Variability and trends in dynamical forcing of tropical lower stratospheric temperatures

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Abstract

The contribution of dynamical forcing to variations and trends in tropical lower stratospheric 70 hPa temperature for the period 1980-2011 is estimated based on ERA-Interim and MERRA reanalysis data. The dynamical forcing is estimated from the tropical mean residual upwelling calculated with the momentum balance equation, and with a simple proxy based on eddy heat fluxes averaged between 25° and 75° on both hemispheres. The thermodynamic energy equation with Newtonian cooling is used to relate the dynamical forcing to temperature. The deseasonalised, monthly mean time series of all four calculations are highly correlated (∼0.85) with temperature for the period 1995-2011 when variations in radiatively active tracers are small. All four calculations provide additional support to previously noted prominent aspects of the temperature evolution 1980-2011: an anomalously strong dynamical cooling (∼−1 to −2 K) following the Pinatubo eruption that partially offsets the warming from enhanced aerosol, and a few years of enhanced dynamical cooling (∼−0.4 K) after October 2000 that contributes to the prominent drop in water entering the stratosphere at that time. The time series of dynamically forced temperature calculated with the same method are more highly correlated and have more similar trends than those from the same reanalysis but different method. For 1980-2011 (without volcanic periods), the eddy heat flux calculations give a dynamical cooling of ∼−0.1 to ∼−0.25 K/decade (magnitude sensitive to latitude belt considered and reanalysis), largely due to increasing high latitude eddy heat flux trends in September and December/January. The eddy heat flux trends also explain the seasonality of temperature trends very well, with maximum cooling in January/February. Trends derived from momentum balance calculations show near-zero annual mean dynamical cooling, with weaker seasonal trends especially in December/January. These contradictory results arising from uncertainties in data and methods are discussed and put in context to previous analyses.
1 Introduction

Temperature trends in the lower stratosphere over the last few decades are substantially larger than predicted by General Circulation Models (GCMs) forced with increasing greenhouse gases only (Ramaswamy et al., 2006). Consequently, trends in stratospheric dynamics and other radiatively active trace constituents (such as ozone) may play a major role for temperature trends in this layer, and decomposition into dynamically and radiatively forced trends has attracted much interest (see e.g. recent analyses of Fu et al. (2010); Ueyama and Wallace (2010); Polvani and Solomon (2012); Bohlinger et al. (2014) ).

The dynamically forced diabatic upwelling in the tropical stratosphere lowers temperatures below radiative equilibrium, and an increase/decrease in the dynamically forced upwelling induces a decrease/increase in tropical lower stratospheric temperatures. In addition to this dynamical control, changes in radiatively active trace constituents such as ozone, water vapor and aerosol, change the local balance of emitted and absorbed radiation which then induces changes in temperature. While the interaction between dynamics, composition and radiation is in principle relatively well understood (Yulaeva et al., 1994; Avallone and Prather, 1996; Randel et al., 2006; Fueglistaler, 2012; Abalos et al., 2013), systematic errors in the time series of any of the relevant quantities (temperature, radiatively active trace constituents, and atmospheric dynamics) have prevented an unambiguous interpretation of the evolution of the lower stratosphere over the past 3 decades.

Here, we focus on quantification of the dynamical forcing of tropical lower stratospheric temperatures at the 70 hPa level over the period 1980-2011 based on meteorological reanalysis data from ERA-Interim (Dee et al., 2011) and MERRA (Rienecker et al., 2011). We use two methods to estimate the dynamically forced temperature variations, namely the momentum balance equation of Randel et al. (2002) that estimates the tropical mean residual upwelling, and the eddy heat flux proxy introduced by Fueglistaler (2012). The residual, i.e. temperature minus estimated dynamically forced temperature, represents the influence from changes in radiatively active trace constituents at the level of interest and changes in up- and downwelling radiative fluxes, and from (i) errors in the reanalysis temperature; (ii) errors in the method to estimate
the dynamically forced temperature; and (iii) errors in the reanalysis temperature and wind data used to calculate the dynamically forced temperature.

Of particular interest here are the following questions concerning the evolution of the tropical lower stratosphere over the last 3 decades: (i) Is there an increase in tropical upwelling (leading to dynamical cooling) in the observations as reported in climate models (e.g. Butchart et al. (2010))? (ii) To what extent are the observed temperature trends due to changes in dynamical forcing (as suggested for example by Fu et al. (2010)), and to what extent due to changes in radiative active trace constituents (as suggested for example by Polvani and Solomon (2012))? (iii) Is the pronounced seasonality in tropical lower stratospheric temperature trends (e.g. Fu et al. (2010); Free (2011); Polvani and Solomon (2012)) the result of seasonal changes in the dynamical forcing, or in radiatively active trace constituents? (iv) Are the new calculations presented here supporting previously published results concerning changes in the strength of the residual circulation following the eruption of Pinatubo in 1991 noted by Fueglistaler (2012), and the increase in the strength of the residual circulation after the year 2000 noted by Randel et al. (2006) that would explain the sudden and prolonged drop of water entering the stratosphere in that period? (v) How consistent are results concerning the dynamical forcing between ERA-Interim and MERRA, and between the two methods to estimate the dynamical forcing of temperatures? An important result of our analysis is that the four calculations give very similar time series, but that their trends over the period 1980-2011 differ significantly. While we cannot unambiguously determine which trends are more accurate with the information available here, we document and discuss which parts of the calculations lead to differing trends.

The paper is structured as follows. Section 2 presents the data and methods used to estimate the variations in dynamically forced temperature. The results are shown in Section 3, with Section 3.1 discussing the evolution of the time series, and Section 3.2 discussing trends. Sections 3.3 and 3.4 document and discuss where the two reanalyses, and the two methods, differ. Finally, Section 4 presents conclusions and outlook.
2 Data and Methods

2.1 Framework

Consider the thermodynamic energy equation in the quasi-geostrophic, transformed Eulerian mean set of equations, and assume that the diabatic heating term can be approximated by Newtonian cooling,

$$\frac{\partial T}{\partial t} + (N^2 H/R) \cdot \bar{w}^* = \frac{T_E - T}{\tau}$$

(see e.g. eqn. 1 of Yulaeva et al. (1994)), where \(\tau\) is the radiative relaxation time scale, \(T_E\) is the radiative equilibrium temperature, \(N^2\) is the buoyancy frequency, \(H\) is the scale height, \(R\) is the gas constant, \(\bar{w}^*\) is the diabatic residual velocity, \(T\) is temperature, \(t\) is time, and all quantities are zonal means (tropical means in this work).

In this framework, we may force temperature \(T\) with \(\bar{w}^*\) and \(T_E\), where variations in \(T_E\) are a consequence of variations in radiatively active tracers. Note that changes in \(\bar{w}^*\) may also affect tracers (here particularly ozone, see e.g. Fueglistaler et al. (2011)) and hence \(T_E\). It is well known that Newtonian cooling is a relatively poor approximation for the lower stratosphere (see e.g. the analysis by Hitchcock et al. (2010)), but in practice there exist reasonably linear relations between local heating rate, temperature and radiatively active tracer amounts for smooth perturbations with vertical scales similar to that of the lower stratosphere (Fueglistaler et al., 2011, 2014). Hence, for the conceptual interpretation of the connection between dynamics, tracers and temperatures, equation 1 is sufficient.

Radiative transfer calculations (not shown) show that the first order radiatively active trace constituents that need to be considered for the lower stratosphere are aerosol and ozone; variations with observed magnitudes of water vapor, carbon dioxide and other long-lived greenhouse gases typically affect temperature about an order of magnitude less.

Under the assumption that temperature variations are only dynamically forced (i.e. \(\bar{w}^*\) in equation 1), the equilibrium temperature is constant and the solution for the difference between
temperature and equilibrium temperature, \( T_{\text{dyn}}(t) \equiv T(t) - T_E \), is of the form

\[
T_{\text{dyn}} = f(t) \ast h(t)
\] (2)

where \( f(t) \) is the forcing, \( \ast \) denotes the convolution, and the unit pulse response \( h(t) = 0 \) for \( t > 0 \) and \( h(t) = e^{t/\tau} \) for \( t \leq 0 \).

We use two methods to estimate the forcing function \( f(t) \). First, we use the momentum balance calculation of Randel et al. (2002) to estimate the tropical mean residual vertical velocity \( \bar{w}^* \) (Section 2.3). Second, we use the eddy heat flux proxy of Fueglistaler (2012) (Section 2.4). For both calculation, the time scale \( \tau \) is empirically determined by optimising the correlation of desesationalised monthly mean temperature and \( T_{\text{dyn}} \). Highest correlations (determined for the period 1995-2011 when radiative perturbations are small) are found for \( \tau \sim 70 \) days for the momentum balance equation, and \( \tau \sim 80 \) days for the eddy heat flux calculation (see Section 2.4). We evaluate the convolution (eqn. 2) over a length of 3 times the e-folding time scale, and correspondingly the first year of data (1979) is omitted, and results are shown for 1980-2011.

With values around 80 days, the empirically determined time scale \( \tau \) is longer than the \( \tau \approx 40 \) days expected from idealized radiative transfer calculations (e.g. Fueglistaler et al. (2014)). The longer-than-expected time scale may reflect variations in \( T_E(t) \) that are correlated, but phase lagged to the dynamical forcing \( f(t) \). Hence, \( T_{\text{dyn}} \) is to be understood as being the dynamically forced temperature including variations in \( T_E \) that are correlated to the dynamical forcing.

The residual,

\[
T_{\text{residual}}(t) = T(t) - T_{\text{dyn}}(t)
\] (3)

thus represents changes in temperature due to (i) radiative changes in \( T_E(t) \) from tracer changes not correlated with dynamics as represented by \( T_{\text{dyn}}(t) \), (ii) errors in the reanalyses’ temperatures and winds, and (iii) errors from dynamical forcing terms not included in the calculation.

With the focus of this analysis on variability and trends over the period 1980-2011, the data is analysed in terms of monthly means. Time series shown are deseasonalised by subtracting the climatological mean of each month of the year determined from detrended data. Since volcanic...
eruptions lead to major disturbances in the radiative conditions (i.e. $T_E$ is not constant), we chose 1995-2011, when stratospheric aerosol variations are small, as reference period for the mean annual cycle. Linear trends are reported for each month of the year, and for annual means of the data. Trends are shown for the full period 1980-2011, and for the period 1980-2011 with the El-Chichon and Pinatubo periods excluded (labeled ‘no-volc’). For consistency between trends with monthly and annual data, 3 full calendar years are excluded (i.e. ‘no-volc’ excludes the years 1982, 1983, 1984, and 1991, 1992, 1993).

### 2.2 Data

Temperature and winds are taken from ERA-Interim (Dee et al., 2011) and MERRA (Rienecker et al., 2011), with ERA-Interim data on the original model levels and MERRA on the (standard) pressure levels of the archived data. Results are shown for the 70 hPa level for MERRA, and for the closest model level of ERA-Interim, which is at 67 hPa. We have also calculated the eddy heat flux proxy using NCEP (Kalnay et al., 1996) and DOE NCEP-2 data; the results from these calculations are fairly similar to those from ERA-Interim and MERRA, and will be mentioned only in specific places to allow comparison with previously published studies that use NCEP data. All terms are calculated from 6-hourly (00/06/12/18UTC) analysis data, at a horizontal resolution of $1^\circ / 1^\circ$ for ERA-Interim and $1.25^\circ / 1.25^\circ$ for MERRA (and $2.5^\circ / 2.5^\circ$ for NCEP).

The reanalysis temperatures are complemented with measurements from the Microwave Sounding Unit (MSU) lower stratospheric channel (‘TLS’, also known as MSU channel 4) as provided by RSS (Mears and Wentz, 2009). The TLS channel’s weighting function is centered near 70 hPa, but the deep vertical weighting function is problematic for interpretation of TLS data in the tropics (Fueglistaler, 2012). The data is shown here for context, and because it provides a tropical mean without sampling bias, and has a strong impact on lower stratospheric temperatures in reanalyses.
2.3 Estimate of temperature variations based on momentum balance

Randel et al. (2002) show that the time-varying zonal mean tropical average upwelling can be calculated from the vertical integral of EP-flux divergence and acceleration at the bounding latitudes (see equation 11 in Randel et al. (2002)). Unlike Randel et al. (2002), we calculate the divergence from the complete EP-fluxes. Problems in this calculation may arise from wave activity not resolved in the reanalyses and, probably more importantly, from spurious drifts in the assimilated observational data (analysed meteorological data is not required to be energetically self-consistent, see e.g. discussion in Fueglistaler et al. (2009a)). The bounding latitudes used here are 30° South and 30° North. The calculated estimate of the tropical mean residual velocity $\bar{w}_{mb}$ (subscript ‘mb’ refers to ‘momentum balance’) is converted to temperature using the Newtonian cooling approximation (see equations 1, 2); with the solution

$$T_{mb}(t) \equiv -K \cdot \bar{w}_{mb}^*(t) e^{t/\tau}$$

where $K = N^2 H / R$.

The correlation with temperature maximises (not shown) for a time scale of $\tau \sim 70$ days. Interestingly, with $\tau = 70$ days the coefficient $K$ determined with an ordinary least squares linear regression (or total least squares fit; implications of this calibration on trends are discussed in Section 3.2) of $T_{mb}$ against actual temperature is very similar to the value obtained by inserting typical values for $N^2$ and $H$ for the lower stratosphere ($N^2 = 6 \cdot 10^{-4} \text{s}^{-2}$, $H = 7000 \text{m}$). This suggests that the magnitude of the residual vertical velocity calculated with the momentum balance equation is actually quite accurate (but recall previous discussion that the empirically determined $\tau$ may account for a modification of temperature variations due to correlated trace gas changes).

2.4 The eddy heat flux proxy for tropical temperatures

Fueglistaler (2012) show that tropical lower stratospheric temperature variations around 70 hPa are well correlated with eddy heat fluxes on the same level, and averaged over a wide latitudinal belt on both hemispheres. The approach is motivated by the success of a similar approach to
predict temperatures in the stratospheric polar vortices by Newman et al. (2001), and a number of related quantities have been used recently to study stratospheric temperatures. For example, Fu et al. (2010) use 3-month mean eddy heat fluxes averaged between 50hPa and 10hPa, Lin et al. (2009) use 3-month means of eddy heat flux between 45° S-90° S at 150 hPa, Ueyama et al. (2013) use an index based on the 100 hPa eddy heat flux, and Bohlinger et al. (2014) use the 100hPa eddy heat flux integrated from 45° N-70° N, and averaged over 45 days.

However, the fact that the simple calculation of Fueglistaler (2012) explains tropical temperatures very well (with correlation coefficients of $\sim 0.85$ for monthly mean data) is an empirical result, indicating that the many neglected aspects (for example where exactly the waves dissipate, and the role of the momentum fluxes) apparently are of secondary importance for variations of monthly mean temperature. Here, we discuss and analyse the sensitivities and limitations of this simple proxy in more detail. We note that, while we use an e-folding of heat fluxes rather than period averages as the studies listed above, our results concerning trends also apply to these studies as the e-folding time scale (or averaging period) is much shorter than the 1980-2011 period for trends.

Similarly to the calculation using the momentum balance equation, we consider the thermodynamic energy equation with Newtonian cooling and simply assume that the forcing from the vertical residual velocity is proportional to the average eddy heat flux. Further, as before, the dynamical forcing $f(t)$ is related to tropical average temperatures using a linear regression to calculate the proportionality coefficient $\alpha$ between the temperature and the e-folded average eddy heat flux (based on eqn. 1 and 2),

$$T_p(t) \equiv \alpha \cdot \left[ v'T' \right]_{25}^{75}(t) * h(t)$$

where $T_p$ is the proxy time series, $v'T'$ is the eddy heat flux, and the operator $\left[ . \right]_{25}^{75}$ is the zonal mean averaged between $25^\circ$ and $75^\circ$ latitude on both hemispheres. As before, $*$ denotes the convolution, and $h(t) = e^{t/\tau}$ for $t \leq 0$ and $h(t) = 0$ for $t > 0$. Note that $\alpha < 0$ (larger eddy heat fluxes force lower temperatures in the tropics). The free parameters are the relaxation time scale $\tau$, and the latitude band over which the eddy heat flux is averaged. The values taken here for these parameters are based on the following analysis.
Figure 1(a,b) shows the correlation coefficients between tropical average temperature and \( T_p(t) \) at the same pressure level, for ERA-Interim (panel a) and MERRA (panel b). The correlations are plotted as function of end latitude of the averaging domain of the eddy heat fluxes, with integration started at 20° latitude, and integration started at 80° latitude. The figure shows that for 70hPa, the proxy’s skill is primarily due to the heat fluxes between 40° and 80° latitude. For this study we use the average between 25° and 75° latitude, but correlations for any proxy that includes the range between about 40° and 70° latitude are similar. Trends, however, are sensitive to choice of latitudes (further discussion in Section 3.4).

In addition to the 70 hPa level, the figure also shows results for the 80 hPa and 96 hPa levels for ERA-Interim, and the 100 hPa level for MERRA. While the correlations are very similar for the 80 hPa level, for 100 hPa the correlations between proxy and temperature are, as expected, weaker (the 100 hPa level in the tropics is in the middle of the TTL, and tropical processes play an important role; see discussion in Fueglistaler et al. (2009b)).

Model intercomparison projects (e.g. Eyring et al. (2010)) often archive (only) the 100 hPa eddy heat fluxes due to their role for polar vortex temperatures (Newman et al., 2001). It is therefore of interest to what extent the 100 hPa eddy heat flux may be used to explain temperatures at 70 hPa. Figure 1(a,b) shows that for ERA-Interim and MERRA, the 100 hPa eddy heat flux is, in terms of correlation, as good as the 70 hPa eddy heat flux for temperatures at 70 hPa.

Figure 1(c) shows the correlation between the deseasonalised eddy heat flux proxy and temperature for the period 1995-2011 as function of the relaxation time scale \( \tau \). For ERA-Interim and MERRA, correlations between tropical average temperature and the proxy maximise for relaxation timescales around 80 days(i.e. about 15% longer than for the momentum balance equation) with a correlation coefficients \( \sim 0.85 \) for the period 1995 to 2011. For NCEP, the corresponding maximum correlation coefficient is 0.75 for a relaxation time scale of \( \sim 60 \) days.

### 2.5 Removal of QBO variability in tropical temperatures

Tropical stratospheric temperatures are strongly affected by the Quasi-Biennial Oscillation (QBO, see e.g. Baldwin et al. (2001)), whose forcing is not well resolved in reanalysis data. The acceleration of the flow in the inner tropics produces a see-saw pattern in temperature
between inner and outer tropics that distorts the relation to meridional eddy heat fluxes. The latitudinal scale of the QBO (order 1000 km) is substantially shorter than the scale of the mid/high latitude eddy forcing, and this scale separation may be used to reduce the variance in tropical temperatures due to the QBO.

Figure 2 shows the correlation and slope of the linear regression of deseasonalised zonal mean zonal wind shear at the equator with the zonal mean deseasonalised temperature for each latitude at 70 hPa. Figure 2(b) shows the slope of the linear regression integrated from the equator to the poles as function of the end latitude (on both hemispheres) of the integral. The figure shows that there exists no latitude belt (symmetric about the equator) where the effect of the QBO on temperature exactly cancels. For this study we have chosen the latitude belt 35° S-35° N as a compromise between a minimisation of QBO-related variance and focus on ‘tropical’ temperatures. The choice of 35° S-35° N for temperature increases the correlation with the eddy heat flux proxy slightly, but does not affect trends (i.e. temperature trends differ by no more than a few percent between 30° S-30° N and 35° S-35° N).

3 Results

In the following, Section 3.1 discusses the deseasonalised time series, specifically also the Pinatubo period and the pre-/post-2000 periods. Section 3.2 discusses the linear trends for the period 1980-2011 in annual mean data, and the seasonality of trends. Sections 3.3 and 3.4 discuss differences between ERA-Interim and MERRA, and between the results using the two different methods.

3.1 Time series

Figure 3(a) shows the deseasonalised global average, the tropical average, and the combined extratropical average of the RSS microwave sounding unit lower stratospheric channel ‘TLS’. The strong anti-correlation between tropical and combined extratropical average temperatures is readily visible, though the fact that they nearly perfectly cancel in the global average in response
to variations in the strength of the residual circulation is a coincidence (Fueglistaler et al., 2011). Also, the apparent step-wise decrease in global average temperatures following the eruptions of El-Chichon and Pinatubo noted by Pawson et al. (1998) is well visible.

Figures 3(b, c) show the tropical average temperatures near 70 hPa, and the dynamically forced temperature variations predicted by the momentum balance equation and the eddy heat flux proxy for ERA-Interim (panel b) and MERRA (panel c). Figure 3(d) shows the residual (temperature minus dynamically forced temperature).

Figure 4 shows the time series of annual means of the dynamically forced temperature variations for both methods, and for both ERA-Interim and MERRA. The time series of annual mean data is used to calculate trends, and some aspects of the time series are clearer seen in the annual mean data.

### 3.1.1 Correlations

The correlations summarized in Tables 1, 2 and 3 confirm the visual impression from Figures 3(b,c) of a remarkably good agreement between the two methods to estimate the dynamically forced temperature variations, and between the estimates of dynamically forced temperature variations and actual temperatures (with the expected exception during the volcanic periods).

Table 1 shows that the correlations between the four calculations for dynamically forced temperature variations have correlations larger than 0.7, with higher correlations for the (shorter) period 1995-2011. The highest correlations are observed between the estimates that use the same method (but different reanalysis), with correlations between the two eddy heat flux proxy calculations being as high as 0.96 (for 1995-2011) and 0.97 (for 1980-2011). This implies that the dynamical information in ERA-Interim and MERRA are very similar. The correlations between the eddy heat flux proxy and the momentum balance equation based on the same reanalysis are still high (1995-2011: 0.83 for ERA-Interim and 0.81 for MERRA), but the fact that they are smaller than those between calculations using the same method indicates that there is a small but noticeable difference in the quantity represented by the two methods.
Table 2 shows the correlations between the calculations of dynamically forced temperature variations and the actual temperatures for ERA-Interim and MERRA. The table shows that for both the 1995-2011 and 1980-2011 (without volcanoes) periods both calculations of dynamically induced temperature variations agree well with the actual temperatures (with correlations as high as 0.87). For the period 1995-2011, the two methods perform equally well, while for the full period 1980-2011 (excluding volcanoes) the eddy heat flux calculations are better correlated (correlations of 0.83 for both ERA-Interim and MERRA). This is both due to different trends in the two methods (discussed below), and due to a generally lower agreement between temperature and the estimated dynamical temperature in the 1980’s particularly for the momentum balance equation (for the period 1980-1990 (excluding volcanoes), the correlation for the momentum balance calculation for MERRA is only 0.51). With the information available here, we cannot address the question to what extent the lower correlation in the 1980’s is due to larger errors in temperature, larger errors in the reanalyses’ dynamical information, or larger variations in temperature due to radiatively active trace constituents.

Finally, Table 3 shows the correlations between the residuals for the period 1995-2011 when variations in $T_E$ due to changes in radiatively active trace constituents are expected to be small, and the residuals may largely reflect errors in the estimates of the dynamical forcing and errors in actual temperature. The residuals are correlated highest between estimates using the same method but different reanalyses (residuals based on eddy heat flux proxy: 0.90; residuals based on momentum balance: 0.67). This result may be expected from the correlations between the dynamical temperature estimates (Table 1), but note that the residuals have additional information, namely the ERA-Interim and MERRA actual temperatures. However, the ERA-Interim and MERRA temperatures are very similar for 1995-2011 and hence introduce only a small amount of additional variance. Conversely, the residuals using different methods show lower correlations (for MERRA, the correlation of the residuals from the momentum balance calculation and the eddy heat flux proxy is as low as 0.36), which supports the previous notion that the main difference between the four calculations is that two methods represent two slightly different quantities.
3.1.2 Volcanic periods

Figure 3(d) shows that the residual is - as expected - largest during the El-Chichon and Pinatubo volcanic periods. The four estimates of the dynamically forced temperature during the Pinatubo period agree well, and all show the anomalously strong forcing noted by Fueglistaler (2012) in ERA-Interim eddy heat flux proxy calculations. Hence, the calculations show additional strong evidence that this response is real and not due to problems in either the eddy heat flux proxy, or in ERA-Interim data. A similar response is not observed following the eruption of El-Chichon, which suggests that there may not be a canonical dynamical response to volcanic eruptions. Further analysis of the dynamical situation following the Pinatubo eruption is beyond the scope of this paper and will be presented elsewhere. Finally, we note that the uneven distribution of volcanic eruptions substantially distorts linear trend calculations for temperature, dynamically forced temperature, and residual. We recommend that stratospheric trends reported in the literature exclude the volcanic periods in order to allow better comparisons between results using slightly different reference periods.

3.1.3 The year 2000 period

Water entering the stratosphere in the tropics shows a pronounced drop around the year 2000 that lasts for several years and is arguably among the most prominent changes in stratospheric composition observed over the last 3 decades. Fueglistaler (2012), based on eddy heat flux proxy calculations using ERA-Interim, locate the onset of the dry period to October 2000 as a result of a dynamical cooling induced by anomalous Southern Hemisphere dynamics. The eddy heat flux proxy based on MERRA, and the momentum balance calculations of both reanalyses (see Figure 3b,c), confirm this result.

Randel et al. (2006) attribute the prolonged dryness over several years to an increase in the strength of the residual circulation of the post-2000 period relative to the pre-2000 period. Table 4 summarizes our results for the dynamically induced temperature change over that period for the 70 hPa level. The table shows that (also visually clearly seen in Figure 4) results depend on the length of comparison period chosen, and that the eddy heat flux calculations give a clearer
separation for the pre-/post year 2000 years. The smallest temperature difference is observed in the ERA-Interim momentum balance calculation, while the other 3 calculations give a period-averaged decrease in dynamically forced temperature at 70 hPa of about -0.4 K for the period 2001-2005 against 1995-2005. Hence, the calculations shown here support the result of Randel et al. (2006). We note that the eddy heat flux results presented here for the 70 hPa level show a much clearer change around the year 2000 than those presented in Fueglistaler (2012) that were based on 96 hPa eddy heat fluxes, and implications for water entering the stratosphere (which is controlled by conditions around 90-80 hPa rather than 70 hPa) remain to be analysed in more detail. Further, we emphasize that the strengthening of the residual circulation is only true for a few years around the year 2000 - for the whole 1990’s versus the 2000’s the residual circulation has been weakening (i.e. dynamical warming of the tropics) due to the anomalous dynamics following the Pinatubo eruption.

3.1.4 Conclusions concerning the methods

To summarise this section, we note that the dynamical information in ERA-Interim and MERRA used for the two methods to calculate the dynamical temperature variations is very similar, and results using the same method are more similar than using the same reanalysis but different methods. The implications for the residual are that the residual temperature time series do not only represent variations in $T_E$ not correlated with dynamical forcing, but also errors from incorrect representation of the dynamical forcing in one or both methods. Large events, however, such as the Pinatubo period and the pre-/post year 2000 periods, are similar for both methods and both reanalyses.

3.2 Trends

The evolution of temperature and of the dynamically forced temperatures shown in Figure 3 shows a large amount of variability even when excluding the volcanic periods, and the time series may be too short to reliably detect a trend. However, linear trends provide an objective metric to compare the time series quantitatively, and for temperature linear trends are routinely
reported in the literature. We therefore calculate and discuss the linear trends in our estimates of dynamically forced temperature, but emphasise that we regard these trends simply as the first moments of the time series.

The trends in dynamically forced temperature - and hence also in the residual - depend on the trend in the dynamical forcing $f(t)$ (equation 2). Further, the magnitude of the trends depends also on the empirically determined proportionality coefficients $K$ (equation 4) and $\alpha$ (equation 5). The 1-sigma uncertainty in the linear regressions to determine $K$ and $\alpha$ is about 10% in all calculations. The coefficients determined with a total least squares fit are about 20% larger than when determined with an ordinary least squares regression. Both of these uncertainties are smaller than the differences between the four calculations, and we therefore focus the discussion primarily on the latter.

### 3.2.1 Overview of trends

Figure 4 shows the trends calculated from the annual mean data, and Figure 5 summarises the trends (annual means and seasonal cycle) for all calculations for the full period 1980-2011 (Figure 5, panels a-d), and for 1980-2011 without volcanic periods (Figure 5, panels e-h). For visual clarity, error bars are not shown. Table 5 summarises the numerical values of the trends based on annual mean data including their statistical 1-sigma uncertainties.

Figure 5 shows that, as argued above, the volcanic periods have a substantial impact on trends. Therefore, we focus below on trends based on data excluding volcanic periods, but the following aspect is noteworthy with respect to previously published temperature trends that did not exclude the volcanic periods: The largest impact of volcanic periods is a change in the annual mean trend in the residual that is dominated by the impact of the volcanic periods on trends in actual temperature. Conversely, the seasonality of trends is less affected, and the anomalous dynamically forced cooling following Pinatubo does not dominate linear trends since the event is roughly in the middle of the period 1980-2011.
3.2.2 Trends in annual means

Table 5 summarises the linear trends based on annual mean data for actual temperatures in ERA-Interim and MERRA. The table and Figure 5 show that the largest trend differences between ERA-Interim and MERRA are about 0.15 K/decade in actual temperature. Trends in dynamically forced temperature are similar between ERA-Interim and MERRA when using the same method. However, the difference in trends between estimates using the momentum balance calculation and the eddy heat flux calculation are about 0.2 K/decade. The eddy heat flux calculation gives a statistically significant cooling of the tropical lower stratosphere when excluding volcanic periods in both ERA-Interim and MERRA. Conversely, the momentum balance calculations give no statistically significant trend, or even a slight warming. Similar results are obtained when using a total least squares fit for $\alpha$ and $K$, except that in this case the magnitude of the trends is about 20% larger.

Finally, we note that, to the extent that the two calculations are comparable, the cooling implied by the homogenised ozone data of Hassler et al. (2013) as shown by Solomon et al. (2012) (order -3K for period 1995-1997 versus 1979-1981) is larger than the largest (no-volc) trend in our residual, or the difference between their two periods qualitatively estimated from our Figure 3(d).

3.2.3 Seasonality of trends

Temperature trends in the tropical lower stratosphere show a prominent seasonality (seen in Figure 5) that has attracted much attention (e.g. Fu et al. (2010); Free (2011); Polvani and Solomon (2012)). Fu et al. (2010) conclude, based on an analysis using eddy heat flux calculations, that the seasonality is largely driven by a seasonality in the dynamical forcing of temperatures. Conversely, Polvani and Solomon (2012) show that in a GCM with prescribed sea surface temperatures, greenhouse gases and ozone, the model’s seasonal cycle of temperature trends is similar to observations only when the model is forced with observed ozone changes (which have a pronounced seasonality).
The results shown in Figure 5 show that not only do the annual mean trends differ particularly between the two methods, but also the seasonality. Figure 6(a) shows the trends in the dynamically forced temperature of the four calculations in one panel (data is identical to that shown in Figure 5e-h). It is evident that the largest differences occur during boreal winter, which is also seen in the seasonality in the residual trend (Figure 5(e-h), shaded in blue/red). Figure 6(b) shows the fractional trends in the dynamical forcing ($f(t)$, equation 2) of the four calculations. The figure shows that from March to October the four estimates roughly agree, but that the magnitude of the trend in the momentum balance calculation for November, December and January is much smaller than in the eddy heat flux calculations. The phase shifting due to the radiative damping then leads to the marked differences in dynamically forced temperatures in January and February. Similarly, the differences in dynamical forcing during December and January largely account for the annual mean trend differences between the two methods. None of the four calculations, however, show the seasonal structure of upwelling trends (indicating an increase in upwelling during boreal summer) in the GCM calculations of Polvani and Solomon (2012) (compare with their Figure 7b).

### 3.3 Eddy heat flux divergence between 100 and 70 hPa

The trends in dynamically forced temperature based on the eddy heat flux proxy are similar in ERA-Interim and MERRA (Table 5), but the difference is large enough to warrant further analysis. Here, we focus on the evolution of the time series and identify when the time series diverge. In Section 3.4 below we also show at which latitudes eddy heat flux trends differ most.

Figure 7(a) shows the difference ERA-Interim minus MERRA eddy heat flux proxy at 70 hPa and at 100 hPa. The figure shows that from about the year 2000 onwards, ERA-Interim drifts (cooling) relative to MERRA. Figure 7(b) shows the ratio of the proxy calculated from 100 hPa eddy heat fluxes to that calculated from 70 hPa eddy heat fluxes. The figure shows that for MERRA this ratio remains approximately constant, while for ERA-Interim this ratio increases after about the year 2000. That is, in ERA-Interim the eddy heat flux at 70 hPa slightly increases, and at 100 hPa slightly decreases. Hence, in the “ERA-Interim world” a change in the eddy dissipation between 100 hPa and 70 hPa occurs in the early 2000’s, which is not seen in the
“MERRA world” (and is also not seen in NCEP data; result not shown). It is unclear at this point what exactly causes these drifts between the reanalyses. We consider a problem in ERA-Interim data more likely than what would be, arguably, an interesting signal. A hypothesis is that the onset of assimilation of GPS temperature data in ERA-Interim (from the early 2000’s onwards CHAMP, and after 2006 COSMIC (Poli et al., 2010; Dee et al., 2011)) may induce a drift in ERA-Interim that is not present in MERRA (which does not assimilate these data (Rienecker et al., 2011)).

3.4 Differences between momentum balance and eddy heat flux proxy

Figures 4, 5 and Table 5 show a cooling due an increase in dynamical forcing according to the eddy heat flux proxy both in ERA-Interim and MERRA, with very similar annual mean trends, and seasonality in trends. These results are similar to those presented by Fu et al. (2010), whose analysis is also based on eddy heat fluxes (albeit they used NCEP and ERA-40 data, and their latitude range and pressure levels differ from ours). Hence, eddy heat flux trends seem fairly robust across different reanalyses, with an overall increase in eddy heat fluxes over the last 3 decades (qualitatively consistent with the notion of an overall strengthening of the stratospheric residual circulation), and the seasonality of temperature trends being also a consequence of a shift in the time of year of wave activity (note the decreases in November and March bracketing the increases in December and January).

Conversely, the results using the momentum balance calculation indicate basically zero trend in upwelling (and temperature) between 30° S-30° N, leaving a much larger trend residual that contributes also significantly to the seasonality in tropical temperature trends (i.e. according to the momentum balance calculations, the cooling seen in January/February is largely due to radiatively active trace constituents not correlated with dynamical forcing).

Both the eddy heat flux proxy and the momentum balance calculations may suffer from difficult-to-quantify problems in the reanalyses, and with the available data it is not possible to conclusively resolve which of the two calculations give more reliable trends. In the following, we analyse which aspects of the data used for the eddy heat flux calculations lead to the differences. Identification of the cause of the differences may motivate future work with tar-
geted primitive equation model calculations to address the question whether the eddy heat flux proxy may be biased for trends, or whether the momentum balance calculations give erroneous trends due to drifts in the reanalysis input data.

Figure 8 shows the trends in monthly mean eddy heat fluxes seasonally resolved (panels a, b for ERA-Interim and MERRA, respectively), and for the annual mean data (panel c). The figure shows that the cooling trend in the eddy heat flux proxy arises from the high latitudes, while over the mid-latitudes the eddy heat fluxes may even decrease (particularly in MERRA). That is, in ERA-Interim and MERRA, the eddy heat fluxes shift polewards and overall intensify. Panels a,b show that the seasonality seen in Figure 5 is a consequence of a temporal shift in eddy heat fluxes in the hemispheric winter months, in agreement with Fu et al. (2010). In the Northern Hemisphere, the eddy heat fluxes increase in December and January (giving maximum cooling in the tropics in January/February due to the phase lag from radiative temperature damping), and in the Southern Hemisphere the polewards eddy heat fluxes increase in September and, to a lesser extent, October and December, while they decrease in November.

The latitudinal structure in eddy heat flux trends raises the question how robust the trend in dynamically forced temperatures is with respect to the specific latitude band over which the eddy heat fluxes are averaged. We find (not shown) that the trends in average eddy heat fluxes are reasonably robust against further widening of the latitude belt (i.e. extending further equatorwards than 25° latitude, and/or extending further polewards than 75° latitude). However, trends are sensitive to narrowing the latitude belt (as may be anticipated from Figure 8c).

Figure 9 shows the trends in dynamically forced temperatures based on the eddy heat flux averaged from 75° latitude equatorwards, as function of the equatorward bounding latitude. Note that for this calculation, not only is the forcing function (the average eddy heat flux) dependent on the end latitude, but also the proportionality coefficient \( \alpha \) (equation 5).

Figure 9 shows that for all latitude bands ending at high latitudes (here, 75° latitude), the eddy heat flux proxy calculations gives a dynamical cooling of the tropical lower stratosphere. The differences between ERA-Interim and MERRA dynamical temperature trends are due to the differences in mid- and low latitude eddy heat fluxes seen in Figure 8(c). The figure also shows that the trend uncertainty arising from the 1-sigma uncertainty in \( \alpha \) is small. When using a total
least squares fit to determine $\alpha$, the latitudinal structure and difference between ERA-Interim and MERRA remain very similar, but the amplitudes of the trends are about 20% larger (not shown).

4 Conclusions

We have estimated the variations in dynamical forcing of tropical lower stratospheric temperatures at 70hPa over the period 1980-2011 due to variations in tropical upwelling. The dynamical forcing is calculated with the momentum balance equation for tropical average upwelling following Randel et al. (2002), and a simple proxy using the average eddy heat flux between 25° and 75° on both hemispheres following Fueglistaler (2012). All four calculations yield very high correlations (of about 0.85) with actual temperature for the period 1995-2011 when temperature variations due to variations in radiatively active trace constituents not correlated to the dynamical forcing are small. For the period 1980-1991 (excluding volcanic periods), correlations with the eddy heat flux proxy are slightly lower (between 0.77 and 0.8). For the momentum balance calculation, the correlations drop to 0.67 (ERA-Interim) and 0.51 (MERRA) for reasons not clear at present.

All four calculations confirm the previously noted anomalously strong dynamical cooling following the Pinatubo eruption (Fueglistaler, 2012), and the role of the stratospheric residual circulation for the marked drop of water entering the stratosphere at the end of the year 2000, initiated by anomalous Southern hemispheric dynamics in October 2000 (Fueglistaler, 2012) and subsequent enhanced upwelling over a few years relative to the years before the year 2000 (Randel et al., 2006).

In all aspects considered, we find that the calculations using the same method, but different reanalysis (i.e. ERA-Interim and MERRA), agree better than the calculations using the same reanalysis but different methods. Hence, we conclude that the dynamical information in the two reanalyses is very similar, but that the two methods evaluate slightly different quantities. Differences between the results of the two methods are most pronounced in trends over the period 1980-2011.
The eddy heat flux proxy indicates a statistically significant cooling of about -0.1K to -0.25K for that period (excluding volcanic periods), with annual mean trends, and the seasonal cycle thereof, being strongly influenced by an increase in very high latitude eddy heat fluxes during December and January. The residual trends (due to trends in radiatively active trace species not correlated to dynamics, and/or errors in data and method) are relatively small for these calculations. Our results based on the eddy heat flux proxy are similar to those presented by Fu et al. (2010), which are also based on eddy heat flux calculations.

Conversely, the momentum balance calculations show no statistically significant trend over the period 1980-2011 (excluding volcanoes), mainly because they do not show the strengthening of upwelling in December and January seen in the eddy heat flux calculations. Consequently, with the momentum balance calculation the residual trends are roughly twice as large as those based on the eddy heat flux calculation, and the seasonality of actual temperature trends during December-April are mainly a consequence of the residual, which then has to be explained by trends in radiatively active trace constituents not correlated with dynamics.

The differences in trends of dynamically forced temperature between the two methods, and the discussed sensitivity of the magnitude of trends in the eddy heat flux proxy calculation to the latitude belt used, requires further attention. The results from the eddy heat flux proxy are highly plausible as they explain the observed temperature trends very well, but the tight relation between average eddy heat fluxes and temperature is an empirical result. The physically correct representation of tropical upwelling calculated with the momentum balance equation, in turn, gives a residual with a much larger seasonality (i.e. trends due to radiatively active tracers not correlated with dynamics would have to account for the cooling during boreal winter, while for boreal fall they would induce barely any temperature trend).

We have identified the very high latitude eddy heat flux trends during December and January to be the main source of the disagreement between the two calculations. Primitive equation model calculations with perturbations of high latitude eddy heat fluxes may be used to resolve the question whether the proxy calculations overestimate the impact of high latitude eddy heat flux trends on tropical temperatures.
Given the currently unresolved differences between methods, the role of dynamical forcing (and consequently also the role of trends in radiatively active trace constituents) for tropical lower stratospheric temperature trends remains unclear at present. Conversely, the excellent correlation of all four estimates of dynamically forced temperature with actual temperature variations is very encouraging and suggests that these calculations can be used to study the mechanisms of interaction between dynamics, radiatively active trace constituents and temperature in observation-based data; and that for specific periods of interest the temperature evolution can be attributed to dynamics and radiatively active trace constituents with reasonable accuracy.

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References


Table 1. Correlation between the dynamical temperature variations predicted by the eddy heat flux proxy and the momentum balance calculation based on ERA-Interim and MERRA, for the periods 1995-2011 (top) and 1980-2011 (bottom).

<table>
<thead>
<tr>
<th></th>
<th>ERA-I v‘T’</th>
<th>ERA-I m-bal</th>
<th>MERRA v‘T’</th>
<th>MERRA m-bal</th>
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<tr>
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<tr>
<td>ERA-I m-bal</td>
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<td>0.84</td>
<td>0.90</td>
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<tr>
<td>MERRA v‘T’</td>
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<td>-</td>
<td>1</td>
<td>0.81</td>
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<tr>
<td>MERRA m-bal</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>1</td>
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Table 2. Correlation between temperature and temperature predicted by the eddy heat flux proxy (labelled $v'T'$) and the momentum balance calculation (labelled ‘m-bal’), for ERA-Interim and for MERRA; for the periods 1995-2011 (no major volcanic eruptions) and the period 1980-2011 with El-Chichon and Pinatubo periods exluded (see text).

<table>
<thead>
<tr>
<th>Period</th>
<th>ERA-I $v'T'$</th>
<th>ERA-I m-bal</th>
<th>MERRA $v'T'$</th>
<th>MERRA m-bal</th>
</tr>
</thead>
<tbody>
<tr>
<td>1995-2011</td>
<td>0.84</td>
<td>0.83</td>
<td>0.86</td>
<td>0.87</td>
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<tr>
<td>1980-2011, no-volc</td>
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<td>0.72</td>
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<td>0.75</td>
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<td>1980-1990, no-volc</td>
<td>0.77</td>
<td>0.67</td>
<td>0.80</td>
<td>0.51</td>
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### Table 3

Correlation between residuals (as shown in Figure 3d) for the period 1995-2011. Duplicate information not shown.

<table>
<thead>
<tr>
<th></th>
<th>ERA-I (v'T)</th>
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<th>MERRA (v'T)</th>
<th>m-bal</th>
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<td>MERRA (v'T)</td>
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<td>0.36</td>
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<td>MERRA m-bal</td>
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<td>-</td>
<td>-</td>
<td>1</td>
</tr>
<tr>
<td>First/last</td>
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<td>MERRA mb</td>
<td>ERA-I v’T‘</td>
<td>MERRA v’T‘</td>
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<td>--------------</td>
<td>----------</td>
<td>----------</td>
<td>------------</td>
<td>------------</td>
</tr>
<tr>
<td>1998 / 2002</td>
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<tr>
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<td>-0.42</td>
<td>-0.25</td>
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<tr>
<td>1993 / 2007</td>
<td>0.21</td>
<td>-0.10</td>
<td>-0.38</td>
<td>-0.16</td>
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**Table 4.** Difference in dynamically forced temperature $T_{\text{dyn}}$ (in Kelvin) of period after the year 2000 minus period before the year 2000, for $T_{\text{dyn}}$ estimated from the momentum balance (‘mb’) calculation and the eddy heat flux proxy (v’T’), based on ERA-Interim and MERRA. Differences are shown for period lengths of 2 to 6 years (i.e. the last row shows the difference of [2001-2007] minus [1993-1999]).
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>ERA-I</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Temp.</td>
<td>-0.50±0.11</td>
<td>-0.35±0.10</td>
</tr>
<tr>
<td>T(v‘T’)</td>
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<td>-0.24±0.08</td>
</tr>
<tr>
<td>T(m-bal)</td>
<td>0.10±0.09</td>
<td>0.03±0.07</td>
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<tr>
<td><strong>MERRA</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Temp.</td>
<td>-0.37±0.12</td>
<td>-0.18±0.11</td>
</tr>
<tr>
<td>T(v‘T’)</td>
<td>-0.06±0.10</td>
<td>-0.12±0.09</td>
</tr>
<tr>
<td>T(m-bal)</td>
<td>0.10±0.10</td>
<td>0.00±0.10</td>
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</table>

**Table 5.** Linear trends and 1-sigma statistical uncertainty for tropical average (35° S-35° N) temperature, and the dynamically forced temperatures estimated with the eddy heat flux proxy and the momentum balance calculation; for the pressure levels 67 hPa (ERA-Interim) and 70 hPa (MERRA). Results shown for the full period 1980-2011, and the period 1980-2011 excluding volcanic periods.
Fig. 1. Correlation between deseasonalised tropical average temperature and dynamical temperature based on integrated eddy heat flux, convolved with e-folding timescale of 85 days, for pressure levels near 100 hPa, 80 hPa (where available) and 70 hPa (color coded as labeled in panels). Also shown (green) are the correlations between the e-folded eddy heat flux near 100 hPa with the temperatures near 70 hPa. Results are shown for (a) ERA-Interim, and (b) MERRA. (c) Correlation as function of relaxation time scale $\tau$ for the eddy heat flux averaged over the latitude range $25^\circ$-$75^\circ$ for ERA-Interim, MERRA, and NCEP DOE. All calculations refer to the period 1995-2011.
Fig. 2. (a) Correlation coefficient and slope of linear regression of zonal mean, deseasonalised temperature at 67hPa and given latitude with deseasonalised equatorial zonal mean zonal wind shear \((dU/d\ln(p))\) at same level, calculated from ERA-Interim over the period 1994-2012. (b) Slope of linear regression shown in (a) integrated from equator, note a small residual remaining even when averaging globally (see text for discussion). Also shown is 35°, taken in this study as boundary for tropical average temperature (see text).
(a)

RSS/TLS: tropics extra-trop global

(b)

ERA-Interim

Temp $T_p$ $T_{mb}$

(c)

MERRA

Temp $T_p$ $T_{mb}$

(d)

Residuals

ElChichon Pinatubo

Fig. 3. (a) RSS Microwave Sounding Unit (MSU) lower stratospheric temperatures (MSU channel 4, or ‘TLS’), global (black), tropical (magenta) and combined extra-tropical (purple). (b,c) Tropical (35° S-35° N) temperature at 70hPa, and estimates of dynamical temperature $T_p$ (based on eddy heat flux calculation, see text) and $T_{mb}$ (based on momentum balance calculation, see text); for ERA-Interim (panel b), and MERRA (panel c). (d) The residuals (tropical average temperature minus dynamical estimates) for ERA-Interim, and MERRA (color coded as in panels b,c). Correlations between the estimates of dynamically forced temperature are given in Table 1, between temperature and dynamical estimates in Table 2, and between the residuals in Table 3. All panels show deseasonalised data, with the mean annual cycle evaluated over the period 1995-2011.
Fig. 4. Time series of annual mean dynamically forced temperature variations ($T_{\text{dyn}}$) from ERA-Interim and MERRA (color coded, conventions as in Figure 3) with results of linear regression excluding the volcanic periods (grey shaded). (a) $T_{\text{dyn}}$ based on the momentum balance calculation (i.e. $T_{\text{mb}}$); (b) $T_{\text{dyn}}$ based on the eddy heat flux calculation (i.e. $T_{\text{p}}$).
**Fig. 5.** Overview of trends in temperature and in estimates of dynamically forced temperature based on the momentum balance calculations ($T_{mb}$, panels a, b, e, f) and eddy heat flux calculations ($T_p$, panels c, d, g, h) for ERA-Interim (panels a, c, e, g) and MERRA (panels b, d, f, h). Panels (a-d) show trends for the period 1980-2011, panels (e-h) show trends for the period 1980-2011 excluding volcanic periods. Temperature trends are shown in black, dynamically forced temperature trends in brown. Residual trends are shown in blue for cooling, and in red for warming.
Fig. 6. (a) Trends for the period 1980-2011 (excluding volcanic periods) in dynamically forced tropical temperatures at 70 hPa for both reanalyses (ERA-Interim and MERRA) and both methods (momentum balance calculation, and eddy heat flux proxy). Data as shown in Figure 5(e-h). (b) The fractional trends in monthly means of the forcing $f(t)$ (equation 2), i.e. $\bar{w}^*$ for the momentum balance calculation, and eddy heat flux for the eddy heat flux proxy. Trends in panel (a) are forced by trends in panel (b), but are phase-shifted (due to e-folding with $\tau \sim 80$ days), and magnitude depends on the empirically determined proportionality coefficients $\alpha, K$ (equations 5,4). Color coding labeled in Figure, conventions as in Figure 3.
Fig. 7. (a) Time series of differences between ERA-Interim and MERRA in deseasonalised, monthly means of dynamical proxy for tropical temperatures at 70 hPa and 100 hPa (with ±1 offsets). The proxy time series have been normalised by their standard deviations over the period 1980-2011, with the sign convention as for tropical temperature (i.e. an increase in proxy corresponds to an increase in tropical temperature, and decrease in eddy heat flux). (b) Deseasonalised ratio of e-folded average eddy heat flux at 70 hPa and 100 hPa. The data in (a) and (b) have been smoothed with a running mean of 12 months for visual clarity.
**Fig. 8.** (a) Latitudinal structure of ERA-Interim annual mean eddy heat flux trends at 67 hPa as function of month of year. El-Chichon and Pinatubo periods excluded. (b) Ditto but for MERRA at 70 hPa. (c) Latitudinal structure of eddy heat flux trends from annual mean data, pressure levels as in panels (a), (b). Grey shading shows the latitude ranges 75° S–25° S and 25° N–75° N used to calculate the eddy heat flux temperature proxy.
Fig. 9. Linear trends for the period 1980-2011 (excluding volcanic periods) in dynamically forced tropical temperature $T_p$ based on the ERA-Interim (blue, at 67 hPa) and MERRA (red, at 70 hPa) eddy heat flux calculation as function of equatorward bound of the latitude belt used to average the eddy heat flux, for start latitude 75 degrees. The error bars show the trend uncertainty in dynamically forced temperature due to the 1-sigma uncertainty in the determination of the proportionality coefficient $\alpha$ in equation 5.