{m}$  were humidified by cooling at a rate of  
628 0.1  $\text{K min}^{-1}$ . Humidification was initialized below ice saturation ( $S_{\text{ice}} < 0.9$ ). The resulting  
629 heterogeneous ice nucleation onsets (brown circles) are shown in Fig. 2C along with the full  
630 deliquescence relative humidity (FDRH, blue solid line) from multiple model runs (spacing: 2  
631 K) mimicking the experimental conditions. Simulations below 215 K (left black square  
632 marker) are found to nucleate in the deposition mode, whereas particles in runs between about  
633 215 K and 238 K (right black square marker) are assumed to undergo immersion freezing.  
634 This result is compliant with the experimental values, none of which exceeds a nucleation  
635 temperature of 235 K. Above 238 K full deliquescence occurs before the ice supersaturation  
636 required for heterogeneous ice nucleation (brown dashed line) is reached. Also, homogeneous  
637 ice nucleation is not possible anymore below the water saturation limit according to Koop et  
638 al. (2000; green dashed line), leaving no remaining ice nucleation pathway.

639

### 640 **B.2. Naphthalene SOA experiments**

641 Wang et al. (2012) generated SOA by oxidation of naphthalene by OH in a potential aerosol  
642 mass (PAM) reactor, deposited the particles on glass slides and investigated the onsets of  
643 water uptake and ice nucleation inside an ice nucleation cell that was mounted on a  
644 microscope. Experimental results are shown in Fig. B1 for three different SOA oxidation  
645 states: Low O/C (0.27) given in red, medium O/C (0.54) in green and high O/C (1.0) in blue.  
646 For the comparing model simulations, we employ our diffusivity estimation scheme with the  
647 glass transition parameterization for naphthalene given above. A humidification rate of 1 %  
648  $\text{RH min}^{-1}$  was employed and temperature varied accordingly to maintain a constant dew point.  
649 In Fig. B1, the lines of full deliquescence relative humidity (FDRH) divide the measured  
650 heterogeneous ice nucleation onsets into two groups, irrespective of the degree of oxidation  
651 used in the simulation. Heterogeneous nucleation at or below 225 K is consistent with

652 simulation results (closed diamonds), whereas ice nucleation at or above 230 K cannot be  
653 explained with the estimated water diffusion properties (open diamonds). According to the  
654 model simulation, naphthalene SOA should be already deliquesced at temperatures and RH  
655 where ice nucleation is still experimentally observed. The model simulations thus suggest that  
656 solid compounds that remained in the otherwise fully deliquesced particle, possibly insoluble  
657 products from Naphthalene OH oxidation, nucleated ice heterogeneously with lower  
658 efficiency. Such insoluble products are not considered in the model.

659 The reliability of the method is confirmed by comparing experimental and modelled water  
660 uptake onsets that show very good correlation. The modelled water uptake onset was defined  
661 as the point where the particle diameter had increased by 100 nm to take into account the fact  
662 that experimental onsets were determined by visible inspection under a light microscope.

663

### 664 **B.3. Citric acid experiments**

665 Murray et al. (2010) observed the process of heterogeneous ice nucleation on glassy aerosols  
666 by investigating citric acid particles in the AIDA cloud chamber. The experimentally  
667 determined onsets of heterogeneous (orange diamonds) and homogeneous ice nucleation  
668 (green circles) are shown in Fig. B2 along with results of simulations mimicking the  
669 experimental conditions. In the calculations, we assumed a particle diameter of 150 nm and a  
670 humidification rate of 12 % RH min<sup>-1</sup>, corresponding to a cooling rate of 1-2 K min<sup>-1</sup>.  
671 Humidification was initiated at  $S_{ice} = 1$  since the cloud chamber walls were covered with ice  
672 during the initial cooling process. We performed two series of simulations for two different  
673 water activity parameterizations available in the literature. According to the parameterization  
674 in Lienhard et al. (2012) (dashed lines), heterogeneous nucleation occurs exclusively above  
675 the (equilibrium) glass transition relative humidity  $RH_g$  and thus in the immersion freezing  
676 regime. With the parameterization from Koop et al. (2011) (solid lines), equilibrium glass  
677 transition and full deliquescence occur at later stages in the humidification process. According  
678 to this data, only the experimental data point at about 206 K would have occurred in the  
679 immersion mode.

680 At 212 K, ice nucleation occurs only homogeneously in Murray's experiments, indicated by  
681 the much later ice nucleation onset. The humidification run started with liquid aerosol  
682 particles that showed retarded deliquescence, but were not able to nucleate ice  
683 heterogeneously.

684 **Author contributions**

685 T. B., M. S., U. P. and T. K. designed research; T. B., M. S. and T. K. developed the model;  
686 T. B. performed research; T. B. and T. K. analysed simulation data; T. B., M. S., U. P. and T.  
687 K. wrote the paper.

688

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697

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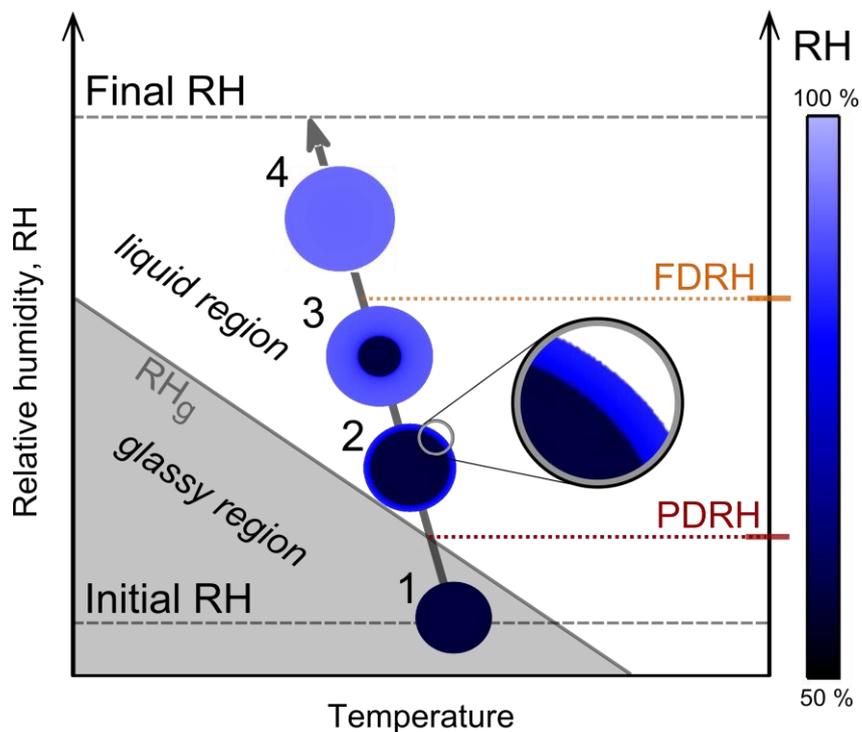
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933

934 Table A1. Assumed physical properties of SOA classes for use in conjunction with diffusivity  
 935 estimation scheme.

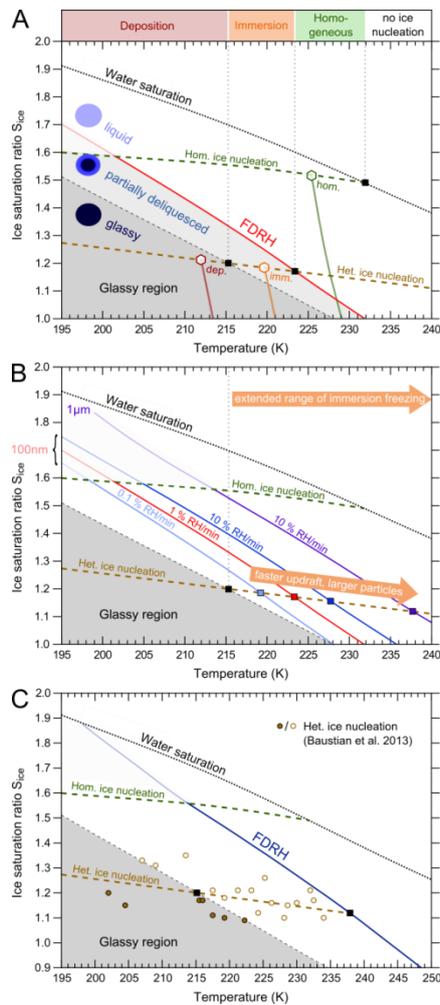
SOA Class	O/C	$T_{g,org}$ (K)	$k_{GT}$	$\kappa_{org}$
A-PINENE	0.3	$228.9 \pm 10.6$	2.5	$0.084 \pm 0.012$
	0.5	$278.5 \pm 7.0$	2.5	$0.120 \pm 0.020$
	0.7	$328.1 \pm 12.8$	2.5	$0.156 \pm 0.028$
ISOPRENE	0.6	$258.2 \pm 22.2$	2.5	$0.138 \pm 0.024$
	0.8	$287.2 \pm 11.9$	2.5	$0.174 \pm 0.032$
	1.0	$316.3 \pm 19.1$	2.5	$0.210 \pm 0.040$
NAPHTHALENE	0.3	$294.2 \pm 5.7$	2.5	$0.084 \pm 0.012$
	0.5	$313.1 \pm 8.8$	2.5	$0.120 \pm 0.020$
	0.7	$332.0 \pm 15.0$	2.5	$0.156 \pm 0.028$
DODECANE	0.1	$210.3 \pm 9.7$	2.5	$0.048 \pm 0.004$
	0.3	$216.8 \pm 5.1$	2.5	$0.084 \pm 0.012$
	0.5	$223.4 \pm 11.4$	2.5	$0.120 \pm 0.020$
KOOP SOA	---	$270 \pm 21$	$2.5 \pm 1$	$0.1008^{+0.1008}_{-0.0504}$

936



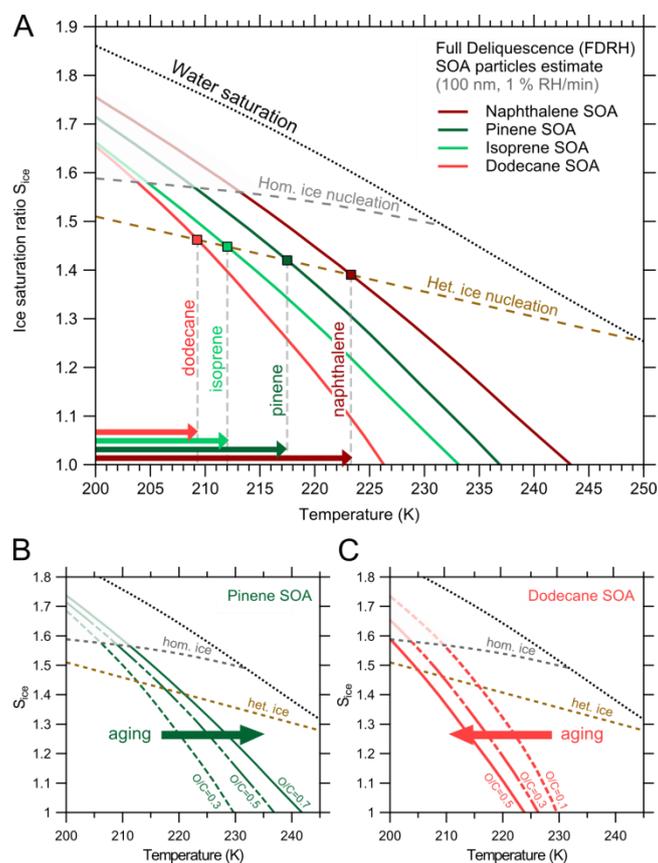
937

938 Figure 1. Schematic temporal evolution of particle morphology along a trajectory of an  
 939 atmospheric updraft (grey arrow). Humidification of ambient air upon adiabatic expansion  
 940 leads to liquefaction of initially glassy particles (dark blue color, 1) via core-shell  
 941 morphologies (2, 3) to liquid particles (light blue color, 4). Whereas partial deliquescence  
 942 (PDRH) coincides with  $RH_g$ , full deliquescence (FDRH) is delayed to much higher RH,  
 943 indicating that diffusion processes occur on much longer time scales than humidification. The  
 944 speed of the displayed trajectory corresponds to that typical for cloud chamber or  
 945 environmental cell experiments ( $0.1 - 1.5 \text{ K min}^{-1}$ ,  $1 - 15 \text{ \% RH min}^{-1}$ ).



946

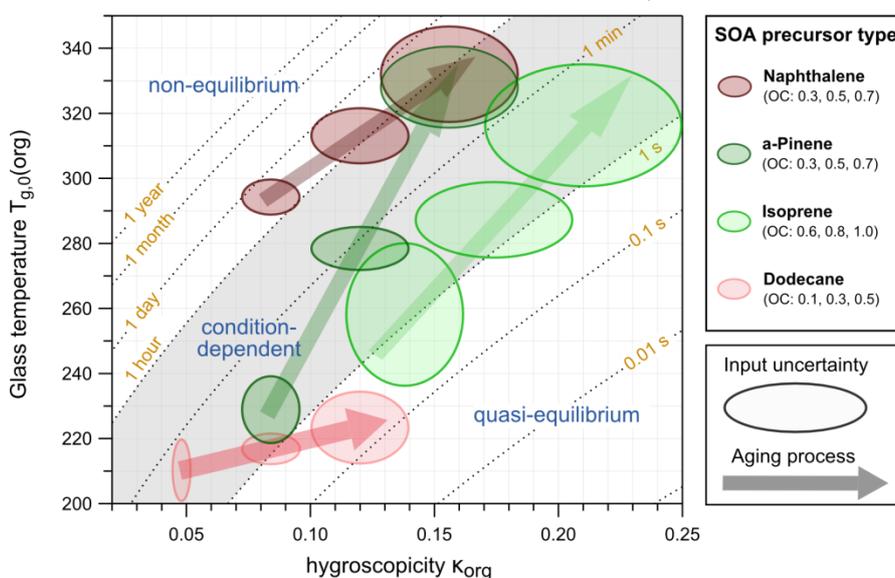
947 Figure 2. (A) Simulated regimes of heterogeneous and homogeneous ice nucleation in the  
 948 humidification of sucrose particles. The red solid line indicates full deliquescence relative  
 949 humidities (FDRH) for 100 nm particles exposed to a humidification rate of 1 % RH min<sup>-1</sup> ( $\approx$   
 950 0.2 m s<sup>-1</sup> atmospheric updraft). Example trajectories start at ice saturation, follow a constant  
 951 dew point line and end at expected ice nucleation (hexagonal markers) with deposition (red),  
 952 immersion (orange), and homogeneous (green) freezing. (B) Effects of different particles  
 953 sizes and humidification rates on FDRH. The upper boundary for immersion freezing is  
 954 extended to high temperatures for large particle radii and high humidification rates and is  
 955 expected to occur up to 238 K for the most extreme scenario (1  $\mu\text{m}$ , 10 % RH min<sup>-1</sup>, purple  
 956 solid line). (C) Application to the experimental conditions in Baustian et al. (2013), i.e. 4  $\mu\text{m}$   
 957 particles humidified at a rate of 1 % RH min<sup>-1</sup>, leads to FDRH that is able to explain all  
 958 observed experimental ice onsets (brown circles). The thermodynamic glass transition divides  
 959 the experimental data in events of deposition ice nucleation (closed circles) and immersion  
 960 freezing (open circles).



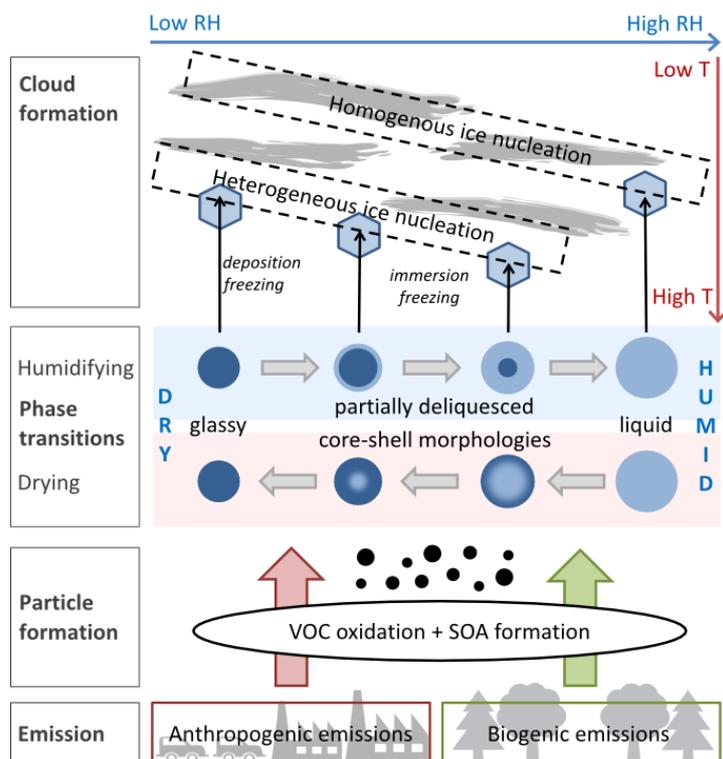
961

962 Figure 3. (A) Simulated humidification of SOA particles from the four different precursors a-  
 963 pinene, isoprene, dodecane and naphthalene. Naphthalene SOA (dark red) shows the latest  
 964 deliquescence, whereas dodecane SOA (light red) liquefied rather early in the simulations.  
 965 The two biogenic SOA estimates lie between both extremes with pinene SOA (dark green)  
 966 showing slightly later deliquescence than isoprene SOA. Intercepts (square markers) with a  
 967 heterogeneous nucleation onset typical for SOA (brown dashed line) indicate upper  
 968 temperature limits for immersion freezing (arrows on x-axis). The effect of particle ageing  
 969 also depends on precursor type: Pinene SOA (B) shows hardening upon increase in O/C  
 970 (indicated by higher FDRH), whereas dodecane SOA (C) exhibits softening (indicated by  
 971 lower FDRH). Similarly, isoprene and naphthalene SOA show only moderate hardening and  
 972 softening, respectively (Fig. S5).

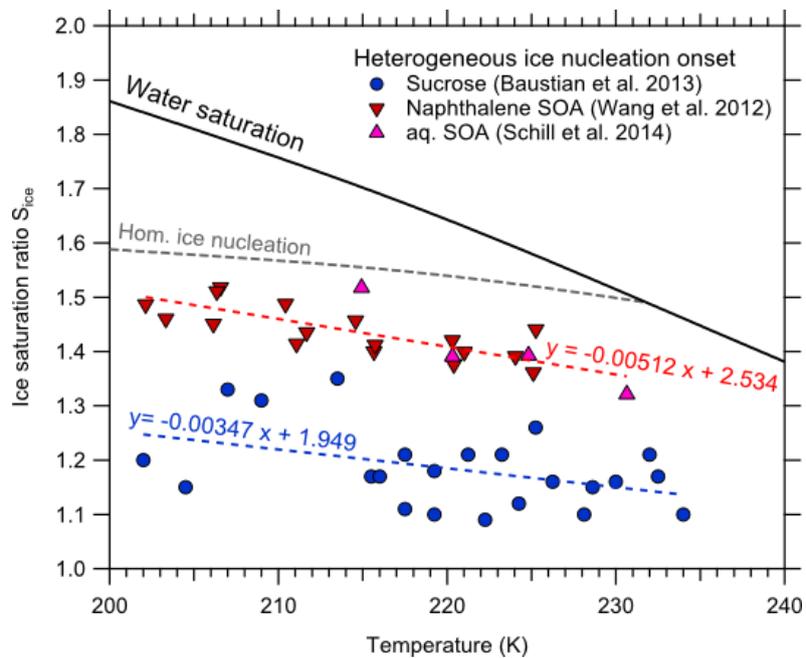
Water diffusion time scales in SOA (220 K,  $S_{ice} = 1.45$ ,  $d_p = 100$  nm)



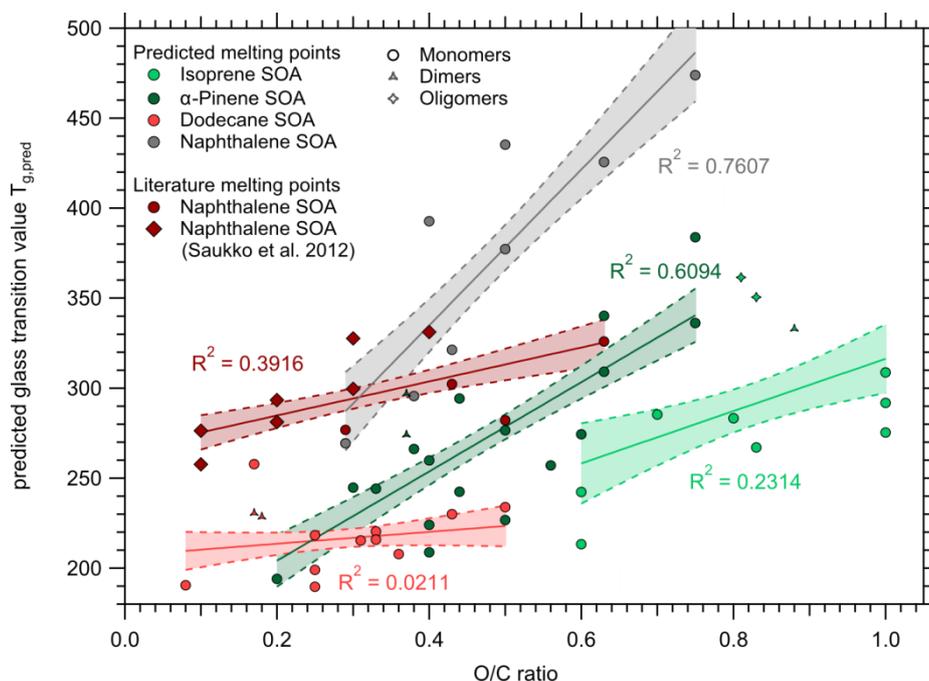
973  
 974 Figure 4. Characteristic time scales of water diffusion in SOA as function of hygroscopicity  
 975  $\kappa_{org}$  and glass transition temperatures of the pure organic matrix  $T_{g,org}$ . Calculations have been  
 976 performed at 220 K,  $S_{ice} = 1.45$  and for 100 nm particles. Oval shapes confine estimated  
 977 ranges in  $\kappa_{org}$  and  $T_{g,org}$  for the four SOA types in three different oxidation states (Appendix A  
 978 and Table A1). The grey area indicates the time scale of typical atmospheric updrafts (1 s to 1  
 979 h) and thus divides the plot in areas of quasi-equilibrium and non-equilibrium water diffusion.  
 980 Within the grey area, the relative speed of both processes depends upon the actual  
 981 atmospheric conditions. The aging process is indicated by arrows pointing from regions of  
 982 low O/C to regions of high O/C.



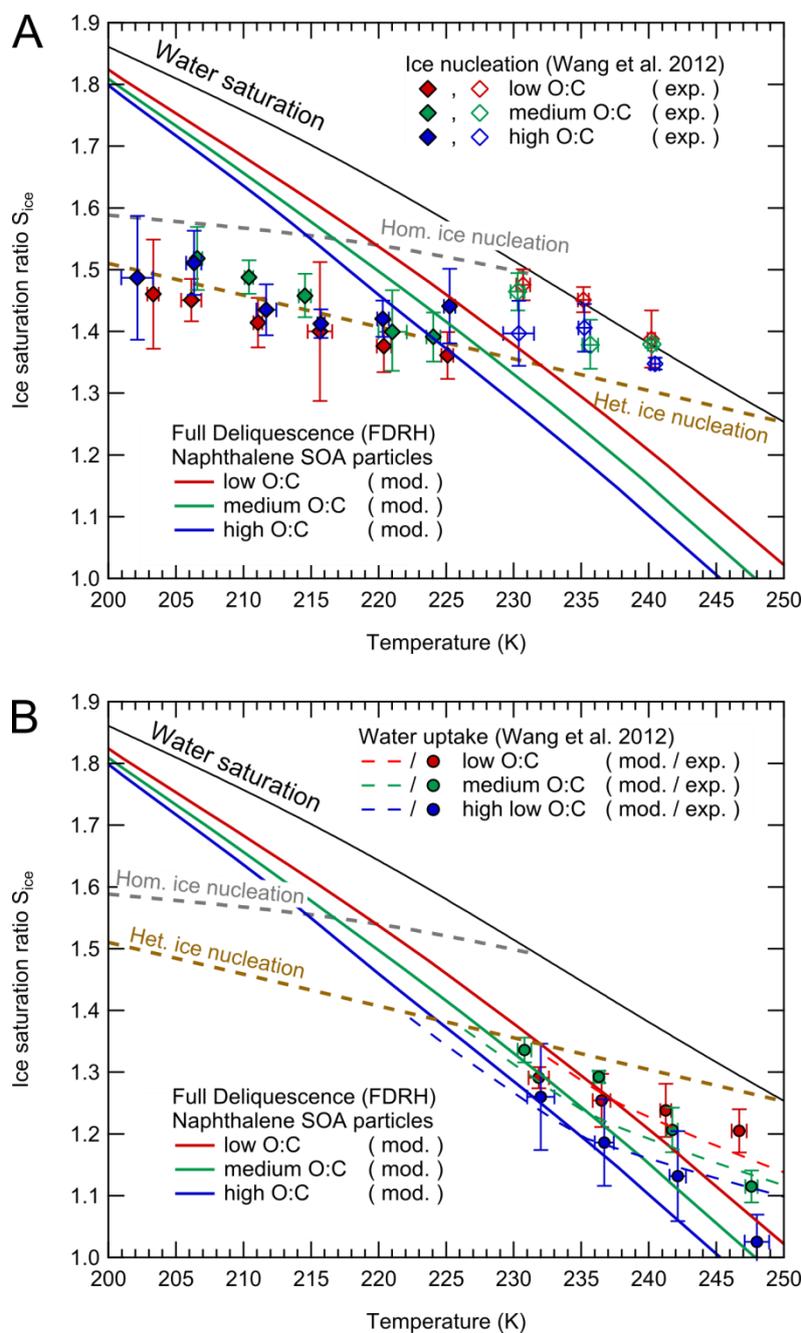
1  
 2 Figure 5. Overview of processes in organic aerosol particles affecting atmospheric cloud  
 3 formation. Particles form by oxidation of volatile organic compounds (VOCs) originating  
 4 from anthropogenic and biogenic emissions. The dominating cloud formation process  
 5 depends on particle phase state, which is a function of temperature and humidity. Humidity-  
 6 induced phase transitions between phase states may be kinetically limited and occur under  
 7 formation of partially deliquesced particles with core-shell morphologies. Glassy or partially  
 8 deliquesced particles are able to undergo heterogeneous ice nucleation, occurring at lower  
 9 relative humidity or higher temperature than homogeneous ice nucleation of liquid particles.



1  
 2 Figure A1. Determination of heterogeneous ice nucleation onsets. For sucrose, data from  
 3 Baustian et al. (2013) (blue circles) are fitted. For SOA, deposition freezing data on  
 4 Naphthalene SOA from Wang et al. (2012) (red downward triangles) as well as nucleation  
 5 data on aqSOA from Schill et al. (2014) (pink upward triangles) are used. The resulting linear  
 6 regression fits (blue and red dashed lines) lie significantly below the homogeneous nucleation  
 7 limit and are displayed along with their parameterizations.



1  
 2 Figure A2. Predicted glass transition values of SOA marker substances as function of O/C  
 3 ratio. The predicted  $T_{g,org}$  exhibit a linear correlation with O/C for each of the four SOA  
 4 systems. Solid lines are robust linear regressions using a bisquare weighting function and  
 5 shaded areas are confidence intervals at the  $1\sigma$  level. Anthropogenic aliphatic SOA  
 6 constituents show the lowest values of  $T_{g,org}$  and a weak dependence on O/C. In contrast,  
 7 aromatic SOA shows the highest glass transition values despite a rather low average O/C  
 8 ratio.



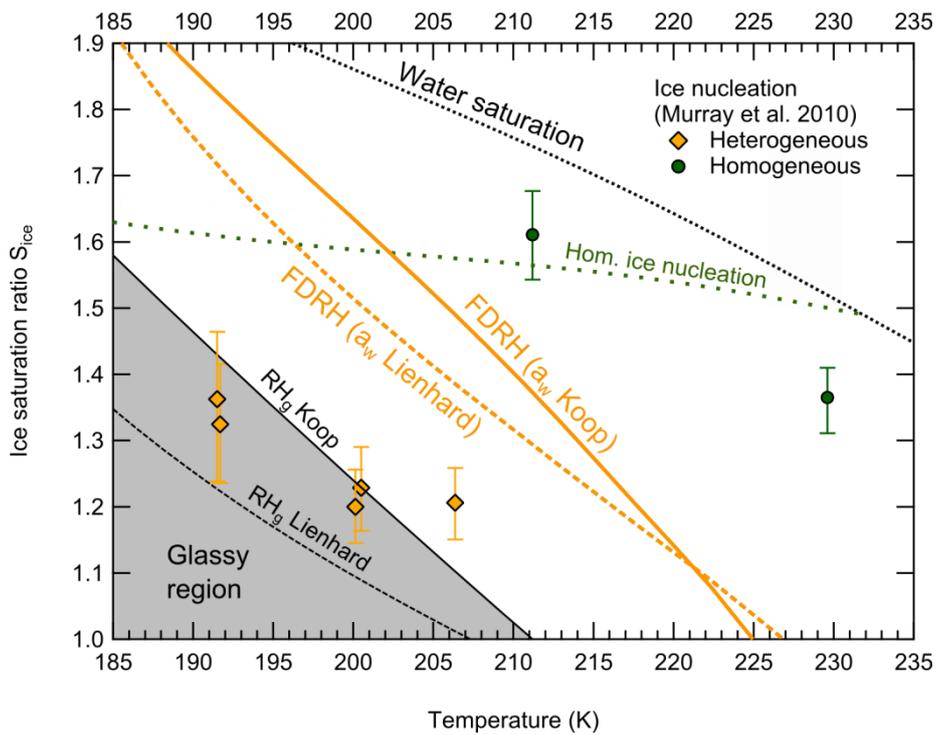
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2 Figure B1. Comparison between calculation results of naphthalene SOA deliquescence and

3 experimental ice nucleation and water uptake data from Wang et al. (2012). For the numerical

4 simulations, aerosol particles are assumed to be 1  $\mu\text{m}$  in diameter and are humidified at a rate

5 of 1 % RH  $\text{min}^{-1}$ , corresponding to a cooling rate of about 0.1 K  $\text{min}^{-1}$  used by Wang et al.



1

2 Figure B2. Comparison between calculation results of citric acid aerosol deliquescence  
 3 (orange lines) and experimental ice nucleation data from Murray et al. (2010) (orange  
 4 diamonds, green circles). In the numerical simulations, 150 nm diameter aerosol particles are  
 5 humidified at a rate of 12 % RH min<sup>-1</sup>, corresponding to a cooling rate around 1-2 K min<sup>-1</sup>  
 6 typical for cloud chamber experiments. Black lines and shaded areas confine the region where  
 7 a glass is the favored thermodynamic state. The dashed lines were obtained using the water  
 8 activity parameterization provided by Lienhard et al. (2012), whereas the solid lines were  
 9 obtained with the parameterization in Koop et al. (2011).