Radiative forcing estimates of sulfate aerosol in coupled climate-chemistry models with emphasis on the role of the temporal variability

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Abstract

This paper describes the impact on the sulfate aerosol radiative effects of coupling the radiative code of a global circulation model with a chemistry-aerosol module. With this coupling, temporal variations of sulfate aerosol concentrations influence the estimate of aerosol radiative impacts. Effects of this coupling have been assessed on net fluxes, radiative forcing and temperature for direct and first indirect effects of sulfate.

The direct effect responds almost linearly to rapid changes in concentrations whereas, the first indirect effect shows a strong non-linearity. In particular, sulfate temporal variability causes a large modification of the short wave net fluxes at the top of the atmosphere of +0.24 and +0.22 W.m⁻² for respectively the present and preindustrial periods. This change is small compared to the value of the net flux at the top of the atmosphere (about 240 W.m⁻²). However, it corresponds to about 10% of the total anthropogenic radiative forcing for the 20th century.

The effect is more important in regions with low-level clouds and intermediate sulfate aerosol concentrations (from 0.1 to 0.8 µg(SO₄) m⁻³ in our model).

If computation of the aerosol direct radiative forcing is quite straightforward and has few effects; quantifying the first indirect radiative forcing requires first to tackle technical issues.

We show that preindustrial sulfate concentrations have to be calculated with the same meteorological trajectory used for computing present ones. If this condition is not satisfied, it introduces a 60% error on the estimation of the first indirect radiative forcing. Solutions are proposed to assess radiative forcing properly. In the reference method, the coupling between chemistry and climate results in a global average increase of 8% in the first indirect radiative
forcing. This change reaches 50% in the most sensitive regions. However, the reference method isn’t suited to run long climate simulations. We present other methods that are simpler to implement in a coupled chemistry/climate model and that offer the possibility to assess radiative forcing.
1. Introduction:

Aerosols affect the Earth’s climate system in two ways: directly and indirectly. Aerosols scatter sunlight and enhance the planetary shortwave (SW) albedo, through the so-called “aerosol direct effect”. Indirect effects relate to the modification of cloud radiative properties due to the change of aerosol concentration or properties by human activities. The increase of aerosol number enhances cloud droplet number concentration. At a constant cloud liquid water content, it is responsible for the decrease of the droplet effective radius and the increase of the cloud reflectivity. One of the first descriptions of this effect, called first indirect effect, is attributed to Twomey (1974). It causes a negative radiative forcing on top of the atmosphere. Despite numerous studies, the uncertainty of the radiative forcing associated with this effect remains much larger than for greenhouse gases. The fourth IPCC report associates to the first indirect effect a negative forcing ranging from -0.2 to -1.9 W/m² (Forster and Ramaswamy, 2007) and stressed the importance to improve these estimates and their associated uncertainties. Chen and Penner (2005) have analysed the uncertainty in the estimation of the first indirect aerosol effect due to emissions, chemical transport model, aerosol size distribution, cloud nucleation parameterization and different clouds properties. The aerosol burden calculation, the cloud fraction, and the representation of the preindustrial aerosol state (size distribution and mass concentration) are the main sources of uncertainty. Chen and Penner (2005) warn about the use of off-line simulations that could cause additional sources of uncertainty since they use monthly average aerosol number concentration and argue for a fully coupled GCM which would give a better estimate of the interactions between aerosols, clouds and radiation.

Part of the difficulty to assess the aerosol effects on climate comes from their high variability. Aerosols have heterogeneous emission sources and a relatively short lifetime (from day to several weeks) that explain their strong variations in space and time. Because of this high spatial variability, aerosol effects on climate should not only be assessed at the global scale but also region by region. High temporal variability of aerosol is induced by their large difference in size and the many processes that affect their properties while they are in the atmosphere (nucleation, coagulation, sedimentation, wet deposition, humidity growth…). Variations in meteorological fields induce to a large degree the temporal variability in aerosol properties, and there is a strong interest to consider the full interactions between them by using coupled climate-chemistry models.
This coupling is expected to introduce non-linearities. Although the direct radiative effect is almost a linear function of aerosol concentration for a given cloud cover, non-linearities could be introduced by the change in time of the relative position of clouds and aerosols. The first indirect effect is non-linear, even if the cloud cover does not change, as the relationship between cloud droplet number concentration (CDNC) and aerosol concentration is not linear. In global models, this relationship may be described using empirical parameterizations that specify the CDNC as a function of the aerosol mass density (Boucher and Lohmann, 1995; Lohmann and Feichter, 1997; Roefols et al., 1998) or the aerosol number concentration (Jones et al., 1994; Menon et al., 2002; Suzuki et al., 2004), or using physically-based parameterizations (Chuang et al., 1997; Abdul-Razak and Ghan, 2002; Nenes and Seinfeld, 2003) in which the CCN activation and the droplets formation processes are described prognostically. In any case, aerosol temporal variability will modify the first indirect effect estimation through the non-linearity of this relationship. Other non-linearities influence the calculation of first indirect effect such as the relationship between cloud droplet size and cloud droplet number or between cloud optical thickness and cloud droplet size.

Several modelling groups have included interactive aerosols in their model and have performed many studies with this model configuration (e.g. Jones and al., 2001, Reddy and al., 2005, Roeckner et al., 2006). But, to our knowledge, none of these studies includes on-line radiative forcing calculation. In effect, estimating radiative forcing with such model configuration is not obvious and needs complex technical development. This limit leads several research groups to elaborate alternative to the radiative forcing concept: the “radiative perturbation” (Penner et al, 2006); the “quasi-forcing” (Rotstayn et Penner, 2001), the « fixed SST forcing » (Hansen et al., 2002) and the « forcing with stratosphere and troposphere adjustment » (Shine et al., 2003). Lohmann et al. (2010) have evaluated such alternatives compared to radiative forcing. However, radiative forcing is a powerful diagnostic for studying climate perturbations. Then, we propose here to tackle this issue and elaborate solutions to compute traditional radiative forcing.

To simplify analyses and focus on the introduction of aerosol temporal variability, aerosol/cloud interactions are treated in a simple way: only sulfate is considered in this paper and we used an empirical formula for the activation parameterisation. The methods presented in this paper are not valid for model using a mechanistic activation scheme. They are also not suited to analyse radiative forcing that directly impact meteorological fields like the cloud lifetime effect or the semi-direct effect.
After a brief presentation of LMDZ GCM features and the aerosol parameterization in the model, a description of the main choices concerning the implementation of aerosol concentrations and radiative effects (Sect. 2) is done. In Sect. 3, weaknesses, strengths and estimates are presented for the two main methods used until now to account for direct and first indirect effects in the LMDZ GCM. We also propose an estimate of the change in short-wave net fluxes due to aerosol temporal variability. In the last part of the paper, we address the question of computing radiative forcing in coupled model. Two solutions to perform simultaneously radiative forcing calculation with interactive chemistry are proposed. We discuss their strengths and weaknesses considering their technical performances and their accuracy concerning radiative forcing estimates.

2. Methodology

2.1. Model Description

In this study, we used the Laboratoire de Météorologie Dynamique general circulation model LMDZ (Hourdin et al, 2006) with a resolution of 3.75° in longitude, 2.5° in latitude and 19 hybrid sigma coordinate levels extending from the surface up to 3 hPa. Climatological sea surface temperatures and sea-ice fractions are used as boundary conditions to the model. The dynamical part of the LMDZ code is based on a finite-difference formulation of the transport primitive equations and resolves the large-scale advection every six minutes. The physical part of the model includes the most relevant subgrid-scale physical processes such as the turbulent mixing in the boundary layer, and is computed with a time step of thirty minutes. Deep convection is parameterized using the Emmanuel scheme (1991). Clouds are represented through a log-normal probability distribution function of subgrid scale total (vapor and condensed) water (Bony and Emmanuel, 2001). Effects of mountains (drag, lifting, gravity waves) are accounted for using state-of-the-art schemes (Lott, 1999). The land surface processes are parameterised through a bucket model. Radiative transfer is calculated using a two-stream approximation, dividing the radiation in an upwelling and a downwelling flux. The parameterization is based on the scheme of Fouquart and Bonnel (1980) in the solar spectrum (SW) and on an updated version of Morcrette (1991) in the terrestrial part.
The direct and first indirect aerosol effects are included in LMDZ radiative calculations in the SW spectrum following closely the work of Quaas et al (2004) with minor modifications. To facilitate the analysis, this study focused on the sulfate component of the aerosol. The optical thickness, \( \tau_a \), single scattering albedo, \( \omega_a \), and particle asymmetry parameter, \( g_a \), are used by the radiative code to derive the direct effect. A Mie scattering model with the refractive index of Toon et al (1976) for ammonium sulfate was used to compute the sulfate optical properties of each aerosol mode taking into account aerosol size distribution. For the particles in the soluble mode, we used the hygroscopic growth factors of Martin et al. (2004) to account for the change in particle diameters due to water absorption.

The first indirect effect depends on the cloud optical thickness which varies with cloud droplet size and number. In the model, cloud optical thickness is parameterised in terms of cloud droplet effective radius \( (r_e) \) and of the cloud liquid water path \( (W) \), in each layer (Stephens, 1978):

\[
\tau = \frac{3}{2} \frac{W}{r_e \rho_{\text{water}}} \tag{1}
\]

The cloud droplet effective radius, \( r_e \), is linked to the volume-mean cloud droplet radius \( (r_d) \) in our model as \( r_e = 1.1 r_d \) and the volume-mean cloud droplet radius for liquid water clouds is calculated assuming spherical particles:

\[
r_d = \left( \frac{4}{3} \pi \rho_{\text{water}} N_d q_l \rho_{\text{air}} \right)^{\frac{1}{3}} \tag{2}
\]

where \( q_l \) is the cloud liquid water mixing ratio, \( \rho_{\text{air}} \) is the air density, \( \rho_{\text{water}} \) is the density of liquid water, and \( N_d \) is the cloud droplet number \( (N_d) \). \( N_d \) \( (\text{cm}^{-3}) \) is diagnosed from sulfate mass concentration, \( m_a \) (\( \mu g(\text{SO}_4) \text{ m}^{-3} \)), using the empirical formula of Boucher and Lohmann (1995) (formula “‘D’”).

\[
N_d = 10^{9.82 + 0.08 \log(m_a)} \tag{3}
\]
We replace the original values of the empirical constants \(a_0 = 2.21\) and \(a_1 = 0.41\) by the re-adjusted values from Quaas and Boucher (2005) who used POLDER space instrument retrievals \(a_0 = 1.7\) and \(a_1 = 0.2\). Figure 1 presents the “Boucher and Lohman” parameterisation for both the original and newer sets of empirical constants. With the new constants, the cloud droplet number sensitivity to aerosol optical depth perturbation is quite well represented in LMDZ-INCA compared to the observation (Quaas et al., 2009). To avoid unrealistic droplet number concentrations, especially in region of small sulfate concentrations, \(N_d\) is restricted to be within a range from 20 to 1000 droplets per cm\(^{-3}\).

2.2. Aerosol concentrations

The LMDZ model has been used in two different configurations that only differ by the way aerosol concentration is considered: prescribed in one case (off-line configuration) and coupled with the INCA chemistry model in the other case (on-line configuration).

2.2.1. Aerosol off-line configuration

In the first configuration, referred as “aerosol off-line”, the aerosol concentration fields are prescribed with a given frequency (month, day…). These concentrations fields have been computed and have been stored from previous simulations including transport and chemistry of aerosols and gases (see below). This method has been implemented in several GCM [IPCC, 2001] and has been used in many studies (e. g. Haywood et al, 1997 ; Mitchell and Johns, 1997 ; Boer et al; 2000 ; Dai et al, 2001 ; Dufresne et al, 2005). In LMDZ, this method has been initially implemented by Quaas et al. (2004) and by default the sulfate concentrations are prescribed with a monthly frequency. The “instantaneous radiative forcing” (Hansen et al, 1997) is easy to estimate: one needs to compute at each time step the radiative fluxes two times, one with perturbed aerosol concentration and one with reference aerosol concentration. The radiative forcing is the difference between these two radiative fluxes.

2.2.2. Aerosol on-line configuration

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In this configuration, referred as “aerosol on-line”, the chemistry processes, the aerosol concentration and the meteorological variables are fully coupled at each time step (30 minutes). The meteorological trajectory is influenced by sulfate concentration and the sulfur chemistry is influenced by the meteorological variables. The chemistry model is the Interaction with Chemistry and Aerosols (INCA) model including sulfate aerosol calculation (Schulz, 2007) and the CH<sub>4</sub>-NO<sub>x</sub>-CO-O<sub>3</sub> chemical scheme representative of the background chemistry of the troposphere (Hauglustaine et al., 2004). Sulfate concentration and size distribution are calculated at each time step by integrating surface and in-situ emissions, wet and dry deposition rates (Schulz et al., 1998; Guelle et al., 1998a and Guelle et al., 1998b), humidity growth (Gerber, 1985), atmospheric chemistry reactions (Boucher et al., 2002) and transport. The chemical transformation of the gaseous sulphur species requires oxidants either in the gas-phase or in the liquid-phase. The sulfur chemistry implemented in INCA is similar to the one described in Boucher et al. [2002]. The oxidant fields are estimated in INCA as part of the dynamic chemistry scheme. DMS and its product DMSO are oxidised using the actual concentrations of OH and NO<sub>3</sub>. SO<sub>2</sub> is transformed to sulfate by H2O2 and O3 in cloud liquid water. The formation of sulfate is limited by the acidity formed in the oxidation process within cloud droplets. SO<sub>2</sub> is also oxidised in the gas-phase. Gaseous H2S and aerosol methane sulphonic acid (MSA) are also included as minor species of the sulphur cycle. The mass of sulfate produced through these reactions is directly injected into the soluble accumulation mode. The nucleation mode is not treated explicitly, hence, there is no new particle formation in this size range and the very fine particles are not represented. The mass median diameter (MMD) of sulfate depends upon the mixing of the ratio of sulfate formation from clouds and via gas phase oxidation. Furthermore, the MMD varies as deposition takes place since large particles will be preferentially scavenged by sedimentation and below cloud scavenging.

2.3. Forcings

The study has been done for present-day period (perturbed conditions) and radiative forcing are assessed relative to the preindustrial one (unperturbed conditions). Sulfate, SO<sub>2</sub> and DMS emissions come from the AEROCOM project emissions inventory.
(http://nansen.ipsl.jussieu.fr/ AEROCOM) [Dentener et al., 2006]. Natural emissions (DMS from ocean; \textit{sulfate} and \textit{SO}_2 from volcanoes) are kept unchanged between preindustrial and present-day periods. Only anthropogenic emissions are modified. The aerosol concentrations fields computed in the on-line simulations are averaged and used in the off-line runs. This ensures that in both on-line and off-line simulations, the monthly mean aerosol concentration are exactly the same.

Each simulation presented in the paper consists of a ten-years snap-shot including one spin-up year. The last nine years of each simulation are used for the radiative fluxes analysis. This nine-year duration allows reducing the noise due to internal model variability compared to the effect of anthropogenic forcing.

3. The radiative impact of aerosols and the effect of the temporal variability

In this section, the radiative forcing or radiative effect of the aerosols are presented for both the on-line and off-line configuration of the model. The global values of these estimates are compared, as well as their geographical distributions. Then, we analyse the effect of the temporal variability of \textit{sulfate} concentrations on radiative net fluxes.

3.1. Aerosol computed on-line

Two simulations have been performed using the “aerosol on-line” configuration of the model. They differ only by the \textit{SO}_2 emissions. For both simulations, greenhouse gas concentrations, sea surface temperature (SST) and sea ice fraction are fixed to present-day conditions. For gaseous chemistry, reactive gas emissions are kept to their 2000 levels. In the first simulation, natural plus preindustrial \textit{SO}_2 emissions are used whereas in the second simulation, natural plus present-day anthropogenic emissions are used. Below, we will refer to the preindustrial fields of the first simulation with the subscript «\textit{PI}» and the present-day fields with the subscript «\textit{PD}».

The radiative perturbation (\textit{\Delta F}_V) of anthropogenic \textit{sulfate} is computed as the difference of short-wave net fluxes (\textit{F}_V) at the top of the atmosphere between the present-day and the preindustrial aerosol emissions (the subscript “\textit{V}” indicates that fluxes have been computed...
including the instantaneous variability of aerosol concentrations).

\[ \Delta F_v = F_{v_{PD}} - F_{v_{PI}} \]  

(4)

This radiative perturbation differs from an instantaneous radiative forcing because present-day and preindustrial net fluxes are estimated for two different atmospheric trajectories after the atmospheric column (troposphere and stratosphere) has had time to adjust. It is identical to the “fixed SST radiative forcing” defined by Hansen et al. (2002). This diagnostic includes both direct and first indirect effects. With this model version, it is not possible to study each effect separately. Fluxes include the two effects.

Values of \( F_{V_{PD}} \), \( F_{V_{PI}} \) and \( \Delta F_v \) are indicated in Fig. 2. The global annual mean value of the radiative perturbation is -0.73 W.m\(^{-2}\).

If we focus now on the geographical distribution of this radiative perturbation, the pattern that one may expect from the aerosol geographical distribution is not discernable and the figure shows a noisy pattern (Fig. 3). This signal is due to the natural variability. The mean cloud distributions of the two simulations are slightly different due to internal variability and this difference strongly impacts the radiative fluxes at the top of the atmosphere. The signal/noise ratio could be improved with long simulations of a hundred years, but the computing time for the chemistry-aerosol module is prohibitive for such long runs.

3.2. Aerosol computed off-line

The same two simulations have been performed using the off-line configuration of the model. The prescribed aerosol concentrations are kept constant during each month and are set to the monthly mean value of the aerosol concentrations previously obtained with the on-line simulations. This ensures that in both on-line and off-line simulations, the monthly mean aerosol concentrations are exactly the same. The fluxes computed with prescribed monthly mean aerosol concentration have the subscript “M”.

Fig. 2 compares the shortwave net fluxes of the off-line configuration (\( F_{M_{PD}} \) and \( F_{M_{PI}} \)) to those of the on-line simulation (\( F_{V_{PD}} \) and \( F_{V_{PI}} \)). With this configuration, the radiative perturbation (\( \Delta F_M \)) amounts to -0.64 W.m\(^{-2}\). It is 12% higher than the value obtained when
sulfate concentration is computed on-line ($-0.73 \text{ Wm}^{-2}$). In addition, the off-line configuration allows to easily compute the radiative forcing of aerosols for both the direct and indirect effect of the aerosol (e.g. Quaas et al., 2004). The total radiative forcing (sum of direct and first indirect effects) amounts to $-0.70 \text{ W.m}^{-2}$. It is close to the radiative perturbation ($AF_M = -0.64 \text{W.m}^{-2}$). This result is consistent with Hansen et al. (2002) who obtained that the radiative perturbation for fixed SST is close to the instantaneous radiative forcing for non absorbing aerosols such as sulfate.

The direct effect value is $-0.31 \text{ W.m}^{-2}$ whereas the indirect effect reaches $-0.39 \text{ W.m}^{-2}$. The simulated direct radiative forcing is very close to the mean value derived in the AEROCOM project of $-0.35 \pm 0.15 \text{ W.m}^{-2}$ (Schulz et al, 2006). This value also lies inside the 90% confidence interval ($-0.4 \pm 0.2 \text{W.m}^{-2}$) reported in the 4th IPCC assessment report (Forster et al., 2007). The first indirect radiative forcing straddles in the lowest part (in absolute value) of the values reported in the 4th IPCC report [$-0.2$ to $-1.9 \text{ W/m}^2$] (Forster et al., 2007). This low value of the first indirect effect comes mainly from the use of new constants $a_0$ and $a_1$ in the Boucher and Lohmann microphysics relationships (Eq. (3)). Quaas and Boucher (2005) showed that with their set of constants, simulated cloud droplet number decreases and the first indirect effect radiative forcing is divided by a factor 2. Dufresne et al. (2005) corroborate this finding in a study on climatic impact of sulfate aerosol performed with IPSL coupled model that also shows the importance of low level clouds over continents.

Figure 4 shows the direct and first indirect aerosol radiative forcing. As expected, sulfate results in a cooling of the surface and displays a very heterogeneous distribution. The direct radiative forcing is strongly correlated to the emission sources. Values up to $-5 \text{ W.m}^{-2}$ can be reached in some industrial regions. Patterns of the first indirect effect are correlated to both emission sources and cloud cover. Some regions in north latitudes show a positive first indirect effect. It comes from a decrease of SO$_2$ emissions by biomass burning between present-day and preindustrial periods.

3.3. Effect of the sulfate temporal variability on the radiative fluxes

The radiative net fluxes of the on-line and off-line simulations may differ because the frequency at which aerosol concentrations vary (prescribed every month in one case, computed every time step in the other case), but also because of the different meteorological
trajectory between the two simulations. In the off-line method, the meteorological trajectory is influenced by monthly mean sulfate concentration whereas in the on-line method, the meteorological trajectory responds to the effect of instantaneous concentrations (Fig. 2). In this part of the study, the effect of the aerosol temporal variability has been isolated from the effect of the meteorological trajectories and then analysed.

3.3.1. Method

The effect of the temporal variability is studied by comparing two simulations which only differ by the frequency at which the sulfate concentration is updated: every model time step (30 min) for the simulation referred as “VAR simulation” and every month in the case of the simulation referred as “MONTH simulation”. The average concentrations fields and the meteorological trajectory are the same for the 2 simulations; therefore the difference in the mean aerosol distribution can not be the reason of the difference between off-line and on-line runs.

For the VAR simulation, the aerosols are computed on-line as presented in Sect. 3.1. The MONTH simulation is run off-line with respect to the meteorological trajectory of the VAR simulation (temperature, pressure, wind, humidity, cloud fraction, LW path,...). Then, the only difference in the MONTH simulation comes from the use of monthly sulfate concentrations that are used to compute aerosol and cloud radiative properties and radiative fluxes.

Two sets of VAR and MONTH simulations have been performed for present-day and preindustrial sulfate emissions. Preindustrial simulations have also been performed off-line with the meteorology based on the present-day fully variable sulfate aerosol retroaction.”

Preindustrial simulations have also been performed with the same physical forcings. Then, the meteorological trajectory is exactly the same in the preindustrial and in the present-day simulations. The only difference is the anthropogenic emission of sulfate aerosols. We examine the change in net fluxes at the top-of-atmosphere between the experiments VAR and MONTH for the present day \((F_{V,PD} - F_{M,PD})\) and the preindustrial periods \((F_{V,PI} - F_{M,PI})\). The net fluxes resulting of this experiment are schematically presented in Fig. 5. The effect of the meteorological trajectory is null.
3.3.2. Global and regional results

Figure 5 indicates the values of the shortwave net fluxes at the top-of-atmosphere for the two simulations VAR and MONTH and for the two periods. Globally, temporal variability of sulfate concentration increases these net fluxes by +0.24 W.m\(^{-2}\) for the present-day conditions and by +0.22 W.m\(^{-2}\) for the preindustrial ones. The regional distribution of this change for present day and preindustrial conditions are shown Fig. 6, impact of direct effect (Fig. 6a and Fig. 6b) and first indirect effect (Fig. 6c and Fig. 6d) are separated. With the exception of a few model grid points, the temporal variability leads to an increase of the total net fluxes (direct and first indirect effects) at the top of atmosphere for the two periods: preindustrial and present day. The changes in total net fluxes are within the interval -0.5 and +2.5 W.m\(^{-2}\).

However, as it is shown in Fig. 6a and Fig. 6b, the direct effect has a negligible role, it tends to slightly decrease net fluxes. The increase of net fluxes results mainly from the first indirect effect. More precisely, this increase is linked to the shape of the relationship between the number concentration of cloud droplet \(N_d\) and the sulfate concentration \(m_s\). Consider \(N_{d,M}\) to be the number concentration of droplets corresponding to the average sulfate concentration in the MONTH experiment. By construction, this value stays unchanged throughout the month.

Let’s consider now, \(N_{d,V}\), the number concentrations obtained from the instantaneous sulfate concentrations in the VAR experiment. Because this relationship grows asymptotically when sulfate concentration increases, the monthly mean of \(N_{d,V}\) values will be less than the \(N_{d,M}\) value. Since net fluxes decrease when the number of cloud droplet increase, the monthly mean net fluxes computed in the experiment VAR, \(F_V\) is greater than the average net fluxes \(F_M\) computed from the monthly mean sulfate concentration.

3.3.3. Analysis

Three main variables contribute to the radiative effect of aerosol: the fraction of low level clouds, their liquid water content and the sulfate concentration. Figure 7 displays the cloud liquid water content and the percentage of the liquid water from low-level clouds. The presence of low clouds shows the same pattern than the changes in fluxes at the top of the atmosphere caused by the variability of sulfate concentrations (Fig. 6c and Fig. 6d). In upwelling regions the change in flux at the top of the atmosphere reaches 1 to 2.5 W.m\(^{-2}\) in present day conditions. Coastal regions West of South and North America together with
coastal regions West of Africa are more affected than others by the variability of aerosol concentrations. In contrast, over Indonesia and India, the impact of the sulfate temporal variability is weak even though the liquid water content is much higher than over the other regions discussed. In these areas, clouds are situated at much higher altitudes (Fig. 7b). Finally, above dry regions without clouds, there is no indirect effect and hence no effect of the sulfate concentrations variability.

The time average value of the sulfate concentration is shown Fig. 8. Regions with low to intermediate sulfate concentration appear to be more sensitive to the aerosol temporal variability than regions with high sulfate concentration. This effect can be seen for instance over Europe. Net fluxes differ substantially in pre industrial conditions when sulfate concentrations are low (Fig. 6d and Fig. 8b) whereas the difference vanishes under present day conditions (Fig. 6c and Fig. 8a). This effect can also be seen in South-East Asia.

The slope of the relationship between cloud droplet concentration ($N_d$) and sulfate concentration ($m_s$) of the first indirect effect (Fig. 1) explains this net fluxes difference between polluted and unpolluted regions. In unpolluted regions a small change in sulfate concentrations corresponds to a large change in cloud droplet number, whereas in polluted regions higher-level sulfate will result in small changes in cloud droplet number.

We identified in our model a concentration threshold of 0.8 µg(SO$_4$) m$^{-3}$ above which temporal changes in sulfate concentrations have little impact on net fluxes. The regions that exceed this threshold are China, Europe and the East coast of the United States which all are areas downwind of the main industrialized regions. Other regions with high sulfate are located downwind of natural volcanic emission regions. For these concentrations levels, the aerosol temporal variability do not affect the top-of-atmosphere net fluxes.

In contrast, the effect of aerosol temporal variability is large for intermediate sulfate concentrations (between about 0.1 and 0.8 µg(SO$_4$) m$^{-3}$) over remote regions. In regions devoid of sulfate (concentration less than 0.1 µg(SO$_4$) m$^{-3}$), the first indirect effect is close to zero. South America constitutes such region with a high liquid water content, abundant low-level clouds but almost no sulfate present.

This impact of clouds and sulfate concentrations is illustrated for six regions that have very different responses to the introduction of sulfate temporal variability: the Pacific Ocean, the Atlantic Ocean, the southern part of South America, India, Indonesia and continental Europe (table 1). The liquid water content, the mean sulfate concentrations for present day and preindustrial and the change in flux for present and pre-industrial conditions are reported in
Table 2 for each of these regions. The comparison of preindustrial and present-day conditions confirms the sensitivity of radiative fluxes in regions of low level clouds and to intermediate sulfate concentration. Vertical profiles of the cloud liquid water content and preindustrial and present-day sulfate concentrations are also displayed for these six regions (Fig. 9). Intermediate levels of sulfate concentrations are reached at the height of the low-level clouds. The maximum of sulfate concentration is reached above the low-level clouds altitude. The first indirect effect shows a marked non-linearity for these intermediate concentration levels (Fig. 1). This is one of the reasons for the strong sensitivity of the first indirect effect to the variability of sulfate in the presence of low-level clouds.

4. Calculation of the radiative forcing for on-line simulations

The estimate of radiative perturbation (defined in the section 3.1) needs very long simulations to reduce the noise due to natural variability. Thus, this approach is not suitable for transient climate simulations. In addition, radiative forcing is a powerful diagnostic to compare the radiative impact of different perturbations (aerosol, greenhouse gases, land use…) and different aerosol types (sulfate, BC, POM, etc). For these reasons, we propose in the next section several methods to compute aerosol radiative forcing for on-line simulations. Their relevance is discussed relatively to their computation time and to their precision. These methods have been developed for model using an empirical parameterization of the cloud droplet number concentration.

4.1. A direct extension of the radiative forcing computation method used for off-line simulations

In the aerosols off-line configuration, the radiative forcing is simply computed as the difference, at each time step, between the radiative fluxes computed with two aerosol concentration fields: the actual concentration and a reference concentration, here chosen as the preindustrial one. These two fields are monthly mean values and remain constant during the whole month. One can directly apply this method for on-line configuration: the actual concentration is now the aerosols concentration calculated on-line by the INCA chemistry model and then varying at each time step. The preindustrial concentration is unchanged and
still prescribed to its monthly mean value. This method is called, $M_{\text{offline, est}}$, which stands for: extended off-line method.

The modification of the direct effect due to the change of aerosol concentration between present-day and preindustrial conditions results in a difference of net fluxes at the top of the atmosphere that amounts to $-0.32$ W m$^{-2}$. It is very close to the value of the direct radiative forcing obtained with the off-line method ($-0.31$ W m$^{-2}$, Sect 3.2). Computing sulphates interactively increases the difference of net fluxes at the top of the atmosphere by 3% relative to the off-line method when these concentrations are read in. The geographical distribution of these two fields is also very similar (Fig. 10a and 10c). Industrial regions where SO$_2$ emissions sources are located are more sensitive to the temporal variability of aerosol. The non-linearity due to the variation with time of the sulfate aerosols concentration is weak. It is consistent with the direct net flux changes analysed in Sect. 3.3.

The modification of the first indirect effect due to the change of aerosol concentration between present-day and preindustrial conditions results in a difference of net fluxes at the top of the atmosphere estimated at $-0.27$ W m$^{-2}$. This value is much lower (a 60% decrease in absolute value) than the radiative forcing obtained with the off-line method ($-0.39$ W m$^{-2}$, Sect 3.2). The geographical difference of these two fields (Fig 10b) displays positive values almost everywhere, the most important values being in regions where low-level clouds are abundant (Fig. 10d). It is worth noticing that these regions are generally remote from the main source regions of SO$_2$, and therefore the atmospheric load of sulfate is small.

In this simple method, there is a major inconsistency: the sulfate concentration field for present day, is computed on-line in the model, varies at each time step and is linked to the meteorology of the simulation. In contrast, the preindustrial field do not vary with time, has no link with the actual meteorology. It has been obtained off-line from a previous simulation with different transport fields, different timing for precipitation and clouds and then different timing for scavenging of aerosols by clouds. This may have an important impact as the first indirect effect is strongly non-linear. Indeed, at any given time, present day sulfate concentrations can be lower than preindustrial values, leading to a positive first indirect effect estimate.

In this simple method, the aerosol concentration difference between preindustrial and present periods has two distinct origins: the sulfate emissions and the variability of the atmosphere.
The first effect is what we wanted to estimate. The second effect is unwanted and may have a large amplitude, as previously shown in section 3.3.

To avoid this inconsistency, the two aerosol fields need to vary both with time, in a consistent manner, and therefore need to be computed with the same meteorological fields.

4.2. A reference method to compute the first indirect radiative forcing:

In order to have a reference estimate of the indirect radiative forcing for on-line simulation, we compute the aerosol concentration for present-day and pre-industrial emissions with two very same meteorological trajectories. The temporal variability of aerosol is taken into account for both periods, the meteorological trajectory is the same, the only difference is the aerosol emission and the impact of the corresponding aerosol concentration on radiative fluxes calculation. The approach is the same as the one described section 3.1 (on-line method), and the simulations used here are the “VAR” experiments with present-day and pre-industrial sulfate emissions.

The instantaneous radiative forcing \( RF_V \) is directly the difference between the net flux at the top of the atmosphere with present-day emissions \( F_{V,PD} \) and with pre-industrial emissions \( F_{V,PI} \):

\[
RF_V = F_{V,PD} - F_{V,PI}
\]  

The first indirect radiative forcing computed using this methods is -0.36 W.m\(^{-2}\), a little less than using the off-line method (-0.39 W.m\(^{-2}\)) where averaged sulfate concentration fields are used. The first indirect effect (Fig. 11a) shows a very similar spatial distribution than that obtained with the off-line method (Fig. 4b). The first indirect effect is more negative over Europe, the United-States and East Asia, and less negative over the boreal forests and in the eastern part of the ocean basins (Fig. 11b). The difference is statistically significant at the 95% confidence level in most regions (non-parametric bootstrap test). These changes are only due to the frequency at which aerosols vary (monthly in the off-line case and 30 minutes in the reference case). The difference of meteorological trajectory between the reference method and the off-line one doesn’t affect the result (not shown). Given that the largest differences of radiative forcing between the two methods are over
continents (Europe and North America), one could expect that in spite of fixed SST, these differences of radiative forcing will have an impact on surface temperature over these regions. To distinguish the real effect of temporal variability on temperature from the noise due to natural variability of climate; 50-years simulations have been performed with off-line and on-line model configurations and for present-day and preindustrial periods. The difference of temperature over continents between the two periods have been estimated for both configurations of the models ($\Delta T_V = T_{V,PD} - T_{V,PI}$ and $\Delta T_M = T_{M,PD} - T_{M,PI}$) and then compared. Globally, the difference ($\Delta T_V - \Delta T_M$) amounts to -0.07°C. Regionally the signal is within the interval [-0.9, 0.8]°C and is not much correlated with radiative forcing (Fig. 12). At a first order, the temporal variability of aerosol doesn’t affect surface temperature fields.

With this method, we get a reference estimate of the first indirect radiative forcing including sulfate temporal variability. However the multiple calls needed that use a lot of CPU make impractical to use it for routine simulations. Thus, we now propose two alternatives to compute aerosol radiative forcing in on-line simulations. They rely on the results of section 4.1 related to the need for both present-day and preindustrial concentrations to be computed with the same meteorological fields.

In the first alternative method (section 4.3), we propose to correct the error introduced on net fluxes by the use of “inconsistent” aerosol fields (one constant during the whole month; one varying at each time step). The correction is based on the difference between net fluxes calculated using pre-calculated monthly preindustrial concentrations and using 30 minutes preindustrial concentrations. Both preindustrial simulations are performed with the same meteorological trajectory. In the second alternative case (section 4.4), we propose to estimate preindustrial sulfate concentration from present-day values. This ensures that both present and preindustrial sulfate concentrations are consistent with the meteorological trajectory of the simulation.

4.3. Correction of off-line/on-line biaisis

Computing preindustrial and present-day aerosol concentrations with two different meteorological trajectory results in an underestimation of 60% of the first indirect radiative forcing (see section 4.1). This “off-line/on-line” error corresponds to the term “$F_{M, PI} - F_{V, PI}$” (Fig. 13). This difference of net fluxes is due to the use of monthly vs varying aerosol concentrations.
concentrations. It amounts to -0.23 W.m$^{-2}$. Its geographical distribution is displayed in Fig. 6b.

This error has a low day to day variability (Table 3). Then, we propose to assess monthly mean values of the error and use them to correct the monthly mean radiative forcings computed with the extended off-line simulation. Finally, the correction consists in summing up the term “$F_{M, PI} - F_{V, PI}$” and the biased radiative forcing $RF_{\text{offline, ext}}$ (Fig. 13):

$$\text{RF}_{\text{offline, ext\_corr}} = \text{RF}_{\text{offline, ext}} + F_{M, PI} - F_{V, PI}$$  

(7)

The direct radiative forcing remains unchanged compared to the estimation of the extended method off-line as any correction are applied for this effect. For the first indirect effect, the corrected radiative forcing amounts to -0.41 W.m$^{-2}$. It is 13% less than the value calculated in our reference simulation. The difference of radiative forcing calculated with this method and with the reference method is presented in Fig. 14. A slight overestimation of the first indirect effect (more negative) concerns a major part of the globe: only a few grid points in North of Europe, East of the United States and in South Africa present an underestimation. This overestimation is statistically significant at the 95% confidence level (bootstrap test).

Compared to the reference method (Section 4.1), the global error (-0.05 W.m$^{-2}$, 13%) is slightly higher that the one computed from monthly averaged concentration fields (-0.03 W.m$^{-2}$, 8%) with the off-line methods and MONTH experiment. However, these values are low, and this method largely improves regional patterns (Fig. 14 versus Fig. 11b).

The residual error is mainly due to a residual difference of meteorological trajectories: the inconsistency related to the calculation of sulfate concentration has been corrected but the terms $RF_{\text{online, ext}}$ and “$F_{M, PI} - F_{V, PI}$” have been estimated from two different meteorological trajectories (see Fig. 13). Secondly the hypothesis for this case is not perfectly matched as the “$F_{M, PI} - F_{V, PI}$” term presents a small variability.

Finally, this method is valid for aerosol studies but not for more complex cases in which several forcings are simultaneously modified (climate simulation).

4.4. Approximation of the on-line aerosol preindustrial concentration

For this method, we expect that at a given time, for a same meteorology, the ratio of preindustrial by actual instantaneous concentrations is the same that the ratio of monthly mean concentrations:
At a given time $t$ of a given month:

$$\frac{[SO_4]_{pi,t}}{[SO_4]_{pi,month}} = \text{preindustrial aerosol fraction} \quad (8)$$

Figure 15 shows that the variability of the instantaneous sulfate concentration ratio is not completely caught by this approach. However one can get a rough estimate using this hypothesis.

In this method, the on-line configuration of the model is used. The preindustrial concentration field is calculated in multiplying the present-day aerosol concentration field (computed interactively in INCA) by the “preindustrial aerosol fraction”. The fraction is prescribed monthly. It is obtained from preindustrial and present sulfate fields that have been computed in previous simulations using the chemical-transport version of LMDZ-INCA.

The direct radiative forcing amounts to -0.31 W.m$^{-2}$. It is very close to the values obtained with the off-line method (section 3.2) and the extended off-line method (section 4.1). The geographical distribution of the direct effect displays the same patterns that those obtained in the two other methods (see Fig. 16a for the difference with the extended off-line method). Only the regions of high sulfate concentrations are impacted.

The first indirect effect amounts to -0.36 W.m$^{-2}$ that matches up to the value of the reference method (-0.36 W.m$^{-2}$). Figure 16b shows the differences that remain in the geographical distribution. As for the other tested methods, this difference is statistically significant (bootstrap test at the 95% confidence level) in most regions. The difference of patterns obtained between this method and the reference method is close to that one obtained between the off-line method and the reference method (Fig. 11b). Using this last method improves spatial patterns (Fig. 17) especially in regions of north high latitude. The remaining error in the estimate of the first indirect effect radiative forcing is caused by how we approximate the preindustrial aerosol concentration fields.

4.5. Comparison of the results

All tested methods give very similar estimates of the direct radiative forcing but significative differences for the first indirect effect. Figure 18 compares the performance of the tested methods to compute the first indirect radiative forcing (mean bias and error on the spatial
pattern). Estimates of the root mean squared error and feasibility of each method are also summarised in Table 4.

Even though the method based on the approximation of the preindustrial \textit{sulfate} concentration leads to the best result regarding the mean bias; the extended off-line method with correction represents best the spatial pattern of the first indirect effect (comparison to the reference method). This method presents also the lowest root mean squared error. Regarding the technical feasibility and ability to perform climate studies, the method based on the approximation of the preindustrial \textit{sulfate} concentration is by far the best method since it is simple to implement, relatively cheap computationally (even though preliminary chemistry-transport simulations are needed to compute the monthly mean aerosol fraction) and enables to analyze several perturbations simultaneously.

This last method has been implemented in the Earth System Model of the Institut Pierre Simon Laplace (IPSL) and will be used for climate simulations including aerosols studies.

5. Conclusions

The impact of coupling a climate model to a chemistry/aerosol model has been tackled using the LMDz general circulation model and the chemistry-aerosol module INCA. This coupling is in agreement with the actual trend of more integrated Earth System Model for studying climate. With this model configuration, simulations include a complete feedback between climate and aerosols. The cloud/aerosol interaction is computed in LMDZ using an empirical parameterization and only sulfate species have been taken into account to carry out this study. The conclusion would be quite the same if a more complex representation of aerosol was used. Absorbing aerosols will introduce additional non-linearities by the semi direct effect (modification of the meteorological conditions of the atmosphere). However, they will have no effects on the CDN/Na relationship that is the main source of non-linearities for this study. This would be different for models using a mechanistic activation scheme.

This study focuses on the direct and first indirect effects. Impact of this coupling on the 2\textsuperscript{nd} indirect effect is beyond the scope of the paper.

Temporal variability results in an increase of net fluxes that is mainly due to the non-linearity of the first indirect effect. The temporal variability has a negligible role on the direct effect. The changes are mainly controlled by two factors: low-level clouds and the magnitude of the
aerosol mass concentrations. The larger the amount of low-level clouds, the larger is the effect on radiative fluxes. The uncertainties associated to the parameterisation of low-level clouds in LMDz [Rio, 2007] have likely repercussion on our estimates of net flux changes.

The level of sulfate concentration has two opposite effects: 1) the non-linearity of the first indirect effect diminishes as the sulfate concentrations increase; 2) the sulfate temporal variability increases with increasing sulfate concentrations. The detailed analysis of several regions around the globe results in the differentiation of three ranges of concentration.

Regions of low sulfate concentration (less than 0.1 µg(SO$_4$)/m$^3$) for which the non-linearity effect of the relationship is dominant but the sulfate variability is very low. Regions of intermediate concentrations (between 0.1 and 0.8 µg(SO$_4$)/m$^3$) for which the effect of temporal variability is maximum. Regions of high sulfate concentrations (above 0.8 µg(SO$_4$)/m$^3$) for which the relationship $N_d$-m$_s$ is almost linear and the effect on the radiative fluxes is negligible. The threshold concentrations indicated here are only indicative and depend undoubtedley on the formulation of the first indirect effect and the GCM used for the study.

Computing sulfate direct radiative forcing with the on-line configuration of the model is quite easy. Global mean (-0.32 W.m$^{-2}$) and regional patterns are very close to those obtained with the off-line configuration (-0.31 W.m$^{-2}$).

In the other hand coupling climate and aerosols in a model makes it difficult to compute the forcing from the first indirect radiative effect. Technical solutions have been proposed to tackle this difficulty. First, a reference method has been developed to compute first indirect radiative forcing with the on-line configuration. Though globally, the radiative forcing is very close to the one computed with the off-line configuration; the climate/aerosols coupling influences largely the regional patterns. However this method is not suited to run long climate simulations because of its difficult implementation and high CPU cost (chemistry module should be run 3 times to get radiative forcing).

Then, alternatives to the reference method have been elaborated to compute radiative forcing in on-line configuration. The alternative methods will need further development to be used with a prognostic cloud number concentration. Making a direct extension of the off-line classical configuration (the present-day concentration is calculated on-line as the preindustrial one is prescribed) results in an error of more than 60% on the first indirect radiative forcing.

We show that it is mainly due to the non-linearity of this effect. This method must be avoided. Two other alternatives give satisfactory results. The first one consists in making a correction
of the bias as described above. This could be achieved via two additional simulations for unperturbed conditions (the first one with the off-line configuration and the second one with the on-line configuration). With this correction, the global mean estimate of the first indirect radiative forcing is overestimated but spatial patterns are improved compared to the results with the offline method.

In the second alternative; the preindustrial sulfate concentration are approximated using the ratio of unperturbed to perturbed sulfate concentration. In spite of an underestimation of the variability of this ratio, this method gives very good global results and improves regional patterns compared to the off-line configuration.

Both of these alternatives would imply running additional simulations (including chemistry module) that will increase significantly the total CPU time. Thus the “lower CPU” method remains still to run additional simulations with the off-line configuration of the model for time-slices of interest.
AKNOWLEDGEMENTS: This work was financed as part of the doctoral Thesis of Celine Deandris by the “Commissariat à l’Energie Atomique”. We would like to thank Johannes Quaas for constructive discussions of previous versions of this paper.
References:


Fouquart, Y., and Bonnel, B.: Computations of solar heating of the Earth’s atmosphere: A


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<th>Inde</th>
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Table 1: Geographical coordinates of the 6 regions that were used for the analysis shown in Fig. 7: 1) South Atlantic Ocean along the West Coast of Africa (referred as AO-WAf), 2) North Pacific Ocean along the West Coast of North America (referred as PO-WNA); 3) the southern part of South America (South Am.); 4) India (India); 5) Indonesia Islands (InIs); 6) Europe (Eu).
Table 2: Cloud liquid water path (LWP in g.m\(^{-2}\)), percentage of this LWP in low-level clouds (%), sulfate load (mg(SO\(_4\)).m\(^{-2}\)) for present and preindustrial periods, short waves top-of-atmosphere net flux difference (W.m\(^{-2}\)) between the VAR and \textit{MONTH} experiments for present (\(\Delta NF_{pr}\)) and preindustrial (\(\Delta NF_{pi}\)) for the 6 regions targeted in Fig. 7: 1) South Atlantic Ocean along the West Coast of Africa (referred as AO-WAf), 2) North Pacific Ocean along the West Coast of North America (referred as PO-WNA); 3) the southern part of South America (South Am.); 4) India (India); 5) Indonesia Islands (InIs); 6) Europe (Eu).

<table>
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<th>Region</th>
<th>LWP (g.m(^{-2}))</th>
<th>% LWP</th>
<th>Present-day sulfate (mg(SO(_4)).m(^{-2}))</th>
<th>(\Delta NF_{pr}) (W.m(^{-2}))</th>
<th>Preindustrial sulfate (mg(SO(_4)).m(^{-2}))</th>
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Table 3: Monthly mean (M), standard deviation of daily values (STD) and ratio (M/STD) of the factor $F_{V.PI} - F_{M.PI}$ used to correct the radiative forcing of the "extended off-line method".
Table 4: Estimation of the error on the root mean squared error (RMSE) of the first indirect radiative forcing for the different methods presented in this paper. The REF method is used as reference. “No RF” indicates that the method doesn’t enable radiative forcing assessment. The second row “feasibility” is related to the technical feasibility of the method.
Figure captions

Figure 1: Relationship between clouds droplet number (cm\(^{-3}\)) and the \textit{sulfate} concentrations (µgSO\(_4\).m\(^{-3}\)) from the Boucher and Lohmann 1995 D formula, with the original empirical constant (dashed) and with the adjusted empirical constant of Quaas et al, 2005 (solid line).

Figure 2: Representation of the radiative perturbation (ΔF) and radiative forcing (RF) calculated from simulations performed with the on-line and off-line model configuration. For each case, both axes indicate that the fluxes are obtained for two different atmospheric model trajectories depending on the \textit{sulfate} concentration: present-day or preindustrial ones. For the on-line configuration, the “V” annotation indicates that variable \textit{sulfate} concentrations are used; as the “M” annotation referred to monthly mean concentration for the off-line configuration.

Figure 3: Difference between the short wave top-of-atmosphere net fluxes (in W.m\(^{-2}\)) computed with present day and with preindustrial \textit{sulfate} emissions. The on-line configuration of the model is used.

Figure 4: Radiative forcings (W.m\(^{-2}\)) estimated with the off-line configuration of the model for present day \textit{sulfate} emissions: a) direct effect b) 1\textsuperscript{st} indirect effect.

Figure 5: Representation of the difference of radiative net fluxes calculated between the VAR (\textit{sulfate} concentration computed each 30 minutes with INCA) and the MONTH (\textit{sulfate} concentration prescribed each month) experiments. All simulations have been performed with the same physical forcings in order to get exactly the same meteorological trajectory: the present-day one with \textit{sulfate} variability.

Figure 6: Difference of the top-of-atmosphere fluxes (W.m\(^{-2}\)) between the simulation in which the aerosol concentration varies at each time step (VAR experiment) and the simulation in which the concentration remains constant, prescribed to the monthly mean values (MONTH experiment) for present day \textit{sulfate} emissions (top) and pre-industrial \textit{sulfate} emission (below). Impact of the \textit{sulfate} 1\textsuperscript{st} indirect effect (left) and the \textit{sulfate} direct effect (right) are presented separately.
Figure 7: (a) Cloud liquid water path \((g/m^2)\) for all the clouds and (b) percentage of this liquid water path in low level clouds \((P>850\ \text{hPa})\).

Figure 8: Annual mean of the sulfate load \((mg(SO_4).m^2)\) for present day (a) and preindustrial periods (b).

Figure 9: Annual mean vertical profile of the cloud liquid water content \((mg.m^3)\), and of the sulfate content \((\mu g(SO_4).m^3)\) for present day \((SO_4-PR)\) and preindustrial emissions \((SO_4-PI)\). 6 regions are considered: 1) South Atlantic Ocean along the West Coast of Africa (referred as AO-WAf), 2) North Pacific Ocean along the West Coast of North America (referred as PO-WNA); 3) the southern part of South America (South Am.); 4) India (India); 5) Indonesia Islands (InIs); 6) Europe (Eu).

Figure 10: radiative forcing calculated from the extended off-line method for: a) sulfate direct effect \((W.m^{-2})\), b) sulfate 1st indirect effect \((W.m^{-2})\). Difference of radiative forcings between the off-line extended method and the off-line method: c) sulfate direct effect \((W.m^{-2})\), d) sulfate 1st indirect effect \((W.m^{-2})\). The statistical significance of the difference was tested at the 95% confidence level using a bootstrap method. Regions where the difference is statistically significant are indicated with dots. The scales of the top row maps is in the range \([-10; +10\ W/m^2]\) whereas the values for the bottom row maps (that represent differences in radiative forcings) vary between \([-2; +2]\) or \([-5; +5]\) \(W.m^2\).

Figure 11: (a) Reference method \((M_{\text{REF}})\) radiative forcing of the first indirect effect \((W.m^2)\); (b): difference of radiative forcing between the reference method \((M_{\text{REF}})\) and the off-line method \((M_{\text{Offline}})\). The statistical significance of the difference was tested at the 95% confidence level using a bootstrap method. Regions where the difference is statistically significant are indicated with dots.

Figure 12: Impact on surface temperature of coupling chemistry and climate: difference of temperature anomaly \((\Delta T=T_{PD}-T_{PI})\) between on-line \((\Delta T_{V})\) and off-line configuration \((\Delta T_{M})\). The statistical significance of the difference was tested at the 95% confidence level using a student test. Regions where the difference is statistically significant are indicated with dots.
Figure 13: Schematical representation of the error in the radiative forcing estimation computed from 2 sulfate fields which don’t satisfy the criteria of having consistent meteorological fields. Correction with the “F_{M.PI} – F_{V.PI}” term estimated in the section 5.5. The fluxes do not include the impact of direct effect. Only the change due to the first indirect effect is taken into account.

Figure 14: Difference of the radiative forcing of the 1st indirect effect calculated from the extended off-line method corrected with the ∆NF_{PI} term and that one calculated in the reference method (experiment VAR) in W.m^-2. The statistical significance of the difference was tested at the 95% confidence level using a bootstrap method. Regions where the difference is statistically significant are indicated with dots.

Color bar of the first map varies from -10 and +10 W/m^-2 whereas values of the second map (difference) vary from -2 and +2 W.m^-2.

Figure 15: Correlation between the present-day sulfate concentration and the preindustrial one for 2 grid points (Paris and Tunisia) and 2 months (January and July). The blue line represents the expected values of the actual by preindustrial instantaneous ratio considering it is the same that the ratio of monthly mean concentrations. Slopes indicate the values of the monthly mean ratio.

Figure 16: Difference of radiative forcing between the method using an approximation of the on-line preindustrial concentration and the extended off-line method for the direct effect (a) and between the method using an approximation of the on-line preindustrial concentration and the reference method for the first indirect effect (in W.m^-2). The statistical significance of the difference was tested at the 95% confidence level using a bootstrap method. Regions where the difference is statistically significant are indicated with dots.

Figure 17: Zonal mean of the difference of first indirect radiative forcing (W.m^-2) of the off-line method (black) and the preindustrial sulfate concentration approximation method (red) compared to the reference method.

Figure 18: Comparison of biases on the estimation of the first indirect radiative forcing computed with the four tested methods and relatively to the reference method: off-line method (red), extended off-line method (green); corrected extended off-line method (cyan)
preindustrial sulfate concentration approximation method (blue). Taylor diagram (left) presents the performance of methods to represent the spatial pattern of the 1st indirect effect (including standard deviation, correlation and centered root mean squared error). Right: scatter plot compares the mean bias and the standard deviation of the error for each method.
Figure 1

\[ \text{cdnc} = f(\text{m}_{\text{sulf}}) \]

- BL adjusted
- BL orig

\[ \text{m}_{\text{sulf}} (\mu gSO_4/m^3) \]

\[ \text{cdnc} (cm^{-3}) \]
\[ \Delta F_V = -0.73 \text{ W.m}^{-2} \]

\[ \Delta F_M = -0.64 \text{ W.m}^{-2} \]

\[ F_{M, PD} = 240.57 \text{ W.m}^{-2} \]

\[ F_{M, PI} = 241.27 \text{ W.m}^{-2} \]

\[ F_{M, PD} = -0.70 \text{ W.m}^{-2} \]

\[ F_{M, PI} = -0.70 \text{ W.m}^{-2} \]

Figure 2
Figure 4
\[
F_{V,PD} - F_{M,PD} = 0.24 \text{ W.m}^{-2}
\]
\[
F_{V,PI} - F_{M,PI} = 0.22 \text{ W.m}^{-2}
\]

Figure 5
Figure 6
Figure 7
(a) present-day period

(b) preindustrial period

Figure 8
Figure 9
Figure 10
Figure 11
\[ RF_{\text{M-Offline-ext}} = -0.17 \text{ W.m}^{-2} \]
\[ FM_{,\text{PI}} - FV_{,\text{PI}} = -0.23 \text{ W.m}^{-2} \]
\[ RF_{\text{CORR}} = -0.40 \text{ W.m}^{-2} \]

Figure 13
Figure 14: Difference between corrected method and reference method.

The map illustrates the difference in values across various regions of the Earth, with color coding indicating the magnitude of the difference.

Legend:
- 2
- 1
- 0.5
- 0.2
- 0.1
- -0.1
- -0.2
- -0.5
- -1
- -2
Figure 15
Figure 16
Figure 17
Figure 18