Carbon dioxide and climate impulse response functions for the computation of greenhouse gas metrics: a multi-model analysis

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CO₂ and climate impulse response functions for metric computation

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Abstract

The responses of carbon dioxide (CO₂) and other climate variables to an emission pulse of CO₂ into the atmosphere are often used to compute the Global Warming Potential (GWP) and Global Temperature change Potential (GTP), to characterize the response time scales of Earth System models, and to build reduced-form models. In this carbon cycle-climate model intercomparison project, which spans the full model hierarchy, we quantify responses to emission pulses of different magnitudes injected under different conditions. The CO₂ response shows the known rapid decline in the first few decades followed by a millennium-scale tail. For a 100 Gt C emission pulse, 24 ± 10 % is still found in the atmosphere after 1000 yr; the ocean has absorbed 60 ± 18 % and the land the remainder. The response in global mean surface air temperature is an increase by 0.19 ± 0.10 °C within the first twenty years; thereafter and until year 1000, temperature decreases only slightly, whereas ocean heat content and sea level continue to rise. Our best estimate for the Absolute Global Warming Potential, given by the time-integrated response in CO₂ at year 100 times its radiative efficiency, is $92.7 \times 10^{-15}$ yr W m⁻² per kg CO₂. This value very likely (5 to 95 % confidence) lies within the range of $(70$ to 115$) \times 10^{-15}$ yr W m⁻² per kg CO₂. Estimates for time-integrated response in CO₂ published in the IPCC First, Second, and Fourth Assessment and our multi-model best estimate all agree within 15 %. The integrated CO₂ response is lower for pre-industrial conditions, compared to present day, and lower for smaller pulses than larger pulses. In contrast, the response in temperature, sea level and ocean heat content is less sensitive to these choices. Although, choices in pulse size, background concentration, and model lead to uncertainties, the most important and subjective choice to determine AGWP of CO₂ and GWP is the time horizon.
1 Introduction

Emissions of different greenhouse gases (GHGs) and other agents that force the climate to change are often compared by simplified metrics in economic frameworks, emission trading and mitigation schemes, and climate policy assessments. The Global Warming Potential (GWP) introduced by the Intergovernmental Panel on Climate Change (IPCC) in 1990 (Shine et al., 1990), is the most widely used emission metric. GWPs are applied for emission reporting under the United Nations Framework Convention on Climate Change (UNFCCC, 2002) and in the emission basket approach of the legally-binding Kyoto Protocol (UNFCCC, 1998) to compare emissions of carbon dioxide (CO₂), methane (CH₄), nitrous oxide (N₂O), sulphur hexafluoride (SF₆), hydrofluorocarbons (HCFs) and perfluorocarbons (PFCs) and to compute the so called “CO₂-equivalent” emissions. The GWP compares the radiative forcing (Forster et al., 2007) integrated over a time period caused by the emission of 1 kg of an agent relative to the integrated forcing caused by the emissions of 1 kg CO₂. As CO₂ is used as a reference gas in the GWP definition, any changes in the computation of the radiative influence of CO₂ affect the GWP of any other agent.

The purpose of this study is to compute the response in atmospheric CO₂, in ocean and land carbon, global mean surface air temperature, ocean heat uptake and sea level change to a pulse-like (i.e., instantaneous) emission of CO₂ into the atmosphere. Best estimates for the mean and the 5 to 95% confidence range are provided for the Absolute Global Warming Potential (AGWP) and the Absolute Global Temperature change Potential (AGTP) introduced by Shine et al. (2005). We analyse the responses of fifteen carbon cycle-climate models, covering the full model hierarchy, and including two large ensembles of simulations by two of the models constrained with observations as well as an ensemble of a box model substituting a suite of more complex models. This allows us to address model-related uncertainties by investigating within-model and between-model differences. Uncertainties related to the size of the emission pulse, the atmospheric and climatic background conditions, and the carbon cycle-climate feedback
are assessed in sensitivity simulations. Results are also compared to CO₂ response functions as published in the IPCC First (FAR) (Shine et al., 1990), Second (SAR) (Schimel et al., 1996), and Fourth Assessment Report (AR4) (Forster et al., 2007).

A reevaluation of the CO₂ response appears timely as (i) past GWP calculations applied results from a single model and (ii) the atmospheric and climatic conditions influencing the CO₂ response continue to change. The GWP adopted for the first commitment period of the Kyoto protocol (2008–2012) (UNFCCC, 1997, 1998) and used for reporting under the UNFCCC (UNFCCC, 2002) are given by the SAR (Schimel et al., 1996) and based on the CO₂ response of the Bern model (Bern-SAR), an early generation reduced-form carbon cycle model (Joos et al., 1996). Its behaviour was compared to other carbon cycle models in Enting et al. (1994) and it was found to be a middle of the range model. The GWP provided in the AR4 (Forster et al., 2007) relies on the CO₂ response from the Bern2.5CC (here Bern2.5D-LPJ) Earth System Model of Intermediate Complexity (EMIC) (Plattner et al., 2008). More recently, the Conference of the Parties serving as the meeting of the Parties to the Kyoto Protocol decided (UNFCCC, 2011a,b) that the GWP from the AR4 should be used for the second commitment period of the Kyoto Protocol and the conference also noted in its decision that metrics are still being assessed by IPCC in the context of its Fifth Assessment Report (AR5).

A much broader set of models covering the whole model hierarchy from reduced-form models, to EMICs, to comprehensive Earth System Models (ESMs) are now available.

The redistribution of additional CO₂ emissions among the major carbon reservoirs in the Earth System depends on previous emissions and on climate. In addition, radiative forcing of CO₂ depends logarithmically on its own concentration. The response functions are calculated by modelling the response to a pulse emission added to a given concentration and climate state, but these background conditions have changed and will continue to change. For example, the concentration of atmospheric CO₂ continued to increase from 354 ppm in 1990, to 378 ppm at the time of the preparation of the IPCC AR4 report to 389 ppm in 2010 (Conway and Tans, 2012).
Additional uncertainties are of a fundamental nature as any metric to compare greenhouse gas emissions represents a crude simplification. Different forcing agents are distinct and have distinct impacts on climate and the Earth system. Differences include different atmospheric perturbation lifetimes ranging from weeks to many millennia, different regional and vertical distributions within the atmosphere and thus different influences on the energy fluxes within the atmosphere and to the Earth’s surface, different indirect effects such as confounding impacts on the lifetimes of other GHGs.

A complication is the complex and regionally and temporally distinct relationship between anthropogenic emissions, atmospheric abundances, radiative forcing, climate change and impacts and damages on socio-economic and natural systems. Other metrics have been proposed in addition to GWP such as global temperature change potential (GTP) (Shine et al., 2005; Fuglestvedt et al., 2010), the integrated temperature change potential (iGTP) (Peters et al., 2011; Azar and Johansson, 2012; Gillett and Matthews, 2010), the TEMPerature proxy index (TEMP) (Tanaka et al., 2009a), global damage potentials (GDP) (Kandlikar, 1995), global cost potentials (GCP) (Tol et al., 2012; Manne and Richels, 2001) and the Cost-Effective Temperature Potential (CETP) (Johansson, 2012). These metrics compare, for equal mass emissions of two GHGs, the global average surface air temperature change at a given point in time (GTP), the relative damages (GDP), or the relative marginal abatement costs for two gases when a given climate change target is achieved at least cost (GCP). TEMP is defined so that it provides a best fit to the temperature projection of a given period and CETP is based on an approximation of the GCP. Uncertainties generally increase along the cause-effect chain from emissions to impacts and there is a trade-off for the selection of metrics between completeness and complexity versus simplicity and transparency and the necessity of subjective judgments (Fuglestvedt et al., 2003; Plattner et al., 2009; Tanaka et al., 2010).

While the GWP is a proxy for climate impacts, non-climatic effects are not captured by the GWP or similar metrics. Air pollutants, such as ozone, aerosols, nitrogen oxides, carbon monoxide, or volatile organic compounds, influence human health and
ecosystems directly. Anthropogenic CO$_2$ emissions cause not only global warming, but also ocean acidification by the uptake of excess CO$_2$ (Orr et al., 2005; Joos et al., 2011; Friedrich et al., 2012) – a threat to coral reefs, marine ecosystems, and related economic sectors (Gattuso et al., 2011).

The different perturbation lifetimes imply that near-term effects of short-lived agents must be compared with the persistent effects of long-lived agents if a metric is to be defined. Attempts involve the restriction to a distinct time horizon for the numerical evaluation of the metric (traditionally 20, 100 or 500 yr for GWP) or the application of discounting rates, typically giving little weight to effects in the more distant future. In summary, any metric used to compare emissions of GHGs and other agents involves subjective choices and value judgments and represents a considerable simplification (e.g. Tanaka et al., 2010; Fuglestvedt et al., 2003; Boucher, 2012).

2 Emission metrics and impulse response functions

2.1 Global Warming Potential

The Global Warming Potential is based on the time-integrated radiative forcing due to a pulse emission of a unit mass of gas at nominal time, $t = 0$. It can be given as an Absolute Global Warming Potential for gas $x$ (AGWP$_x$) or as a dimensionless value by dividing the AGWP$_x$ by the AGWP of a reference gas, usually CO$_2$. The GWP is thus defined as:

$$\text{GWP}_x(\text{TH}) := \frac{\text{AGWP}_x(\text{TH})}{\text{AGWP}_{\text{CO}_2}(\text{TH})}$$

and the AGWP by:

$$\text{AGWP}_x(\text{TH}) = \int_0^{\text{TH}} \text{RF}_x(t) dt = \int_0^{\text{TH}} A_x \cdot \text{IRF}_x(t) dt$$
where $RF_x(t)$ is the radiative forcing at time $t$ caused by the emission pulse released at time $t = 0$. TH is the time horizon of choice over which the radiative forcing is integrated. For the GWP used by the UNFCCC and in the Kyoto Protocol, a time horizon TH of 100 yr is applied, though this choice lacks a scientific basis (Shine et al., 1990).

The radiative forcing $RF_x$ of gas $x$ can be written as the product of its radiative efficiency, $A_x$, and the perturbation in its abundance, $IRF_x$. $A_x$ is defined as the radiative forcing per kg increase in atmospheric abundance of gas $x$. $IRF_x(t)$ is the impulse response function (IRF) or Green’s function. $IRF_x$ represents the time-dependent abundance of gas $x$ caused by the additional emission of one kg of gas $x$ at time 0. In other words, the $IRF_x(t)$ is the fraction of the additional emission pulse remaining in the atmosphere at time $t$. For sufficiently small emissions and approximately constant background conditions the radiative efficiency, $A_x$, can be approximated as time-invariant.

It is convenient to describe the $IRF_x$ by exponential functions. Many agents, although not CO$_2$, are removed from the atmosphere with an approximately constant decay rate, $1/\tau$, and thus their removal can be represented by exponential decay. In this case, the IRF is:

$$IRF_x(t) = \exp\left(-\frac{t}{\tau_x}\right), \quad (3)$$

where $\tau_x$ is the mean perturbation lifetime of agent $x$. Then, the integrated radiative forcing up to TH is given by:

$$AGWP_x(TH) = A_x \cdot \tau_x \cdot \left(1 - \exp\left(-\frac{TH}{\tau_x}\right)\right) \quad (4)$$

AGWP increases with increasing time horizon TH to finally approach a constant value for TH several times larger than $\tau_x$. The AGWP becomes the product of the mean lifetime and the radiative efficiency, i.e., $AGWP_x = A_x \tau_x$. This implies that a change in the integration horizon from, for example, 100 yr to 1000 yr has no impact on the AGWP of gases with up to decadal perturbation lifetimes such as methane, but AGWP increases.
for long-lived gases such as CO$_2$. Consequently, the GWP of gases with a short-life time decreases with increasing time horizon and the variation in GWP values with time horizon only reflects properties of the reference gas CO$_2$. For instance, the GWP values for CH$_4$ (which has an adjustment time of approximately 12 yr) decrease with increasing time horizon, since GWP is defined with the integrated RF of CO$_2$ in the denominator. As TH increases past the adjustment time of CH$_4$, the development in GWP$_{CH_4}$ with time horizon is purely controlled by the development in AGWP$_{CO_2}$. For long-lived gases (e.g. SF$_6$) the development in GWP is controlled by both the increasing integrals of SF$_6$ and CO$_2$ radiative forcing. In conclusion, the GWP depends sensitively on the (subjective) choice of the time horizon (see e.g. Shine, 2009).

CO$_2$ is, unlike most other agents, not destroyed by chemical reactions in the atmosphere or deposited on the earth surface, but redistributed within the major carbon reservoirs atmosphere, ocean, land biosphere involving multiple timescales for exchange among and for overturning within these reservoirs. A substantial fraction of the emissions remains airborne for millennia. This fraction is only removed by ocean-sediment interactions and interactions with the weathering and burial cycle of carbon involving timescales from many millennia to hundred thousand years (Archer et al., 2009).

The IRF for CO$_2$ is commonly approximated by a sum of exponentials:

$$\text{IRF}_{CO_2}(t) = \sum_{i=0}^{n} a_i \cdot \exp\left(\frac{-t}{\tau_i}\right)$$

(5)

The unitless coefficients $a_i$ represent a fraction that is associated with a certain nominal lifetime $\tau_i$ and their sum equals 1. In turn the AGWP for CO$_2$ is:

$$\text{AGWP}_{CO_2}(t) = A_{CO_2} \sum_{i=0}^{n} a_i \cdot \tau_i \left(1 - \exp\left(\frac{-TH}{\tau_i}\right)\right)$$

(6)

Generally the coefficients $a_i$ and $\tau_i$ have no direct process-based meaning, but are fitting parameters chosen to represent a given model-based IRF$_{CO_2}$. The IRF of a model
is normally computed by calculating the response to a pulse-like perturbation. In our case, the IRF for atmospheric CO$_2$ is computed within the suite of carbon cycle-climate models by monitoring the simulated decrease of an initial atmospheric CO$_2$ perturbation due to a pulse-like CO$_2$ release into the model atmosphere. Similarly, IRFs for surface temperature, ocean heat uptake, sea level rise or any other variable of interest are obtained by monitoring its simulated evolution after the initial perturbation.

The IRFs or Green’s functions computed in this study are also useful to characterize the carbon cycle-climate models. The theoretical justification is that IRFs represent a complete characterization of the response of a linear system to an external perturbation. For CO$_2$, the value of the IRF at any particular time is the fraction of the initially added carbon which is still found in the atmosphere. In a linear approximation, the change in atmospheric CO$_2$ inventory at time $t$ can be represented as the sum of earlier anthropogenic emissions, $e$, at time $t'$ multiplied by the fraction still remaining airborne after time $t - t'$, IRF$_{CO_2}(t - t')$:

$$CO_2(t) = \int_{t_0}^{t} e(t') \cdot IRF_{CO_2}(t - t') dt' + CO_2(t_0),$$

where $CO_2(t)$ is the atmospheric CO$_2$ inventory at a time when the system was in (approximate) equilibrium. The IRF is thus a first-order approximation how excess anthropogenic carbon is removed from the atmosphere by a particular model.

Non-linearities in the carbon cycle-climate system, however, limit the accuracy of the above equation substantially. The IRF$_{CO_2}$ is not an invariant function, but depends on the magnitude of the carbon emissions (Maier-Reimer and Hasselmann, 1987). Non-linearities arise from the non-linearity of the carbonate chemistry in the ocean, from changes in ocean circulation with global warming that affect the surface-to-deep transport of excess anthropogenic CO$_2$ as well as from other effects such as non-linear dependencies of terrestrial productivity or soil overturning rates on climate and atmospheric CO$_2$. It has been shown that the atmospheric response, as simulated with
a comprehensive model, is better approximated using oceanic and terrestrial impulse response functions that include major non-linearities of the carbon cycle (Joos et al., 1996; Meyer et al., 1999). In conclusion, the IRF and thus also the AGWP for CO₂ depends on the details of the experimental setup as well as on the characteristics of the carbon cycle-climate model used for its determination.

2.2 Global Temperature change Potential

The GWP has been critiqued from several angles (e.g. Shine, 2009; O’Neill, 2000), but an important critique is that the AGWP does not directly translate into a well-known climate response. The Global Temperature change Potential (GTP) was developed as an alternative (Shine et al., 2005). The Absolute Global Temperature change Potential (AGTP) is the change in global mean surface temperature, \( \Delta T \) at time \( TH \) in response to a pulse emission, \( e \) of one unit of agent \( x \) at time \( t = 0 \). It corresponds to \( IRF_{T,x} \), the impulse response of temperature, \( T \), to a unit emission of agent \( x \):

\[
AGTP_x(TH) = \frac{\Delta T(TH)}{e_x(t = 0)} = IRF_{T,x}(t = TH)
\]  

The Global Temperature change Potential, \( GTP_x \) is the AGTP of \( x \) compared to that of CO₂:

\[
GTP_x(TH) = \frac{AGTP_x(TH)}{AGTP_{CO_2}(TH)}
\]  

The AGTP is often written as convolution integral of the radiative forcing:

\[
AGTP_x(TH) = \int_0^{TH} RF_x(t) \cdot R(TH - t) dt
\]  

where \( R(t) \) is the response in \( T \) to a unit change in radiative forcing and not to be confused with \( IRF_{T,x} \). \( R \) is influenced by the uncertain properties of the global climate
While the AGWP is an integrated metric, the AGTP is an instantaneous (end-point) metric. In most previous work (Fuglestevedt et al., 2010), the AGTP has been estimated from the convolution of the $RF_x$ with $R_T$ (Eq. 10), where the $RF_x$ and $R_T$ often come from different models that are likely not consistent in terms of ocean heat and carbon uptake (for example, the $RF_{CO_2}$ is from the Bern-SAR model and the $R_T$ is from HadCM3). It is also possible to estimate $AGTP_{CO_2}$ and $IRF_{T,CO_2}$ directly from a climate-carbon cycle model in response to a pulse emission. This is done in this study with the suite of carbon-cycle climate models. Apart from the box models, these models feature a consistent treatment of heat and carbon transport. Following similar logic, it is possible to derive similar expressions for the time-integrated GTP, ocean heat content and sea level rise. Recent research has shown that the GWP and the time-integrated GTP are numerically similar over a range of time horizons, other than for very short lived species like black carbon (Peters et al., 2011; Azar and Johansson, 2012).

3 Model description and experimental setup

An open call was directed to the carbon cycle-climate modelling community to participate in this $IRF_{CO_2}$ intercomparison project (Joos et al., 2012). A common protocol defines model setup and requested simulations (Table 1) and output and is given as supporting online information (SI). The procedure corresponds to that for the calculation of the $IRF_{CO_2}$ for the IPCC SAR (Enting et al., 1994) and the IPCC AR4. In addition, output was also requested for the change in global mean surface air temperature as well as ocean heat content, and steric sea level rise. This allows us to derive the impulse response functions for temperature, ocean heat content and steric sea level rise to an emission pulse of $CO_2$ and correspondingly the AGWP and AGTP for $CO_2$ and similar metrics for ocean heat content and steric sea level rise.
Results from fifteen models were submitted (Tables 2 and 3) and these are briefly described and referenced in the Appendix A. The models include three comprehensive Earth System Models (HadGEM2-ES, MPI-ESM, NCAR CSM1.4), seven Earth System Models of Intermediate Complexity (EMICs), and four box-type models (ACC2, Bern-SAR, MAGICC6, TOTEM). Many of these EMICs also participated in three model intercomparison projected targeted to study the evolution of the climate and the carbon cycle over the historical period (Eby et al., 2012) and under different future scenarios (Zickfeld et al., 2012) and to explore the evolution of the North Atlantic Meridional Overturning Circulation scenarios (Weaver et al., 2012). The EMICs are of varying complexity and include either a 3-dimensional dynamic ocean (Bern3D-LPJ, GENIE, LOVECLIM, MESMO, Uvic-2.9), a 2-dimensional dynamic ocean (Bern2.5D-LPJ, Climber2.4-LPJmL), or a box-type ocean (DCESS). Nine models include a Dynamic Global Vegetation Model (HadGEM2-ES, MPI-ESM, Bern2.5-LPJ, Bern3D-LPJ, Climber2.4-LPJmL, GENIE, LOVECLIM, MESMO, UVic-2.9), one model a spatially-resolved terrestrial carbon cycle with prescribed vegetation distribution (NCAR CSM1.4) and five models (ACC2, Bern-SAR, DCESS, MAGICC6, TOTEM) a box-type biosphere with a simple logarithmic dependency of NPP on CO$_2$. Land use and land use changes and their impacts on the carbon cycle and biophysical forcing are explicitly included as internal part of the model in five models (HadGEM2-ES, MPI-ESM, Bern3D-LPJ, GENIE, UVic-2.9). The equilibrium climate sensitivity of the models ranges between 1.5 to 5.7$^\circ$C for a nominal doubling of atmospheric CO$_2$. Eight models include an ocean-sediment and weathering/burial module to address long-term (multi-millennial) carbon cycle changes. However, here we restrict the time horizon to 1000 yr and do not provide results for the multi-millennial CO$_2$ evolution. The models used to compute IRF$_{CO_2}$ for the SAR (Bern-SAR) and for the AR4 (Bern2.5-LPJ) as used by the UNFCCC are included for traceability of results.

The “standard” setup corresponds to a pulse input of 100 GtC added to a constant background concentration of 389 ppmv. The emission pulse is equivalent to a mean atmospheric change of 47.10 ppmv when using a unit conversion factor of...
2.123 Gt C ppmv\(^{-1}\) (Enting et al., 1994). Three simulations are performed to determine the “standard” IRF from individual models. An example figure showing results from these three simulations in terms of atmospheric CO\(_2\) can be found in the protocol added in the SI.

In run 1, a model is forced with historical concentration up to a reference year (here \(t_{\text{ref}} = 2010\)) and then concentration is kept fixed thereafter at a constant value (here \(\text{CO}_2,\text{ref} = 389\) ppm). A data file with the reconstructed distribution of atmospheric CO\(_2\) over the period 850 to 2010 AD was distributed to all groups. The model emissions, that are compatible with the prescribed CO\(_2\) evolution, are diagnosed from the simulated change in total carbon inventory (prescribed atmospheric change plus modelled ocean and terrestrial carbon uptake and any imbalance in the weathering/burial cycle).

In run 2, a model is forced with the diagnosed emissions obtained from run 1 with the same model. Run 2 serves for control purposes only and was not provided for the MPI-ESM and NCAR CSM1.4 model as CPU time was lacking. In run 3, the same forcing and setup as in run 2 is applied, but in addition 100 Gt C are added instantaneously to the atmosphere five years after the reference year (here in 2015.0). The normalised IRF is then approximately:

\[
\text{IRF}_{\text{CO}_2}(t = t_{\text{model}} - 2015.0) = \frac{\text{CO}_2(t_{\text{model}}) - \text{CO}_2,\text{ref}}{100\text{ Gt C}/(2.123\text{ Gt C ppm}^{-1})} \quad \text{for } t_{\text{model}} \geq 2015
\]

The general advice in the protocol was to include non-CO\(_2\) forcing and land use area changes to the extent possible. Non-CO\(_2\) forcing as well as land use area are kept constant at 2010 level after 2010. While the total radiative forcing is kept constant in run 1 and 2 after 2010, the climate is evolving freely. The response to a 100 Gt C pulse obtained from run 1 to 3 for a present day (PD) background is also termed “PD100” and represents our standard case.

In addition to these standard experiments, groups were also asked to provide results for emissions pulses of 100 Gt C (run 5, case PI100) and 5000 Gt C (run 6, PI5000) added to a preindustrial (PI) background. A preindustrial control simulation
with constant boundary conditions and freely evolving CO$_2$ was also requested (run 4). 5000 GtC is of the same order as available conventional (coal, oil, gas) fossil carbon resources and has been used in past pulse experiments (e.g. Archer et al., 2009; Eby et al., 2009). This experiment is thus indicative of the long-term consequences for burning all conventional fossil resources. The influence of different background CO$_2$ concentrations is quantified by comparing the standard run with the 100 GtC pulse added to the preindustrial CO$_2$ concentration.

Sensitivity simulations with one model (Bern3D-LPJ, see figures in protocol in SI) for PD100 suggest that the simulated response is insensitive to the inclusion of non-CO$_2$ forcing and whether the emissions pulse is released at the beginning of the year or distributed over one year. On the other hand, the simulated IRF$_{CO_2}$ is about 0.02 higher if anthropogenic land use is explicitly included compared to a simulation with natural vegetation only as less carbon is taken up on the converted land.

Three of the participating modeling groups delivered results from an ensemble of simulations. The GENIE group reported results from an ensemble with 69 members where model parameters where varied within uncertainties. The 69-member ensemble was derived from a set of around 1500 simulations combined with a statistical modelling and filtering procedure applying eight preindustrial climatic constraints (Holden et al., 2012). The 69 member ensemble was reduced to 20 members by requiring a plausible present-day CO$_2$ concentration in an emission–forced simulation over the industrial period and beyond. Here, median and 5 % to 95 % intervals from these 20 different model setups are reported.

The 69-member ensemble has an ensemble-averaged CO$_2$ concentration of $404 \pm 50$ ppm (mean $\pm 1$ sdv) at 2000 AD, compared to 370 ppm measured at Mauna Loa. CO$_2$ is on average lowered to $364 \pm 14$ ppm at 2000 AD in the reduced set. The cases that give the better agreement with observed CO$_2$ have the larger land uptake through the model’s CO$_2$ fertilization mechanism. Gross primary productivity in GENIE increases by $27 \pm 18$ % (mean $\pm 1$ sdv) in the full set and by $39 \pm 17$ % in the reduced
The MAGICC model version 6.3 has been run in 171 different parameter settings that emulate 19 AOGCMs and 9 coupled climate-carbon cycle models from the Coupled Model Intercomparison Project Three (CMIP3) and the Coupled Carbon Cycle Climate Model Intercomparison Project (C4MIP). The application of this model to simulate IRFs has been described in Reisinger et al. (2010).

The Bern3D-LPJ model was run in 1069 different setups selected from a 5000-member ensemble following a Bayesian approach. Nineteen key model parameters are varied. These are related to terrestrial and ocean carbon and heat exchange, uncertainties in anthropogenic radiative forcing, and the transient and equilibrium climate sensitivity of the model. The 5000 member ensemble is constrained by a large set of observation-based data including estimates for surface air temperature change, ocean heat uptake, atmospheric CO$_2$ change and ocean and land carbon uptake rates, seven physical and biogeochemical 3-D ocean tracer fields, and land carbon stocks and fluxes.

Additional sensitivity simulations were carried out with the standard setup of the Bern3D-LPJ model. These include a series of runs with emission pulses ranging from 10 to 10,000 GtC added to a preindustrial background. These simulations are used to demonstrate the dependency of the IRF on the magnitude of emissions. The model was also run in a mode where climate was kept constant for emission pulses of 100 and 5000 GtC. These simulations allow us to quantify the impact of carbon-cycle climate feedbacks on the IRF$_{CO_2}$ within the Bern3D-LPJ model.

The pulse size of 100 GtC applied in the standard simulation (run 3) is larger than the pulse size of 10 GtC applied to determine the IRF$_{CO_2}$ in the Bern-SAR model for the SAR and the pulse of 40 GtC applied in the Bern2.5D-LPJ for the AR4. The choice of the larger pulse size is to improve signal-to-noise ratio in the simulated response. The simple Bern-SAR model does not feature any internal variability and a small pulse size permits us to compute its response reliably. In contrast, the Bern2.5d-LPJ used...
in the AR4 and even more the ESM used in this study feature considerable internal variability in atmospheric CO$_2$ and climate that would mask the response to a small emission pulse.

Model output was smoothed to remove short-term variability using a spline-fit method (Enting, 1987). A cut-off period is chosen as input parameter to the spline routine such that the amplitude of a sine wave with this period is attenuated by 50%. Results from the control simulations from the models with a dynamic atmosphere (NCAR CSM1.4, HadGEM2-ES, MPI-ESM, and LOVECLIM) are smoothed with a cut-off period of 30 yr during nominal year 0 to 30 after the pulse emission; afterwards a cut-off period of 200 yr was applied. This choice of cut-off periods yields the removal of interannual-to-decadal variability, while still following the initial adjustment of the system after the trend in atmospheric CO$_2$ is abruptly changed five years before the emission pulse release in year 2010. Smoothing was not applied for the control runs of the other models. The results from run 3 are subtracted from the (smoothed) control run (run 2; run 1 for MPIM-ESM and NCAR CSM1.4). The resulting response is smoothed using cut-off periods of 4, 20, 50, 250, and 500 yr for the periods from year 0 to 10, from year 10 to 50, from year 50 to 100, from year 100 to 300 and year 300 to 1000, respectively. The response of all models to the 100 GtC pulse added to a 389 ppm background was smoothed in this way for consistency. This treatment has virtually no effect on results from box-models and from EMICs with small or absent internal variability and on the integrated IRF$_{CO_2}$ that is used to compute the AGWP and GWP.

4 Results

4.1 Impulse response functions and Absolute Global Warming Potentials for CO$_2$

The evolution of the IRF$_{CO_2}$ (Fig. 1a) shows a rapid decrease in the first few years after the emission pulse and then a continued but slow decline. It reaches a fraction
of $0.60 \pm 0.14$ (± two sdv) at year 20 and $0.41 \pm 0.13$ at year hundred. In other words, while 40% of the initial atmospheric CO$_2$ perturbation is on model-average removed from the atmosphere within 20 yr, it takes additional 80 yr to mitigate the next 19% of the perturbation. At year 1000, 24% (±10%) of the perturbation is still airborne. This evolution is consistent with earlier model results (Maier-Reimer and Hasselmann, 1987; Cao et al., 2009; Siegenthaler and Joos, 1992; Sarmiento et al., 1992; Enting et al., 1994; Archer et al., 2009; Eby et al., 2009). It is also consistent with our understanding of the carbon cycle as two-way transfers of carbon between reservoirs with different timescales (Prentice et al., 2001; Denman et al., 2007; Oeschger et al., 1975).

The time-integrated IRF$_{CO_2}$ (Fig. 1b), and thus AGWP$_{CO_2}$, increases continuously with time and there is no sign of approaching an equilibrium value at year 1000. The time-integrated IRF$_{CO_2}$ for the individual models is tabulated in Table 4. The multi-model mean increases from $14.3 \pm 1.8$ yr (mean ± 2 sdv) at year 20, to $30.2 \pm 5.7$ at year 50, to $52.4 \pm 11.7$ at year 100, to $185.6 \pm 47$ at year 500, and to $308 \pm 95$ at year 1000.

The multi-model mean IRF$_{CO_2}$ over the first 1000 yr is fitted by a sum of exponentials and the conditions that the sum of the coefficients $a_i$ equals 1:

$$\text{IRF}_{CO_2}(t) = a_0 + \sum_{i=1}^{3} a_i \cdot \exp\left(-\frac{t}{\tau_i}\right) \quad \text{for} \quad 0 \leq t \leq 1000\text{yr}$$ (11)

The coefficients are $a_0 = 0.21787$, $a_1 = 0.22896$, $a_2 = 0.28454$, $a_3 = 0.26863$ and the time scales $\tau_1 = 381.33$ yr, $\tau_2 = 34.785$ yr, and $\tau_3 = 4.1237$ yr. We note that the time-integrated IRF$_{CO_2}$ as calculated with this fit is the same for a time horizon of 100 yr and slightly different for the time horizons of 20, 50, 500, and 1000 yr than those given in Table 4 (the values from the fit are: 14.2 yr, 30.3 yr, 52.4 yr, 184 yr, 310 yr).

There are uncertainties in the IRF$_{CO_2}$ and the AGWP$_{CO_2}$. The range in integrated IRF$_{CO_2}$ across all models is 45 to 67 yr at year hundred. This is comparable to the 5–95% interval ranging from 40 to 64 yr for the MAGICC6 ensemble that emulates a number of carbon-climate models. The 5–95% confidence interval for the Bern3D-LPJ ensemble, constrained with a broad set of observations, is 49 to 65 yr at year 19816.
100 and somewhat smaller than the model range. The ensemble interval from the GENIE model is larger than the other ranges at year 100; the time-dependence of this ensemble was constrained only by preindustrial to modern CO$_2$ change. At year 20 and 50, the situation with regard to uncertainties ranges is qualitatively similar as for year 100. However, the 5–95% confidence range for the MAGICC6 ensemble is smaller than the range across all models at year 500, whereas the width of the confidence range is larger than that of the model range for the observation-constrained Bern3D-LPJ and GENIE ensembles. This may suggest that observational-constraints as applied in the Bern3D-LPJ narrow the uncertainty range for a time horizon of up to 100 yr.

An alternative approach is to constrain the uncertainty in IRF$_{CO_2}$ by assuming a linear carbon system and constraining the IRF$_{CO_2}$ with estimates of the 20th century airborne fraction of CO$_2$. If we consider the uncertainty in the integrated response, then clearly if IRF$_{CO_2}$ lies between 0 and 1, the integral to time TH will lie between 0 and TH, regardless of the form of the function IRF$_{CO_2}$. However not all functions have physically reasonable behaviour and not all functions will be consistent with the 20th century pattern of emissions and concentrations. Including such considerations can narrow the range of possible values of the integrated response. Finding the maximum and minimum possible values of the integral (and the functions that give these extrema) is a problem in mathematical optimisation that can be analysed using the calculus of variations. If the constraints are linear, then the discretised form of the optimisation can be expressed as a problem in linear programming for which well-established computational techniques are available (Press et al., 1986). Such an approach to analysing the carbon cycle response was introduced earlier (Enting and Mansbridge, 1987).

For the present study we consider functions with IRF$_{CO_2}(t = 0) = 1$, IRF$_{CO_2}(t) \geq 0$, $d/dt$ IRF$_{CO_2}(t) \leq 0$, and $d^2/dt^2$ IRF$_{CO_2}(t) \geq 0$, and which give behavior consistent with observations for the 20th century. This last condition is expressed in terms of the airborne fraction $\gamma$. If we take $\gamma$ as known precisely then we find that for TH = 100, the integrated response is constrained to lie in the range 39.7 to 52.4 yr. The implication is that regardless of the model structure, no model that exhibits the dissipative behaviour
expressed by the constraints on the derivatives, can have an integrated response that lies outside this range. This range of 13 yr is thus an upper bound on the amount of uncertainty that can arise from differences in model structure (and termed “structural uncertainty”, Enting et al., 2012).

If, however, it is acknowledged that the 20th century airborne fraction is not known precisely, mainly because of uncertainties in land-use emissions (Stocker et al., 2010), then a wider class of response functions and a wider range of integrals is possible. Constraining the airborne fraction to lie in the range 0.5 ± 0.05 gives the range 33.6 to 57.6 yr for possible values of the integral for TH = 100. This expanded range of uncertainty is a combination of the “structural uncertainty” described above, and a “calibration uncertainty” arising from uncertainties in the calibration data (Enting et al., 2012).

Since we are primarily concerned with the range rather than the specific value, the 20th century constraint has been approximated in terms of carbon emissions that grew exponentially over 150 yr with a time scale of 50 yr (emissions are proportional to $\exp(t/(50 \text{yr}))$). This is a truncation of the expression for the airborne fraction in terms of the Laplace transform of the response (Enting, 1990). In principle, the same approach can be used for TH = 20 yr but because the 20 yr time scale is less representative of 20th century changes, the “calibration” constraint does little to constrain the range of uncertainty for the integral.

In conclusion, different approaches to estimate the uncertainty in the integrated IRF$_{\text{CO}_2}$ for a time horizon of 100 yr yield comparable results. Taken together, these approaches yield an average uncertainty range of 26 yr or of 49% for the 100-yr integrated response (Table 4). We assume that this average range represents approximately a 5–95% confidence range and that it is symmetrically distributed around the multi-model mean to arrive at our best estimates for the mean and 5–95% confidence range for the time-integrated IRF$_{\text{CO}_2}$.

The MAGICC6 and Bern3D-LPJ ensemble ranges are roughly symmetrically distributed around the median for time horizons of 20, 50, and 100 yr and skewed, but in different directions, for 500 yr. These results tend to support the assumption that the
uncertainty range is symmetric around the best estimate, though the ensemble range from the GENIE model is skewed towards high values.

Multiplying the time-integrated IRF\(_{\text{CO}_2}\) with the radiative efficiency of CO\(_2\), \(A_{\text{CO}_2}\), yields the Absolute Global Warming Potential, AGWP\(_{\text{CO}_2}\). Here, \(A_{\text{CO}_2}\) is computed for an atmospheric background of 389 ppm and in the limit of a small perturbation by using the derivative of the simplified radiative forcing expression of (Myhre et al., 1998):

\[
A_{\text{CO}_2} = 5.35 \text{ W m}^{-2} \text{ (389 ppm)}^{-1} \times (2.123 \times 10^{12} \text{ kg C ppm}^{-1})^{-1} \times (12 \text{ kg C/44 kg CO}_2) = 1.7710^{-15} \text{ W m}^{-2} \text{ (kg CO}_2)^{-1}.
\]

The uncertainty in the radiative efficiency of CO\(_2\) is given as 10% in the IPCC TAR and AR4 and guided by the spread in published estimates. The overall uncertainty in AGWP\(_{\text{CO}_2}\) is insignificantly larger than that for IRF\(_{\text{CO}_2}\) as the uncertainty in \(A_{\text{CO}_2}\) is much smaller than that of the time integrated IRF\(_{\text{CO}_2}\). Assuming quadratic error propagation, the uncertainty range in AGWP\(_{\text{CO}_2}\) (TH = 100 yr) would be 50% (\(\sqrt{0.49^2 + 0.1^2} = 0.50\)) compared to 49% of the integrated IRF\(_{\text{CO}_2}\). Here, we use the same relative uncertainty for AGWP\(_{\text{CO}_2}\) and IRF\(_{\text{CO}_2}\). Our best estimate for the AGWP\(_{\text{CO}_2}\) is a mean value of \(92.7 \times 10^{-15} \text{ yr W m}^{-2} \text{ (kg CO}_2)^{-1}\) and a 5–95% confidence range of \((70.1 \text{ to } 115) \times 10^{-15} \text{ yr W m}^{-2} \text{ (kg CO}_2)^{-1}\) for a time horizon of 100 yr. In IPCC uncertainty language (Solomon et al., 2007), it is very likely that the AGWP\(_{\text{CO}_2}\) for a time horizon of 100 yr is within a range of \((70 \text{ to } 115) \times 10^{-15} \text{ yr W m}^{-2} \text{ (kg CO}_2)^{-1}\).

### 4.2 Response in surface air temperature and AGTP, ocean heat uptake and steric sea level rise

The response in radiative forcing to the 100 GtC pulse as computed from the multimodel mean IRF\(_{\text{CO}_2}\) (RF\((t) = 5.35 \text{ W m}^{-2} \ln((389 \text{ ppm} + \text{IRF}_{\text{CO}_2}(t) \times 47.1 \text{ ppm})/389 \text{ ppm}))\) (Myhre et al., 1998) corresponds to a step increase by 0.61 W m\(^{-2}\) at year 0, followed by a decrease to 0.26 W m\(^{-2}\) at year 100 and to 0.15 W m\(^{-2}\) at year 1000. The equilibrium response in global mean surface air temperature (SAT) to these forcing values are
0.49°C, 0.22°C and 0.12°C and when assuming a typical mid-range climate sensitivity of 3°C for a nominal doubling of CO₂.

The multi-model mean response in SAT to the 100 GtC pulse emission (Fig. 2a, Table 5) is an increase by 0.19 ± 0.10 °C within the first 20 yr. Afterwards, SAT remains almost constant until year 100. This evolution is a consequence of the delayed response in SAT to the initial increase in radiative forcing as it takes time to heat the surface layers of the ocean with its large heat capacity and heat exchange with the deep ocean. After year 100, SAT is generally closer to equilibrium with the simulated radiative forcing and decreases slowly to 0.14 ± 0.09°C by year 1000. Our best estimates for the mean and 5 to 95% uncertainty ranges in SAT changes and AGTP for CO₂ are tabulated for a range of time horizons in Table 5. For a time horizon of 100 years, AGTP of CO₂ is 0.46 × 10⁻¹⁵°C per kg CO₂ and the estimated 5 to 95% confidence range is (0.22 to 0.74) × 10⁻¹⁵°C per kg CO₂.

Fuglestvedt et al. (2010) applied the analytical response functions for CO₂ as given in the AR4 and the analytical response function for temperature to a change in radiative forcing (R) by (Boucher and Reddy, 2008) to estimate AGTP_{CO₂} to 0.68, 0.58 and 0.51 × 10⁻¹⁵°C per kg CO₂ for time horizons of 20, 100, and 500 yr respectively. These values are higher than our best estimates of 0.52, 0.46 and 0.38 × 10⁻¹⁵°C per kg CO₂, but well within the 5 to 95% confidence range (Table 5).

The response in SAT is fairly smooth in most EMICs and box models and the response in SAT is well defined in these models. However, the models that feature a dynamic atmosphere (HadGEM2-ES, MPI-ESM, NCAR CSM1.4, LOVECLIM) show strong interannual-to-decadal variability in SAT of several tenths of a degree Celsius both in the control and in the pulse simulation. This internal variability of the more comprehensive models makes the extraction of the response in SAT challenging for these models and a well-defined separation of the forced response from the models’ internal variability is not achieved. For example HadGEM2-ES shows a positive variation in annual SAT values of several tenths of a degree Celsius towards the end of the simulation in the standard pulse experiment. This yields a difference in SAT of about 0.3 °C be-
between the smoothed HadGEM2-ES response and the multi-model mean response near year 100 (Fig. 2). This indicates that it is difficult to extract the temperature response for use in GTP from comprehensive models when they are forced with a pulse of modest size as applied here.

The response in ocean heat content (OHC) and steric sea level rise (SSLR) is of multi-century type (Fig. 2b, c, Table 6). The responses in these quantities are in general much smoother than for SAT as they mainly reflect the time-integrated, cumulative perturbation in air-sea heat fluxes. Multi-model SSLR is $1.7 \pm 1.7 \text{ cm} (\pm 2 \text{ sdv})$ at year 100 and $4.6 \pm 6.0 \text{ cm}$ at year 1000 in response to the 100 GtC pulse. The median in SSLR response in the Bern3D-LPJ ensemble is close to the multi-model mean at year 100, while the 5 to 95% confidence interval ranges from 0.7 to 2.8 cm and is thus smaller than the multi-model range.

The multi-model response in OHC reaches $14 \pm 11 \times 10^{22} \text{ J}$ by year 100 and $40 \pm 41 \times 10^{22} \text{ J}$ by year 1000. The upper and lower extreme cases in the multi-model ensemble are the ESM: the MPIM and NCAR CSM1.4 on the low side and the HadGEM2-ES on the high side. This indicates that the responses in globally aggregated values do not depend on the type of model, e.g. ESM versus EMIC. The 5 to 95% interval in OHC of the MAGICC ensemble and of the observation-constrained Bern3D-LPJ ensemble is smaller at year 100 and comparable to the model range at year 500.

In conclusion, AGTP of CO$_2$ varies much less than AGWP for time horizons between 20 and 1000 yr. However, uncertainties in the estimates of AGTP are much larger than those for AGWP, as also inferred with a box model ensemble by (Reisinger et al., 2010), and uncertainties in the response in ocean heat content and steric sea level rise are also larger than for AGTP.

4.3 Response in ocean and land carbon

The carbon that is removed from the atmosphere is taken up by the ocean and the land biosphere (Fig. 3). In the first decade, both the ocean and the land contribute sub-

19821
stantially to removing the atmospheric carbon perturbation. Land and ocean absorb on multi-model mean close to 20 GtC during the first 20 yr after the emission. The ocean continues to absorb carbon from the atmosphere and the multi-model perturbation in the ocean carbon inventory is $19 \pm 8$ GtC by year 20, $32 \pm 15$ GtC by year 100 and $60 \pm 18$ GtC by year 1000. In other words, 60% of the emission pulse (multi-model average) has been transferred to the ocean by year 1000 (Fig. 3a).

In contrast, the land perturbation remains fairly constant after a few decades up to year 100 and decreases thereafter in most models. On multi-model average, the land has sequestered $18 \pm 16$ GtC by year 20, $22 \pm 21$ GtC by year 100 and $17 \pm 18$ GtC by year 1000. It is interesting to note that the three ensembles include also cases where the land loses carbon to the atmosphere in response to the 100 GtC emission pulse (Fig. 3b). In these model realizations, the climate change resulting from an emission pulse forces a carbon loss from land ecosystems that is larger than the positive impacts of elevated atmospheric CO$_2$. This loss is likely predominantly driven by accelerated turnover of soil and litter carbon in response to warming (Joos et al., 2001).

The response in ocean carbon inventory to an emission pulse is relatively well understood. Ocean uptake is mainly driven by physico-chemical processes and uptake rates are governed by the quantitatively well-understood carbonate chemistry in surface waters and by the rates of surface-to-deep transport. The latter are constrained by the distribution of transient tracers such as CFCs and bomb-produced radiocarbon in the thermocline (Key et al., 2004). In early generation carbon cycle models such as the Bern-SAR model only these physico-chemical processes were included. This first-order response is modified by other processes such as ocean warming and changes in ocean circulation and marine biogeochemistry (Plattner et al., 2001; Sarmiento et al., 1998; Joos et al., 1999).

The response of the land biosphere carbon inventory is associated with considerable uncertainties. It is currently not clear whether the land will continue to act as a strong carbon sink or whether climate change will lead to a loss of land carbon that overwhelms the potentially positive influence of elevated atmospheric CO$_2$ and nitrogen.
input on net primary productivity and carbon stocks. This limited understanding is re-
lected in the large uncertainty range. We estimate the 5 to 95% confidence range for the response in land carbon inventory to 45 GtC at year 100. For comparison, the corresponding uncertainty range for the ocean inventory is 29 GtC.

In conclusion, carbon uptake by the land biosphere is about equally important for
the evolution of IRF CO₂ as uptake by the ocean during the first two decades after the
release. Subsequently, the ocean becomes the dominant carbon sink. The uncertainty
range of the terrestrial and oceanic carbon inventories remain substantial over the
1000 yr analysis period.

4.4 Influence of background conditions, pulse size, and carbon cycle-climate
feedback

4.4.1 Background conditions

The response in atmospheric CO₂ and cumulative air-to-sea and air-to-land carbon
fluxes depends sensitively on the background conditions (Fig. 4). Ten out of fifteen
models were also used to run the simulations where a 100 GtC emission pulse is added
to preindustrial (PI) in addition to present day (PD) conditions. For these models, the
time integrated IRF CO₂ at year 100 ranges between 34 and 47 yr for the PI100 case
and between 45 and 62 yr for the PD100 case. The lower CO₂ perturbation for PI100
is generally due to a higher uptake by both the ocean and the land biosphere and is
consistently lower for PI than PD conditions for all individual models.

The responses in SAT, OHC, and SSLR are similar for PI100 and PD100. This is due
to two compensating effects (Caldeira and Kasting, 1993; Wuebbles et al., 1995). The
time-integrated CO₂ response decreases by roughly 25% from PD to PI conditions. On
the other hand, the radiative forcing per unit change in atmospheric CO₂ increases by
39% from PD to PI conditions. The range in time-integrated forcing at year 100 is then
almost identical (30 to 42 yr W m⁻² for PI100 versus 29 to 40 yr W m⁻² for PD100).
The ocean uptake capacity regulated by the carbonate chemistry decreases with increasing CO$_2$ and warmer climate conditions are generally associated with a lower solubility of CO$_2$ and a more sluggish surface-to-deep transport (Joos et al., 1999; Roy et al., 2011). As expected, the model range in cumulative air-to-sea flux is smaller for PD (24 to 40 GtC) than for PI (32 to 47 GtC) conditions and at year 100. The ocean carbon uptake is consistently lower for PD than PI conditions in all models during the first hundred years. In the long-run, the time-integrated ocean uptake becomes larger for PD100 than PI100 in the Bern3D-LPJ model. This is likely related to the large difference in the land carbon responses (∼27 GtC at year 500) between the PI100 and PD100 cases in this model.

The land carbon uptake in the model depends on factors such as the spatio-temporal evolution of net primary productivity (NPP) under changing CO$_2$ and climate and the change in soil and litter carbon turnover rates with changing climate conditions. It is beyond the scope of this paper to discuss the processes affecting land carbon stocks in detail for the range of models. The response in land carbon inventory to changes in CO$_2$ and climate is complex and regionally distinct. Generally, the models react with an increase in NPP to increasing atmospheric CO$_2$. Temperature and precipitation changes can have both positive and negative effects on NPP, while most models assume that soil and litter turnover rates increase approximately exponentially with increasing temperatures.

The response in land carbon inventory at year 100 ranges between 22 and 35 GtC for PI100 compared to 10 to 42 GtC for PD100. The model spread is thus considerably smaller for the PI100 than for the PD100 case. The response is not consistent among models. LOVECLIM shows a higher land carbon uptake under PD than PI conditions, NCAR CSM1.4 and DCESS show similar changes, whereas most models simulate a reduced land uptake for PD100 compared to PI100.
4.4.2 Pulse size

We next turn to the case where 5000 GtC were released into the atmosphere (PI5000) (Fig. 5). With this higher input, a considerably greater proportion of CO$_2$ remains in the atmosphere, compared to the release of 100 GtC (PI100). For the PI5000 simulation, the integral of IRF$_{CO_2}$ through to year 100 is about double that from the PI100 simulation.

In other words, the time integrated IRF$_{CO_2}$ depends sensitively on the pulse size. In particular the ocean uptake of carbon per unit carbon emitted is substantially smaller for the PI5000 than PI100 case.

As for pulse sizes of 100 GtC, the SAT increases rapidly within the first two decades after the pulse and remains high for the centuries to follow, while ocean heat content and steric sea level rise increase more gradually. The simulated SAT at year 100 per unit carbon emission is roughly 40% smaller in the PI5000 than the PI100 case (2.6 to 8.6°C versus 4 to 15°C per 5000 GtC). Similarly, the responses in ocean heat content and steric sea level rise are smaller per unit emission for the larger pulse.

4.4.3 Carbon cycle-climate feedbacks

The influence of the carbon cycle-climate feedbacks is investigated with the Bern3D-LPJ model for emission pulses of 100 and 5000 GtC added to preindustrial conditions (Fig. 6). Results are compared between a setup where climate varies in response to an emission pulse and a setup where climate is kept invariant at preindustrial conditions and for a range of pulse sizes. The time-integrated IRF$_{CO_2}$ at year 100 is around 13% and 15% lower for the 100 and 5000 GtC pulses if the carbon cycle-climate feedback is suppressed. At year 1000, the reduction is similar for the small pulse, but about 40% for the 5000 GtC pulse. The reductions in the time-integrated IRF$_{CO_2}$ due to the carbon cycle-climate feedback are similar to the effects of reducing the pulse size from 5000 GtC to about 2000 GtC and from 100 GtC to 10 GtC, respectively (Fig. 6).
In summary, IRF$_{\text{CO}_2}$ and its time integral is lower for preindustrial than present day background conditions and for smaller compared to larger emission pulses. On the other hand, the ocean uptake per unit emission decreases with increasing background CO$_2$ concentrations (and related warmer climate conditions) and increasing pulse sizes. The responses in SAT, ocean heat content and steric sea level rise show little differences between the two 100 GtC cases and a smaller response per unit emission for larger pulse sizes. The time-integrated IRF$_{\text{CO}_2}$ and thus the AGWP depend also on the carbon cycle-climate feedback. However, the most important factor that determines the time-integrated IRF$_{\text{CO}_2}$ and AGWP is the choice of time horizon.

5 Discussion and Conclusion

We have reassessed the response of the coupled carbon cycle-climate system to an emission pulse of carbon for present day CO$_2$ and climate conditions using a suite of models of various complexity. The multi-model mean response in atmospheric CO$_2$ was fitted by an analytical function (sum of exponentials) for easy use by others. A novel element of the study is a thorough assessment of uncertainties in the simulated responses based on the spread of the multi-model ensemble and of three ensembles with individual models as well as using a linear programming approach constrained by observations. These different approaches to estimate the uncertainty in the integrated IRF$_{\text{CO}_2}$ yield comparable results. We also quantified the sensitivity of the responses to the magnitude of the emission pulse and the atmospheric and climatic background conditions. The influence of the climate-carbon cycle feedback on results was investigated within one model.

We find that the absolute global warming potential (AGWP) of CO$_2$ for a time horizon of 100 yr is $92.7 \times 10^{-15}$ yr W m$^{-2}$ per kg CO$_2$ with a 5 to 95% confidence range of (70 to 115) $\times 10^{-15}$ yr W m$^{-2}$ per kg CO$_2$ (Table 4). Although, the ocean absorbs most of the emission pulse, the uncertainty in the perturbation of the land carbon inventory (in absolute units) is larger than for the perturbation in the ocean carbon inventory.
This is related to different responses of the land biosphere models to changes in atmospheric CO$_2$ and climate and reflects our incomplete knowledge on these terrestrial processes.

There are also uncertainties related to the experimental setup. The time-integrated CO$_2$ impulse response at year 100 is about twice as large for an emission pulse of 5000 GtC compared to our standard pulse size of 100 GtC. An emission of 5000 GtC is an extreme case in the context of Global Warming Potential (GWP), though within reach when burning all fossil resources. An increase of the pulse size to 1000 GtC yields an increase in the time-integrated CO$_2$ impulse response, used to compute AGWP and GWP, by one third. The influence of the carbon-cycle climate feedback is found to be of order 10% to 20% on the time integrated CO$_2$ impulse response and the AGWP of CO$_2$. The magnitude of this effect varies across models (Friedlingstein et al., 2006; Gillett and Matthews, 2010). The carbon-cycle climate feedback was not included in the IRF of CO$_2$ derived with the Bern-SAR model, but is included in the Bern model versions as used in the TAR and AR4 and corresponding IRFs. Although, choices in pulse size, background concentration, and model lead to considerable uncertainties in AGWP and GWP, the most important variable is the time horizon (Table 7).

The subjective choice of the time horizon dominates uncertainties in the absolute global warming potential of CO$_2$ and related uncertainties in global warming potential of most other agents. The uncertainty in AGWP (in units of yr W m$^{-2}$ per kg CO$_2$) can be mapped to an uncertainty in the time horizon (in units of year). For a time horizon of 100 yr, the lower and upper bound of the 5–95% confidence range of the AGWP for CO$_2$ correspond to the multi-model mean value of AGWP evaluated at the time horizon of 70 yr and 132 yr. This uncertainty range of 62 yr, stemming from uncertainties in the carbon cycle-climate model response, is much smaller than the differences resulting from the subjective choice of alternative time horizons; in the IPCC report GWP are tabulated for illustrative time horizons of 20, 100, and 500 yr. Table 7 illustrates how the GWP of methane, nitrous oxide, and sulphur hexafluoride with perturbation life times of 12 yr, 114 yr and 3200 yr changes with the choice of time horizon. For example, one
could select a time horizon of 1000 yr instead of 100 yr in the UNFCCC process and thereby account somewhat more explicitly for the long-time scales involved in the Earth System. In this case, the GWP for methane would be more than 5 times smaller and only 17% (13 to 25%; 5 to 95% confidence range) of that for 100 years. The GWP for N$_2$O would be more than 3 times smaller and only 29% (22 to 42%) of that for 100 yr, whereas the GWP for SF$_6$ would be about 48% (13% to 114%) larger than that for a time horizon of 100 yr. On the other hand, selecting a time horizon of 20 yr instead of 100 yr yields a three times larger GWP for methane. A strong influence of the time horizon is also found for GTP and time-integrated GTP (Peters et al., 2011).

The IPCC presented impulse response functions of CO$_2$, IRF$_{CO_2}$, in its major assessment reports. Figure 7 shows how IRF$_{CO_2}$ has changed from the IPCC First Assessment Report (FAR), to the Second Assessment Report (SAR), to the Fourth Assessment Report (AR4) and compares these responses with the results of this study. IRF$_{CO_2}$ was not updated in the Third Assessment Report. Differences in the IRF$_{CO_2}$ are relatively small. The higher initial airborne fraction published in the FAR is related to the application of an atmosphere-ocean model with a neutral land biosphere, whereas in subsequent reports the land biosphere model absorbs a considerable fraction of the initial emission pulse during the first few decades. The responses published in the SAR and the AR4 are lower than the multi-model mean response of this study. This is predominantly due to the smaller pulse size and lower CO$_2$ background in the SAR and AR4 setup. The time-integrated IRF$_{CO_2}$ for the AR4 (Bern2.5D-LPJ) and SAR (Bern-SAR) models under the setup of this study (Table 4) are with 49 and 51 yr only slightly lower than the multi-model mean of 52 yr at year 100. We do not find indications that there are systematic differences in IRF$_{CO_2}$ between models of different complexities such as EMICs and comprehensive Earth System Models.

In addition to the Absolute Global Warming Potential, we have also quantified the Absolute Global Temperature change Potential and corresponding responses in ocean heat content and steric sea level rise by directly applying the suite of carbon cycle-climate models. The uncertainty in these responses is much larger than the uncertainty...
in the IRF$_{\text{CO}_2}$ and the AGWP of CO$_2$. This is mainly a consequence of the large range in the climate sensitivity of the different models (Table 2) and their ocean heat uptake efficiency. More general, uncertainties increase along the cause-effect chain from emissions to atmospheric abundance to radiative forcing to climate change. In addition, it is difficult to extract the temperature signal from a relatively small CO$_2$ emission pulse from results of comprehensive ESM as these models feature considerable interannual-to-decadal temperature variability. Larger pulse sizes and/or running ensembles instead of single simulations would improve signal-to-noise ratio. Intercomparison study that looks into the responses of non-CO$_2$ agents might further improve the quantification of metrics and their uncertainties. Yet fundamental issues will remain. Different forcing agents are distinct and any simple metric intended to compare forcing agents relies on subjective choices.

CO$_2$ continues to dominate man-made warming. For the current crop of emission scenarios from the integrated assessment community (Weyant et al., 2006; Van Vuuren et al., 2008), the contribution of CO$_2$ to the anthropogenic warming by 2100 is estimated using an emission-driven climate model to be 58 to 76% of that of all greenhouse gases together (Strassmann et al., 2009). Independent from the choice of emission metric, the long life time of the anthropogenic CO$_2$ perturbation implies that anthropogenic emissions of CO$_2$ must be reduced if greenhouse gas forcing and anthropogenic climate change are to be stabilized (Siegenthaler and Oeschger, 1978).

Appendix A

Model descriptions

ACC2 The Aggregated Carbon Cycle, Atmospheric Chemistry and Climate model (ACC2) (Tanaka et al., 2007; Tanaka, 2008) consists of a box model of the global carbon cycle, simple parameterizations of the atmospheric chemistry, and a land-ocean energy balance model. Most relevant to this study is the carbon cycle component,
which is a four-layer atmosphere-ocean box model coupled with a four-reservoir land biosphere box model (Sect. 2.1 of Tanaka, 2008). The saturation of the ocean CO$_2$ uptake under rising atmospheric CO$_2$ concentration is dynamically reproduced by the thermodynamic equilibrium for carbonate species. The CO$_2$ fertilization effect is parameterized by the $\beta$ factor. The temperature sensitivity of the soil respiration is modeled through the Q10 parameter. The land and ocean CO$_2$ uptake is influenced by the temperature change. Values of uncertain parameters (including the $\beta$ factor and the Q10 parameter) are estimated based on an inverse estimation setup (Sect. 3 of Tanaka, 2008) in which a large number of parameters are simultaneously optimized by using associated historical observations and prior parameter estimates including their uncertainties from year 1750 to 2000 (Tables 3.1 and 3.2 of Tanaka, 2008). Parameter values estimated through the inverse estimation are consistently used in projections beyond 2000. The simplified process representations in ACC2 allow one to perform a sensitivity analysis for the CO$_2$ response under various sets of assumptions. ACC2 has been applied to several studies (Tanaka et al., 2009a,b, 2012).

**Bern-SAR** This model was applied to calculate the CO$_2$ impulse response function as used for the Global Warming Potentials of IPCC 1994 report on Radiative Forcing, the IPCC Second Assessment Report and the Kyoto Protocol. The Bern model (Siegenthaler and Joos, 1992; Joos et al., 1996) is designed to compute the uptake of anthropogenic carbon by land and ocean. It links a well-mixed atmosphere with the High-Latitude Exchange/Interior Diffusion-Advection (HILDA) ocean model and a 4-box representation of the land biosphere (Siegenthaler and Oeschger, 1987). Model parameters of the box-diffusion-type ocean model were determined such that the model reproduces the oceanic distribution of natural and bomb-produced radiocarbon. Net primary production on land increases with the natural logarithm of CO$_2$ and the scaling factor ($\beta = 0.27$) was chosen in order to close the atmospheric CO$_2$ budget in the early nineties.

**Bern2.5D-LPJ** This model was used to calculate the CO$_2$ impulse response function for the IPCC AR4 report (Forster et al., 2007, p. 213). Here, the same code version
as in the AR4 was used and subsequent updates of the land biosphere component (LPJ) are not included. The Bern2.5D-LPJ (or Bern2.5CC in Plattner et al., 2008) reduced complexity climate model includes components describing (1) the physical climate system, (2) the cycling of carbon and related elements, and (3) a module to calculate concentrations of non-CO$_2$ greenhouse gases and radiative forcing by atmospheric CO$_2$, non-CO$_2$ greenhouse gases, and aerosols (Plattner et al., 2008). The ocean physical component is the zonally averaged, three-basin circulation model of Stocker et al. (1992), coupled to a zonally and vertically averaged atmospheric energy balance model, including an active hydrological cycle (Schmittner and Stocker, 1999). The ocean biogeochemical component includes a simple prognostic description of the cycles of carbon, carbon isotopes, oxygen, and carbon-related tracers (Marchal et al., 1998; Joos et al., 1999; Plattner et al., 2001). The terrestrial biosphere component is the Lund–Potsdam–Jena (LPJ) dynamic global vegetation model at 3.75° × 2.5° resolution as used by Joos et al. (2001) and Gerber et al. (2003) and described in detail by Sitch et al. (2003). Vegetation is represented by nine plant functional types. Fertilization of plants by increasing atmospheric CO$_2$ concentrations is modeled according to a modified Farquhar scheme (Farquhar et al., 1980; Haxeltine and Prentice, 1996). The module designed to calculate radiative forcing by atmospheric CO$_2$, non-CO$_2$ greenhouse gases, and aerosols is based on work summarized in Fuglestvedt and Berntsen (1999) and Joos et al. (2001). The climate sensitivity is 3.2 K for a nominal doubling of CO$_2$.

**Bern3D-LPJ** Bern3D-LPJ is an Earth System Model of Intermediate Complexity with a fully coupled carbon cycle and components that represent the ocean and sea ice, ocean sediments, the atmosphere, and the terrestrial biosphere. The ocean component is a seasonally forced three-dimensional frictional geostrophic global ocean model (Edwards et al., 1998) with a resolution of 36 × 36 boxes in the horizontal direction and 32 vertical layers (Müller et al., 2006). Marine biogeochemical cycles are implemented following OCMIP-2 (Najjar and Orr, 1999; Orr et al., 1999; Najjar et al., 2007) with the addition of prognostic formulations for biological productivity and the cycling of iron,
silica, $^{13}\text{C}$ and $^{14}\text{C}$ (Parekh et al., 2008; Tschumi et al., 2008), as well as a sedimentary component (Tschumi et al., 2011; Gehlen et al., 2006; Heinze et al., 1999). The atmosphere is represented by a single-layer energy and moisture balance model with the same horizontal resolution as the ocean component (Ritz et al., 2011). The CO$_2$ forcing is calculated after (Myhre et al., 1998) and the model is tuned to simulate an equilibrium climate sensitivity of 3°C. Other greenhouse gases and volcanic aerosols are prescribed as global radiative forcing, while tropospheric sulphate aerosols are taken into account by changing the surface albedo locally (Steinacher, 2011; Reader and Boer, 1998). The climate sensitivity is 3 K for a nominal doubling of CO$_2$. The terrestrial biosphere component is based on the Lund-Potsdam-Jena (LPJ) Dynamic Global Vegetation Model at $3.75^\circ\times 2.5^\circ$ resolution (Joos et al., 2001; Sitch et al., 2003). Vegetation is represented by 12 plant functional types and CO$_2$ fertilization is modeled according to the modified Farquhar scheme (Farquhar et al., 1980; Haxeltine and Prentice, 1996). The model has recently been extended with modules to account for land use (Strassmann et al., 2008; Stocker et al., 2011), peatlands and permafrost dynamics (Gerten et al., 2004; Wania et al., 2009a,b), and land surface albedo (Steinacher, 2011). The LPJ component is driven by global mean CO$_2$ concentrations and changes in surface air temperature relative to a reference period by scaling global mean surface temperature change simulated by the Bern3D with spatial patterns of precipitation and temperature (Steinacher, 2011; Stocker et al., 2011).

**CLIMBER2-LPJmL** CLIMBER2-LPJml (Kleinen et al., 2010) consists of the Earth System Model of Intermediate Complexity (EMIC) CLIMBER2, coupled to the dynamic global vegetation model (DGVM) LPJmL. CLIMBER2 (Petoukhov et al., 2005) consists of a 2.5-dimensional statistical-dynamical atmosphere with a resolution of roughly $51^\circ$ (longitude) by $10^\circ$ (latitude), a zonally averaged ocean resolving three basins with a latitudinal resolution of $2.5^\circ$, and a sea ice model. CLIMBER2 also contains oceanic biogeochemistry, a model for marine biota, and a sediment model (Archer, 1996; Brovkin et al., 2002, 2007). Weathering rates scale to runoff from the land surface. To this EMIC we have coupled the DGVM LPJmL (Sitch et al., 2003; Bondeau et al., 2007; Fader
et al., 2010; Portmann et al., 2008) in order to investigate land surface processes at a significantly higher resolution of 0.5°x0.5°. Agricultural land use is included in this version of LPJ. Monthly anomalies from the climatology of the climate fields are passed to LPJ, where they are added to climate patterns based on the Climatic Research Unit CRU-TS climate data set (New et al., 2000). The carbon flux between atmosphere and land surface is determined from the annual change in the LPJ carbon pools, and employed in CLIMBER2 to determine the CO$_2$ concentration. Biogeochemical feedbacks are thus determined by the combination of CLIMBER2 and LPJmL, while biogeophysical effects are solely determined by CLIMBER2. The climate sensitivity is 3 K.

**DCESS** The DCESS model consists of fully coupled modules for the atmosphere, ocean, ocean sediment, land biosphere and lithosphere (Shaffer et al., 2008). The model geometry consists of one hemisphere, divided into two 360° x 52° zones. Long term climate sensitivity has been calibrated to 3 °C. The atmosphere component considers radiation balance, heat and gas exchanges with other modules, and meridional transport of heat and water vapor between low-mid latitude and high latitude zones. The ocean component is 270° wide and extends from the equator to 70° latitude. Both ocean sectors are divided into 55 layers with 100 m vertical resolution. Each layer is assigned an ocean sediment section, with width determined from observed ocean depth distributions. Sea ice and snow cover are diagnosed from estimated atmospheric temperature profiles. Circulation and mixing are prescribed, with values calibrated from observations as in the HILDA model (Shaffer and Sarmiento, 1995). Biogenic production of particulate organic matter in the ocean surface layer depends on phosphate availability but with lower efficiency in the high latitude zone. The calcite to organic carbon rain ratio depends on surface layer temperature. The ocean sediment component considers calcium carbonate dissolution as well as oxic-anoxic organic matter remineralisation. The land biosphere component includes leaves, wood, litter and soil. Here, it has been modified to include prescribed land use change carbon losses, distributed in proportion to the initial inventory sizes of the module components. With this change, the model CO$_2$ fertilization factor, originally 0.65, has been recalibrated to 0.37. Finally,
the lithosphere component considers outgassing and climate-dependent weathering of carbonate and silicate rocks, as well as rocks containing old organic carbon and phosphorus. The atmospheric methane module was not used here.

**GENIE** The GENIE-1 physical model comprises the 3D frictional geostrophic ocean model GOLDSTEIN, with a resolution of 36 × 36 boxes in the horizontal direction and 16 vertical levels, coupled to a 2D energy moisture balance atmosphere and a thermodynamic-dynamic sea-ice model (Edwards and Marsh, 2005). Recent developments (Marsh et al., 2011) include the incorporation of stratification-dependent mixing, a more general equation of state through a parameterization of thermobaricity, and improvements to the representation of fixed wind forcing. The land surface component is ENTS, a dynamic model of terrestrial carbon storage (Williamson et al., 2006) with a relatively simple implementation of spatiotemporal land use change. Ocean chemistry is modeled with BIOGEM (Ridgwell et al., 2007), including iron limitation (Annan and Hargreaves, 2010), and is coupled to the sediment model SEDGEM with fixed weathering, diagnosed during the model spin-up to simulated observed ocean alkalinity (Ridgwell and Hargreaves, 2007). All GENIE results are derived from ensembles applying the same 20-member parameter set. The selected parameters were filtered from a 100-member, 28-parameter pre-calibrated ensemble, constrained for plausible present-day CO₂ concentrations.

**HadGEM2-ES** HadGEM2-ES (Collins et al., 2011) couples interactive ocean biogeochemistry, terrestrial biogeochemistry and dust, interactive tropospheric chemistry and aerosol components into an update of the physical model HadGEM1. The physical model contains a 40 level 1 × 1 degree, moving to 1/3rd degree at the equator ocean, and a 38 level 1.875 × 1.25 atmosphere (Martin et al., 2011). HadGEM2-ES has been set-up and used to perform all of the CMIP5 simulations as described by (Jones et al., 2011). The ocean biogeochemistry uses the Diat-HadOCC model (Totterdell and Halloran, 2012), an update of HadOCC (Palmer and Totterdell, 2001), now simulating diatom and non-diatom phytoplankton functional types, a single zooplankton, and cycling of nitrogen, silica and iron. Diat-HadOCC is coupled to other earth system components
through the model’s physics, iron supplied through dust, air-sea exchange of CO$_2$ and oceanic emission of dimethylsulphide. The terrestrial carbon cycle is represented by the MOSES2 land surface scheme (Essery et al., 2003) which simulates exchange of water, energy and carbon between the land surface and the atmosphere, and the TRIFFID dynamic global vegetation model (Cox, 2001) which simulates the coverage and competition between 5 plant functional types (broadleaf tree, needleleaf tree, C3 and C4 grass and shrub) and 4 non-vegetated surface types (bare soil, urban, lakes and land-ice).

**LOVECLIM** The Earth system model of intermediate complexity LOVECLIM (version 1.1) (Menviel et al., 2008) links the ECBilt atmosphere, the CLIO sea-ice ocean model and a bucket model for land hydrology with the VECODE dynamic vegetation model and the LOCH ocean carbon model. The atmosphere model (ECBilt) is a spectral T21 model, based on quasigeostrophic equations with 3 vertical levels and a horizontal resolution of about 5.625 × 5.625 degree. Ageostrophic forcing terms are estimated from the vertical motion field and added to the prognostic vorticity equation and thermodynamic equation. The sea ice-ocean component (CLIO) (Goosse et al., 1999) consists of a primitive equation ocean general circulation model with 3 × 3 degree resolution on a partly rotated grid in the North Atlantic. CLIO uses a free surface and is coupled to a thermodynamic-dynamic sea ice model (Fichefet and Maqueda, 1997). In the vertical there are 20 unevenly spaced levels. Mixing along isopycnals, diapycnal mixing, as well as the effect of mesoscale eddies on transports and mixing and downsloping currents at the bottom of continental shelves are parameterized (Goosse et al., 2010). The ocean, atmosphere and sea ice components model are coupled by exchange of momentum, heat and freshwater fluxes. The hydrological cycle over land is closed by a bucket model for soil moisture and simple river runoff scheme. The global dynamic terrestrial vegetation is modeled using VECODE (Brovkin et al., 1997). Annual mean values of precipitation and temperature are communicated to the vegetation from the atmospheric model. On the basis of these mean values the evolution of the vegetation cover described as a fractional distribution of desert, tree, and grass in each land grid

19835
cell is calculated once a year. In the current version, only land albedo (as seen by the atmospheric model) outside the ice sheets is changed by VECODE. LOCH is a three-dimensional global model of the oceanic carbon cycle with prognostic equations for dissolved inorganic carbon, total alkalinity, phosphate, dissolved and particulate organic matter, oxygen and silicates (Goosse et al., 2010; Menviel et al., 2008). The phytoplankton growth is a function of temperature, light and phosphate concentration. The sink term depends on grazing and mortality. Although phytoplankton biomass is a prognostic variable it is not subject to advective transports. Remineralization below the euphotic zone (0–120 m) is a function of oxygen concentrations. Anoxic remineralization can occur in oxygen-depleted areas but is less efficient. The export production is accompanied by the export of opal assuming a constant silicate-to-phosphate ratio. Furthermore CaCO$_3$ (calcite and aragonite) shells are formed as a function of phytoplankton growth. The dissolution of shells occurs in the deepest ocean layer. LOCH is coupled to CLIO, using the same time step. Biogeochemical tracers that are subject to advection and mixing are advected and mixed using the same circulation field and mixing parameters respectively as in CLIO.

**MAGICC6** MAGICC is a reduced-complexity climate model with an upwelling-diffusive-entrainment ocean and is coupled to a simple carbon cycle model including CO$_2$ fertilization and temperature feedback parameterizations of the terrestrial biosphere and oceanic uptake. MAGICC version 6 has been calibrated to AOGCMs (Meehl et al., 2007) and carbon cycle models (Friedlingstein et al., 2006) used in the Fourth IPCC Assessment Report (see Meinshausen et al., 2011a,b for details). Varying the parameters in MAGICC to emulate AOGCM/C4MIP model combinations allows to explore the climate response space in terms of concentrations, radiative forcing, and hemispheric land/ocean surface air temperatures spanned by the range of complex climate models. This version of MAGICC6 was also used to produce harmonized GHG concentrations for the new set of Representative Concentration Pathways (Meinshausen et al., 2011b). For this intercomparison, we used a set of 19 AOGCM calibrations and 9 coupled climate-carbon cycle model calibrations.
MESMO MESMO version 1 (Matsumoto et al., 2008) is based on the C-GOLDSTEIN ocean model (Edwards and Marsh, 2005). It consists of a frictional geostrophic 3-D ocean circulation model coupled to a dynamic-thermodynamic sea ice model and atmospheric model of energy and moisture balance. Ocean production is based on prognostic nutrient uptake kinetics of phosphate and nitrate with dependence on light, mixed layer depth, temperature, and biomass. Interior ocean ventilation is well calibrated against natural radiocarbon on centennial timescale and against transient anthropogenic tracers on decadal time scale. Here MESMO1 is coupled to a simple prognostic land biosphere model (Williamson et al., 2006) that calculates energy, moisture, and carbon exchanges between the land and the atmosphere. Prognostic variables include vegetation and soil carbon as well as land surface albedo and temperature.

MPI-ESM The fully comprehensive Earth System Model MPI-ESM of the Max-Planck-Institute for Meteorology in Hamburg, Germany consists of the atmospheric model ECHAM6 (here in T63L47 resolution) with land surface model JSBACH, (Raddatz et al., 2007). Each land grid cell is divided into tiles covered with 8 natural and 4 anthropogenic PFTs; vegetation model in JSBACH includes an efficient module for vegetation dynamics (Brovkin et al., 2009). Anthropogenic land use is predetermined. The physical ocean model is MPIOM, which further includes a sea-ice model (Marsland et al., 2003) on a nominal 1.5° grid with higher resolution in the North Atlantic. Marine biogeochemistry is represented by the Hamburg Ocean carbon cycle HAMOCC 5.1 which operates on the same grid as MPIOM and includes the full carbonate chemistry and a NPZD type model of the biological pump (Maier-Reimer et al., 2005; Maier-Reimer, 1993). MPI-ESM is used here in the same version that is employed for the CMIP5 experiments “MPI-ESM-LR”. CO₂ is allowed to float freely between the model's carbon reservoirs (i.e. atmosphere, land, and ocean) depending on the state of the compartments and climate-carbon cycle feedbacks are simulated by the model.

NCAR CSM1.4 The physical core of the Climate System Model of the National Centre for Atmospheric Research (NCAR CSM1.4-carbon) (Doney et al., 2006; Fung et al., 2005) is a modified version of the NCAR CSM1.4 coupled physical model, consisting of
ocean, atmosphere, land and sea ice components integrated via a flux coupler without flux adjustments. Atmospheric CO$_2$ is treated as a prognostic variable whose balance is determined by exchange fluxes with the land and ocean. The ocean model includes a derivate of the OCMIP-2 (Ocean Carbon-Cycle Model Intercomparison Project Phase 2) ocean biogeochemistry model (Najjar et al., 2007) with prognostic formulations for marine biological production. The main processes of the organic and inorganic carbon cycle within the ocean and air-sea CO$_2$ flux are included. A parameterization of the marine iron cycle (Doney et al., 2006) considers atmospheric dust deposition/iron dissolution, biological uptake, vertical particle transport and scavenging. Prognostic variables in the ocean include phosphate, dissolved inorganic carbon, alkalinity, oxygen, and dissolved organic phosphorus. The land carbon module combines the NCAR Land Surface Model with a modified version of the terrestrial biogeochemical Carnegie-Ames-Stanford Approach (CASA; Randerson et al., 1997) providing full coupling of energy (via dynamic leaf phenology and hence albedo), water (via transpiration), and carbon cycles of the atmosphere and land. CASA follows the life cycles of plant functional types from carbon assimilation via photosynthesis, to mortality and decomposition, and the return of CO$_2$ to the atmosphere via respiration. NPP is allocated to leafs, roots, and wood with preferred allocation to roots during water-limited conditions and to wood/leaves during light-limited conditions. There are nine soil carbon pools. The transfer rates between them and to the atmosphere are sensitive to soil temperature and soil moisture saturation. The land model does not include other land surface processes that affect atmosphere-biosphere interactions such as an explicit nitrogen cycle, fires and other disturbances, herbivory, dynamic vegetation cover, or anthropogenic land cover change.

**TOTEM2** TOTEM2 (Ver et al., 1999; Mackenzie et al., 2011) is a global biogeochemical model of the life-essential elements carbon, nitrogen, and phosphorus. The model comprises thirteen reservoirs: the atmosphere; six terrestrial reservoirs (living biota, humus, inorganic soil, continental soilwater, shallow groundwater, and lakes); three coastal-zone reservoirs (organic matter, water, and sediments); and three open ocean
reservoirs (organic matter, surface water, and deep water). The coupling of the individual cycles is achieved by the average C:N:P ratios associated with oceanic and terrestrial photosynthesis (Redfield ratios), autorespiration on land and in ocean waters, humus formation, and sedimentation of organic matter in the coastal zone and open ocean. We make a simplifying assumption that these biologically mediated coupling processes apply over many different species and environments, and occur with the same global mean elemental ratios on the decadal to century time scale. All the transfer processes between the model reservoirs are represented by linear or nonlinear equations describing reaction mechanisms and physical transport processes. The model has been shown to reproduce well the atmospheric CO$_2$ concentration for the past 300 yr (Ver et al., 1999).

**UVic ESCM** The UVic ESCM version 2.9 (Eby et al., 2009) consists of a primitive equation 3-D ocean general circulation model coupled to a dynamic-thermodynamic sea-ice model and an atmospheric energy-moisture balance model with dynamical feedbacks (Weaver et al., 2001). The model conserves heat, moisture, and carbon between components to machine precision without flux adjustments. The land surface and terrestrial vegetation components are represented by a simplified version of the Hadley Centre’s MOSES land-surface scheme coupled to the dynamic vegetation model TRIFFID (Meissner et al., 2003). Land carbon fluxes are calculated within MOSES and are allocated to vegetation and soil carbon pools (Matthews et al., 2004). Ocean carbon is simulated by means of an OCMIP-type inorganic carbon-cycle model and a NPZD marine ecosystem model with two nutrients (PO$_4$ and NO$_3$), two phytoplankton classes, and prognostic denitrification (Schmittner and Galbraith, 2008). Sediment processes are represented using an oxic-only model of sediment respiration (Archer, 1996). Terrestrial weathering is diagnosed from the net sediment flux during spin-up and held fixed at the equilibrium pre-industrial value for transient simulations. The model was spun up with boundary conditions from the year 1800 for more than 10 000 yr.
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ACPD
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CO₂ and climate impulse response functions for metric computation
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**Table 1.** Overview on main simulations. All simulations are started from a preindustrial state.

<table>
<thead>
<tr>
<th>Simulation</th>
<th>Model setup</th>
</tr>
</thead>
<tbody>
<tr>
<td>PD100, standard impulse</td>
<td>run 1: Atmospheric CO$_2$ prescribed to follow the historical evolution up to year 2010 and kept at 389 ppm thereafter. Compatible emissions are diagnosed. Non-CO$_2$ and land use forcing constant after 2010.</td>
</tr>
<tr>
<td>run 2: Model is forced with diagnosed emissions from run 1 and atmospheric CO$_2$ is computed. Other forcings as in run 1.</td>
<td>run 2: Model is forced with diagnosed emissions from run 1 and atmospheric CO$_2$ is computed. Other forcings as in run 1.</td>
</tr>
<tr>
<td>run 3: Setup as in run 2. An emission pulse of 100 GtC is added in 2015 AD</td>
<td>run 3: Setup as in run 2. An emission pulse of 100 GtC is added in 2015 AD</td>
</tr>
<tr>
<td>PI100 and PI5000 preindustrial impulses</td>
<td>run 4: Control simulation under preindustrial conditions and freely evolving CO$_2$</td>
</tr>
<tr>
<td>run 5: As run 4. An emission pulse of 100 GtC is added in year 10</td>
<td>run 6: As run 4. An emission pulse of 5000 GtC is added in year 10</td>
</tr>
</tbody>
</table>
Table 2. Characterization of the climate models: physical components, $\Delta T_{2\times}$ denotes the equilibrium climate sensitivity for a nominal doubling of CO$_2$. $\Delta T_{2\times}$ reported here for the Bern3D-LPJ, CLIMBER2, DCESS, LOVECLIM, MESMO1.0, UVic2.9 are those determined by doubling preindustrial CO$_2$ in a simulation over 1000 yr (Eby et al., 2012).

<table>
<thead>
<tr>
<th>Model</th>
<th>Atmosphere</th>
<th>Ocean and Sea ice</th>
<th>Land surface</th>
<th>$\Delta T_{2\times}$ (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ACC2</td>
<td>Land-ocean energy balance model</td>
<td>Diffusion model, simple sea-ice correction factor</td>
<td>Simple land surface albedo parameterization</td>
<td>4.04</td>
</tr>
<tr>
<td>Bern-SAR</td>
<td>1-box</td>
<td>upwelling-diffusion-entrainment model</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>Bern2.5D-LPJ (or Bern2.5CC)</td>
<td>1-dim (zonally and vertically averaged) energy moisture-balance model, $7.5' \times 15'$</td>
<td>2-d friction-geostrophic circulation model with thermodynamic sea ice; 3 ocean basins, connected in Southern Ocean, $7.5' \times 15'$, 14 vertical levels</td>
<td>n/a</td>
<td>3.2</td>
</tr>
<tr>
<td>Bern3D-LPJ</td>
<td>2-dim energy-moisture balance model; $10' \times (3-19')$</td>
<td>3-d friction-geostrophic circulation model with sea ice; $10' \times (3-19')$, 32 levels</td>
<td>1-layer soil temperature, no soil moisture storage, river routing</td>
<td>3.3</td>
</tr>
<tr>
<td>CLIMBER-2-LPjml</td>
<td>3-dim statistical-dynamical model; $10' \times 51'$, 10 layers</td>
<td>2-d friction-geostrophic circulation model with sea ice; $2.5'$, 21 levels</td>
<td>1-layer soil temperature, 2-layer soil hydrology, snow cover, river routing</td>
<td>3.0</td>
</tr>
<tr>
<td>DCESS</td>
<td>2-box energy-moisture balance model</td>
<td>2-box parameterized circulation and exchange, no explicit sea ice; 55 levels</td>
<td>No explicit soil temperature and moisture calculation</td>
<td>2.8</td>
</tr>
<tr>
<td>GENIE</td>
<td>2-dim energy-moisture balance model</td>
<td>3-d friction-geostrophic circulation model with sea ice; $10' \times (3-19')$, 16 levels</td>
<td>1-layer soil temperature, bucket soil moisture model, river routing</td>
<td>4.0 ± 0.8</td>
</tr>
<tr>
<td>HadGEM2-ES</td>
<td>3-d ocean GCM, 1-degree, increasing to 1/3 degree at equator, 40 vertical levels</td>
<td>MOSES-2: tiled land-surface with 4-layer soil temperature and hydrology, river routing</td>
<td>4.58</td>
<td></td>
</tr>
<tr>
<td>LOVECLIM 1.1</td>
<td>3-d quasi-geostrophic circulation model; $5.6' \times 5.6'$, 3 levels</td>
<td>3-d primitive equation circulation model with sea ice; $3' \times 3'$, 20 levels</td>
<td>1-layer soil temperature, bucket soil moisture model, river routing</td>
<td>1.5</td>
</tr>
<tr>
<td>MAGICC6</td>
<td>4-box energy-balance model</td>
<td>2 hemispheric columns, upwelling-diffusion-entrainment, 50 levels, simple sea-ice correction factor</td>
<td>Simple land surface albedo parameterization; soil temperature/moisture only parameterized for permafrost area.</td>
<td>1.9 to 5.7 (Avg. 2.88)</td>
</tr>
<tr>
<td>MESMO 1.0</td>
<td>2-dim energy-moisture balance model; $10' \times (3-19')$</td>
<td>3-d friction-geostrophic circulation model with sea ice; $10' \times (3-19')$, 16 levels</td>
<td>1-layer soil temperature, bucket soil moisture model, river routing</td>
<td>3.7</td>
</tr>
<tr>
<td>MPI-ESM</td>
<td>ECHAM6 3D GCM T63L47</td>
<td>MPIOM 3-d primitive equation GCM + sea ice GR15L40 grid</td>
<td>JSBACH: tiled land-surface, 5-layer soil temperature, 1-layer hydrology, HD river routing model</td>
<td>3.4</td>
</tr>
<tr>
<td>NCAR CSM1.4</td>
<td>CCM3 T31, L18</td>
<td>NCOM 3.6' Ion 0.8–1.8 lat, 25 levels with sea ice</td>
<td>LSM T31</td>
<td>2.0</td>
</tr>
<tr>
<td>TOTEM UVic 2.9</td>
<td>n/a</td>
<td>3-d primitive equation circulation model with dynamic &amp; thermodynamic sea ice $1.8' \times 3.6'$, 19 levels</td>
<td>1-layer soil temperature, complex soil moisture model, river routing</td>
<td>3.6</td>
</tr>
</tbody>
</table>
### Table 3. Characterization of the carbon cycle models.

<table>
<thead>
<tr>
<th>Model</th>
<th>Land Carbon Cycle</th>
<th>Land use (LU)</th>
<th>Marine Biogeochemistry &amp; Ecosystem</th>
<th>Sediment/Weathering</th>
</tr>
</thead>
<tbody>
<tr>
<td>ACC2</td>
<td>4-box, ( \beta )-factor (CO(_2) fertilization) and Q10 temperature sensitivity of soil respiration</td>
<td>n/a</td>
<td>4-box global atmosphere-ocean, temperature-sensitive carbonate chemistry</td>
<td>n/a</td>
</tr>
<tr>
<td>BernSAR</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a (perturbation approach)</td>
<td>n/a</td>
</tr>
<tr>
<td>Bern2D-LPJ(Dyn. Vegetation Model, 9 Plant Functional Types, multiple-litter/soil pools, 3.75° × 2.5°)</td>
<td>n/a</td>
<td>Prognostic export production, P, DIC, DOC, (POC), ALK, O(_2), no ecosystem</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>Bern3D-LPJ(Dyn. Vegetation Model, 9 Plant Functional Types, multiple-litter/soil pools, 3.75° × 2.5°)</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, Si, DIC, DOC,POC ALK, O(_2), no ecosystem</td>
<td>yes/diagnosed</td>
<td></td>
</tr>
<tr>
<td>CLIMBER2-LPJmL(Dyn. Vegetation Model, 9 Plant Functional Types, 12 Crop Functional Types, 0.5° × 0.5°)</td>
<td>n/a</td>
<td>Prognostic export production, P, O(_2), POC Picnic and ALK, no ecosystem</td>
<td>yes/diagnosed</td>
<td></td>
</tr>
<tr>
<td>DCESS</td>
<td>4-box, ( \beta )-factor (CO(_2) fertilization) and Q10 temperature sensitivity of soil respiration</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, DIC, DOC,POC ALK, O(_2), no ecosystem</td>
<td>yes/diagnosed</td>
</tr>
<tr>
<td>GENIE Efficient Numerical Terrestrial Scheme (ENTS).</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, Si, DIC, DOC,POC ALK, O(_2), no ecosystem</td>
<td>yes/diagnosed</td>
<td></td>
</tr>
<tr>
<td>HadGEM2-ES(1 Plant Functional Type; 10° × (3–19)°)</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, DIC, DOC,POC ALK, O(_2), no ecosystem</td>
<td>yes/diagnosed</td>
<td></td>
</tr>
<tr>
<td>LOVECLIM1.1</td>
<td>n/a</td>
<td>Prognostic P, DIC, DOC, ALK, O(_2), export production/no ecosystem</td>
<td>preservation/no</td>
<td></td>
</tr>
<tr>
<td>MAGICC6 4-box global carbon cycle model, calibrated towards 9 CMIP carbon cycle model's pools and fluxes.</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, Si, N, DIC,DOC,POC, ALK, O(_2), no ecosystem</td>
<td>n/a</td>
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</tr>
<tr>
<td>MESMO 1.0 Efficient Numerical Terrestrial Scheme (ENTS).</td>
<td>n/a</td>
<td>Prognostic export production, P, Fe, Si, N, DIC,DOC,POC, ALK, O(_2), no ecosystem</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>MPI-ESM 1 Plant Functional Type; 10° × (3–19)°</td>
<td>n/a</td>
<td>Prescribed 1994 distribution of agricultural land</td>
<td>Full carbonate chemistry, NPZD type ecosystem, PO4, NO3, Fe colimitation of biological production</td>
<td>yes/diagnosed</td>
</tr>
<tr>
<td>NCAR CSM1.4 CASA, prescribed veg. distribution</td>
<td>n/a</td>
<td>Modified OCMIP-2 with prognostic epxort</td>
<td>Modified OCMIP-2 with prognostic epxort</td>
<td>n/a</td>
</tr>
<tr>
<td>TOTEM Global carbon-nitrogen-phosphorus cycle model, explicit treatments of rivers, erosion, fertilizer app</td>
<td>n/a</td>
<td>Global carbon-nitrogen-phosphorus cycle model, explicit treatments of coastal zone</td>
<td>Param/param.</td>
<td></td>
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<tr>
<td>UVic 2.9 Dynamic Vegetation Model, 5 Plant Functional Types, 3.6° × 1.8°, 3 carbon pools per PFT, 1 soil carbon pool</td>
<td>n/a</td>
<td>Prognostic PO4, NO3, O(_2), DIC, ALK, denitrification</td>
<td>yes/diagnosed</td>
<td></td>
</tr>
</tbody>
</table>

**Note:** The table provides a snapshot of the carbon cycle models used in the study, including their basic characteristics and the specific processes they simulate. Each model has unique features such as land carbon cycle types, land use, marine biogeochemistry, ecosystem, and sediment/weathering capabilities. The table is essential for understanding the methodologies and assumptions behind the climate and carbon cycle simulation studies.
Table 4. Time-integrated airborne fraction for different time horizons in units of years and corresponding uncertainty ranges. Multiplication with $1.77 \times 10^{-15}$ Wm$^{-2}$ (kgCO$_2$)$^{-1}$ yields the Absolute Global Warming Potential (AGWP) for CO$_2$. Values in parentheses for the Bern3D-LPJ, GENIE, and MAGICC6 ensembles represent median and 5% to 95% confidence range. The median for each of these models is included in the multi-model mean; reference setup of the Bern3D-LPJ is not included. The errors of the multi-model mean represent ± two standard deviations. Our best estimate for the mean is the multi-model mean and the best estimate for the 5 to 95% confidence range is the average range from the different methods centered at the mean.

<table>
<thead>
<tr>
<th>Time Horizon</th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>time-integrated IRF$_{CO_2}$ (yr)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NCAR CSM1.4</td>
<td>13.8</td>
<td>27.8</td>
<td>46.6</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>HadGEM2-ES</td>
<td>14.8</td>
<td>30.8</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>MPI-ESM</td>
<td>14.2</td>
<td>29.8</td>
<td>48.5</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>Bern3D-LPJ (reference)</td>
<td>15.4</td>
<td>34.3</td>
<td>61.9</td>
<td>241</td>
<td>418</td>
</tr>
<tr>
<td>Bern3D-LPJ ensemble</td>
<td>15.1</td>
<td>32.7</td>
<td>57.6</td>
<td>205</td>
<td>n/a</td>
</tr>
<tr>
<td>(14.0–16.0)</td>
<td>(28.9–36.0)</td>
<td>(48.9–65.6)</td>
<td>(160–265)</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>Bern2.5D-LPJ</td>
<td>13.9</td>
<td>29.7</td>
<td>51.1</td>
<td>163</td>
<td>283</td>
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<tr>
<td>CLIMBER2-LPJ</td>
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<td>26.8</td>
<td>49.2</td>
<td>181</td>
<td>305</td>
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<tr>
<td>DCESS</td>
<td>14.6</td>
<td>31.8</td>
<td>56.3</td>
<td>199</td>
<td>329</td>
</tr>
<tr>
<td>GENIE ensemble</td>
<td>13.6</td>
<td>28.9</td>
<td>50.5</td>
<td>173</td>
<td>n/a</td>
</tr>
<tr>
<td>(10.9–17.6)</td>
<td>(21.7–41.4)</td>
<td>(38.3–77.9)</td>
<td>(143–68–271)</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>LOVECLIM</td>
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<td>27.6</td>
<td>45.3</td>
<td>170</td>
<td>280</td>
</tr>
<tr>
<td>MESMO</td>
<td>15.1</td>
<td>33.6</td>
<td>61.1</td>
<td>238</td>
<td>411</td>
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<tr>
<td>UCI2.9</td>
<td>13.7</td>
<td>29.5</td>
<td>53.0</td>
<td>209</td>
<td>377</td>
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<td>ACC2</td>
<td>13.7</td>
<td>27.9</td>
<td>46.5</td>
<td>151</td>
<td>253</td>
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<tr>
<td>Bern-SAR</td>
<td>14.0</td>
<td>29.0</td>
<td>48.9</td>
<td>161</td>
<td>271</td>
</tr>
<tr>
<td>MAGICC6 ensemble</td>
<td>14.0</td>
<td>29.6</td>
<td>51.8</td>
<td>199</td>
<td>n/a</td>
</tr>
<tr>
<td>(12.0–16.1)</td>
<td>(23.6–35.7)</td>
<td>(40.0–64.2)</td>
<td>(148–233)</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>TOTEM2</td>
<td>16.9</td>
<td>38.3</td>
<td>66.6</td>
<td>180</td>
<td>281</td>
</tr>
<tr>
<td>multi-model mean</td>
<td>14.3 ± 1.8</td>
<td>30.2 ± 5.7</td>
<td>52.4 ± 11.7</td>
<td>186 ± 48</td>
<td>308 ± 95</td>
</tr>
</tbody>
</table>

Uncertainty ranges (yr)

<table>
<thead>
<tr>
<th></th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
</tr>
</thead>
<tbody>
<tr>
<td>multi-model range</td>
<td>3.6</td>
<td>11.4</td>
<td>23.4</td>
<td>96</td>
<td>189</td>
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<tr>
<td>Bern3D-LPJ</td>
<td>2.1</td>
<td>7.2</td>
<td>16.7</td>
<td>105</td>
<td>n/a</td>
</tr>
<tr>
<td>GENIE</td>
<td>6.7</td>
<td>19.8</td>
<td>39.5</td>
<td>128</td>
<td>172</td>
</tr>
<tr>
<td>MAGICC6</td>
<td>4.1</td>
<td>12.1</td>
<td>24.2</td>
<td>85</td>
<td>n/a</td>
</tr>
<tr>
<td>Linear Programming</td>
<td>n/a</td>
<td>n/a</td>
<td>24.0</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>Average of ranges</td>
<td>4.1</td>
<td>12.6</td>
<td>25.6</td>
<td>103</td>
<td>180</td>
</tr>
<tr>
<td>in % of multi-model mean</td>
<td>28.8</td>
<td>41.8</td>
<td>48.8</td>
<td>56</td>
<td>59</td>
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</tbody>
</table>

Best estimates for time-integrated IRF$_{CO_2}$ (yr)

<table>
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<th>5–95% confidence range</th>
</tr>
</thead>
<tbody>
<tr>
<td>mean</td>
<td>14.3</td>
<td>(12.5–16.0)</td>
</tr>
<tr>
<td>5–95% confidence range</td>
<td>30.2</td>
<td>(24.5–35.9)</td>
</tr>
<tr>
<td></td>
<td>52.4</td>
<td>(39.6–65.2)</td>
</tr>
<tr>
<td></td>
<td>186</td>
<td>(138–233)</td>
</tr>
<tr>
<td></td>
<td>308</td>
<td>(214–403)</td>
</tr>
</tbody>
</table>

Best estimates for AGWP of CO$_2$ ($10^{-15}$ yr Wm$^{-2}$ (kgCO$_2$)$^{-1}$)

<table>
<thead>
<tr>
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<th>mean</th>
<th>5–95% confidence range</th>
</tr>
</thead>
<tbody>
<tr>
<td>mean</td>
<td>25.2</td>
<td>(22.1–28.3)</td>
</tr>
<tr>
<td>5–95% confidence range</td>
<td>53.4</td>
<td>(43.4–63.5)</td>
</tr>
<tr>
<td></td>
<td>92.7</td>
<td>(70.1–115)</td>
</tr>
<tr>
<td></td>
<td>328</td>
<td>(244–412)</td>
</tr>
<tr>
<td></td>
<td>546</td>
<td>(379–713)</td>
</tr>
</tbody>
</table>
Table 5. Response in global mean surface air temperature to an emission pulse of 100 GtC added to an atmospheric concentration of 389 ppm.

<table>
<thead>
<tr>
<th>Time Horizon</th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
</tr>
</thead>
<tbody>
<tr>
<td>temperature response (°C)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>NCAR CSM1.4</td>
<td>0.13</td>
<td>0.09</td>
<td>0.09</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>HadGEM2-ES</td>
<td>0.22</td>
<td>0.23</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>MPI-ESM</td>
<td>0.21</td>
<td>0.11</td>
<td>0.15</td>
<td>0.23</td>
<td>0.17</td>
</tr>
<tr>
<td>Bern3D-LPJ (reference)</td>
<td>0.26</td>
<td>0.26</td>
<td>0.24</td>
<td>0.23</td>
<td>0.17</td>
</tr>
<tr>
<td>Bern3D-LPJ ensemble</td>
<td>0.18</td>
<td>0.18</td>
<td>0.17</td>
<td>0.14</td>
<td>n/a</td>
</tr>
<tr>
<td>(0.10–0.27)</td>
<td>(0.10–0.30)</td>
<td>(0.09–0.33)</td>
<td>(0.06–0.39)</td>
<td>n/a</td>
<td></td>
</tr>
<tr>
<td>Bern2.5D-LPJ</td>
<td>0.18</td>
<td>0.17</td>
<td>0.17</td>
<td>0.13</td>
<td>0.13</td>
</tr>
<tr>
<td>CLIMBER2-LPJ</td>
<td>0.16</td>
<td>0.17</td>
<td>0.18</td>
<td>0.12</td>
<td>0.11</td>
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<tr>
<td>DCESS</td>
<td>0.21</td>
<td>0.22</td>
<td>0.21</td>
<td>0.15</td>
<td>0.12</td>
</tr>
<tr>
<td>GENIE ensemble</td>
<td>0.22</td>
<td>0.23</td>
<td>0.22</td>
<td>0.16</td>
<td>n/a</td>
</tr>
<tr>
<td>(0.17–0.35)</td>
<td>(0.17–0.46)</td>
<td>(0.15–0.49)</td>
<td>(0.12–0.29)</td>
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</tr>
<tr>
<td>LOVECLIM</td>
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<td>0.08</td>
<td>0.11</td>
<td>0.07</td>
<td>0.06</td>
</tr>
<tr>
<td>MESMO</td>
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<td>0.27</td>
<td>0.28</td>
<td>0.23</td>
<td>0.2</td>
</tr>
<tr>
<td>UVic2.9</td>
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<td>0.19</td>
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<td>0.19</td>
<td>0.19</td>
</tr>
<tr>
<td>ACC2</td>
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<td>0.12</td>
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</tr>
<tr>
<td>Bern-SAR</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>MAGICC6 ensemble</td>
<td>0.19</td>
<td>0.17</td>
<td>0.16</td>
<td>0.13</td>
<td>n/a</td>
</tr>
<tr>
<td>(0.14–0.26)</td>
<td>(0.12–0.27)</td>
<td>(0.10–0.26)</td>
<td>(0.09–0.26)</td>
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</tr>
<tr>
<td>TOTEM2</td>
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<td>n/a</td>
<td>n/a</td>
<td>n/a</td>
</tr>
<tr>
<td>multi-model mean</td>
<td>0.19 ± 0.10</td>
<td>0.18 ± 0.11</td>
<td>0.17 ± 0.09</td>
<td>0.14 ± 0.08</td>
<td>0.14 ± 0.09</td>
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</tbody>
</table>

Uncertainty ranges (°C)

<table>
<thead>
<tr>
<th></th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
</tr>
</thead>
<tbody>
<tr>
<td>Multi-model range</td>
<td>0.19</td>
<td>0.22</td>
<td>0.19</td>
<td>0.17</td>
<td>0.18</td>
</tr>
<tr>
<td>Bern3D-LPX</td>
<td>0.17</td>
<td>0.21</td>
<td>0.25</td>
<td>0.33</td>
<td>n/a</td>
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<tr>
<td>GENIE</td>
<td>0.18</td>
<td>0.28</td>
<td>0.34</td>
<td>0.16</td>
<td>0.13</td>
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<tr>
<td>MAGICC6</td>
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<td>0.15</td>
<td>0.16</td>
<td>0.17</td>
<td>n/a</td>
</tr>
<tr>
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<td>0.23</td>
<td>0.21</td>
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<tr>
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<td>121</td>
<td>134</td>
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Best estimates for temperature response (°C)

<table>
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<th>5–95 % confidence range</th>
</tr>
</thead>
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<tr>
<td>mean</td>
<td>0.19</td>
<td>(0.09–0.28)</td>
</tr>
<tr>
<td>5–95 % confidence range</td>
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<td>(0.07–0.29)</td>
</tr>
<tr>
<td>0.17</td>
<td>(0.08–0.27)</td>
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</tr>
<tr>
<td>0.14</td>
<td>(0.06–0.23)</td>
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</tr>
<tr>
<td>0.14</td>
<td>(0.05–0.23)</td>
<td></td>
</tr>
</tbody>
</table>

Best estimates for AGTP of CO₂ (10⁻¹⁵ °C (kgCO₂)⁻¹)

<table>
<thead>
<tr>
<th></th>
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<th>5–95 % confidence range</th>
</tr>
</thead>
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<td>0.49 0.46</td>
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<td>5–95 % confidence range</td>
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<tr>
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<td>0.22–0.74</td>
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<tr>
<td>0.16–0.63</td>
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<td></td>
</tr>
<tr>
<td>0.14–0.63</td>
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</tr>
</tbody>
</table>

19860
Table 6. Response in ocean heat content and steric sea level rise to an emission pulse of 100 GtC added to an atmospheric concentration of 389 ppm. Multiplication by \((12/(44 \times 10^{12})\) yields the change per kg CO₂.

<table>
<thead>
<tr>
<th>Time Horizon</th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
</tr>
</thead>
<tbody>
<tr>
<td>Best estimates for steric sea level rise (cm)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>mean</td>
<td>0.84</td>
<td>1.32</td>
<td>1.73</td>
<td>3.58</td>
<td>4.57</td>
</tr>
<tr>
<td>5–95 % confidence range</td>
<td>(−0.1–1.8)</td>
<td>(0.2–2.4)</td>
<td>(0.01–3.5)</td>
<td>(−0.1–7.3)</td>
<td>(1.5–10.6)</td>
</tr>
<tr>
<td>Best estimates for ocean heat content change ((10^{22} \text{ J}))</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>mean</td>
<td>6.69</td>
<td>10.57</td>
<td>14.64</td>
<td>32.15</td>
<td>39.6</td>
</tr>
<tr>
<td>5–95 % confidence range</td>
<td>(3.1–10.3)</td>
<td>(3.0–18.1)</td>
<td>(3.5–25.8)</td>
<td>(10.9–53.4)</td>
<td>(1.0–80.2)</td>
</tr>
</tbody>
</table>
Table 7. Sensitivity of GWP on the time horizon TH and the perturbation life time of a gas.

<table>
<thead>
<tr>
<th>Gas/TH</th>
<th>20 yr</th>
<th>50 yr</th>
<th>100 yr</th>
<th>500 yr</th>
<th>1000 yr</th>
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</thead>
<tbody>
<tr>
<td></td>
<td>life time (yr)</td>
<td>ratio of GWP(TH) to GWP(TH = 100)</td>
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<tr>
<td>CH₄</td>
<td>12</td>
<td>2.97</td>
<td>1.71</td>
<td>1.00</td>
<td>0.28</td>
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<tr>
<td>N₂O</td>
<td>114</td>
<td>1.01</td>
<td>1.05</td>
<td>1.00</td>
<td>0.48</td>
</tr>
<tr>
<td>SF₆</td>
<td>3200</td>
<td>0.74</td>
<td>0.87</td>
<td>1.00</td>
<td>1.33</td>
</tr>
</tbody>
</table>
Fig. 1. (a) The evolution of the impulse response function for CO$_2$, IRF$_{\text{CO}_2}$, for an emission pulse of 100 GtC added to an atmospheric background concentration of 389 ppm (PD100) for a range of Earth System Models (thick solid), EMICs (dashed and thin solid), and reduced-form models (dotted). The multi-model mean, computed by giving each available model equal weight, and the corresponding ± two standard deviation range is shown by the black solid line and the grey shading. Note that not all models were run to year 1000 and thus the number of models included in the average changes with time. For three models, Bern3D-LPJ (red), GENIE (brown) and MAGICC6 (green), an ensemble of simulations is available and the ensemble median and 5 to 95 % confidence intervals are given by error bars for year 20, 100, and 500. Only the ensemble medians are included in the multi-model mean and range. (b) Same as (a) but for the time-integrated IRF$_{\text{CO}_2}$. 
Fig. 2. As Fig. 1 but for the perturbation in global mean surface air temperature (a), in ocean heat content (b), and in steric sea level rise (c). Results are for a CO$_2$ emission pulse of 100 GtC added to a current CO$_2$ concentration of 389 ppm (PD100). We note that the signal-to-noise ratio is small for the models that feature a dynamic atmosphere (HadGEM2-ES, MPI-ESM, NCAR-CSM1.4, and LOVECLIM) and the plotted evolutions for these models represent both the forced response and a contribution from the models’ internal (unforced) climate variability. Small abrupt changes in the multi-model mean and confidence range arise from a change in the number of model simulations; different groups run their model over different periods, pending on CPU availability.
Fig. 3. As Fig. 1, but for the time-integrated perturbation in air-to-sea (a) and air-to-land biosphere carbon fluxes (b). Results are for a CO$_2$ emission pulse of 100 GtC added to a present day CO$_2$ concentration of 389 ppm (PD100).
Fig. 4. Influence of the background conditions on the climate-carbon cycle response to a pulse emission of 100 GtC into the atmosphere. Solid lines are for current conditions (CO$_2$,ref = 389 ppm, PD100) and dashed lines for preindustrial conditions (CO$_2$,ref ~ 280 ppm, PI100).
Fig. 5. Response of the carbon cycle-climate system to a pulse emission of 5000 GtC (solid, PI5000) and 100 GtC (dashed, PI100) added to the atmosphere under preindustrial conditions.
Fig. 6. Influence of pulse size and climate-carbon cycle feedback on the response in atmospheric CO$_2$ and the time-integrated IRF$_{CO_2}$ as simulated with the Bern3D-LPJ model (standard setup). Pulse emissions, ranging from 10 to 10 000 Gt C in the individual simulations, are added to the atmosphere under preindustrial conditions. Dashed lines represent simulations where climate was kept constant in the model.
Fig. 7. The impulse response function for CO₂ (IRF_{CO₂}) as used to compute GWP in the IPCC First (FAR), Second (SAR) and Fourth (AR4) Assessment Report and from this study. The red curve is a fit to the multi-model mean shown in black. The inset shows the time-integrated IRF_{CO₂} for the first 100 yr after the emission pulse.