Ice water content of arctic, midlatitude, and tropical cirrus – Part 2: Extension of the database and new statistical analysis

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Abstract

Ice clouds are known to be major contributors to radiative forcing in the Earth’s atmosphere, yet describing their microphysical properties in climate models remains challenging. Among these properties, the ice water content (IWC) of cirrus clouds is of particular interest both because it is measurable and because it can be directly related to a number of other radiatively important variables such as extinction and effective radius. This study expands upon the work of Schiller et al. (2008), extending a climatology of IWC by combining datasets from several European and US airborne campaigns and ground-based lidar measurements over Jüllich, Germany. The relationship between IWC and temperature is further investigated using the new merged dataset and probability distribution functions (PDFs). A PDF-based formulation allows for representation of not only the mean values of IWC, but also the variability of IWC within a temperature band. The IWC-PDFs are found to be bimodal over the whole cirrus temperature range, which might be attributed to different cirrus formation mechanisms such as heterogeneous and homogeneous freezing. The PDFs of IWC are further compared to distributions of cirrus ice crystal number and mass mean radius, which show that the general relationship between IWC and temperature appears to be influenced much more by particle number than by particle size.

1 Introduction

Cirrus clouds are ice clouds found in the upper troposphere at altitudes where temperatures range from about 235 K to 185 K. They have been observed to cover close to 40 % of the Earth at any given time, with the greatest coverage at the tropics and along the midlatitude storm tracks (Wylie and Menzel, 1999). Although there is considerable research on cirrus clouds, the 2007 Intergovernmental Panel on Climate Change (IPCC) report says little about them, focusing mostly on their interaction with aircraft emissions, another area in which very little is known.

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Cirrus clouds have the ability to both trap infrared terrestrial radiation and reflect solar radiation. Therefore, they are able to produce either a warming or a cooling effect on the Earth, depending on the balance between these two processes. The microphysical properties of an individual cirrus cloud, such as the cloud particle sizes (Liou et al., 2008) and the crystal habits (van Zadelhoff et al., 2007), determine whether absorption or reflection will dominate for a particular cloud. Determining the exact role of cirrus in the radiation budget of the atmosphere is difficult, however, owing to the number and variability of the microphysical, and thus radiative, properties involved, as well as the current lack of understanding of how and why some of those variations occur.

One of the microphysical properties of cirrus that is essential for more completely describing their radiative role is ice water content (IWC) (Liou et al., 2008). IWC is related to particle size and extinction, both of which are used to determine the radiative properties of a cirrus cloud. Currently, it is known that the IWC of cirrus varies over at least six orders of magnitude (from $10^{-3}$ ppmv to $10^3$ ppmv) and is influenced by factors such as the water vapor content of the air and temperature (Schiller et al., 2008). A few studies have provided data to demonstrate how IWC in cirrus varies. For example, data obtained with a millimeter-wave cloud radar at the Atmospheric Radiation Measurement (ARM) Climate Research Facility (ACRF) in Oklahoma was used to document the macrophysical and microphysical properties of cirrus clouds over the site for six years. The results are reported by Mace et al. (2006) and reveal the relationships between atmospheric conditions, such as the vertical velocities, and cloud properties, such as IWC. Though the dataset is large and spans several years, it covers only a single location. In the results of a similar project by Sassen and Campbell (2001), the authors note that, since the formation of clouds results from weather processes, their properties will vary across the planet, thus stressing the importance of obtaining datasets with global coverage.

While efforts have been made to obtain more comprehensive datasets through projects such as the Cirrus Regional Study of Tropical Anvils and Cirrus Layers – Florida Area Cirrus Experiment (CRYSTAL-FACE), logistical considerations dictate that
a particular campaign focuses on a specific geographic region (e.g. the tropics, mid-latitude, or poles) and there is little to no overlap. Schiller et al. (2008) created an extensive dataset of IWC values by combining data from ten airborne field campaigns. In this paper, we report the extension of that dataset by including measurements from four US field campaigns of similar design.

One of the most common ways to parameterize ice cloud properties in models is to use IWC (Heymsfield and Platt, 1984). For example, Liou et al. (2008) used IWC to determine the mean effective crystal size, which was then used for radiative transfer calculations. In this case, IWC was calculated based on an assumed ice crystal density, in situ measurements of the ice crystal size distribution, and the measured volumes of individual ice crystals. Though the authors take into account the differences between tropical, midlatitude, and arctic regions in terms of cloud formation processes, the datasets used for their parameterization come from only a few experiments, and measured variability is not considered.

A number of published studies present parameterizations of IWC as a function of temperature, but most have had relatively little data at their disposal to create these models (McFarquhar and Heymsfield, 1997; Mace et al., 2001). Although they have described the general behavior of IWC with respect to temperature, these studies have concluded that the variability of IWC measurements is difficult to parameterize on the basis of temperature alone. Heymsfield and Donner (1990) parameterized IWC as a function of large-scale meteorological variables that could be used in climate models for evaluating optical cloud properties. By including vertical velocity, they added a focus on the conditions necessary for cloud formation to their parameterization. Their results showed that while each IWC-temperature relationship at a given vertical velocity represented the in situ data well, the use of multiple expressions for a range of vertical velocities provided a more complete picture of the variability of IWC with temperature. However, the addition of more variables into a parameterization makes its implementation more complex.
In the following sections, the new, extended IWC dataset is introduced. First, the instrumentation and data processing methods are discussed (Sect. 2.1). Also, a comparison between the airborne in situ data and IWC derived from extinction measurements from a ground-based lidar is shown to demonstrate the consistency of the lowest IWC values obtained with the in situ measurements (Sect. 2.2). Next, the comprehensive nature of the merged datasets is established and the differences between the original and merged climatologies are described (Sect. 3.1). From the merged dataset, it is possible to perform a more detailed statistical analysis of IWC than that provided by Schiller et al. (2008). In Sect. 3.2, we explore the analysis of IWC solely as a function of temperature, based on probability distribution functions, an analysis method that captures the measured variability of IWC. Additional cloud properties are also included in the discussion of the analysis with the goal of offering some explanation for the distribution of IWC in a given temperature range.

2 Instruments and analysis methods

The in situ IWC climatology obtained from aircraft presented in this study is the result of merging two large datasets, one provided by the University of Colorado Boulder and one from the Forschungszentrum Jülich, Germany. In situ data from 13 flight campaigns, comprising 67 flights and totaling approximately 38 h of cirrus observations, and from two different total water instruments are included (see Table 1). In addition, observations of 142 cirrus clouds obtained with a ground-based lidar system placed in Jülich, Western Germany are compared to the in situ observations.

2.1 FISH and CLH instruments

2.1.1 CLH instrument

Four of the thirteen campaign datasets are the result of measurements by the University of Colorado closed-path laser hygrometer (CLH), which was situated aboard the
NASA WB-57F aircraft or the NCAR Gulfstream G-V aircraft, depending on the campaign. A detailed description of the CLH instrument, its calibration, and data analysis procedures can be found in Davis et al. (2007a). The instrument works by measuring the total water amount, which is the gas phase water plus the water vapor that results from evaporating cloud particles. A heated inlet and flow path are used for sampling. Water vapor is detected by second harmonic (2f) infrared spectroscopy for smaller mixing ratios and by direct absorption for larger mixing ratios. The instrument has the ability to measure water vapor quantities ranging from about 50 ppmv to more than 20 000 ppmv.

One of the key features of this instrument is that it is coupled to a subisokinetic inlet. The inlet is forward-facing and is situated on the right-wing pod of the WB-57F aircraft with the CLH mounted behind it or on the top fuselage of the G-V, with the CLH in a rack inside the cabin. The purpose of the inlet is to enhance the small ice particle concentrations over the ambient amounts, which occurs because the particles cannot follow streamlines around the inlet (Davis et al., 2007a; Hallar et al., 2004; Krämer and Afchine, 2004). The resulting measurement is an enhanced value called enhanced total water (H$_2$O$_{\text{enh}}$), which has an uncertainty of 10% (Davis et al., 2007a). Further discussion on this topic as well as a brief description of how H$_2$O$_{\text{enh}}$ is converted to IWC is contained in Sect. 2.3.

The CLH was used in the 2002 CRYSTAL-FACE, the 2004 Midlatitude Cirrus Experiment (MidCiX), the 2006 Tropical Composition, Cloud, and Climate Coupling mission (TC4), and the 2008 Stratosphere-Troposphere Analyses of Regional Transport (START08) campaign. The IWC measurements from these campaigns were taken primarily in the midlatitudes and the northern tropics.

### 2.1.2 FISH instrument

Data from the remaining nine campaigns were obtained by using the Fast In Situ Stratospheric Hygrometer (FISH), which spent time aboard the Russian high-altitude M55 Geophysica aircraft and the GFD Lear Jet throughout various campaigns. FISH...
is a closed-cell Lyman-α hygrometer that is situated inside the research aircraft with a forward-facing inlet. Similar to the CLH, FISH measures enhanced total water, but in the range of 1–1000 ppmv and with an uncertainty of $6\% \pm 0.2$ ppmv. Additional information concerning FISH is provided by Schiller et al. (2008).

The campaigns in which FISH was utilized cover the tropics, higher midlatitudes, and the polar latitudes. The tropical measurements come from the Third European Stratospheric Experiment on Ozone in 1999 (APE-THESEO), the 2005 Stratospheric-Climate Links with Emphasis on the UTLS campaign (SCOUT-O3), and the 2005 Tropical Convection, Cirrus, and Nitrogen Oxides Experiment (TROCCINOX). The midlatitude data used by Schiller et al. and in this study are a result of the 2003, 2004, and 2006 CIRRUS experiments and the 2002 ENVISAT validation experiment. The field campaigns that yielded the arctic measurements for the climatology were the 2003 ENVISAT validation experiment and the 2003 European Polar Stratospheric Cloud and Lee Wave Experiment (EUPLEX). It should be noted that the FISH data that was included in this analysis comes from the 29 flights where water vapor ($H_2O_{gas}$) was measured separately and could be used to calculate IWC from the enhanced total water ($H_2O_{enh}$) measurement. The full Schiller climatology contains data in which IWC was determined by the difference between the total water measurement made by FISH and the water vapor saturation mixing ratio (see Schiller et al., 2008, for additional information).

2.1.3 **FISH and CLH analysis methods**

One of the first steps in the analysis was to calculate the IWC from the $H_2O_{enh}$ directly measured by the instruments. This calculation requires ambient water vapor measurements and was carried out according to the methods described in Davis et al. (2007a). In the case of the CLH instrument, water vapor measurements were made by the Jet Propulsion Laboratory (JPL) tunable diode laser (TDL) hygrometer (JLH), which was flown in tandem with the CLH during the flight campaigns. Data from the FISH instrument had been processed previously to obtain an IWC measurement, the details of which may be found in Schiller et al. (2008). The water vapor measurements for their
calculations were made by the Lyman-α Stratospheric Hygrometer (FLASH) of the Central Aerological Observatory and the open-path tunable diode laser spectrometer (OJSTER) of Forschungszentrum Jülich.

A critical piece of this analysis was the development of a method that could be used to determine whether the aircraft was in or out of clouds and thus where the data is representative of cirrus versus clear air. Based on the methods described in Krämer et al. (2009) and Schiller et al. (2008) for the FISH, FLASH, and OJSTER instruments, this can be accomplished for the CLH data using the water vapor measurements from the JLH. It should be noted that these methods have been previously applied to the datasets from the FISH instrument, so they were incorporated without further processing.

The first step is to perform a data quality check on the water vapor measurements. This is done by comparing $H_2O_{gas}$ and $H_2O_{enh}$ to one another. During periods of the experiment spent in clear air, the two measurements should agree within their respective uncertainties. During periods of the flight spent in cloud, $H_2O_{enh}$ should be greater than $H_2O_{gas}$. Flights with good fidelity to those rules are used for the analysis while flights that do not pass the test are left out. Before they are removed, however, an attempt is made to adjust the value of $H_2O_{enh}$ to ensure that $H_2O_{enh}$ and $H_2O_{gas}$ match in cases where the IWC is equal to zero. This is a reasonable procedure because the CLH has a higher detection limit than the JLH as a result of its short path length. When the ambient water vapor is 5 ppmv, for example, the CLH will report an $H_2O_{enh}$ measurement that is at least 20 ppmv. Davis et al. (2007b) discuss this in more detail. In the case of the CLH data, the $H_2O_{enh}$ value was adjusted to the $H_2O_{gas}$ value. This was done by first calculating an adjusted water vapor measurement ($H_2O_{gas,adj}$) using the expression

$$H_2O_{gas,adj} = H_2O_{enh} - eIWC$$  \hspace{1cm} (1)
a rearrangement of that relationship. Since $H_2O_{gas}$ is a measured value and $H_2O_{gas,adj}$ is a value calculated from the enhanced CLH measurement, they will not likely be equal, particularly in cases of low ambient water vapor due to the limitations of the CLH as previously mentioned. What this calculation does is adjust the value of $H_2O_{gas}$ to $H_2O_{enh}$ so that it passes the data quality check. However, the value of $H_2O_{gas,adj}$ is not physically meaningful since the adjusted water vapor measurement will always be greater than the saturation water vapor mixing ratio, indicating that the aircraft was always inside cloud. To correct for this, the original enhanced total water measurement, $H_2O_{enh}$ is adjusted to $H_2O_{gas}$ thus creating $H_2O_{enh,adj}$, which is defined here as

$$H_2O_{enh,adj} = H_2O_{enh} - (H_2O_{gas,adj} - H_2O_{gas})$$

(2)

The difference between the adjusted water vapor and the measured water vapor should be the same value as the difference between the adjusted and measured enhanced total water, thus it can be used in the above calculation. Now, $H_2O_{enh,adj}$ and $H_2O_{gas}$ are both physically meaningful values that can potentially pass the data quality check. There is still the chance that the adjustment will not work, and in that case, the data are taken out of the analysis. An example graphical representation of these values and the adjustment can be seen in Fig. 1 where $H_2O_{gas}$ (red), $H_2O_{enh}$ (turquoise), and $H_2O_{enh,adj}$ (dark blue) are shown. $H_2O_{sat}$ (black) is also shown to illustrate that $H_2O_{gas}$ and $H_2O_{enh,adj}$ are physically meaningful values.

After completing the data quality check, the water vapor data are usable for calculating the relative humidity with respect to ice ($RH_{ice}$) and the enhanced relative humidity with respect to ice ($eRH_{ice}$), which together is the basis for the method used to determine whether a particular data point was measured “in-cloud” or in clear air. The parameter $RH_{ice}$ was chosen to distinguish between clouds and clear air because it is more sensitive to changes than water vapor (Krämer et al., 2009). $eRH_{ice}$ is calculated from the $H_2O_{enh}$ measurement while $RH_{ice}$ is calculated from $H_2O_{gas}$. The ratio of $eRH_{ice}$ to $RH_{ice}$, called a cloud limit, is the parameter that defines where a cloud exists and is instrument specific. When $eRH_{ice}/RH_{ice}$ is greater than 1, and $eRH_{ice}$ is greater
than 100%, saturated or supersaturated cirrus is being sampled. However, due to measurement uncertainties and data scatter, when the ratio is barely greater than 1, it is difficult to determine if the sample is in cloud or not (Krämer et al., 2009). Thus, a cloud limit value that is greater than, but not equal to, 1 must be employed. A second, higher cloud limit is also needed for cases where the eRH\textsubscript{ice} values are less than 100%, which could indicate subsaturated cirrus. For example, in Krämer et al. (2009), the cloud limits used are 1.03 and 1.3. When those specific values are applied to the IWC data from the CLH instrument, IWC measurements smaller than the detection limits of the instrument remain included in the dataset as measurements from inside a cloud. Since those measurements cannot be confidently determined to be in cloud, they should not be included in the dataset. In order to remove those values, higher cloud limits were put in place. In the case of the CLH data, the cloud limits were determined to be 1.3 and 3.

There are three possible scenarios for each data point, which are as follows. The first is a scenario indicating that the data point definitely represents a measurement taken inside a cirrus cloud. In this scenario, RH\textsubscript{ice} and eRH\textsubscript{ice} are both greater than 100% and eRH\textsubscript{ice}/RH\textsubscript{ice} is greater than 1.3. In the second scenario, eRH\textsubscript{ice} is greater than 100% but RH\textsubscript{ice} is not. As long as eRH\textsubscript{ice}/RH\textsubscript{ice} is greater than 1.3, the data point is most likely in cloud. The last scenario is for data points where neither eRH\textsubscript{ice} nor RH\textsubscript{ice} is greater than 100%. For this case, the larger cloud limit is used to ensure that if a data point is to be included and labeled “in-cloud”, it is definitely a cirrus measurement. Thus, in order for it to be included, eRH\textsubscript{ice}/RH\textsubscript{ice} must be greater than 3. Data that do not fall into one of these three categories are assumed to be measurements made in clear air and are not included in the climatology.

Another screening method that was applied to the data is the determination of geographic location for the datasets. It is understood that cirrus properties vary from region to region due to the differences in atmospheric conditions that exist between them (McFarquhar and Heymsfield, 1997). Similar to Schiller et al. (2008), the divisions between regions were made based on familiar latitudinal definitions. The tropics were defined to
be between the Tropics of Cancer and Capricorn at 23.5° N and 23.5° S, respectively; the midlatitudes are between 23.5° and 60° in either hemisphere; and the polar region was considered to be latitudes greater than 60° in either hemisphere. In general, these definitions work well. However, in the case of the START-08 dataset, there was cause for some uncertainty, because this campaign began in the late spring and ended in the early summer, a time during which atmospheric conditions change because of the increasing height of the tropopause with the heating of the atmosphere. Since the tropical region is partly defined by a high tropopause, a shift in the latitudes where the tropopause is highest makes using a rigid latitudinal definition of geographic regions questionable. To accommodate this, a different scheme was developed to use the polar and subtropical jet streams as boundaries between the arctic and the midlatitudes, and between the midlatitudes and tropics, respectively. Since the jet streams change locations depending on the season, they were ideal for this analysis. The geographic region for each dataset from the START-08 campaign was determined using upper-level weather maps, which revealed the positions of the jet streams for that day. The data were then labeled and separated accordingly. For data points falling in the midst of a jet stream, the assumption is made that those points display the characteristics of both geographic regions and they are thus displayed as part of both.

2.2 Comparison of Leo-Lidar with FISH-CLH

Lidar (Light Detection and Ranging) is an active remote sensing instrument measuring the optical properties of atmospheric particles. The backscatter and extinction coefficients as well as the depolarization of a particle ensemble (e.g. cirrus ice particles) can be determined from the backscattered light. The lidar used here is a commercial mobile backscatter lidar system (Leosphere), named Leo-Lidar, that works at a wavelength of 355 nm with a repetition rate of 20 Hz. The extinction coefficient is proportional to the ice particle number concentration and the effective radius and therefore depends on the same quantities as the IWC of the ice particle ensemble. Thus, IWC and extinction (σ) are approximately proportional to each other. Here, the IWC of cirrus clouds is
determined by using the relation provided by Heymsfield et al. (2005)

\[ \text{IWC (gm}^{-3}\text{)} = a \cdot \sigma (m^{-1})^b \]  

which is derived from extinction and IWC measurements from aircraft in situ sensors compared with data from the spaceborne instruments CloudSat radar and Calipso Lidar. The parameters \(a\) and \(b\) are given by \(89 + 0.6204 \cdot T (°C)\) gm\(^{-2}\) and \(1.02 - 0.00281 \cdot T (°C)\), respectively.

The extinction \(\sigma\) of a cirrus cloud and thus IWC is determined as follows. First, the Leo-Lidar measurements are averaged in time over the whole observed cirrus cloud with a vertical resolution of 60 m. This gives a cloud profile with a high signal to noise ratio to be used in further analysis. To determine the extinction profile, a fixed lidar ratio has to be assumed. This ratio is usually constant for one ice particle composition, shape, and particle size distribution within a cirrus layer. Under the assumption of a particle-free atmosphere directly below and above the cirrus cloud, the lidar ratio is estimated as described by Seifert et al. (2007). In the vicinity of clouds this assumption is valid for wavelengths \(\lambda \leq 532\) nm as reported in Ansmann (2002). A multiple scattering correction is also applied to the cirrus extinction profile. The particle size-dependent multiple scattering occurs when the forward scattered laser light is scattered again by an ice particle, which leads to an underestimation of the extinction coefficient (for more details see Rolf et al., 2012).

The Leo-Lidar measures IWC in the range 0.01–400 ppmv with an uncertainty of 12%. Thus, the upper detection limit is below those of CLH and FISH, but the lower detection limit is below the minimum IWC that can be detected with certainty by CLH and FISH (Schiller et al., 2008; see red dotted line in Fig. 2). For lower IWC from CLH and FISH it is uncertain if the signal stems from instrument uncertainties or from a cloud (see Krämer et al., 2009, their in-cloud definition is applied to the IWC measurements). Thus, the inclusion of Leo-Lidar cirrus observations provides the opportunity to compare the small IWC values from CLH and FISH with these measurements.
During the period of Spring 2011 to Spring 2012, 142 ground based cirrus observations were performed with the Leo-Lidar over mid-latitude Jülich, Western Germany (50°54' N, 6°24' E). In Fig. 2 the complete CLH and FISH IWC datasets are shown as a function of temperature in blue and grey, respectively. The Leo-Lidar measurements are plotted in orange. The upper IWC detection limit of the Leo-Lidar is clearly visible. The lower Leo-Lidar IWC values coincide nicely with those of the in situ dataset for temperatures > 230 K. Most notable is the agreement of the data below the red dotted line, the minimum IWC that can be detected with certainty by CLH and FISH. At temperatures below 230 K, CLH and FISH measured IWCs even smaller than those detectable by the Leo-Lidar, but that is with low certainty.

The Leo-Lidar IWC dataset is not merged with that of CLH and FISH for the remaining analyses presented here, since high IWC values are not included in the Leo-Lidar observations, thin cirrus are missed in the temperature range 200–230 K and no measurements exist below 200 K. However, from the comparison of the lidar and in situ IWC climatologies there is strong indication that the low IWC data measured with the in situ instruments are cirrus clouds and not artificial instrument effects. Moreover, it seems that the in situ instruments do not miss very thin cirrus clouds but cover the whole atmospheric cirrus IWC range.

### 3 Results and discussion

#### 3.1 Extended cirrus dataset

One major result of this study is the merging of two large datasets, which yields an even larger and more comprehensive picture of cirrus IWC than that published by Schiller et al. (2008) and one that is representative of nearly all latitudes. The latitudinal coverage of the data is illustrated by Fig. 3; combining the US and European datasets minimized the gaps in latitudinal sampling. For example, the MidCiX, CRYSTAL-FACE, and START-08 data filled a hole in the Schiller data between 0 and 40° N.
To further demonstrate the comprehensive nature of the dataset, Fig. 4 shows the range of altitudes and temperatures that are covered. Although the Arctic data are sparser than that in the other regions, in general, observations were obtained throughout the mid and upper troposphere and even slightly above the tropopause. Thus, the temperatures and altitudes at which cirrus occur are well represented.

The datasets further complement each other as a result of differences in instrument capabilities. For example, the lower limit of the FISH instrument allows for accurate measurements in very thin cloud not accessible by the CLH. On the other hand, the CLH has the ability to measure water vapor mixing ratios that are too large for the FISH to measure. In this regard, the two datasets are able to offer the full range of atmospheric IWC values, but only when used together.

As stated earlier, one of the most often used methods for describing IWC and consequently developing an IWC parameterization scheme is through an IWC-temperature relationship. As expected, IWC increases with temperature, a general relationship that is already well documented (see Fig. 5 of Schiller et al., 2008). Consistent behavior of IWC with temperature is seen in both the CLH and FISH datasets (see Fig. 5) lending confidence to their use in combination. Another feature that is obvious in Fig. 5 is the broad range of IWC values for a given temperature. Based on this observation, it is clear that the temperature-IWC relationship is complicated and requires the use of additional variables to explain it.

One variable that is known to play a role in the temperature-IWC relationship is geographic region. Thus, the dataset was divided by geographic region: arctic, midlatitude, or tropics. Figure 5 shows how the temperature-IWC relationship changes as a function of geographic region. By comparing the three plots, it is easily observed that for each region, the relationship has a unique shape. Median fit lines have been developed to more clearly define the relationships. The fit lines are a function of the form $10^{(ab^T + c)}$ as in Schiller et al. (2008). For this paper, the fit lines were developed using data that came only from flights where the purpose was to sample cirrus other than that associated with tropical deep convection. The flights focused on convection
include the SCOUT-O3 flights on 23, 29, and 30 November 2005, the START-08 flight on 16 June 2008, and the TC4 flights on 5, 6, 8, and 9 August 2007. Cirrus formed in association with tropical deep convection have been shown to have very high IWC values at very low temperatures (Schiller et al., 2008) so data from these flights have been removed from the development of any fit lines in this analysis. Using those data in the analysis has the potential to yield results that inaccurately depict the relationship between temperature and IWC. It should be noted, however, that all data, convective and nonconvective, is shown in Fig. 5, as well as in the previous figures.

It can clearly be seen that new fit lines developed for the merged dataset compare well to those developed from the FISH observations by Schiller et al. (2008). For the tropical data, the new median fit line is very close to the old one, with the obvious differences occurring at the lower and higher temperatures where smaller and larger IWC values, respectively, are now more evenly represented. In the case of the mid-latitudes, the difference between the new and old median fit lines is more significant. Once again, smaller IWC values are now influencing the median fit line more heavily in the lower temperature ranges, while the larger IWC values are doing the same at the higher temperature ranges. The new median fit line for the arctic data appears to have changed the most from the median fit line used by Schiller et al. For all temperatures the new median fit line is located at a smaller IWC, but the overall shape of the fit line has been preserved. This is most likely due to the differences in arctic datasets used for this analysis versus the data that were used by Schiller et al. since only a subset of those data is used in this analysis.

For all regions, the alterations in the fit lines could be a result of seasonal differences between the two original datasets. The observations from FISH resulted from experiments that took place in the boreal fall and winter months while the experiments that the CLH was a part of took place in the boreal spring and summer months. The possibility of a seasonal effect is not explored further in this paper.
3.2 New statistical analysis

In the introduction we noted work that has been done to parameterize IWC. Although the use of multiple variables helps to describe the range of IWC observed in nature, it does not fully capture the variability and is thus incomplete. Rather than attempting to incorporate multiple variables in this work, we describe the IWC-temperature relationship through probability density functions (PDFs). These represent the distribution of IWC values for specific temperature bins without considering the mechanism(s) responsible for the variation.

The first step in our analysis is to develop PDFs from the full, merged dataset separated into 5-K temperature bins (Fig. 6). The full dataset (grey and blue dots in Fig. 6) was utilized because there is not sufficient data to accurately describe the behavior in each temperature bin for each geographic region. Note that the lowest temperature bin spans 180–194 K and the highest temperature bin spans 235–249 K. These bins are wider due to the limited amount of data that was collected at those temperatures. However, it is likely that the clouds in these bins share common development mechanisms. The 180–194 K temperature range is known to have cirrus formation mechanisms that are different from those seen in warmer regions of the troposphere (Krämer et al., 2009; Jensen et al., 2010; Spichtinger and Krämer, 2012). The 235–249 K temperature range, on the other hand, probably contains mixed-phase clouds that would alter the distribution of condensed water content with respect to temperature. It should be noted that the data used to develop the PDFs do not include samples taken in tropical deep convection for the same reasons discussed previously. While tropical deep convection is important as a mechanism for cirrus formation, the temperature-IWC relationship that results is different enough from that of other cirrus formation mechanisms that we feel it should be analyzed separately.

As expected, the IWC distribution changes from bin to bin, with smaller IWC values dominating the distribution in the lower temperature bins and the largest IWC values dominating the distribution in the higher temperature bins. This is consistent with the
known IWC-temperature relationship. The shape of the distribution is similar in each temperature bin, and it is bimodal in nature, except for the 195 K–199 K bin, where the PDF shows several peaks. This difference is likely due to a smaller number of data points in the bin or potentially to the presence of multiple formation mechanisms exerting influence on the PDF. In general, the two peaks of the distribution shift monotonically in IWC value with temperature. As the temperature increases, the height of the first peak decreases, while the second peak shifts to larger values.

The PDF plots shown in Fig. 6 are ideal for capturing the IWC variability over small temperature ranges. Using the approximately Gaussian shape of the two modes in the PDFs, we have developed a fit function that describes IWC as a function of temperature, while also representing the variability of the IWC. It should be noted that this parameterization is meant to describe the observations found in the statistical analysis of our data, not as a parameterization for use in modeling. We have used a modified Gaussian fit developed in the data analysis software package OriginPro 8.1 (Origin-Lab, Northampton, MA) that was originally intended for use in chromatography. In the equation

\[ f(x) = y_0 + \frac{A}{t_0} \exp \left[ \frac{1}{2} \left( \frac{w}{t_0} \right)^2 - \frac{x - x_c}{t_0} \right] \int_{-\infty}^{z} \frac{1}{\sqrt{2\pi}} \exp \left( -\frac{y^2}{2} \right) \, dy \]  

where \( z \) is given as

\[ z = \frac{x - x_c}{w} - \frac{w}{t_0} \]  

\( x \) and \( f(x) \) are the IWC (ppmv) and IWC frequency (%), respectively. The remaining coefficients are constants fit by the OriginPro program and do not hold any physical meaning in terms of the contributing variables associated with IWC. They are purely used as descriptors of the curves fitting the PDFs. To accommodate the fact that the curves are bimodal, each PDF was treated as two Gaussian curves that overlap one

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another between peaks. The division between where one curve stopped and the other started was made on a case-by-case basis and was determined based on what appeared to provide the best fit. Figure 6 also illustrates the curves that were fit to each PDF. The coefficients for each curve and temperature bin can be found in the Supplement.

An additional depiction of the PDF parameterization is provided in Fig. 7 to show its representative nature. The two most frequently observed IWC values are plotted for each temperature bin, along with median fit functions to the entire dataset as determined here and in Schiller et al. (2008). It can easily be seen that there is a defined structure to the relationship between those IWC values and temperature and that it is similar in shape to the median fit. Also, the median fit lines fall directly between the two IWC values. In Schiller et al. (2008), a core region was defined where the frequency of occurrence was greater than 5%. The minimum and maximum values of that core region are illustrated in Fig. 7 by the dotted and dashed red lines, respectively. The peak IWC values for each temperature fall well within that core region, which lends confidence to the idea that these values are representative of a large portion of the data.

In order to interpret the meaning of these PDFs, we look at IWC PDFs where the data have been divided into three temperature ranges, as seen in Fig. 8a. The ranges used here directly correspond to the three temperature ranges used in Fig. 7a of Salzmann et al. (2010), a PDF graph produced from the observations of ice crystal number shown in Krämer et al. (2009) in (reproduced here in Fig. 8b). Unlike the previous PDFs, these were constructed with all data including tropical deep convective data (but note that the PDFs excluding convective data, not shown here, are nearly identical). In comparing the two plots, it is clear that for each of the three temperature ranges (blue: < 205 K, red: 205–227 K, yellow: > 227 K), there is a similarity in the overall shape of the distribution for IWC and ice number, suggesting a connection. For example, and most noticeably, the narrow peak in ice number of approximately 0.005 cm$^{-3}$ in the very low temperature range (blue curve), which is representative of conditions found at the tropical
tropopause layer (TTL), coincides with a peak in IWC at approximately 0.1 ppmv, while a second broader peak appears at higher ice crystal numbers and IWCs. It is remarkable that the bimodal nature of the cirrus PDFs is found by two completely independent measurements. As a possible explanation of this structure of the ice crystal number frequencies, Spichtinger and Krämer (2012) propose, from extensive model simulations in comparison to the TTL cirrus observations of Krämer et al. (2009), that the first peak around 0.005 cm$^{-3}$ is caused by heterogeneous ice nucleation, while the higher ice crystal numbers stem from homogeneously formed cirrus clouds.

The remaining two temperature ranges are more difficult to interpret. It is clear, however, that there are two modes for each temperature range, both in IWC and ice particle number, thus providing us with good reason to infer that they are linked to one another.

A graph of the PDF of mass mean radius seen in Fig. 7b of Salzmann et al. (2010) can also be used for comparison and interpretation purposes. This figure has been reproduced here in Fig. 8c. Previous work, such as that of Liou et al. (2008), has shown that there is a good correlation between IWC and mean effective crystal size. While that relationship is also seen in this comparison, it is also apparent that this correlation is not as strong as the one between IWC and ice crystal number. The distribution of mass mean radius changes little with temperature whereas the ice crystal number is much more variable over the three temperature ranges, similar to the distribution of IWC. Hence, it seems that the relationship between IWC and temperature is mainly determined by ice particle number and not by size.

We summarize our findings as follows: (i) the IWC is mainly determined by the ice crystal number, (ii) the IWC PDFs are bimodal over the complete cirrus temperature range, (iii) for cold TTL cirrus it is highly likely that the mode with only a few ice crystals (low IWC) corresponds to heterogeneous ice formation while the mode with a higher number of ice crystals (higher IWC) can be attributed to homogeneously formed cirrus clouds. Extending the physical explanation of the two ice number/IWC modes from TTL cirrus to higher temperatures would lead to the hypothesis that both heterogeneously and homogeneously formed cirrus clouds are visible in the IWC PDFs as two modes of
lower and higher IWC. This might be a hint that heterogeneous freezing plays a larger role in cirrus modification than believed hitherto (Kärcher et al., 2009).

4 Conclusions

The importance of cirrus in the climate system is well documented, but the details are not yet well understood. The IWC of these clouds is also known to have a crucial role in that system through its effect on terrestrial and solar radiation, but it is difficult to parameterize owing to the large variability in IWC values possible for a given set of atmospheric conditions. Here, we have presented the extension of a cirrus IWC climatology originally developed by Schiller et al. This extension provides a highly comprehensive dataset in terms of covering the temperature, altitude, and latitude ranges at which cirrus are observed and the IWC values that are known to be present in those clouds. It was also shown here through a comparison with lidar data that the reported smallest IWC values are valid cirrus measurements.

Previous work to create IWC parameterizations has been successful in exploiting the general relationship between those IWC and temperature, but has been unable to capture the variability of IWC at a single temperature without the use of additional variables. Through the use of PDFs, we have been able to demonstrate and create a parameterization of IWC in 5-K temperature bins that relies solely on the IWC-temperature relationship, but is also able to describe the large range of IWC in a small temperature range.

The peak IWC values of the PDFs were shown to be consistent with the IWC-temperature relationship seen with the full, extended climatology and were easily bounded within a core region of the most frequent IWC values. It was also shown that the use of PDFs for describing the microphysical properties of ice clouds is both appropriate and useful. The comparison between IWC, ice crystal number, and mass mean radius PDFs indicate that the relationship between IWC and temperature is mainly determined by particle number and not by particle size. Further, we found hints that
the general bimodal nature of the IWC PDFs might be caused by the two pathways for ice formation, namely heterogeneous and homogeneous freezing. We will continue to utilize the expanded climatology to make further inquiries into the mechanisms responsible for determining IWC in order to enhance our understanding and improve the parameterizations used in global climate models.

Supplementary material related to this article is available online at: http://www.atmos-chem-phys-discuss.net/12/29443/2012/acpd-12-29443-2012-supplement.zip.

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References


Table 1. Description of the flight campaigns used to develop the IWC climatology\(^a\).

<table>
<thead>
<tr>
<th>Instrument</th>
<th>Campaign</th>
<th>Date</th>
<th># of flights</th>
<th>Time in cloud (h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CLH</td>
<td>CRYSTAL-FACE</td>
<td>Jul 2002</td>
<td>11</td>
<td>9.74</td>
</tr>
<tr>
<td></td>
<td>MidCiX</td>
<td>Apr–May 2004</td>
<td>9</td>
<td>11.31</td>
</tr>
<tr>
<td></td>
<td>START-08</td>
<td>Apr–Jun 2008</td>
<td>13</td>
<td>1.32</td>
</tr>
<tr>
<td></td>
<td>TC4</td>
<td>Aug 2008</td>
<td>5</td>
<td>6.01</td>
</tr>
<tr>
<td>FISH</td>
<td>APE-THESEO</td>
<td>Feb–Mar 1999</td>
<td>1</td>
<td>0.28</td>
</tr>
<tr>
<td></td>
<td>Cirrus 2003</td>
<td>Dec 2003</td>
<td>2</td>
<td>1.20</td>
</tr>
<tr>
<td></td>
<td>Cirrus 2004</td>
<td>Nov 2004</td>
<td>2</td>
<td>1.58</td>
</tr>
<tr>
<td></td>
<td>Cirrus 2006</td>
<td>Nov 2006</td>
<td>4</td>
<td>1.63</td>
</tr>
<tr>
<td></td>
<td>Envisat 2002</td>
<td>Oct 2002</td>
<td>1</td>
<td>0.04</td>
</tr>
<tr>
<td></td>
<td>Envisat 2003</td>
<td>Mar 2003</td>
<td>2</td>
<td>0.05</td>
</tr>
<tr>
<td></td>
<td>Euplex 2003</td>
<td>Jan–Feb 2003</td>
<td>2</td>
<td>0.09</td>
</tr>
<tr>
<td></td>
<td>Troccinox 2005</td>
<td>Jan–Feb 2005</td>
<td>4</td>
<td>0.95</td>
</tr>
<tr>
<td><strong>Total</strong></td>
<td></td>
<td></td>
<td>67</td>
<td>38.38</td>
</tr>
</tbody>
</table>

\(^a\) CLH: Closed-path Laser Hygrometer. FISH: Fast In Situ Stratospheric Hygrometer; for details of FISH and the corresponding field campaigns see Schiller et al. (2008).
Fig. 1. This figure illustrates the H$_2$O data quality check using data obtained by the CLH during the CRYSTAL-FACE campaign on 9 July 2002. The black line is H$_2$O$_{\text{sat}}$, the red line is H$_2$O$_{\text{gas}}$, the turquoise line is H$_2$O$_{\text{enh}}$, and the dark blue line is H$_2$O$_{\text{enh,adj}}$. 
Fig. 2. IWC as a function of temperature for CLH (blue), FISH (grey) and Leo-Lidar (orange). The red dotted lines represent the IWC maximum and the minimum that can be detected with certainty by CLH and FISH (Schiller et al., 2008; Krämer et al., 2009), respectively. The back solid line is the median of the merged CLH and FISH dataset.
Fig. 3. The latitudinal coverage achieved by the combined dataset. The color scheme in the legend is used consistently throughout the rest of the analysis.
Fig. 4. (a) Temperature and altitude coverage of all data taken during all campaigns. (b) Same as (a) but for in-cloud data only. The color scheme is the same as in Fig. 3.
Fig. 5. IWC as a function of temperature and geographic region. Color scheme as in Fig. 3. Data points represented as small dots are a combination of geographic locations and thus included in two plots (see text). The black line represents the median fit, while the dashed black line is the median fit from Schiller et al. (2008). It should be noted that the median fit lines from the Schiller climatology include convective data.
Fig. 6. PDFs of IWC in various temperature ranges. The black lines are the PDF, the red lines are the curve fits.
Fig. 7. Peaks of the bimodal PDFs from Fig. 6. “x” is the value of the first (lower IWC) peak, a square is the value of the second. The temperature at which they are plotted is the weighted mean temperature for each temperature bin. The black line represents the median fit line for the merged climatology, not including tropical deep convective data. The black dashed line is the median fit from Schiller et al. (2008) and includes convective data. The red dashed/dotted lines depict the maximum/minimum envelope of the most frequent (> 5 %) IWC as seen in Fig. 6 of Schiller et al. (2008).
Fig. 8. (a) Top: PDF of IWC; (b) bottom-left: PDF of crystal number; (c) bottom-right: PDF of mass mean radius. (b) and (c) are reproduced from Fig. 7a and b of Salzmann et al. (2010), respectively.