Differences between downscaling with spectral and grid nudging using WRF

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Abstract

Dynamical downscaling has been extensively used to study regional climate forced by large-scale global climate models. During the downscaling process, however, the simulation of regional climate models (RCMs) tends to drift away from the driving fields. Developing a solution that addresses this issue, by retaining the large scale features (from the large-scale fields) and the small-scale features (from the RCMs) has led to the development of “nudging” techniques. Here, we examine the performance of two nudging techniques, grid and spectral nudging, in the downscaling of NCEP/NCAR data using Weather Research and Forecasting (WRF) Model. The simulations are compared against the results with North America Regional Reanalysis (NARR) data set at different scales of interest. We show that with the appropriate choice of wave numbers, spectral nudging outperforms grid nudging in the capacity of balancing the performance of simulation at the large and small scales.

1 Introduction

Global climate models (GCMs) serve as the primary tool to understand how global climate will respond to emissions (IPCC, 2007). Information on regional scales, however, may be unreliable at scales below about 200 km (Meehl et al., 2007), which is still too coarse to be directly used in regional climate impact studies (Houghton et al., 2001). Downscaling of global model results has been used to address this issue by bridging the gap of scales between the global and regional climate information. Downscaling can be achieved by statistical methods (called statistical downscaling) or by high-resolution regional climate models (RCMs) (called dynamical downscaling).

Dynamical downscaling has been at the forefront of model development of regional climate models (e.g., Dickinson et al., 1989), and now is being used to address how regional air quality would change in future climate. In the process of dynamical downscaling, errors are introduced primarily in two ways. One is due to incomplete model
physics. The other type of error results from the downscaling itself. For example, dynamical downscaling typically starts with a set of coarse-resolution large-scale fields, which are used as the initial conditions (ICs) and lateral and surface boundary conditions (LBCs) for the RCMs. As the simulation evolves, the internal solution developed by RCMs may be affected by the size of domain, the spin-up period and update frequency of LBCs. A good summary of such issues are provided by Warner et al. (1997), Giorgi and Mearns (1999) and Denis et al. (2002).

A key source of downscaling errors is the inconsistency along boundaries (Davies, 1976, 1983) since RCM simulation drifts away from the GCMs driving fields. It has been a challenge to balance the performance of RCMs in adding small-scale features and simultaneously retaining the large-scale features. Nudging techniques are introduced to RCMs to address this issue. A nudging term is added to the predictive equation of the variable to be nudged in its grid-point model. Davies (1976) introduced the lateral boundary relaxation technique, in which the solution of RCM is nudged to the driving field in a “buffer zone” along boundaries. However, this technique is still unable to fulfill the goal of retaining the large-scale information provided by GCMs at the interior of the modeling domain. In order to capture the features of the driving force through the domain, grid nudging (Stauffer and Seaman, 1990) was developed and has been applied to downscaling reanalysis data for regional air quality modeling of historical episodes. In this technique, nudging is conducted in every grid cell. Another nudging technique that has gained interest is spectral nudging (Waldron et al., 1996; von Storch et al., 2000), in which the nudging term is spectrally expanded in both the zonal and meridional directions and only the waves under selected wave numbers are kept in the nudging term. All other waves are filtered out. By keeping the long waves in the nudging term, Miguez-Macho et al. (2004, 2005) found that spectral nudging can help to eliminate the large-scale bias in precipitation patterns, and, at the same time, maintain the features of small scale.

Studies have used dynamical downscaling for the purpose of regional air quality modeling (e.g., Forkel and Knoche, 2006; Gustafson and Leung, 2007; Hogrefe et al.,...
2004; Leung and Gustafson, 2005; Steiner et al., 2006; Tagaris and Liao, et al., 2008), using boundary (Davies, 1976), grid nudging (Stauffer and Seaman, 1990), or no nudging at all. However, spectral nudging may have an advantage over boundary nudging (von Storch et al., 2000; Rockel et al., 2008), and could theoretically outperform grid nudging. From the perspective of spectrum, grid nudging modifies the RCMs results throughout the spectrum with the same strength, however, the short-wave information provided by RCMs is thought to be more reliable than that provided by GCMs. Therefore, grid nudging has the risk of over-forcing the RCMs at small scales. However, few studies discuss the comparison between grid and spectral nudging and how to determine optimal cut-off wave numbers for spectral nudging. This study aims at improving the performance of downscaling using spectral nudging, with a particular focus on developing regional-scale fields for assessing the impact of climate change on air quality. The main difficulties involve how to evaluate the results between grid and spectral nudging and how to determine the appropriate wave numbers for spectral nudging. We use NCEP/NCAR reanalysis data for four historical periods and Weather Research and Forecasting (WRF) Model (Skamarock et al., 2008) to address these issues. The NCEP/NCAR data is used both to provide the information needed for downscaling and to evaluate the downscaling results.

2 Method

The 2.5 × 2.5 degree NCEP/NCAR reanalysis data archived every 6 h is utilized to drive the WRF (version 3.1.1) downscaling. We compare results developed using grid and spectral nudging for four episodes: July 2009, October 2009, January 2010 and April 2010. The modeling domain covers the CONtiguous United States (CONUS) and portions of southern Canada and northern Mexico and is centered at 40° N and 97° W with dimensions of 162 × 126 horizontal grids cells with a grid-spacing of 36 km. It contains 35 vertical levels, with the top pressure of 5000 pa.
Physical configurations in WRF are kept the same, except the nudging (FDDA) technique employed. Both grid and spectral nudging are configured to nudge temperature and horizontal winds, but water vapor mixing ratio can only be nudged in grid nudging, and geo-potential height only in spectral nudging. Only horizontal winds are nudged at all vertical levels, while no nudging is conducted for other variables within the planetary boundary layer (PBL). The nudging coefficients for all variables for both grid and spectral nudging are set to be $0.0003 \, \text{s}^{-1}$ (Stauffer et al., 1985; Stauffer and Seaman, 1990). During the simulation, nudging is conducted every 6 h consistent with the frequency of the NCEP/NCAR reanalysis data. When spectral nudging is conducted, all waves with wave numbers greater than the preset wave number are filtered. In other words, no nudging is conducted for those waves. In this study, the wave number in both directions is set to be 3 ($m = n = 3$, where $m$ and $n$ represent the wave number in zonal and meridional directions, respectively). This preliminary choice is made based on two considerations. One is the scale of driving field, in which the GCM is able to provide reliable information and this information is also expected to be captured by RCM. von Storch et al. (2000) determined that scales of about $15^\circ$ and larger are considered to be reliably analyzed by NCEP. The other consideration is the size of WRF domain. In our study, the WRF domain size is about $6000 \times 4600$ km in zonal and meridional direction, respectively. Hence, wave number 3 is employed as the first choice in both directions in order to capture NCEP/NCAR features of scale about 2000 km. Sensitivity tests on cut-off wave number choice are conducted.

3 Results

3.1 Evaluation methods

The concept of similarity is used to evaluate the results at different scales, using a metric, $P(t)$, proposed by von Storch et al. (2000):
where $P(t)$ is the similarity at time $t$, $\Psi(t)$ is the input field (e.g., the NCEP/NCAR data), $\Psi^*(t)$ the output field (e.g., the WRF output), $< >$ the spatial average over the modeling domain, and $t$ the simulation time. Similarity at different scales of interest is calculated every six hours just after the nudging is updated by calculating the representative values of $\Psi(t)$ and $\Psi^*(t)$ at different scales. The performance of downscaling in large and small scales is evaluated in the opposite way with respect to similarity using Eq. (1). For large scales, it is better when the downsampling results are more consistent with the input fields, so higher similarities are desired; while for small scales, the results are better when more variance is added, so lower similarities are desired.

The question arises as to how the large and small scales are determined. As mentioned previously, information at about $15^\circ$ and larger is considered to be reliably analyzed by NCEP. Accordingly, 2000 km and larger is chosen as the “large scale”. At this scale, when comparing WRF output with NCEP/NCAR input data, the higher the similarity is, the RCM is viewed as performing better. As to the “small scale”, instead of the WRF resolution of 36 km, 300 km is chosen in order to capture features that occur at multiple grids, which are more reliably captured by RCMs than individual grid cells. And compared to the NCEP/NCAR data, 300 km is a small scale, and the RCMs should be adding details. Therefore, 300 km is chosen as the “small scale” and lower similarities are desired.

The calculation of similarity at 2000 or 300 km involves three steps. First, the WRF input field, namely the NCEP/NCAR data, is interpolated to the same resolution as the WRF results. Second, grid cells of 36 km resolution in the modeling domain are re-divided according to the scale of interest so that each new “aggregated” cell includes multiple original grid cells. For each new cell, its representative values of input and output fields, namely $\Psi(t)$ and $\Psi^*(t)$ in Eq. (1), are derived by the spatial average of the
NCEP/NCAR data and WRF results of the cells of 36 km resolution. Finally, similarity is calculated by Eq. (1). At the large-scale case, for instance, the NCEP/NCAR $2.5 \times 2.5$ degree data is first interpolated to a 36 km resolution, so that for both input and output fields, the modeling domain includes 162 (zonal) by 126 (meridional) cells. Because we are concerned about the features at the scale of about 2000 km, the modeling domain could be re-divided into $3 \times 3$ new cells, each of which has $54 \times 42$ original cells, and then $\Psi(t)$ and $\Psi^*(t)$ at the scale of 2000 km are calculated by averaging the $54 \times 42$ cells of input and output fields, respectively.

Another important question is whether the decrease in similarity at the small scale is of reasonable magnitude. In other words, if spectral nudging with the current choice of wave numbers, still leaves too much freedom for the RCM and makes the similarity decrease too much at the small scale, or does it still over-force the results and make the similarity decrease inadequately. To answer this question, the 32 km resolution North America Regional Reanalysis (NARR) data set (Mesinger et al., 2006) is used to assess the appropriate level of similarity decrease between large and small scales. The quality of NARR data has been evaluated with surface station and sounding measurements (Mesinger et al., 2006). In one case, if NARR data set is consistent with NCEP/NCAR data at the large scale, which means similarities between these two data set are high, NARR data set is viewed as the best result we could have after downscaling from NCEP/NCAR data, and the similarity between NCEP/NCAR and NARR data at the small scale could serve as the criteria for a reasonable range of similarity for the small-scale results. In the other case, if the NARR data set can not provide enough high similarity at the large scale, which means similarity between NCEP/NCAR and NARR is much lower than that between NCEP/NCAR and WRF downscaling results, similarity between NCEP/NCAR and NARR in small scale can not be used directly as the criteria. Instead, the difference of similarity between large and small scale would be used as the reference when assessing whether the change in similarity between input and downscaled fields is reasonable.
3.2 Similarity at different scales for grid and spectral nudging

Since our ultimate goal is to use the downscaled meteorological fields to drive a regional chemical transport model, we are especially concerned about the fields that will significantly affect the concentration of pollutants. Therefore, we investigate temperature, horizontal kinetic energy (as a surrogate for wind speed), and water vapor mixing ratio; analysis is carried out at three vertical levels, the surface, 850 and 500 hpa. Only the results of July 2009 are shown here, since other tested episodes give similar results.

Temperature is nudged in both grid and spectral nudging. At 850 hpa, at the large scale, spectral and grid nudging results have high similarities (Fig. 1a) through the simulation period. For example, the means of similarity \( P(t) \) at the large scale (as summarized in Table 1) is over 0.99999 for both. Hence, the spatial averaged relative difference of temperature is less than the square root of 0.000001, or 0.3\%, which means at the large scale, both of the nudging techniques are equally capable of capturing the features of the driving fields. This is not the same at small scales. Spectral nudging gives a much lower similarity than grid nudging at small scale. As mentioned before, at the small scale, lower similarity is expected because variance is expected to be added by the RCM, and similarity between the NCEP/NCAR and NARR data (Fig. 1b) is calculated to determine whether or not the lower similarities given by nudging techniques at the small scale are consistent with using NARR data. The decrease in similarity for NCEP/NCAR and NARR data between large and small scale indicates that at the small scale, spectral nudging performs better than grid nudging because of a lower similarity. The results at 500 hpa are very similar to the results at 850 hpa (Table 1), except that the difference of similarity between grid and spectral nudging is even smaller in the magnitude. At the small scale, for instance, the difference of the mean between the two nudging techniques is on the order of \( 10^{-6} \), and the difference of standard deviation of similarity on the order of \( 10^{-7} \). We have to ask does the small difference in similarity really matter? In other words, we want to know if the similarity
is still able to be used to assess the performance of downscaling, or it is just noise when the difference of similarity is very small. To answer this question, we compare the probability distribution of the temperature difference between the NCEP/NCAR data and the WRF output (by grid and spectral nudging, respectively) with the distribution of temperature difference between NCEP/NCAR data and NARR data (Table 2). Changing from the large to small scale, the width of the distribution provided by grid nudging changes little compared with spectral nudging and NARR data, which indicates that for the temperature field at 500hpa, grid nudging over-forces the RCM results towards the driving fields and the small-scale features expected from RCM are hindered. To further investigate whether the larger variance provided by spectral nudging is reasonable or not, the correlation between WRF output and NARR data is investigated by orthogonal regression (Fig. 2). At the small scale, spectral nudging improves the correlation with NARR data compared with grid nudging by giving a slope more close to 1. Other regression methods, such as least square regression, are also tested and we get consistent results. The results above indicate that the metric of similarity at different scales is important in evaluating the performance of downscaling, even when the difference between similarity values is very small. At the surface, grid and spectral nudging show little difference in similarity, which is not unexpected because no nudging of temperature is conducted within the PBL.

Spectral nudging, likewise, performs better than grid nudging for horizontal kinetic energy (KE) with comparable similarity at the large scale and lower similarity at the small scale at both 850 hpa (Fig. 3) and 500 hpa (Table 1), consistent with NARR. The improvement in the decrease of similarity implies significant differences of the nudged variable between grid and spectral nudging. For example, at 500 hpa (Table 1), grid nudging leads to a mean KE similarity of 0.997 at the small scale; while spectral nudging decreases the mean of similarity to 0.940. The kinetic energy difference between grid and spectral nudging is around 20%. In addition, at the small scale, the similarity found using spectral nudging varies temporally with the same trend as that of NCEP/NCAR and NARR data (Fig. 3), However, the similarity found using grid nudging
shows little such variability. The variance of similarity (Table 1) also indicates that at small scale, spectral nudging performs better than grid nudging in the magnitude of variability. The results at the surface are similar to those at 500 and 850 hpa (Table 1).

Different similarities for KE suggest that the results from grid and spectral nudging can be very different for fields closely related to KE, such as clouds and precipitation, both of which are important in regional air quality modeling. Cloud hydrometeor mixing ratios provided by WRF are used to calculate the monthly averaged mass of cloud (including cloud water, cloud rain, ice, snow and graup) in each column and compared with the convective cloud fraction averaged from NARR data archived every 3 h. The convective cloud instead of total cloud from NARR data is used for comparison because the horizontal resolution of WRF in this study is not high enough to explicitly resolve such clouds. The two nudging techniques lead to greater differences over the middle and the eastern regions of the US, with spectral nudging better capturing the cloud features (Fig. 4). This becomes more apparent when comparing the precipitation with NARR data (Fig. 4). In the southeast, results from spectral nudging more closely resemble NARR data than grid nudging by moving the rain belt eastward. Another field closely related to KE is surface pressure. Similarities of surface pressure at different scales are calculated and compared with the similarities of NARR data (Table 1), with little difference in the mean and standard deviation of similarity between grid and spectral nudging. The spatially averaged change in surface pressure is on the order of 10 Pa between the large and small scales (Eq. 1). However, the similarity between NCEP/NCAR and NARR data shows that the change in surface pressure is of magnitude of 100 Pa between the large and small scales. Therefore, nudging does not impact the surface pressure significantly, although spectral nudging improves the simulated KE at the small scale.

Grid nudging, not spectral nudging, is applied to water vapor mixing ratio in WRF version 3.1.1. If spectral nudging is used, the correction to water vapor mixing ratio results from the changes in other fields. At the large scale, the similarity using spectral nudging is still as high as that by grid nudging at the surface and 850 hpa (Table 1).
At 500 hpa, however, spectral nudging does not maintain the large-scale features as well as grid nudging (Fig. 5a), although the similarity of grid and spectral nudging at 500 hpa differs little for temperature and horizontal kinetic energy. This can be linked to the prediction of cloud formation, which is at a scale smaller than that is captured by the GCM, and is very sensitive to a number of local factors. At the small scale, for all the vertical layers of interest, spectral nudging provides the desired decrease in similarity of water vapor mixing ratio as compared to NARR; while for grid nudging, little difference occurs at small and large scales (Table 1).

Spectral nudging was found to perform better for the July 2009 episode than for January 2010 when compared to the similarity between NCEP/NCAR and NARR data. This relates to errors accumulated in the boundary regions (Noguer et al., 1998; Staniforth, 1997). In summer, when the boundary forcing is weaker, bias in the boundary regions accumulates and interacts with circulation and alters the large-scale flow over the domain. Spectral nudging is able to correct this error. In winter, bias may not show a large-scale pattern as strong as that in summer. Hence, the correction made by spectral nudging is not as effective.

### 3.3 Sensitivity to wave numbers in spectral nudging

Choice of wave numbers in spectral nudging impacts the quality of downscaling. If the wave number is too large, which means the nudging term includes all the longer waves under the selected wave numbers, the results of spectral nudging would approach grid nudging, because the results are overly forced at the smaller scale. If the wave number is too small, the long waves included in the nudging term may not be able to represent enough energy to force the RCMs to replicate the large scale features. Here, we conduct a sensitivity test to investigate how the fields of interest respond to changes in wave numbers.

In our initial tests, the wave numbers for spectral nudging were 3 in both zonal and meridional directions. Here, wave number sets of $m = n = 2$ and $m = n = 6$ ($m$ and $n$ represent the wave number in zonal and meridional direction, respectively) are tested.
as applied to the four episodes simulated and the similarity at the large and small scales are investigated. For the horizontal kinetic energy, at both large and small scales (Fig. 6), when the wave numbers decrease, the ability of spectral nudging to follow large scale features becomes weaker as the similarity markedly decreases; while when wave numbers increase, the performance of spectral nudging approaches grid nudging by giving high similarity values, particularly at the small scale. The results suggest that similarity at the small scale is more sensitive to wave number choice than that at the large scale. Therefore, smaller wave numbers are preferred as long as the features at the large scales of interest can be captured. The choice of wave number had little impact on temperature and water vapor.

4 Conclusions

Compared with grid nudging, spectral nudging provides a better balance between the need to keep RCM results consistent with the large scale driving forces that would be provided by GCMs, and at the same time, allows more variance added at the smaller scales. The performance of spectral nudging is very good for temperature and horizontal kinetic energy at 850 and 500 hpa. In addition, the improvement at the small scale allowed by spectral nudging is not only reflected in spatial variability, but temporal variability as well.

In order to take the advantage of spectral nudging, appropriate wave numbers should be chosen and sensitivity analysis should be conducted. The results of sensitivity tests show that for the case studied here, the choice of wave numbers set at $m = n = 3$, or wave lengths of about 2000 km is well supported. The choice of wave numbers is determined by the size of modeling domain and the scale of driving forces that RCMs should retain. Results suggest that the similarity at the small scale is more sensitive to wave numbers than that at the large scale, and as wave numbers increase, spectral nudging performs more similarly to grid nudging and begins to over-force the RCMs results at the small scale. Therefore, smaller wave numbers are preferred so long as the large-scale features are captured.
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Table 1. Summary of the Mean and Standard Deviation of Similarities for Temperature, Kinetic Energy (KE), Surface Pressure and Water Vapor Mixing Ratio (QV) of July 2009 at Different Scales.

<table>
<thead>
<tr>
<th>Fields</th>
<th>Scale of 2000 km</th>
<th>Scale of 300 km</th>
<th>Scale of 2000 km</th>
<th>Scale of 300 km</th>
<th>Scale of 2000 km</th>
<th>Scale of 300 km</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_s$</td>
<td>$0.99999 \pm 0.8 \times 10^{-5}$</td>
<td>$0.99995 \pm 1.6 \times 10^{-5}$</td>
<td>$0.99999 \pm 0.5 \times 10^{-5}$</td>
<td>$0.99995 \pm 1.3 \times 10^{-5}$</td>
<td>$0.99998 \pm 1.0 \times 10^{-5}$</td>
<td>$0.99994 \pm 1.9 \times 10^{-5}$</td>
</tr>
<tr>
<td>$T_{850}$</td>
<td>$0.99999 \pm 1.0 \times 10^{-6}$</td>
<td>$0.99999 \pm 5.4 \times 10^{-6}$</td>
<td>$0.99999 \pm 1.4 \times 10^{-6}$</td>
<td>$0.99998 \pm 4.7 \times 10^{-6}$</td>
<td>$0.99992 \pm 3.8 \times 10^{-6}$</td>
<td>$0.99997 \pm 6.7 \times 10^{-6}$</td>
</tr>
<tr>
<td>$T_{500}$</td>
<td>$1.00000 \pm 0.1 \times 10^{-6}$</td>
<td>$0.99999 \pm 0.2 \times 10^{-6}$</td>
<td>$1.00000 \pm 0.1 \times 10^{-6}$</td>
<td>$0.99997 \pm 0.7 \times 10^{-6}$</td>
<td>$0.99999 \pm 1.6 \times 10^{-6}$</td>
<td>$0.99999 \pm 2.4 \times 10^{-6}$</td>
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<td>KE$_s$</td>
<td>$0.98 \pm 0.9 \times 10^{-2}$</td>
<td>$0.94 \pm 1.7 \times 10^{-2}$</td>
<td>$0.94 \pm 3.4 \times 10^{-2}$</td>
<td>$0.83 \pm 5.8 \times 10^{-2}$</td>
<td>$0.90 \pm 5.3 \times 10^{-2}$</td>
<td>$0.76 \pm 7.8 \times 10^{-2}$</td>
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<tr>
<td>KE$_{850}$</td>
<td>$0.10 \pm 0.5 \times 10^{-2}$</td>
<td>$0.99 \pm 0.7 \times 10^{-2}$</td>
<td>$0.97 \pm 1.9 \times 10^{-2}$</td>
<td>$0.84 \pm 5.7 \times 10^{-2}$</td>
<td>$0.97 \pm 1.4 \times 10^{-2}$</td>
<td>$0.84 \pm 4.5 \times 10^{-2}$</td>
</tr>
<tr>
<td>KE$_{500}$</td>
<td>$0.99 \pm 0.5 \times 10^{-3}$</td>
<td>$0.97 \pm 0.9 \times 10^{-3}$</td>
<td>$0.99 \pm 3.3 \times 10^{-3}$</td>
<td>$0.94 \pm 2.1 \times 10^{-2}$</td>
<td>$0.993 \pm 4.5 \times 10^{-3}$</td>
<td>$0.940 \pm 2.1 \times 10^{-2}$</td>
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<tr>
<td>$P_s$</td>
<td>$0.999999 \pm 1.7 \times 10^{-7}$</td>
<td>$0.999994 \pm 2.1 \times 10^{-7}$</td>
<td>$0.9999998 \pm 1.8 \times 10^{-7}$</td>
<td>$0.9999992 \pm 2.4 \times 10^{-7}$</td>
<td>$0.999999 \pm 3.8 \times 10^{-7}$</td>
<td>$0.9999913 \pm 6.5 \times 10^{-7}$</td>
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<tr>
<td>QV$_s$</td>
<td>$0.993 \pm 4.3 \times 10^{-3}$</td>
<td>$0.986 \pm 7.3 \times 10^{-3}$</td>
<td>$0.990 \pm 5.4 \times 10^{-3}$</td>
<td>$0.979 \pm 8.8 \times 10^{-3}$</td>
<td>$0.994 \pm 3.5 \times 10^{-3}$</td>
<td>$0.981 \pm 6.9 \times 10^{-3}$</td>
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<tr>
<td>QV$_{850}$</td>
<td>$0.999 \pm 1.8 \times 10^{-3}$</td>
<td>$0.991 \pm 6.6 \times 10^{-3}$</td>
<td>$0.996 \pm 1.4 \times 10^{-3}$</td>
<td>$0.969 \pm 7.5 \times 10^{-3}$</td>
<td>$0.994 \pm 2.2 \times 10^{-3}$</td>
<td>$0.967 \pm 6.4 \times 10^{-3}$</td>
</tr>
<tr>
<td>QV$_{500}$</td>
<td>$1.000 \pm 0.8 \times 10^{-3}$</td>
<td>$0.996 \pm 3.2 \times 10^{-3}$</td>
<td>$0.970 \pm 1.7 \times 10^{-2}$</td>
<td>$0.880 \pm 2.6 \times 10^{-2}$</td>
<td>$0.992 \pm 4.6 \times 10^{-3}$</td>
<td>$0.950 \pm 1.4 \times 10^{-2}$</td>
</tr>
</tbody>
</table>

Subscripts “s”, 850 and 500 stand for surface, 850 and 500 hpa.
Table 2. Summary of the Mean and Standard Deviation (SD) of the Distribution of Temperature Difference at 500 hpa of July 2009 at Different Scales.

<table>
<thead>
<tr>
<th>Data set</th>
<th>at the Scale of 2000 km</th>
<th>at the Scale of 300 km</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Mean (K)</td>
<td>SD (K)</td>
</tr>
<tr>
<td>NARR minus NCEP/NCAR</td>
<td>−0.11</td>
<td>0.533</td>
</tr>
<tr>
<td>Grid Nudging minus NCEP/NCAR</td>
<td>−0.09</td>
<td>0.173</td>
</tr>
<tr>
<td>Spectral Nudging minus NCEP/NCAR</td>
<td>−0.08</td>
<td>0.209</td>
</tr>
</tbody>
</table>
Fig. 1. Time series plots of similarity for temperature at 850 hpa at 2000 km and 300 km scales for July 2009. (a) Similarity between NCEP/NCAP and downscaling results by WRF by grid and spectral nudging; (b) similarity between NCEP/NCAR and NARR data.
Fig. 2. Correlation for the temperature anomaly from NCEP/NCAR data at 500 hpa at 2000 km and 300 km scales for July 2009 with linear regression of 95% confidence. (a) Anomaly of WRF output by spectral nudging vs. anomaly of NARR data; (b) anomaly of WRF output by grid nudging vs. anomaly of NARR data.
Fig. 3. Time series plots of similarity for horizontal kinetic energy at 850 hpa at 2000 and 300 km scales for July 2009. (a) Similarity between NCEP/NCAP and downscaling results by WRF by grid and spectral nudging; (b) similarity between NCEP/NCAR and NARR data.
Fig. 4. Comparison of monthly averaged cloud fraction and monthly accumulated precipitation using WRF and NARR data for July 2009. (a) Convective cloud fraction of NARR; (b) column cloud water of WRF using spectral nudging; (c) column cloud water of WRF using grid nudging; (d) accumulated precipitation of NARR; (e) accumulated precipitation of WRF using spectral nudging; (f) accumulated precipitation of WRF using grid nudging.
**Fig. 5.** Time series plots of similarity for water vapor mixing ratio at 500 hpa at 2000 and 300 km scales for July 2009. (a) Similarity between NCEP/NCAP and downscaling results by WRF by grid and spectral nudging; (b) similarity between NCEP/NCAR and NARR data set.
Fig. 6. Time series plots of similarity of horizontal kinetic energy at 850 hpa for January 2010 by spectral nudging with different wave numbers. (a) Similarity between NCEP/NCAP and downscaling results by WRF at 2000 km scale; (b) similarity results at 300 km scale. $m$ and $n$ represent the wave number in zonal and meridional direction, respectively.