Sensitivity analysis of an updated bidirectional air-surface exchange model for elemental mercury vapor

Xun Wang¹,², Che-Jen Lin¹,³,⁴, Xinbin Feng¹

¹ State Key Laboratory of Environmental Geochemistry, Institute of Geochemistry, Chinese Academy of Sciences, Guiyang, China
² University of Chinese Academy of Sciences, Beijing, China
³ Department of Civil Engineering, Lamar University, Beaumont, TX, USA
⁴ College of Environment and Energy, South China University of Technology, Guangzhou, China

Correspondence to: C.-J. Lin (jerry.lin@lamar.edu); X. Feng (fengxinbin@vip.skleg.cn)

Abstract

A box model for estimating bidirectional air-surface exchange of gaseous elemental mercury (Hg⁰) has been updated based on the latest understanding of the resistance scheme of atmosphere-biosphere interface transfer. Simulations were performed for two seasonal months to evaluate diurnal and seasonal variation. The base-case results show that water and soil surfaces are net sources while vegetation is a net sink of Hg⁰. The estimated net exchange in a domain covering the contiguous US and part of Canada and Mexico is 38 and 56 Mg as evasion in the summer and winter month. The smaller evasion in summer is due to the stronger Hg⁰ uptake by vegetation. Modeling experiments using a 2-level factorial design were conducted to examine the sensitivity of flux response to changes of physical and environmental parameters in the model. It is shown that atmospheric shear flows (surface wind over water and friction velocity over terrestrial surfaces), dissolved gaseous mercury (DGM) concentration, soil organic and Hg content, and air temperature are the most influential factors. The positive effect of friction velocity and
soil Hg content on the evasion flux from soil and canopy can be effectively offset by the negative effect of soil organic content. Significant synergistic effects are identified between surface wind and DGM level for water surface, and between soil Hg content and friction velocity for soil surface, leading to ~50% enhanced flux compared to the sum of their individual effects. The air-foliar exchange is mainly controlled by surface resistance terms influenced by solar irradiation and air temperature. Research in providing geospatial distribution of Hg in water and soil will greatly improve the flux estimate. Elucidation on the kinetics and mechanism of Hg(II) reduction in soil/water and quantification of the surface resistances specific to Hg species will also help reduce the model uncertainty.

1 Introduction

Mercury (Hg) is a persistent, bioaccumulative pollutant released into the atmosphere from a variety of anthropogenic and natural sources. The anthropogenic release (2000~2400 Mg yr\(^{-1}\)) primarily comes from fossil fuel combustion, waste incineration, metal smelting and cement production (Pacyna et al., 2006; Pacyna et al., 2003; Streets et al., 2005; Streets et al., 2009; Pirrone et al., 2010). The natural sources include geological weathering from Hg enriched substrates, biomass burning, volcanic activities and other Hg\(^0\) exchange, including so-called re-emission, at the atmosphere-biosphere interface (Gustin et al., 2008; Mason and Sheu, 2002). While the men-made emissions have been estimated and continuously updated with reasonable consistency since the 1990s, the estimates for natural emissions have been highly uncertain (1500-5207 Mg yr\(^{-1}\)), primarily due to a lack of understanding in the air-surface exchange of Hg\(^0\). Since the natural release can account for up to two-thirds of global mercury input to the atmosphere (Friedli et al., 2009; Pirrone et al., 2010), better quantification of the mass input is critical in assessing the global biogeochemical cycling of mercury (Lindberg et al., 2007).

Air-surface exchange is an important component in atmospheric mercury modeling for estimating Hg\(^0\) evasion and deposition over soil, water and vegetation. For terrestrial surfaces, the soil Hg evasion has
been calculated using the statistical relationships obtained from the measured Hg\textsuperscript{0} flux and observed
environmental factors such as temperature, solar irradiance, leaf area index, and Hg content (Bash et al.,
2004; Gbor et al., 2006; Lin et al., 2005; Shetty et al., 2008; Xu et al., 1999; Selin and Jacob, 2008; Smith-
Downey et al., 2010). Such an approach oversimplifies the role of environmental factors in the exchange
process because Hg\textsuperscript{0} flux was measured only in a limited number of locations where the environmental
parameters (such as soil properties and meteorology) are specific to those sites. Using the limited
measurement data for extrapolating the flux estimate in a large geographical area may not representative.
In addition, most of these models treat vegetation as a net evasion source of Hg\textsuperscript{0}, which is inconsistent
with later assessments that suggest vegetation a net sink (Gustin et al., 2008; Hartman et al., 2009). Recent
isotopic tracer studies showed that that plant roots serve as a barrier that prevents translocation of
inorganic Hg in soil to other parts of plants (Cui et al., 2014). It has also been suggested that Hg absorbed
on foliage can be transported to stem and root (Yin et al., 2013). In addition, algorithms representing the
transport resistances at soil and foliage interfaces were developed to calculate the multilayered,
bidirectional flux through a Hg concentration gradient between ambient level and a "compensation" point
inferred from the surface characteristics (Bash, 2010; Bash et al., 2007; Scholtz et al., 2003; Zhang et al.,
2009a; Sutton et al., 2007). This approach is more scientifically sound and mathematically robust. The
model results also seem to be more consistent with those from stable isotope studies (Bash, 2010).
However, the complicated model parameterization makes it difficult to understand the relative importance
of model variables on the simulated flux. It also requires assumptions for numerous model variables that
lack field data to estimate their values. Although the model results can be constrained by air concentration
and wet deposition, the assumptions could increase the uncertainty of model estimates and limits the
improvement of model algorithms.
The objectives of this study are to present an updated Hg\textsuperscript{0} air-surface exchange model and to
quantitatively examine the relative importance of the physical and environmental variables implemented
in the model. Coupled with the latest understanding in the partitioning and mass transfer at different atmosphere-biosphere interfaces, we integrated the bidirectional air-surface exchange model (Bash, 2010; Bash et al., 2007) and the surface resistance schemes of Hg dry deposition and photochemical reaction (Zhang et al., 2003; Zhang et al., 2009a; Lin et al., 2006) for quantifying the air-surface exchange of Hg$^0$. Two monthly simulations were performed to investigate the seasonal and diurnal variability of the model-estimated flux. A systematic set of sensitivity simulations using multi-step factorial designs of experiments were performed to investigate the effect of significant model parameters and their interconnections. Based on the sensitivity results, processes that control Hg$^0$ air-surface exchange over different natural surfaces are discussed and research needs for future model improvement are proposed.

2 Methods

2.1 Model Description

The total air-surface exchange is the sum of Hg$^0$ fluxes from water, soil (including bare lands and soil under the canopy) and foliage surfaces. The direction (evasion or deposition) of the flux is driven by the gradient between atmospheric Hg$^0$ concentration and a surface compensation point that represents the Hg$^0$ concentration at the interface between the atmosphere and a natural surface. The magnitude of the flux is determined by the ratio of concentration gradient to surface resistance (for terrestrial surfaces) or by the product of overall mass transfer coefficient and concentration gradient (for water surfaces). The nomenclature and dimension of the entire set of model variables are detailed in Table 1. The parameterization of each model component is briefly described below.

2.2 Air-water Exchange

The flux over fresh water and oceanic surfaces, $F_{w}$, is calculated using a two-film mass transfer model with the transfer rate limited by the diffusion in the water boundary layer (Poissant et al., 2000):
where $K_w$ is the overall mass transfer coefficient estimated by the wind speed at 10 m above water surface and the mass transfer ratio of CO$_2$/Hg across the air-water interface (Shetty et al., 2008), $C_w$ is the DGM concentration in surface water, $H_w$ is the dimensionless Henry’s law constant. $K_w$ and $H_w$ are calculated using formulation described earlier (Poissant et al., 2000; Lin and Tao, 2003).

2.3 Air-terrestrial Exchange

The terrestrial system is divided into two categories: the canopy biomes (leaf area index, LAI > 0) and the bare lands (LAI = 0, referring to barren or sparsely vegetated land, bare ground tundra and snow or ice surface). The total flux from the canopy is made up of the air-soil exchange flux and the air-foliar exchange flux (air-stomata and air-cuticle). Over the canopy system, a multi-layer canopy resistance scheme modified after Bash (2010) and Zhang et al. (2003) was applied (Figure 1). Compared to the earlier mechanistic schemes, this model also (1) includes foliage storage effect is included, (2) considers photochemical reduction on foliage, and (3) updates the resistance terms. The flux over canopy biomes, $F_{cnp}$, is estimated as:

$$F_{cnp} = \frac{\Delta t}{(R_a + R_b)} (\chi_{cnp} - C_{atm})$$  \hspace{1cm} (2)

where $\Delta t$ is time duration, $R_a$ is the aerodynamic resistance, $R_b$ is the quasi-laminar sub-layer resistance, $C_{atm}$ is the atmospheric Hg concentration. $R_a$ and $R_b$ are calculated according to (Marsik et al., 2007).

$\chi_{cnp}$ is the overall compensation point parameterized as a weighted average of exchange coefficients at the air-cuticle, air-stomata, and air-soil interfaces as illustrated in Figure 1 (Bash, 2010; Zhang et al., 2009a):

$$\chi_{cnp} = \frac{\chi_c \frac{X_c}{R_c} + \chi_s \frac{X_s}{R_s} + \chi_g \frac{X_g}{R_g + R_{ac}} + \frac{C_{atm}}{R_a + R_b}}{\frac{1}{R_c} + \frac{1}{R_s} + \frac{1}{R_g + R_{ac}} + \frac{1}{R_a + R_b}}$$  \hspace{1cm} (3)
where $\chi_c$ is the cuticular compensation point, $\chi_s$ is the stomatal compensation point, $\chi_g$ is the soil compensation point, $R_c$ is the cuticular resistance, $R_s$ is the stomatal resistance, $R_g$ is the soil diffusion resistance, $R_{ac}$ is the in-canopy aerodynamic resistance. The individual compensation points are described by Equations 6, 9 and 15.

2.3.1 Air-soil Exchange

In absence of vegetation (when LAI=0), the flux from bare lands ($F_{bts}$) can be estimated as:

$$F_{bts} = \frac{\Delta t}{R_a + R_b + R_g} (\chi_g - C_{atm})$$  \hspace{1cm} (4)

In the presence of vegetation (when LAI > 0), the flux from soil under canopy ($F_g$) is calculated as:

$$F_g = \frac{\Delta t}{R_g + R_{ac}} (\chi_g - \chi_{cnp})$$  \hspace{1cm} (5)

where $R_{ac}$ accounts for the resistance of gas diffusion from ground to the lower canopy and is assumed to be common for all gaseous species (Zhang et al., 2002b). The compensation point at air-soil interface ($\chi_g$) can be expressed as (Bash, 2010):

$$\chi_g = \frac{[Hg_0]_{st} H}{f_{ac} K_{ac}}$$  \hspace{1cm} (6)

where $[Hg_0]_{st}$ is the concentration of $Hg_0$ bound to soil, calculated as a reduction product of $Hg(II)$ using soil $Hg$ content and a pseudo-first-order rate constant related to solar irradiance (Gustin et al., 2002). $H$ is Henry's constant parameterized following Andersson et al. (2008). $f_{ac}$ is the fraction of organic carbon in surface soil (0-5 cm). $K_{ac}$ is the partition coefficient of $Hg_0$ between soil organic carbon and water.

$R_g$ is the $Hg^0$ diffusion resistance over a ground surface (soil, ice/snow) (Zhang et al., 2002b):

$$\frac{1}{R_g} = \alpha_{Hg^0} \frac{R_g(SO_2)}{R_g(O_3)} + \beta_{Hg^0} \frac{R_g(O_3)}{R_g(SO_2)}$$  \hspace{1cm} (7)

where $R_{g(SO_2)}$ and $R_{g(O_3)}$ are the diffusion resistances of $SO_2$ and $O_3$, $\alpha_{Hg^0}$ is the $Hg^0$ scaling factor based on $SO_2$, $\beta_{Hg^0}$ is $Hg^0$ scaling factor based on $O_3$. The formulation of $R_{g(SO_2)}$ and $R_{g(O_3)}$ has been described previously (Zhang et al., 2003).
2.3.2 Air-cuticle Exchange

Air-cuticle exchange flux is calculated as (Bash, 2010):

\[ F_c = \frac{\Delta t}{R_c} (\chi_c - \chi_{cnp}) \]  

\[ \chi_c = \frac{[Hg_0^0]}{LAP} \]  

where \(LAP\) denotes the leaf-air partitioning coefficient for \(\text{Hg}^0\) (Rutter et al., 2011), \([Hg_c^0]\) is the concentration of \(\text{Hg}^0\) bound to foliar cuticular surface, calculated as the photoreduction product of a fraction of newly deposited \(\text{Hg(II)}\) on foliar interfaces (Graydon et al., 2009):

\[ [Hg_c^0] = f_{rxn}[Hg_{c,DD}^{II+}] \]  

\[ [Hg_c^{II+}] = (1 - f_{rxn} - f_{fixed})[Hg_{c,DD}^{II+}] \]  

\[ [Hg_{c,DD}^{II+}] = \frac{[Hg_{w}^{II+}]}{T_l} \]  

where \([Hg_{c,DD}^{II+}]\) is the concentration loading of total dry deposited \(\text{Hg(II)}\) on cuticle, \([Hg_c^{II+}]\) is the concentration of the deposited \(\text{Hg(II)}\) residing on cuticular surfaces, \([Hg_{w}^{II+}]\) is the concentration of \(\text{Hg(II)}\) that can be washed off from leaves, \(f_{rxn}\) is the fraction of \(\text{Hg(II)}\) that can be photo-reduced, \(f_{fixed}\) is the fraction of \(\text{Hg(II)}\) fixed into tissue and not available for re-emission or wash-off, \(T_l\) is the leaf thickness. \(f_{rxn}, f_{fixed}\) are parameterized following Smith-Downey et al. (2010). \(R_c\) is the cuticular resistance calculated as (Zhang et al., 2002b):

\[ \frac{1}{R_c} = \frac{\alpha_{Hg^0}}{R_{c(SO_2)}} + \frac{\beta_{Hg^0}}{R_{c(O_3)}} \]  

2.2.3 Air-stomata Exchange

The air-stomata exchange flux is estimated as (Bash, 2010):

\[ F_s = \frac{\Delta t}{R_s} (\chi_s - \chi_{snp}) \]
It is assumed that the uptake of Hg species through stomata is predominantly Hg$^0$ due to its abundance in the atmosphere (Capiomont et al., 2000; Millhollen et al., 2006; Stamenkovic and Gustin, 2009). As such, the dissolved Hg$^0$ in the stomatal compartment, \([Hg_s^0]\), can be formulated as:

\[
[Hg_s^0] = (1 - f_{fixed})[Hg_{s,DD}^0]
\]  

(16)

where \([Hg_{s,DD}^0]\) is the concentration of newly deposited Hg$^0$ stored in the stomatal compartment. The overall stomatal resistance is calculated as (Zhang et al., 2002b):

\[
R_s = \frac{R_{st} + R_{me}}{1 - W_{st}}
\]  

(17)

where \(R_{st}\) is the resistance associated with stomata, \(R_{me}\) is resistance associated with mesophyll reservoir, \(W_{st}\) is the fraction of stomatal blocking under wet condition. The detailed formulation of \(R_{st}\) and \(R_{me}\) and \(W_{st}\) can be found elsewhere (Zhang et al., 2012; Zhang et al., 2003; Zhang et al., 2002b).

2.4 Modeling Experiments for Sensitivity Analysis

A series of 2-level factorial designs of experiments were performed to assess the sensitivity to changes of model variables as well as their synergistic and antagonistic interactions. A brief discussion of the use of factorial design of experiments is provided in the Supplementary Material document. The studied variables include both physical and environmental parameters. Their respective experimental levels are show in Tables 2-4. The principle of factor sparsity (Myers et al., 2009) states that the main effects and lower-order interactions dominate most system responses and the higher-order interactions are not significant. Therefore, the effect of interaction terms higher than second order was not considered.

For water surface, there are four factors driving the model simulation (Table 2). Therefore, a $2^4$ full factorial design was applied. For bare lands, the 11 model parameters (Table 3) form a $2^{11-6}$ fractional
design (Resolution IV) enabling main effects free from aliasing. The number of runs (32), although intensive, is still manageable. After this initial screening, a two-level full factorial design was applied for the significant factors based on a 95% confidence level (results of the $2^{11-6}$ design are shown in Supplementary Material). For the canopy ecosystem, 15 main factors (Table 4) were selected to form a $2^{15-9}$ fractional design (Resolution IV, 64 experiments). In this case, the alias system is more complex because of the large number of study factors. Therefore, a successive $2^{(11-6)}$ design (Supplementary Material) was applied to the pre-screened significant factors to obtain 5 most significant factors for a $2^5$ full factorial design (Supplementary Material). The sensitivity results were illustrated based on the final full factorial design for watersheds, bare lands, canopy ecosystems. The data analysis of the factorial experiments was conducted using Minitab®16.

2.5 Model Configuration and Data

The modeling domain is in Lambert Conformal projection covering mainly the Contiguous United States (CONUS), with 156×118 grid cells at 36-km spatial resolution. Hourly meteorological data were prepared using the Weather Research and Forecasting (WRF) model Version 3.4 with the Noah Land Surface Model. The model algorithms were coded in FORTRAN 90 and Network Common Data Form (NetCDF) version 4.1. The gridded model results were visualized by the Visualization Environmental for Rich Data Interpretation (VERDI) version 1.4.

A base-case simulation was performed in a summer and a winter month (August & December 2009) to evaluate the seasonal and diurnal variability of the air-surface exchange. The base case refers to the modeling utilizing the values listed in Table 1 with the meteorological parameters extracted from WRF output. In the simulation, the atmospheric Hg$^0$ concentration retrieved from the output of the Hg extension of Community Multi-scale Air Quality modeling system (CMAQ-Hg) version 4.6 for the same
modeling period was applied to represent the air concentration of Hg\textsuperscript{0}. The simulation does not directly incorporate the feedback of the air-surface exchange to the air concentration. However, for a regional model domain (CONUS), natural evasion and deposition of Hg\textsuperscript{0} does not significantly modify the ambient concentration (Lin et al., 2005; Gbor et al., 2006), since the time required for air turnover is relatively short (typically 3-4 days) and the air concentration of Hg is mainly controlled by the boundary conditions (Pongprueksa et al., 2008). In the model experiments, the concentration of Hg\textsuperscript{0} was tested as a sensitivity parameter.

3 Results and Discussion
3.1 Results of Base-case Simulations
The model estimates a net emission of 38.4 Mg in the summer month (16.6 Mg from water, 45.0 Mg from soil and -23.2 Mg from foliage) and 56.0 Mg in the winter month (33.9 Mg from water, 29.5 Mg from soil and -7.4 Mg from foliage) for the entire domain. The evasion from water body accounts for ~50% of the total natural emission (the cumulative net release of Hg\textsuperscript{0} caused by the air-surface exchange process) because of the large water areal coverage in the domain (59%). Vegetation represents a net sink, this is different from earlier estimates using the evapotranspiration approach (Bash et al., 2004; Shetty et al., 2008) but consistent with recent observational studies (Gustin et al., 2008; Stamenkovic and Gustin, 2009). For the terrestrial system, the total emission is 43.9 Mg in two months. Assuming the annual emission is 5-6 times of the two monthly sum and excluding the emission from Canada, Mexico and Caribbean lands, the model-estimated annual emission in the contiguous US is 118-141 Mg yr\textsuperscript{-1}, comparable to the recent estimates (95-150 Mg yr\textsuperscript{-1}) using flux scaling methods (Ericksen et al., 2006; Hartman et al., 2009; Zehner and Gustin, 2002).

3.1.1 Air-water Exchange
Over water surface, the mean simulated flux is 1.6 and 3.1 ng m$^{-2}$ hr$^{-1}$ in the summer and winter month (Figures 2a&3a) respectively. Water bodies in the domain are net sources, producing fluxes typically in the range of 1-4 ng m$^{-2}$ hr$^{-1}$, similar to earlier measurements (Mason et al., 2001a; Andersson et al., 2011). The spatial distribution is primarily driven by the surface wind speed. Temperature, air Hg$^0$ and DGM concentration play a much less significant role because a constant DGM was assumed (40 ng m$^{-3}$) and the Hg$^0$ level over water was in a narrow range (1.4 ~1.8 ng m$^{-3}$). The Pearson's correlation coefficient (r) between flux and wind speed is much stronger than the value between flux and temperature (0.56 vs. 0.18). The flux in the winter month is greater because of stronger winds in the northeastern corner of the domain. The emission flux does not show clear diurnal variation in both months because wind speed is the most dominant factor (Figure 4a).

3.1.2 Air-soil Exchange

Soil surfaces have been suggested to be a net source of Hg (Gustin et al., 2008; Hartman et al., 2009), which is also shown in the base-case model results (Figure 2&3). The mean flux from bare lands (0.7 and 0.6 ng m$^{-2}$ hr$^{-1}$ in the summer and winter month) is lower than the value from soil under the canopy (4.3 and 2.7 ng m$^{-2}$ hr$^{-1}$) because of the landuse classification. The bare lands in the domain include sparsely vegetated land, bare ground tundra and snow/ice land. The flux contribution from such landuse types is largely from the southern portion of the domain. The simulated flux from soil under canopy is comparable to those reported at background sites, -0.1~7 ng m$^{-2}$ hr$^{-1}$ (Ericksen et al., 2006; Kuiken et al., 2008b; Kuiken et al., 2008a; Carpi and Lindberg, 1998).

The simulated Hg$^0$ flux from soil under canopy is controlled by the degree of vegetation coverage (LAI), air temperature, friction velocity, air Hg concentration and solar irradiation. In the summer month, the flux in Eastern US is lower due to heavy vegetation coverage that increases the in-canopy aerodynamic
resistance \( (R_{res}) \) (Zhang et al., 2002a). Higher flux occurs in the Central and Western US because of the smaller LAI and higher air temperature (Figure 2c, Figure 8). In the winter month, the higher air temperature and longer sunlit hours cause the higher flux in the south (Figure 3c, Figure 8). Among the environmental parameters, LAI has the greatest influence on the estimated flux \( (r = 0.45) \). The spatially average soil flux for the entire domain shows a typical diurnal variation caused by air temperature and solar irradiance (Gabriel et al., 2006). The detailed impact of the model variables is discussed in the sensitivity analysis.

3.1.3 Air-foliage Exchange

Vegetation represents a net sink of Hg\(^{0}\) in the base-case simulations. The mean simulated air-foliar exchange is -2.2 and -0.7 ng m\(^{-2}\) hr\(^{-1}\) in the summer and winter month (Figures 2d, 3d). The magnitude is similar to those measured in August by Ericksen et al. (2003) (a mean flux of -3.3 ng m\(^{-2}\) hr\(^{-1}\)) and Millhollen et al. (2006) (-4.1~-0.3 ng m\(^{-2}\) hr\(^{-1}\)). In summer, the greatest vegetative uptake of Hg\(^{0}\) occurs in the Northeast US because of the dense vegetation coverage. In winter, the uptake becomes much weaker due to the reduced LAI, particularly in the north (Smith-Downey et al., 2010). The simulated deposition flux is highly correlated with LAI \( (r = 0.71 \text{ and } 0.88 \text{ in winter and summer}) \); while the correlations with friction velocity, GEM, air temperature and solar radiation are comparatively weaker. The diurnal variation for foliar flux is shown in Figure 4c. Higher deposition occurs during daytime due to the higher air temperature and solar irradiance (Rutter et al., 2011). The overall diurnal variation in the model domain exhibits the feature of air-foliage exchange (Figure 4d).

The simulated flux from soil under canopy and foliar surfaces is highly dependent on the resistance terms. Presently the values of cuticular \( (R_c) \), stomatal \( (R_g) \) and soil \( (R_s) \) resistances of Hg are not well understood (Holmes et al., 2011) and have been estimated by relating to the measured resistance of O\(_3\), SO\(_2\) and H\(_2\)O.
There has been experimental efforts to determine $R_c$ and $R_s$ based on Fick's Law by introducing isotopic Hg tracer to plants grown in an environmentally controlled chamber (Rutter et al., 2011). The resistances were found to depend on temperature, solar irradiance and Hg species with reported $R_c$ and $R_s$ ranging from 150 to 50000 m s$^{-1}$ at 0-35°C and 0-170 W m$^{-2}$ (Millhollen et al., 2006; Rutter et al., 2011). The simulated flux in the base case applied similar resistance values in the model. However, the lack of deterministic relationships between the resistance terms and environmental parameters still represents an uncertainty and there is a need to better quantify the resistance for Hg$^0$.

### 3.2 Sensitivities Analysis

#### 3.2.1 Sensitivity of Exchanges over Water Bodies

Figure 5 shows the change of air-water flux due to the change of model variables from the low to the high experimental level (Table 2). Individually, wind speed is the most significant parameter ($p = 0.003$) followed by DGM ($p = 0.004$) and surface temperature ($p = 0.059$). On average, increasing wind speed from 0.001 to 20 m s$^{-1}$ enhanced the flux by 7.6 ng m$^{-2}$ hr$^{-1}$ ($p = 0.003$); increasing the DGM from 15 to 240 ng m$^{-3}$ increases the flux by 7.0 ng m$^{-2}$ hr$^{-1}$ ($p = 0.004$). A higher air Hg$^0$ concentration slightly decreases the evasion flux. There is a significant synergistic effect caused by wind speed and DGM concentration ($p = 0.004$). Increasing both variables simultaneously from the low to high level (Table 2) causes an additional 48% increase of the evasion flux. The wind speed and surface temperature also have a synergistic effect, although not as significant ($p = 0.059$), followed by the effect enhanced by DGM concentration and surface temperature ($p = 0.076$). The effects of higher DGM concentration and air Hg$^0$ concentration offset each other, leading to a nearly zero effect on flux ($p = 1.000$).

In the base case, a uniform DGM concentration was assumed. The spatially constant DGM level
represents a significant uncertainty since other environmental parameters such as temperature, wind speed can be estimated reliably through meteorological simulations at a high spatial resolution. The mechanism leading to the net DGM formation in surface water is complex and not fully understood (Qureshi et al., 2010). It has been suggested that dissolved organic matter (Amyot et al., 1994; Amyot et al., 1997), hydroxyl radicals (Zhang and Lindberg, 2001) and oxyhalide radicals (e.g. OCl, OBr) (Lalonde et al., 2001) can participate in the sunlight-induced processes that produce DGM, in addition, DGM is also consumed by some oxidation reactions in water bodies. Data on measured net DGM concentration over vast water bodies are not readily available because of a limited number of cruise campaigns (Mason et al., 1998; Mason et al., 2001b; Andersson et al., 2011). Strode et al. (2007) and Soerensen et al. (2010) estimated the global distribution of DGM in sea water and showed that accurate representation of GDM concentration is key for calculating air-water exchange. More knowledge on the temporal and spatial distribution of net DGM concentration in surface water can greatly reduce the model uncertainty. Experimental investigation to better understand the chemical pathways leading to net DGM formation will also help constrain the model estimate.

3.2.2 Sensitivity of Exchange over Bare Lands

Figure 6 illustrates the model response to the model variables at the two experimental levels in Table 3. Soil Hg content, friction velocity, air temperature and the scaling factor $\beta_{Hg}$ (Eq. 7) have a positive effect on the simulated Hg flux while the soil organic content has a negative effect. On average, increasing soil Hg content from 50 to 1000 ng g$^{-1}$ soil enhances the flux by 55.3 ng m$^{-2}$ hr$^{-1}$ ($p = 0.013$); increasing friction velocity from 0.0001 to 1 m s$^{-1}$ increases the flux by 54.8 ng m$^{-2}$ hr$^{-1}$ ($p = 0.014$). On the other hand, increasing the soil organic content from 0.6 to 10 % reduce the flux by 54.2 ng m$^{-2}$ hr$^{-1}$ ($p = 0.015$). There are several notable interactions among the model variables. First, the positive effects of soil Hg content and friction velocity can be completely offset by soil organic content (Figure 6). An
increase in soil organic content substantially decreases the soil Hg compensation point (Eq. 6), suggesting the significant role of soil organic matter in retaining Hg from evading ($p = 0.025$). There is a strong synergistic effect between friction velocity and soil Hg content ($p = 0.022$), leading to an additional 46% increase compared to the sum of the two individual effects (Figure 6). Quasi-laminar sub-layer resistance ($R_s$) and aerodynamic resistance ($R_a$) both decrease with increasing friction velocity. Coupled with the increased soil Hg compensation point at higher soil Hg content (Eq. 6), the flux is greatly enhanced (Figure 6). Overall, that friction velocity, soil Hg and organic content are the most influential parameters for Hg exchanges over bare lands. Other pre-screened parameters including temperature, Hg scaling factor ($\beta_{Hg}$ in Eq. 7) and other interaction terms have less significant impact.

3.2.3. Sensitivity of Exchange over Canopy

Figure 7 illustrates the sensitivity of simulated Hg flux over canopy to the model variables at the two experimental levels in Table 4. For comparison, the sensitivity results for air-soil exchange under canopy are also shown. It is clear that the forcing of air-canopy exchange is dominated by the air-soil exchange under canopy at the two experimental levels. This resembles the Hg$_0$ emission characteristics observed in a gas exchange system, which suggested that the evasion from soils is much greater than the emission from the plants grown in the chamber (Frescholtz and Gustin, 2004; Frescholtz et al., 2003). After the factor pre-screening step (Figures s2-s7 in Supplementary Material), the simulated flux is particularly sensitive to the change of five parameters. Friction velocity (positive effect, $p = 0.020$), soil Hg content (positive effect, $p = 0.028$) and soil organic content (negative effect, $p = 0.030$) are the most significant model parameters (Figure 7). These effects are similar to the sensitivity results of air-soil exchange over bare lands (Figures 6 & 7), but slightly weaker based on the $p$ values because of the "shielding" of vegetation coverage that modifies the values of the resistance terms ($R_s$ and $R_a$) (Zhang et al., 2002a). Highly moist soil (soil moisture content > 20%, Table 4) has a negative effect because it effectively
increases soil diffusion resistance ($R_g$) (Zhang et al., 2003), although the effect is less significant ($p = 0.289$). Air temperature also has a positive effect as anticipated ($p = 0.180$).

The synergistic effect caused by friction velocity and soil Hg content is significant for the air-canopy exchange ($p = 0.028$, Figure 7), enhancing the evasion flux by 47% (77.8 ng m$^{-2}$ hr$^{-1}$). Both soil organic content and highly moist soil condition can offset the positive effects caused by higher friction velocity, soil Hg content and air temperature at different degrees (Figure 7), with the soil organic content being more influential. Higher soil organic content at high soil moisture (>20%) yields a weak positive effect ($p = 0.340$), this is interpreted as the combined negative effect of the two parameters is smaller than the sum of the two individual effects. Overall, these characteristics resemble the air-soil exchange because the air-canopy exchange is dominated by the air-soil exchange under canopy.

Atmospheric mercury can deposit on the surface of cuticle or be accumulated in leaves through stomatal uptake (Figure 1). For cuticular exchange, air temperature has a significant positive effect (Figure 8). Since air-cuticle exchange is mainly deposition (negative flux), this means that a higher air temperature leads to smaller deposition or greater evasion ($p < 0.001$). Friction velocity has a strong negative effect (i.e., higher deposition at higher friction velocity, $p < 0.001$) on the simulated flux. Higher soil organic content ($p = 0.009$) and highly moist (>20%) soil ($p = 0.194$) increase the simulated flux (i.e., weaken the deposition) by decreasing the canopy compensation point ($\chi_c$ in Eq. 8). Under the circumstance, Hg deposits preferentially to soil and therefore a reduced deposition on cuticle. Higher soil Hg content decreases the flux ($p = 0.008$) by increasing the overall compensation point ($\chi_{cmp}$ in Eq. 8), suggesting greater deposition on cuticle at higher soil Hg content. For stomatal exchange, the trend of single factor effect is the same as that of cuticular exchange.
Several notable interaction effects are observed for foliar exchanges. For cuticle exchange, the deposition is reversed from deposition to evasion at the high air temperature level, leading to the overall positive interaction effect for air temperature and friction velocity (Figure 8, $p < 0.001$). The positive effect of soil organic content significantly offsets the negative effect of friction velocity ($p = 0.010$) and soil Hg content ($p = 0.016$). For stomatal exchange, the only significant interaction effect is between soil organic and Hg content, which is more dominated by soil organic content. Overall, the foliar exchange is primarily controlled by air temperature and friction velocity because the resistance terms can be affected by the two variables. This is in contrast to the evapotranspiration approach where soil Hg content plays a predominant role in simulated Hg$^0$ evasion flux (Bash et al., 2004; Gbor et al., 2006).

In this analysis, the effect of solar irradiance is not as significant as the selected parameters under the resistance model scheme and has been ruled out during the pre-screening for the model variables (Section 2.4 and Figures s2–s6). In the model, solar irradiation can influence the flux in three ways: (1) through modifying the rate constant of Hg(II) reduction in soils and foliage (Eqs. 6 & 10 & 16), (2) through forcing the change of aerodynamic resistance ($R_a$ and $R_{ac}$), and (3) through forcing the change of cuticular and stomatal resistance terms ($R_c$ and $R_{st}$). For air-soil exchange, the effect of solar irradiance on the reduction rate constant is the most sensitive process (Eqs. 6 & 10). The photoreduction of Hg(II) in soils has been suggested to be responsible for the increased soil flux observed under sunlit condition (Gustin et al., 2002). There have been kinetic studies showing that increasing UV-A intensity by 75% approximately doubles the photoreduction rate in the aqueous phase (Qureshi et al., 2010). However, the effect of lights on the kinetics of Hg(II) reduction in soils is poorly understood. In this modeling, the photoreduction rate constant was set to a mean value (Eq. 6). This limits a full examination of the true impact of solar irradiation on the simulated Hg flux. Results from experimental studies on Hg(II) photoreduction rates will help reduce this model uncertainty. For foliar exchange, solar irradiation has a weak positive effect.
on the flux (i.e., slightly weakens deposition, Figure s4), but has a significant positive effect on the stomatal exchange (p= 0.004, Figure s5).

4 Conclusions

An updated model for estimating the bidirectional air-surface exchange of Hg is presented based on the current understanding of surface resistance schemes. From the base-case results, water and soil surfaces are net sources and vegetation is a net sink of Hg\(^0\). Each natural surface exhibits a different diurnal and seasonal variation. Sensitivity analysis of model variables using a 2-level factorial design of experiments shows that atmospheric shear flows (surface wind over water and friction velocity of terrestrial surfaces), dissolved gaseous mercury (DGM) concentration, soil organic and Hg content, and air temperature are the most influential factors controlling the magnitude of the atmosphere-biosphere exchange of Hg\(^0\). However, the positive effect of friction velocity and soil Hg content on the evasion flux from soil and canopy can be greatly offset by the negative effect of soil organic content. Significant synergistic effects are identified between surface wind and DGM level for water surface, and between soil Hg content and friction velocity for soil surface, leading to ~50% enhanced flux in the combined effect compared to the sum of their individual effects. The air-foliar exchange is mainly controlled by surface resistance terms controlled by environmental parameters such as solar irradiation and air temperature.

The uncertainty in this modeling assessment is primarily from the lack of knowledge in (1) the spatial distribution of organic and Hg content in soil and DGM concentration in water, (2) the reduction mechanism and kinetics of Hg(II) in soil and water, and (3) the values of resistance terms over different natural surfaces. More research in providing geospatial distribution of Hg in water and soil will greatly improve the model estimate. Further elucidation on the interaction of Hg and organic carbon in top soil and surface water as well as quantification of the surface resistance terms specific to Hg species will also
help improve the model scheme. Recent field and experimental investigations have suggested that organic carbon in soil potentially shapes the distribution of Hg in forest at continental scales (Obrist et al., 2011) and that the long-term Hg evasion from soil is highly related to the Hg and organic carbon interactions (Smith-Downey et al., 2010). Given the predominance of soil organic content in reducing soil Hg evasion flux using the mechanistic approach in this study, soil organic content is likely the controlling factor determining the intensity of air-soil Hg\(^0\) exchange.

Acknowledgements

This work was funded by National "973" Program of China (2013CB430003), National Institute of Food and Agriculture, U.S. Department of Agriculture (2009-38899-20017), and State Key Laboratory of Environmental Geochemistry, IGCAS. The funding support is gratefully acknowledged. We thank Pruek Pongprueksa for providing Hg concentration/deposition data for this work and Pattaraporn Singhasuk for creating the visualization in Figure 1.

References


Yin, R. S., Feng, X. B., and Meng, B.: Stable Mercury Isotope Variation in Rice Plants (Oryza sativa L.) from the Wanshan Mercury Mining District, SW China, Environmental Science & Technology, 47, 2238-2245, Doi 10.1021/es304302a, 2013.


<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
<th>Value or units</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F_w$</td>
<td>Flux from water bodies</td>
<td>ng m$^{-2}$ hr$^{-1}$</td>
</tr>
<tr>
<td>$K_w$</td>
<td>Mass transfer coefficient of mercury through water layer</td>
<td>m hr$^{-1}$</td>
</tr>
<tr>
<td>$C_w$</td>
<td>DGM concentration</td>
<td>40 ng m$^{-3}$ water $^a$</td>
</tr>
<tr>
<td>$H_w$</td>
<td>Henry's law constant under water conditions</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$F_{cnp}$</td>
<td>The flux over canopy biomes</td>
<td>ng m$^{-2}$ hr$^{-1}$</td>
</tr>
<tr>
<td>$\Delta t$</td>
<td>Time duration</td>
<td>s</td>
</tr>
<tr>
<td>$R_a$</td>
<td>Aerodynamic resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_b$</td>
<td>Quasi-laminar sub-layer resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$C_{atm}$</td>
<td>Atmospheric Hg concentration</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\chi_{cnp}$</td>
<td>The total compensation point</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\chi_c$</td>
<td>Cuticular interfaces compensation point</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\chi_s$</td>
<td>Stomatal interfaces compensation point</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$\chi_g$</td>
<td>Soil interfaces compensation point</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$R_c$</td>
<td>cuticular resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_s$</td>
<td>stomatal resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_g$</td>
<td>soil diffusion resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_{ac}$</td>
<td>in-canopy aerodynamic resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$F_{bns}$</td>
<td>the flux from bare land soil</td>
<td>ng m$^{-3}$</td>
</tr>
<tr>
<td>$[Hg^0]_{st}$</td>
<td>elemental mercury content bound to organic matter</td>
<td>ng g$^{-1}$ soil</td>
</tr>
<tr>
<td>$H$</td>
<td>Henry's Law constant in soil condition</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$f_{oc}$</td>
<td>fraction of organic carbon in topsoil (0-5cm)</td>
<td>2% (dimensionless) $^b$</td>
</tr>
<tr>
<td>$K_{oc}$</td>
<td>soil organic carbon to water partitioning coefficient</td>
<td>m$^3$ water g$^{-1}$ organic carbon</td>
</tr>
<tr>
<td>$[Hg(II)]_{st}$</td>
<td>Hg(II) content in the soil</td>
<td>90 ng g$^{-1}$ soil $^c$</td>
</tr>
<tr>
<td>$R_{g(SO_2)}$</td>
<td>SO$_2$ soil diffusion resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_{g(O_3)}$</td>
<td>O$_3$ soil diffusion resistance</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$\alpha_{Hg^0}$</td>
<td>Hg$^0$ scaling factor basing on SO$_2$</td>
<td>0 (dimensionless) $^d$</td>
</tr>
<tr>
<td>$\beta_{Hg^0}$</td>
<td>Hg$^0$ scaling factor basing on O$_3$</td>
<td>0.1 (dimensionless) $^e$</td>
</tr>
<tr>
<td>LAP</td>
<td>leaf-air partitioning coefficient for Hg$^0$ between leaves and air</td>
<td>30000 (dimensionless) $^f$</td>
</tr>
<tr>
<td>$[Hg^0_{c}]$</td>
<td>Hg$^0$ content bound to foliar cuticular surface</td>
<td>ng m$^{-3}$ leaf</td>
</tr>
<tr>
<td>Symbol</td>
<td>Description</td>
<td>Unit</td>
</tr>
<tr>
<td>--------------</td>
<td>------------------------------------------------------------------------------</td>
<td>-----------------------</td>
</tr>
<tr>
<td>$[Hg_c^{ll+}]$</td>
<td>newly dry deposited Hg(II) residing on cuticular surfaces</td>
<td>ng m$^{-2}$ leaf</td>
</tr>
<tr>
<td>$[Hg_c^{ll+}]$</td>
<td>the total dry deposited Hg(II) loading on cuticular compartment</td>
<td>ng m$^{-2}$ leaf</td>
</tr>
<tr>
<td>$[Hg_w^{ll+}]$</td>
<td>Hg(II) leaf wash concentration</td>
<td>0.04 ng m$^{-2}$ leaf</td>
</tr>
<tr>
<td>$f_{rxn}$</td>
<td>fraction of Hg(II) potentially photo-reduced to Hg$^0$</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$f_{fixed}$</td>
<td>fraction of Hg(II) being fixed into tissue</td>
<td>dimensionless</td>
</tr>
<tr>
<td>$T_l$</td>
<td>leaf thickness</td>
<td>0.000152 m$^h$</td>
</tr>
<tr>
<td>$[Hg_s^{0}]$</td>
<td>Dissolved elemental mercury in stomatal compartment</td>
<td>ng m$^{-3}$ leaf</td>
</tr>
<tr>
<td>$[Hg_{s,DD}^{0}]$</td>
<td>deposited Hg$^0$ concentration stored inside stomatal compartment</td>
<td>0.39 ng m$^{-2}$ leaf hr$^{-1}$</td>
</tr>
<tr>
<td>$R_{st}$</td>
<td>resistance associating stomata apertures</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$R_{me}$</td>
<td>resistance associating mesophyll reservoir</td>
<td>s m$^{-1}$</td>
</tr>
<tr>
<td>$W_{st}$</td>
<td>fraction of stomatal blocking under wet condition</td>
<td>dimensionless</td>
</tr>
</tbody>
</table>

---

a Value for base-case simulation, Xu et al. (1999);

b For 0-20 cm topsoil, the bulk density is 1.1-1.3 g cm$^{-3}$ and organic carbon content is 3.3 kg m$^{-2}$ in the US (Calhoun et al., 2001; Guo et al., 2006), so assuming in the 0-5 cm topsoil foc is 2%;

c Value for base-case simulation, Bash (2010);

d Basing on the negligible solubility ($Henry's constant=0.139$ M atm$^{-1}$) and chemical inertness (Zhang et al., 2009b; Zhang et al., 2012);

e Zhang et al. (2012);

f Rutter et al. (2011a);

g Value for base-case simulation, Frescholtz et al. (2003);

h Value for base-case simulation, Abrams and Kubiske (1990);

i Value for base-case simulation, Poissant et al. (2008).
Table 2. Examined model variables and the experimental levels of factorial design for air-water exchange

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
<th>Low level</th>
<th>High level</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>Sea surface temperature (°C)</td>
<td>-2&lt;sup&gt;a&lt;/sup&gt;</td>
<td>35&lt;sup&gt;a&lt;/sup&gt;</td>
</tr>
<tr>
<td>GEM</td>
<td>Air Hg&lt;sup&gt;0&lt;/sup&gt; concentration (ng m&lt;sup&gt;3&lt;/sup&gt;)</td>
<td>1.0&lt;sup&gt;b&lt;/sup&gt;</td>
<td>2.0&lt;sup&gt;b&lt;/sup&gt;</td>
</tr>
<tr>
<td>DGM</td>
<td>Dissolved Hg&lt;sup&gt;0&lt;/sup&gt; concentration in surface water (ng m&lt;sup&gt;3&lt;/sup&gt;)</td>
<td>15&lt;sup&gt;c&lt;/sup&gt;</td>
<td>240&lt;sup&gt;c&lt;/sup&gt;</td>
</tr>
<tr>
<td>W</td>
<td>Wind speed at 10 m above water surface (m s&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>0.001&lt;sup&gt;d&lt;/sup&gt;</td>
<td>20&lt;sup&gt;d&lt;/sup&gt;</td>
</tr>
</tbody>
</table>

<sup>a</sup> Kwun and You (2009);

<sup>b</sup> According to global background of air Hg<sup>0</sup> at 1.1~1.7 ng m<sup>3</sup> (Lindberg et al., 2007);

<sup>c</sup> Morel et al. (1998);

<sup>d</sup> Andersson et al. (2011).
Table 3. Examined model variables and the experimental levels of factorial design for air-soil exchange over sparsely vegetated land, bare ground tundra and snow/ice land

<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
<th>Low level</th>
<th>High level</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>Air temperature at 2 meters (°C)</td>
<td>-2</td>
<td>40</td>
</tr>
<tr>
<td>Q2</td>
<td>Water vapor mixing ratio (Kg Kg⁻¹)</td>
<td>0.0005ᵃ</td>
<td>0.05ᵃ</td>
</tr>
<tr>
<td>f_{oc}</td>
<td>Fraction of organic carbon in surface soil</td>
<td>0.006ᵇ</td>
<td>0.1ᶜ</td>
</tr>
<tr>
<td>UST</td>
<td>Friction velocity(m s⁻¹)</td>
<td>0.0001ᵈ</td>
<td>1.0ᵈ</td>
</tr>
<tr>
<td>SM</td>
<td>Soil Hg content (ng g⁻¹ soil)</td>
<td>50 ᵇ</td>
<td>1000 ᵇ</td>
</tr>
<tr>
<td>GEM</td>
<td>Air Hg⁰ concentration (ng m⁻³)</td>
<td>1.0</td>
<td>2.0</td>
</tr>
<tr>
<td>SNOWH</td>
<td>Snow depth (m)</td>
<td>0 ᵇ</td>
<td>0.4999 ᵇ</td>
</tr>
<tr>
<td>β_{Hg⁰}</td>
<td>Scaling factor of reactivity Hg</td>
<td>0.1ᵍ</td>
<td>0.2ʰ</td>
</tr>
<tr>
<td>DC</td>
<td>Dew condition</td>
<td>No ᵯ</td>
<td>Yes ᵯ</td>
</tr>
<tr>
<td>RC</td>
<td>Rain condition</td>
<td>No ᵯ</td>
<td>Yes ᵯ</td>
</tr>
<tr>
<td>MC</td>
<td>Moist soil condition</td>
<td>No ᵯ</td>
<td>Yes ᵯ</td>
</tr>
</tbody>
</table>

ᵃ Kwun and You (2009);  
ᵇ Suggested default value for modeling of volatilized contaminant to air by USEPA (2004);  
ᶜ Upper limit of the forest soils (Jones et al., 2004);  
ᵈ Akkarappuram and Raman (1988)  
ᵉ Carpi and Lindberg (1998);  
ᶠ Has effect on ground and cuticular resistance, Zhang et al. (2003);  
ᵍ Zhang et al. (2012);  
ʰ Zhang et al. (2009a);  
ⁱ Air temperature below dew point represents low level and vice versa, has effect on ground and cuticular resistance (Zhang et al., 2003);  
ʲ Has effect on ground and cuticular resistance terms (Zhang et al., 2003);  
ᵏ Soil moisture > 20% represents low level and vice versa, the high level suggests highly moist soil (Zotarelli et al., 2010).
<table>
<thead>
<tr>
<th>Term</th>
<th>Description</th>
<th>Low level</th>
<th>High level</th>
</tr>
</thead>
<tbody>
<tr>
<td>T</td>
<td>Air temperature at 2 meters (°C)</td>
<td>-2</td>
<td>40</td>
</tr>
<tr>
<td>f_{oc}</td>
<td>Fraction of organic carbon in surface soil</td>
<td>0.006</td>
<td>0.1</td>
</tr>
<tr>
<td>UST</td>
<td>Friction velocity(m s(^{-1}))</td>
<td>0.0001</td>
<td>1.0</td>
</tr>
<tr>
<td>SM</td>
<td>Soil total Hg content (ng m(^{-3}))</td>
<td>50</td>
<td>1000</td>
</tr>
<tr>
<td>β_{Hg0}</td>
<td>Scaling factor of reactivity Hg</td>
<td>0.1</td>
<td>0.2</td>
</tr>
<tr>
<td>SNOWH</td>
<td>Snow depth (m)</td>
<td>0</td>
<td>0.4999</td>
</tr>
<tr>
<td>LAI</td>
<td>Leaf area index (m(^2) m(^{-2}))</td>
<td>1.0 (^{a})</td>
<td>5.0 (^{a})</td>
</tr>
<tr>
<td>SR</td>
<td>Solar irradiation (W m(^{-2}))</td>
<td>0</td>
<td>1000</td>
</tr>
<tr>
<td>Leaf_Hg</td>
<td>Hg concentration in leaf rinse (ng m(^{-2}) leaf)</td>
<td>0.02 (^{b})</td>
<td>2.10 (^{c})</td>
</tr>
<tr>
<td>Stomata_Hg</td>
<td>Hg previously deposited to leaf stomata (ng m(^{-2}) leaf)</td>
<td>0.13 (^{d})</td>
<td>0.59 (^{d})</td>
</tr>
<tr>
<td>GEM</td>
<td>Air Hg(^{\circ}) concentration (ng m(^{-3}))</td>
<td>1.0</td>
<td>2.0</td>
</tr>
<tr>
<td>LAP</td>
<td>Leaf-air partitioning coefficient (m(^3) air m(^{-3}) leaf)</td>
<td>30000 (^{e})</td>
<td>6000000 (^{e})</td>
</tr>
<tr>
<td>DC</td>
<td>Dew condition</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>RC</td>
<td>Rain condition</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>MC</td>
<td>Moist soil condition</td>
<td>No</td>
<td>Yes</td>
</tr>
</tbody>
</table>

\(^{a}\) Gower et al. (1999)
\(^{b}\) Frescholtz et al. (2003)
\(^{c}\) Fay and Gustin (2007)
\(^{d}\) Poissant et al. (2008)
\(^{e}\) Rutter et al. (2011)
Figure 1. Resistance scheme implemented in the air-surface exchange model following Sutton et al. (2007) and Zhang et al. (2009a)
Figure 2. Monthly mean of the simulated Hg\textsuperscript{0} flux (ng m\textsuperscript{-2} hr\textsuperscript{-1}) in the summer month: (a) flux from water body, (b) flux from bare lands, (c) flux from soil under the canopy, and (d) flux from foliage.
Figure 3. Monthly mean of the simulated Hg$^0$ flux (ng m$^{-2}$ hr$^{-1}$) in the winter month: (a) flux from water body, (b) flux from bare lands, (c) flux from soil under the canopy, and (d) flux from foliage.
Figure 4. Diurnal variation of mean simulated Hg\textsuperscript{0} for the entire model domain (UTC-7): (a) flux from water body, (b) total flux from soils (soil under the canopy and bare lands), (c) flux from foliage, and (d) flux for the total domain.
Figure 5. Sensitivity analysis based on the 2^4 factorial design shown in Table 2 (water body). T denotes air temperature at water surface; GEM denotes air Hg concentration; DGM denotes dissolved gaseous Hg concentration in surface water; W denotes wind speed. "*" denotes the interaction effects.
Figure 6. Sensitivity analysis based on the $2^5$ factorial design for bare lands after pre-screening model variables shown in Table 3 to isolate the significant factors. T denotes surface air temperature; foc denotes fraction of organic carbon in soil; UST denotes friction velocity; SM denotes soil mercury content; b denotes scaling factor for Hg reactivity ($\beta_{Hg}$). "*" denotes interaction effects.
Figure 7. Sensitivity analysis based on the $2^5$ factorial design at canopy level after pre-screening model variables shown in Table 4 to isolate the significant factors. The overall flux at canopy level is dominated by the soil flux under the canopy (the sensitivity of foliar exchange is shown in Figure 8). T denotes surface air temperature; foc denotes fraction of organic carbon in soil; UST denotes friction velocity; SM denotes soil Hg content; MC denotes soil moisture. "*" denotes interaction effects.
Figure 8. Sensitivity analysis based on the $2^5$ factorial design for foliar exchange after pre-screening model variables shown in Table 4 to isolate the significant factors. T denotes surface air temperature; foc denotes fraction of organic carbon in soil; UST denotes friction velocity; SM denotes soil Hg content; MC denotes soil moisture. "*" denotes interaction effects.
Supplementary Material: Sensitivity analysis of an updated bidirectional air-surface exchange model for mercury vapor

Xun Wang\textsuperscript{1,2}, Che-Jen Lin\textsuperscript{1,3,4}, Xinbin Feng\textsuperscript{1}

\textsuperscript{1} State Key Laboratory of Environmental Geochemistry, Institute of Geochemistry, Chinese Academy of Sciences, Guiyang, China
\textsuperscript{2} University of Chinese Academy of Sciences, Beijing, China
\textsuperscript{3} Department of Civil Engineering, Lamar University, Beaumont, TX, USA
\textsuperscript{4} College of Environment and Energy, South China University of Technology, Guangzhou, China

Correspondence to: C.-J. Lin (jerry.lin@lamar.edu); X. Feng (fengxinbin@vip.skleg.cn)

1. Use of 2\textsuperscript{k-p} factorial design for

Design of experiments is a series of tests in which purposeful changes are made to the input variables of a process systematically and the effects on response variables are measured. It is widely applied in the experiments involving many influencing factors, when it is necessary to study the combined effect of these factors. For a two-level design involving a high-level and a low-level value for each factor, the number of all possible combinations is 2\textsuperscript{k} (for example, for two factors the combinations is low-low, low-high, high-low and high-high), which also represent the number of experiments. This exponential relationship rapidly increases the number of experiments when the number of studied factors is increased. To reduce the experimental effort without losing the analytical power of the experiments, the number of experiment can be decreased strategically by choosing the experiments that investigate the main effects (i.e., the effect of single factor) and interaction effects of lower order. This is called fractional design and the number of experiment can be reduced by 2\textsuperscript{p} times (i.e., the number of experiment becomes 2\textsuperscript{k-p}). The term “Resolution” is used by statisticians to indicate how the experiments are chosen. For IV resolution design, all the main effects are completely isolated from confounding with...
all other experimental runs and the second-order (two-factor) interactions are maintained without confounding with higher order interactions. Based on the factorial experiment results, statistical test can be performed to understand the significance of each factor using P value.

An excellent online presentation on factorial design of experiments is also available at http://www.jhuapl.edu/techdigest/td/td2703/telford.pdf.

2. Initial parameter screening for bare lands

Normal plot of the standardized effects of $2^{11-6}$ (Figure s1) suggests significant effect from fraction of organic carbon, friction velocity, soil Hg content at 95% confidence level. The P-value of main effects from air temperature at 2 meters and scaling factor for reactivity of mercury on ozone ($\beta_{Hg^0}$) were close to 0.05 (0.069 and 0.073, respectively). For the second order interactions, air temperature and $\beta_{Hg^0}$ are important. Therefore fraction of organic carbon, friction velocity, soil Hg concentration, air temperature, $\beta_{Hg^0}$, were chosen for the final $2^5$ full factorial design.

3. Initial parameter screening for canopy system

The alias structure of the $2^{15-9}$ fractional design is complex (Figure s2). To ensure that the most significant factors are selected for the final full factorial design, all parameters confounded in alias system were chosen to run $2^{11-6}$ experiment except for air Hg$^0$ concentration because its weak significance ($P = 0.437$). From the results of the $2^{11-6}$ fractional design (Figure s3) result, the fraction of organic carbon, friction velocity, soil Hg concentration, $\beta_{Hg^0}$, soil moisture condition are significant. The P-value of main effects from Hg previously deposited to leaf stomata and air temperature were close to 0.05 (0.069 and 0.136, respectively). Therefore, fraction of organic carbon, friction velocity, soil Hg concentration, $\beta_{Hg^0}$, soil under moisture condition, Hg previously deposited to leaf stomata and air temperature were chosen to for another $2^{7-1}$ fractional
experiments. Based on the results (Figure s7), the main effects from fraction of organic carbon, friction velocity, soil Hg concentration are significant. To get the full design, Hg previously deposited to leaf stomata and $\beta_{Hg^0}$ were eliminated because of the relatively weaker significance.
Figure s1: Results of $2^{11-6}$ fractional design for bare lands. Significance at P<0.05. T denotes air temperature at 2 meters, Q2 denotes water vapor mixing ratio, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, GEM denotes air Hg(0) concentration, SNOWH denotes snow depth, b denotes scaling factor of reactivity Hg, DC denotes dew condition, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: T*DC + Q2*SNOWH + foc*UST + SM*b, T*RC + Q2*MC + foc*b + UST*SM, foc*SM + UST*b + SNOWH*MC + DC*RC.
Figure S2: Results of $2^{15-9}$ fractional design for canopy system. Significance at $P<0.05$. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, b denotes scaling factor of reactivity Hg, SNOWH denotes snow depth, LAI denotes Leaf area index, SR denotes solar irradiation, Leaf_Hg denotes Hg concentration in leaf rinse, Stomata_Hg denotes Hg previously deposited to leaf stomata, GEM denotes air Hg(0) concentration, LAP denotes leaf-air partitioning coefficient, DC denotes dew condition, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: $T*\text{LAI} + \text{foc}*\text{UST}, T*\text{SR} + \text{foc}*\text{SM}, \text{UST}^*\text{SM} + \text{LAI}^*\text{SR} + \text{GEM}^*\text{LAP}, b*\text{Stomata}_\text{Hg} + \text{RC}^*\text{MC}$. 
Figure s3: Results of $2^{11-6}$ fractional design for canopy system. Significance at $P<0.05$. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, LAI denotes leaf area index, SR denotes solar irradiation, b denotes scaling factor of reactivity Hg, Stomata_Hg denotes Hg previously deposited to leaf stomata, SNOWH denotes snow depth, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: T*SR + foc*UST + SM*b + Stomata_Hg*MC, T*SNOWH + foc*b + UST*SM + LAI*Stomata_Hg, foc*LAI + SM*MC + b*Stomata_Hg, foc*Stomata_Hg + UST*MC + LAI*b + SR*RC.
Figure s4: Results of $2^{11-6}$ fractional design for foliage. Significance at $P<0.05$. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, LAI denotes leaf area index, SR denotes solar irradiation, b denotes scaling factor of reactivity Hg, Stomata_Hg denotes Hg previously deposited to leaf stomata, SNOWH denotes snow depth, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: $T*SR + foc*UST + SM*b + Stomata_Hg*MC$, $T*SNOWH + foc*b + UST*SM + LAI*Stomata_Hg$, $foc*LAI + SM*MC + b*Stomata_Hg$, $foc*Stomata_Hg + UST*MC + LAI*b + SR*RC$. 
Figure s5: Results of $2^{11-6}$ fractional design for cuticle. Significance at $P<0.05$. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, LAI denotes leaf area index, SR denotes solar irradiation, b denotes scaling factor of reactivity Hg, Stomata_Hg denotes Hg previously deposited to leaf stomata, SNOWH denotes snow depth, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: T*SR + foc*UST + SM*b + Stomata_Hg*MC, T*SNOWH + foc*b + UST*SM + LAI*Stomata_Hg, foc*LAI + SM*MC + b*Stomata_Hg, foc*Stomata_Hg + UST*MC + LAI*b + SR*RC.
Figure s6: Results of $2^{11-6}$ fractional design for stamata. Significance at P<0.05. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, LAI denotes leaf area index, SR denotes solar irradiation, b denotes scaling factor of reactivity Hg, Stomata_Hg denotes Hg previously deposited to leaf stomata, SNOWH denotes snow depth, RC denotes rain condition, MC denotes moist soil condition. Alias information for significant terms: T*SR + foc*UST + SM*b + Stomata_Hg*MC, T*SNOWH + foc*b + UST*SM + LAI*Stomata_Hg, foc*LAI + SM*MC + b*Stomata_Hg, foc*Stomata_Hg + UST*MC + LAI*b + SR*RC.
Figure s7: Results of $2^{7-1}$ fractional design for canopy system. Significance at P<0.05. T denotes air temperature at 2 meters, foc denotes fraction of organic carbon in surface soil, UST denotes friction velocity, SM denotes soil total Hg concentration, MC denotes moist soil condition. Alias information for significant terms: T*SR + foc*UST + SM*b + Stomata_Hg*MC, T*SNOWH + foc*b + UST*SM + LAI*Stomata_Hg, foc*LAI + SM*MC + b*Stomata_Hg, foc*Stomata_Hg + UST*MC + LAI*b + SR*RC.
Figure s8: (a) the average spatial distribution of LAI ($m^2 m^{-2}$) in the summer month; (b) the average spatial distribution of LAI ($m^2 m^{-2}$) in the winter month; (c) the average spatial distribution of air temperature at 2 meters (K) in the summer month; (d) the average spatial distribution of air temperature at 2 meters (K) in the winter month