Exploring the atmospheric chemistry of $\text{O}_2\text{SO}_3^-$ and assessing the maximum turnover number of ion catalysed $\text{H}_2\text{SO}_4$ formation

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Abstract

It has recently been demonstrated that the $\text{O}_2\text{SO}_3^-$ ion forms in the atmosphere as a natural consequence of ionizing radiation. Here, we present a density functional theory-based study of the reactions of $\text{O}_2\text{SO}_3^-$ with $\text{O}_3$. The most important reactions are (a) oxidation of $\text{O}_2\text{SO}_3^-$ to $\text{O}_3\text{SO}_3^-$ and (b) cluster decomposition into $\text{SO}_3$, $\text{O}_2$ and $\text{O}_3^-$. The former reaction is highly exothermic and the nascent $\text{O}_3\text{SO}_3^-$ will rapidly decompose into $\text{SO}_4^-$ and $\text{O}_2$. If the origin of $\text{O}_2\text{SO}_3^-$ is $\text{SO}_2$ oxidation by $\text{O}_3^-$, the latter reaction closes a catalytic cycle wherein $\text{SO}_2$ is oxidized to $\text{SO}_3$. The relative rates between the two major sinks for $\text{O}_2\text{SO}_3^-$ is assessed, thereby providing a measure of the maximum turnover number of ion catalysed $\text{SO}_2$ oxidation, i.e. how many $\text{SO}_2$ can be oxidized per free electron. The rate ratio between reactions (a) and (b) is significantly altered by the presence or absence of a single water molecule, but reaction (b) is in general much more probable. Although we are unable to assess the overall importance of this cycle in the real atmosphere due to the unknown influence of $\text{CO}_2$ and $\text{NO}_x$, we roughly estimate that ion induced catalysis may contribute with several percent of $\text{H}_2\text{SO}_4$ levels in typical $\text{CO}_2$ free and low $\text{NO}_x$ reaction chambers, e.g. the CLOUD chamber at CERN.

1 Introduction

One of the most significant uncertainties in weather and climate forecasts are related to the processes leading to cloud formation (Simpson and Wiggert, 2009; Rosenfeld, 2006; Spracklen et al., 2008; Carslaw et al., 2002). It is well known that each cloud droplet forms around a cloud condensation nucleus (CCN). CCN’s may originate from a solid particle e.g. soot, salt, or pollen, but recently it has become increasingly clear that a significant part originate from clustering of purely gaseous molecules (Kulmala et al., 2004; Wiedensohler et al., 2009; Yu and Luo, 2009; Kazil et al., 2010). Although molecular clustering and aerosol particle formation has been intensively studied, fundamental uncertainties prevail. One of the most significant uncertainties
concerns the chemical composition of the very smallest molecular clusters. Sulfuric acid has repeatedly been found in atmospheric clusters and the concentration of sulfuric acid is known to correlate well with nanoparticle formation rates (Sipilä et al., 2010; Nieminen et al., 2009). Traditionally, binary nucleation of H$_2$SO$_4$ and H$_2$O has been the most studied mechanism, but during the last couple of decades it has become evident that a third species e.g. ammonia or an amine is needed as well (Kirkby et al., 2011; Ortega et al., 2012). However, the critical importance of sulfuric acid remains undisputed.

The main source of atmospheric sulfuric acid is UV induced oxidation of SO$_2$ which is emitted from volcanoes and through fossil fuel combustion. The oxidation mechanism involves several elementary reactions, but is relatively well understood (Bondybey and Beyer, 2002). The rate limiting step is the initial S(IV) to S(V) oxidation (Li and McKee, 1997)

\[ \text{SO}_2 + \text{OH} + M \rightarrow \text{HSO}_3 + M \]  

(R1)

where $M$ is a stabilizing molecule. HSO$_3$ is then further oxidized to SO$_3$ by O$_2$ before hydration to H$_2$SO$_4$. The final hydration is known to be catalyzed by one or more excess water molecules and is the main sink of atmospheric SO$_3$ (Morokuma and Muguruma, 1994). In addition to this, a mechanism where SO$_2$ is oxidized by Criegee biradicals has been proposed (Welz et al., 2012; Mauldin III et al., 2012).

During the last decades, the influence of ions in aerosol formation has been targeted by several chamber studies (Kirkby et al., 2011; Enghoff and Svensmark, 2008). Here, it has been firmly established that ions enhance formation of nanometer-sized aerosol particles in SO$_2$- and O$_3$- containing atmospheres under UV exposure. One possible explanation, based on classical nucleation theory, is that the energy barrier of nucleation is lowered by the charge hereby increasing the total nucleation rate (Tohmfor and Volmer, 1938; Lovejoy et al., 2004). The lower barrier might result from reduced evaporation rates from ionic clusters due to charge delocalization or from increased collision rates between ionic particles and dipolar molecules or between oppositely charged particles (Su and Bowers, 1973; Kupiainen et al., 2011).
A fundamentally different approach to explain ion induced nucleation is through ion induced chemistry altering the composition of the metastable gas phase. This idea is supported by several experimental studies where mainly collision limited ionic gas-phase chemical reactions were found, see e.g. Fehsenfeld and Ferguson (1974) and references therein. Further, a successful chamber study lead Svensmark et al. (2007) to suggest an ion induced SO$_2$ oxidation mechanism. Despite of this, little research has been dedicated to enhanced nucleation from ion induced chemistry, see however Sorokin and Arnold (2007, 2009) and Enghoff et al. (2012).

Atmospheric ions are mainly products of radioactivity and galactic cosmic rays. Although both cations and free electrons are produced, most attention have gathered around the influence of the electrons and subsequent anions (Nadykto et al., 2006; Kurtén et al., 2009). It is well known that some of the first stable products are O$_2^-$($\text{H}_2\text{O}$)$_m$ and O$_3^-$($\text{H}_2\text{O}$)$_n$ clusters (Luts and Parts, 2002). The first 5 water molecules are strongly bound to the ion, but several more may attach under cold and/or humid conditions (Bork et al., 2011b).

Further, it has been shown that O$_3^-$($\text{H}_2\text{O}$)$_n$ may oxidize SO$_2$ to SO$_3^-$ via the reaction

$$\text{O}_3^-(\text{H}_2\text{O})_n + \text{SO}_2 \rightarrow \text{SO}_3^-(\text{H}_2\text{O})_n + \text{O}_2.$$  

(R2)

This reaction is probably the dominant sink of O$_3^-$ in most reaction chambers since CO$_2$ most often is omitted. Initially, the product cluster might partially decompose due to the large release of internal energy in the oxidation. However, the high concentrations of both O$_2$ and H$_2$O ensures that the equilibrium quickly settles. Hereafter, the predominant products are O$_2$SO$_3^-$ and O$_2$SO$_3^-$($\text{H}_2\text{O}$) (Bork et al., 2011a; Möhler et al., 1992). This is supported by a recent field study by Ehn et al. (2010), finding that after HSO$_4^-$, O$_2$SO$_3^-$ is the second most common sulfur based anion in a boreal forest.

The further chemical fate of O$_2$SO$_3^-$ and the extra electron is largely unknown, but is potentially important. We have investigated the most probable reactions of de- and monohydrated O$_2$SO$_3^-$ under standard conditions focusing mainly on the reaction with O$_3$. The two main reactions are,
\[ O_2SO_3^-W_{0-1} + O_3 \rightarrow \begin{cases} O_3SO_3^-W_{0-1} + O_2 \\ O_3^-W_{0-1} + O_2 + SO_3 \end{cases} \]  
(R3a)  
(R3b)

where \( W \) is shorthand for water. The latter reaction is of particular interest since a catalytic cycle of \( SO_2 \) oxidation thereby is closed, see Fig. 1.

Using ab initio calculations we have determined the structures, energies and thermodynamics of reactants, transition states and products. We proceed to evaluate the rates of the relevant reactions and hereby evaluate the total turnover number, i.e. how many \( SO_2 \) oxidations a single electron on average will induce. Finally, we estimate the maximum fraction of \( H_2SO_4 \) originating from ionic catalysis under typical conditions in \( CO_2 \) free reaction chambers.

## 2 Computational details

As always when treating weakly bound systems, anionic systems and radical reactions, special care must be taken to ensure reliable results. Of special interest of this study is the relative adiabatic electron affinity of \( SO_3 \) and \( O_3 \) since this energy difference will be the thermodynamic driving force behind Reaction (R3b). The experimental electron affinity of \( O_3 \) has been determined to 202.9 kJ mol\(^{-1}\) with high certainty (Novick et al., 1979; Arnold et al., 1994). On the contrary, despite several studies, the electron affinity of \( SO_3 \) remains highly uncertain. The most recent studies find values of 183 ± 10 kJ mol\(^{-1}\) (Gleason, 1987) and 190 ± 10 kJ mol\(^{-1}\) (Dobrin et al., 2000). However, the accumulated experimental evidence suggest that most likely the electron affinity of \( O_3 \) exceeds that of \( SO_3 \) by ca. 15 kJ mol\(^{-1}\).

While scanning a variety of methods, we found that most ab initio methods actually predict a larger electron affinity of \( SO_3 \) than of \( O_3 \), despite large basis sets. However, the CAM-B3LYP functional is an exception to this (Yanai et al., 2004). At basis sets of at least triple zeta quality, both the order and magnitude of the electron affinity difference is in accordance with the experimental value. Therefore, we have used
the CAM-B3LYP functional with aug-cc-pVTZ basis set throughout (Dunning, 1989), predicting the difference in electron affinity between O\(_3\) and SO\(_3\) to be 18 kJ mol\(^{-1}\). Further, it has been shown that CAM-B3LYP is superior to B3LYP with respect to determining activation energies for a range of typical chemical reactions (Peach et al., 2006; Yanai et al., 2004). All DFT calculations were performed using the Gaussian09 package (http://gaussian.com/).

The present reactions involve both neutral and charged ozone as well as highly oxidized sulfur species with unknown electronic properties. Therefore, we have performed CCSD(T)-F12 calculations with the VDZ-F12 basis set to test the DFT results (Adler et al., 2007; Peterson et al., 2008). These calculations have been performed using the MOLPRO package (http://molpro.net/) and are described in detail elsewhere (Bork et al., 2011b).

Energy barriers were determined by scans of the potential energy surface and confirmed by frequency analyses showing exactly one imaginary frequency. Further, by following the reaction coordinate in both directions it was ensured that transition states indeed connected the desired reactants and products.

The temperature dependent reaction rate constants, \(k(T)\), were determined using harmonic transition state theory (Hänggi et al., 1990; Billing and Mikkelsen, 1996),

\[
k(T) = A \times \exp\left(\frac{-E_A}{RT}\right), \quad \text{where}
\]

\[
A = \frac{\prod \nu_{\text{reac}}}{\prod \nu_{T S}^{\dagger}}. \quad (2)
\]

\(E_A\) is energy barrier separating reactants and products, \(R\) is the molar gas constant and \(\nu\) are the harmonic frequencies for the reactant and transition state. The \(\dagger\) indicates that the imaginary frequency should be omitted.

We finally note that in all cases molecular oxygen is treated as an electronic triplet and all reactions are spin allowed.
3 Results and discussion

3.1 Self dissociation

The simplest reaction of $O_2SO_3^-$ based clusters is spontaneous dissociation into $O_2$ and $SO_3^-$, i.e.

$$O_2SO_3^-W_{0-1} \rightleftharpoons SO_3^-W_{0-1} + O_2.$$  \hspace{1cm} (R3)

This reaction is potentially important since the reaction

$$SO_3^-W_{0-1} + O_3 \rightarrow SO_3 + O_3^-W_{0-1}$$  \hspace{1cm} (R4)

is distinctly exothermic, thus providing a direct path to complete the catalytic cycle in Fig. 1. Further, both $SO_3^-$ and $O_2SO_3^-$ have recently been measured by Ehn et al. (2010) in a Finnish boreal forest, where typical ratios of 1:10 was found, suggesting that this reaction may be significant.

After optimizing all species we found Gibbs free $O_2$ binding energies of 50.4 and 41.3 kJ mol$^{-1}$ for the de- and monohydrated clusters, respectively. Little experimental data is available but Möhler et al. (1992), based on mass spectroscopical data, concluded that $O_2$ is bound stronger to $SO_3^-$ than $H_2O$ is to $CO_3^-$, $HCO_3^-$, and $NO_3^-$. This implies that $\Delta G_{(R3)} \leq -25$ kJ mol$^{-1}$ at room temperature (Keesee et al., 1979; Payzant et al., 1971).

Since these binding energies suggest much lower $[SO_3^-]$:[$O_2SO_3^-]$ ratios than the observed ratio of 1:10, the field data may be explained by $SO_3^-$ being stabilized by more than one water or that the sources and sinks of $SO_3^-$ and $O_2SO_3^-$ induces a dynamic rather than a thermal equilibrium. Although interesting, these considerations are beyond the scope of this study.

We conclude that although some $SO_3^-$ exists, the population of $O_2SO_3^-$ is significantly higher and we will thus focus on this species in the remaining of this article. Finally, we note that, contrary to all previous studies, we generally avoid referring to $O_2SO_3^-$.  

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as \( \text{SO}_5^- \) since the \( \text{O}_2-\text{SO}_3^- \) bond resembles that of a molecular cluster more than a molecular covalent bond, concerning both distance and strength.

### 3.2 \( \text{O}_3 \) collision and formation of \( \text{O}_2\text{SO}_3^-\text{W}_{0-1}\text{O}_3 \)

First, the \( \text{O}_2\text{SO}_3^-\text{O}_3 \) and \( \text{O}_2\text{SO}_3^-\text{WO}_3 \) molecular complexes were optimized, see Fig. 2. In the dehydrated system, only a few different stable configurations were found, while at least 10 stable configurations were found in the monohydrated cluster. Most configurations were within 10 kJ mol\(^{-1}\) and are thus predicted to co-exist at typical atmospheric temperatures. However, for the remaining of this article mainly the single most stable configurations with respect to \( \Delta G \) will be considered.

Structurally, only small changes were apparent upon ozonation since the binding preference of the \( \text{O}_3 \) and \( \text{H}_2\text{O} \) are very different. In accordance with this, the binding energy of \( \text{O}_3 \) to \( \text{O}_2\text{SO}_3^- \) is only minutely affected by hydration. Considering the equilibrium,

\[
\text{O}_2\text{SO}_3^-\text{W}_{0-1} + \text{O}_3 \rightleftharpoons \text{O}_2\text{SO}_3^-\text{W}_{0-1}\text{O}_3, \quad (R5)
\]

and regardless of the presence or absence of water, we found \( \Delta H_{(R5)} \) values of ca. \(-12 \text{ kJ mol}^{-1}\) and \( \Delta G_{(R5)} \) values of ca. \(+12 \text{ kJ mol}^{-1}\) implying a short lifetime towards de-ozonation.

Not only does the water molecule not change the thermodynamics of ozonation, but neither does the ozone change the thermodynamics of hydration. Considering the condensation-evaporation equilibrium, i.e.

\[
\text{O}_2\text{SO}_3^-(\text{O}_3)^{0-1} + \text{W} \rightleftharpoons \text{O}_2\text{SO}_3^-(\text{O}_3)^{0-1}\text{W}, \quad (R6)
\]

we find \( \Delta H_{(R6)} \) and \( \Delta G_{(R6)} \) of \(-42\) and \(-7 \text{ kJ mol}^{-1}\), respectively. Also this reaction was investigated by Möhler et al. (1992) whom determined \( \Delta G_{(R6)} \) to \(-17.2 \text{ kJ mol}^{-1}\). To clarify this discrepancy, we optimized all relevant species with CCSD(T)-F12 and found an electronic binding energy of 51.3 kJ mol\(^{-1}\). Assuming \( \Delta S_{(R6)} = -120 \text{ J mol}^{-1} \text{ K}^{-1}\)
K$^{-1}$, which is typical of water condensation reactions we find $\Delta G_{(R6)} = -15 \text{ kJ mol}^{-1}$, in good accordance with M"ohler et al. (1992).

Using the law of mass action

$$\frac{[O_2SO_3^-W]}{[O_2SO_3^-]} = [W] \times \exp\left(\frac{-\Delta G_{R7}}{RT}\right)$$

we find that roughly 90% of $O_2SO_3^-$ are hydrated at $T = 298 \text{ K}$ and 50% relative humidity and the fate of the hydrated cluster is thus of primary importance. However, in all but extremely dry conditions both hydrated and dehydrated clusters co-exist and should both be considered when evaluating Reaction (??).

Having established the structures and relative populations of the relevant clusters, we proceed to evaluate the possible chemical reactions.

### 3.3 Cluster decomposition

The most important reaction considered here is decomposition of the reactant cluster as

$$O_3\cdot O_2SO_3^-W_{0-1} \rightarrow O_3^-W_{0-1} + O_2 + SO_3$$

As mentioned, the binding energy of the $O_2SO_3^-$ cluster is at least 25 kJ mol$^{-1}$, which is only partially compensated by the transferring of the electron. Hence, the dehydrated Reaction (R4) is ca. 15 kJ mol$^{-1}$ exothermic.

However, the water molecule is bound significantly stronger to the $O_3^-$ ion than to the $SO_3^-$ ion. Considering also this effect we find that the monohydrated cluster decomposition reaction is ca. 10 kJ mol$^{-1}$ exothermic at $T = 298 \text{ K}$. The Gibbs free potential energy surface is shown in Fig. 3 for $T = 298 \text{ K}$ and tabulated in the supplement.

Considering first the dehydrated reaction, we identified three normal modes of the $O_2SO_3^-O_3$ clusters clearly leading towards dissociation via

$$O_2SO_3^- \rightarrow O_2 + SO_3^-.$$
These modes are shown in Fig. 2. Sometimes the modes will interfere constructively and in other cases destructively. Assuming that the modes are all in the ground state, we manually determined an effective frequency of 540 cm\(^{-1}\). We use this as prefactor, \(A\), in Eq. (1).

By analysing the Mulliken charges (Mulliken, 1955) during these vibrations it was confirmed that electronic density was smoothly being transferred to \(O_3\) from \(SO_3^-\) during a vibration and that no electronic barrier separated the charge transfer Reaction (R4). Hence, the minimum energy required to dissociate the dehydrated cluster is exactly the energy of the net reaction, here 31.9 kJ mol\(^{-1}\) above the reactants. This implies an overall rate constant of \(1.6 \times 10^{-12}\) cm\(^3\) molecule\(^{-1}\) s\(^{-1}\) at \(T = 298\) K, see also Fig. 4.

Contrary to the dehydrated cluster, in the monohydrated cluster the dissociation into \(SO_3\), \(O_2\), and \(O_3^-\)W is almost thermo neutral. In this case the rate limiting step is formation of the \(O_3\) \(O_2SO_3^-\)W cluster itself and the effective barrier is hence just 12.3 kJ mol\(^{-1}\) at 298 K. The mechanism leading to cluster decomposition is however identical to the dehydrated cluster and the modes leading to dissociation are almost identical. These are given in parenthesis in Fig. 2. Due to the small energy barrier we find that this reaction essentially is collision limited, see also Fig. 4.

Comparing the decomposition rates of the dehydrated and monohydrated systems, we see that the water molecule is significantly facilitating cluster decomposition. The main reason is the more favourable thermodynamics since \(H_2O\) is bound significantly stronger to \(O_3^-\) than to \(O_2SO_3^-\).

### 3.3.1 Formation of \(O_3SO_3^-\)

The other major reaction sink of \(O_2SO_3^-\) considered here is oxidation by \(O_3\). The sulfur is already tetrahedrally coordinated by oxygen, so the only possible oxidation is from further O-O binding. Most likely is the formation of \(O_3SO_3^-\) since the reaction

\[
O_2SO_3^-W_{0-1} \cdot O_3 \rightarrow O_3SO_3^-W_{0-1} + O_2
\]

(R9)
is ca. 175 kJ mol⁻¹ exothermic. The de- and monohydrated O₃SO₃⁻ structures are shown in the supplement.

The two transition states of Reaction (R9) were then determined and the monohydrated structure is shown in Fig. 5a. Besides the absent water molecule, the dehydrated structure differs only slightly from the monohydrated and is shown in the supplement. However, considering the barrier heights, the effect of water is very significant. At standard conditions the de- and monohydrated energy barriers are 27.1 and 39.6 kJ mol⁻¹ respectively, implying that the water is significantly hindering the oxygen transfer due to destabilisation of the transition state, see Fig. 3. Finally, the pre-factors (Eq. 1) were determined to 3.12 × 10¹⁰ s⁻¹ and 1.90 × 10⁹ s⁻¹ respectively.

The reaction rate constant of Reaction (R9) was readily determined from Eq. (1) using the parameters described above, see Fig. 4. It is thus clear that the water molecule, while favouring charge transfer, effectively is hindering the oxidation of O₂SO₃⁻. The main reason is the increased energy barrier. The effect is largest at high temperatures but at all temperatures investigated here the hydrated Reaction (R9) is at least 2.5 orders of magnitude slower than the dehydrated.

To our knowledge O₃SO₃⁻ has not previously been described in the literature, nor has it been observed in experiments or in field studies. This suggests that O₃SO₃⁻ is reactive and has too short lifetime to allow for observation. We therefore proceeded to investigate the possible decomposition of O₃SO₃⁻ via

\[
\text{O}_3\text{SO}_3^- W_{0-1} \rightarrow \text{SO}_4^- W_{0-1} + \text{O}_2.
\]  

(R10)

The monohydrated transition state is shown in Fig. 5(b) and the dehydrated transition state is shown in the supplement. We hereby determine the energy barrier to ca. 22 kJ mol⁻¹ at standard conditions, practically independent of hydration, see Fig. 3. Since the energy release of Reaction (R9) is so much larger than the energy barrier, it is evident that Reaction (R10) is almost instantaneous.
3.4 Overall catalytic turnover

The presence of an ion catalysed SO$_2$ oxidation cycle is of interest since an extra source of atmospheric H$_2$SO$_4$ significantly may alter the conditions for aerosol particle formation and growth. Although this assessment is the overall goal of this line of studies, several unresolved factors remain.

Considering the real atmosphere the most noticeable shortcoming is the influence of CO$_2$. This is known to be the dominant sink of O$_3^-$ via

$$\text{O}_3^- + \text{CO}_2 \rightarrow \text{CO}_3^- + \text{O}_2.$$ (R11)

and cannot be neglected in any realistic model (Dotan et al., 1977; Luts and Parts, 2002). The chemical fate of CO$_3^-$ is uncertain although the reaction

$$\text{CO}_3^- + \text{SO}_2 \rightarrow \text{CO}_2 + \text{SO}_3^-$$ (R12)

is known to proceed at collision rates, similar to Reaction (R2) (Fehsenfeld and Ferguson, 1974). However, extending the catalytic cycle in Fig. 1 to include these reactions is beyond the scope of this study.

Presently, we are able to assess the overall catalytic turnover in CO$_2$ free atmospheres, including most of the until now conducted chamber studies of ion induced nucleation. Taking all investigated clusters, their relative concentrations, and all reactions into account we find that the probability for cluster decomposition through Reaction (R3b) is $10^5$-$10^6$ times more likely than other reactions between O$_3$SO$_3^-$W$_{0-1}$ and O$_3$. Details are presented in the supplement. This thus suggests that each free electron may induce up to $10^5$-$10^6$ SO$_2$ oxidations in atmospheres consisting of N$_2$, O$_2$, O$_3$, H$_2$O and SO$_2$ only.

This is consistent with recent experimental results from Enghoff et al. (2012). In the absence of UV light it was found that each electron yielded a production of $10^6$ sulfates in atmospheres heavily enriched in SO$_2$ and O$_3$. Further it was found that the isotopic fingerprint of this ion produced sulfate was very different of sulfate from UV induced SO$_2$ oxidation, clearly pointing at two different chemical mechanisms.
More commonly chamber atmospheres are made to resemble typical atmospheric conditions and hence various pollutants become important. In those cases, the catalytic cycle may be terminated by mechanisms different from the ones presented so far, most likely involving species different from \( \text{SO}_2 \) and \( \text{O}_3 \). Considering e.g. a collision between \( \text{O}_3^-(\text{H}_2\text{O})_n \) and a \( \text{NO}_2 \) radical, this will rapidly be oxidized to \( \text{NO}_3^- \) with large energy gain,

\[
\text{O}_3^-\text{W}_n + \text{NO}_2 \rightarrow \text{NO}_3^-\text{W}_n + \text{O}_2.
\] (R13)

Due to the stability of \( \text{NO}_3^- \), the catalytic cycle for that particular electron is most likely terminated. Other potential scavengers include any species in which an electron may be more stabilized than on \( \text{O}_3^- \) or \( \text{O}_2\text{SO}_3^- \), either through immediate charge transfer or after some chemical reaction. These include most radicals, \( \text{NO}_x \), cations and pre-existing aerosol particles or molecular clusters. Typically, \( \text{NO}_x \) will be the dominant electron scavenger.

We here outline two methods of determining the rate of ion induced \( \text{H}_2\text{SO}_4 \) formation. Most simply, if the actual concentrations of the involved ions are known, the rate of ion induced \( \text{H}_2\text{SO}_4 \) formation may be determined based on the mechanism outlined in Fig. 1. Assuming \([\text{O}_3]>>[\text{SO}_2]\) we obtain

\[
r_{\text{ion cat.}} = Z \times [\text{O}_3^-(\text{H}_2\text{O})_n] \times [\text{SO}_2]
\] (4)

where \( Z \) denote the collision rate.

Alternatively, the ion induced \( \text{H}_2\text{SO}_4 \) formation rate may be determined by realising that the incoming flux of electrons, \( J_{\text{ion}} \), is the primary limiting factor. As shown in Fig. 1, the electron will remain catalytically active until scavenged, which occurs when the ionic cluster is hit by a scavenger. Again assuming \([\text{O}_3]>>[\text{SO}_2]\) and that \( \text{NO}_x \) is the dominant...
scavenger, the number of catalytic cycles per electron is thus determined as

\[
\text{Max.cyc.} = \frac{Z(\text{SO}_2)}{Z(\text{electron scavenger})} \approx \frac{[\text{SO}_2]}{[\text{NO}_x]} \tag{5}
\]

where \( Z \) denotes the collision rate. The overall catalytic efficiency and is then given as

\[
 r_{\text{ion.cat.}} = J_{\text{ion}} \times \text{Max.cyc.} \tag{7}
\]

We now proceed to evaluate the relevance of ion catalyzed \( \text{SO}_2 \) oxidation in a typical \( \text{CO}_2 \) free chamber. Since we have no data for the ionic concentrations we will use the latter approach. The well known UV induced \( \text{H}_2\text{SO}_4 \) production rate via Reaction (R1) is

\[
r_{\text{UV}} = k_{\text{UV}} \times [M] \times [\text{OH}] \times [\text{SO}_2], \tag{8}
\]

where \( k_{\text{UV}} = 4.5 \times 10^{-31} \text{cm}^6 \text{molecule}^{-2} \text{s}^{-1} \) (Atkinson et al., 2004).

We here assume the following conditions: \([\text{OH}] = 5 \times 10^5 \text{ cm}^{-3} \) (day and night average), \([\text{NO}_x] = 10 \text{ ppt} = 2.5 \times 10^8 \text{ cm}^{-3} \), \([\text{SO}_2] = 5 \text{ ppb} = 1.25 \times 10^{11} \text{ cm}^{-3} \), \([\text{O}_3] \gg [\text{SO}_2] \), and \( J_{\text{ion}} = 20 \text{ ion pairs cm}^{-3} \text{ s}^{-1} \) corresponding to mid-troposphere. We thus obtain \( \text{Max.cyc.} = 500 \), and further obtain the contribution of \( \text{H}_2\text{SO}_4 \) from ion catalysis as

\[
\frac{[\text{H}_2\text{SO}_4]_{\text{ion.cat.}}}{[\text{H}_2\text{SO}_4]_{\text{total}}} = \frac{r_{\text{ion.cat.}}}{r_{\text{ion.cat.}} + r_{\text{UV}}} = 1.5\%. \tag{9}
\]

Obviously, this is merely a rough estimate intended mainly as an illustrative example. However, variations in \([\text{H}_2\text{SO}_4]\) on the order of a few percent are important and the lack of this contribution in models of gaseous sulfur chemistry may lead to significant inaccuracies in predicting aerosol formation and growth rates.
4 Conclusions

It has previously been determined that de- or monohydrated clusters of $\text{O}_2\text{SO}_3^-$ are natural products of free atmospheric electrons. We have investigated the chemical fate of $\text{O}_2\text{SO}_3^-$ after various reactions with $\text{O}_3$.

Using a combination of DFT and coupled cluster levels of theory we have optimized several possible reactants and products. We have linked the most important of these either through transition states or shown that the reactions are barrierless with respect to $\Delta E$. We have determined pre-factors and free energy barrier heights and, using transition state theory, also the reaction rates.

We find two major reaction mechanisms leading to fundamentally different products, shown in Fig. 3. The first mechanism is a conventional oxidation eventually leading to $\text{SO}_4^-$ with large energy gain. However, significant energy barriers must be overcome and we find that this reaction is of minor importance.

Of primary importance is the transferring of the electron from $\text{O}_2\text{SO}_3^-$ to $\text{O}_3$. In the dehydrated system this is distinctly endothermic but still requires a lower energy than crossing the energy barrier of oxidation. In the hydrated systems, the water molecule can transfer with the charge from $\text{O}_2\text{SO}_3^-(\text{H}_2\text{O})$ to $\text{O}_3^-(\text{H}_2\text{O})$ with significant energy gain. We find that this path is $10^5$ to $10^6$ times more probable than $\text{O}_2\text{SO}_3^-(\text{H}_2\text{O})$ oxidation. This reaction closes a catalytic cycle of $\text{SO}_2$ oxidation shown in Fig. 1. Both the chemical mechanism and the catalytic turnover number is in accordance with a recent chamber study by Enghoff et al. (2012).

Considering also the concentrations of other typical reactants we conclude that the cycle is more probable to terminate due to reactions with an electron scavenger, most likely some $\text{NO}_x$, than due to its own inherent side reactions. We are unable to assess the influence of this cycle in the real atmosphere, most noticeable due to $\text{CO}_2$. In chamber studies under UV exposure and in realistic gas mixtures we roughly estimate the contribution of ion catalysed $\text{H}_2\text{SO}_4$ to be on the order of several percent.
Besides being a source of atmospheric H$_2$SO$_4$, we note that the previously unknown origin of both O$_2$SO$_3^-$ and SO$_4^-$, seen in several experiments and field studies, readily is explained through this mechanism. Finally, this mechanism is also in accordance with the absence of SO$_6^-$ from any observations since it explains why SO$_6^-$ immediately decomposes to SO$_4^-$ and O$_2$.

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References


Sorokin, A. and Arnold, F.: Laboratory study of cluster ions formation in H$_2$SO$_4$-H$_2$O system: Implications for threshold concentration of gaseous H$_2$SO$_4$ and ion-induced nucleation kinetics, Atmos. Environ., 41, 3740–3747, 2007. 30180


Fig. 1. Schematics of a simple catalytic SO₂ oxidation cycle. The net reaction is \( O_3 + SO_2 \rightarrow O_2 + SO_3 \) and the catalyst is the electron. All reaction rates are mainly collision limited.
Fig. 2. Top: the molecular complex between $\text{O}_2\text{SO}_3^-$, $\text{H}_2\text{O}$ and $\text{O}_3$ including some descriptive bond lengths. Removing either the $\text{H}_2\text{O}$ or $\text{O}_3$ causes little structural rearrangement. Bottom: Directions and frequencies of the three normal vibrational modes along the $\text{SO}_3^--\text{O}_2$ bond in the dehydrated (monohydrated) cluster. Sulfur is yellow, oxygen is red, and hydrogen is white.
Fig. 3. Schematic overview of the Gibbs free energy of the relevant species at standard conditions. The barrier height for $\text{O}_2\text{SO}_3^-$ oxidation is increased by ca. 12 kJ mol$^{-1}$ by the presence of a water molecule while the thermodynamics of charge transfer and cluster decomposition is changed from distinctly endothermic to almost thermo neutral. At standard conditions and 50 % relative humidity ca. 90 % of $\text{O}_2\text{SO}_3^-$ is monohydrated.
Fig. 4. Bimolecular rate constants of cluster decomposition mechanism and $O_2SO_3^-$ oxidation in cm$^3$ molecule$^{-1}$ s$^{-1}$ as function of temperature. For both the dehydrated and the monohydrated systems, cluster breakup is favoured although much more so in the hydrated systems. At standard conditions and 50% relative humidity, ca. 90% of $O_2SO_3^-$ is monohydrated. The collision rate with $H_2O$ is indicated (50% relative humidity).
Fig. 5. Transition states for (a) the oxidation of $\text{O}_2\text{SO}_3^-\text{W}$ to $\text{O}_3\text{SO}_3^-\text{W}$ and (b) the following dissociation to $\text{SO}_4^-\text{W}$. The active bonds are shown as broken grey and some descriptive bond lengths are indicated. Sulfur is yellow, oxygen is red and hydrogen is white.