Supplementary Material for

Particle Mass Yield from β-Caryophyllene Ozonolysis

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Manuscript submitted to Atmospheric Chemistry and Physics, October 2011

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A. β-Caryophyllene dark ozonolysis in a continuously mixed flow reactor (CMFR)

Based on the reaction rate constants of \( k_1 \) and \( k_2 \), a simplified gas-phase reaction scheme for the β-caryophyllene ozonolysis can be described as:

\[
\text{VOC} + O_3 \rightarrow^k G_1 + O_3 \rightarrow^k G_2
\]  

(S1)

where VOC, G₁, and G₂ represent the precursor volatile organic compound, the first-generation products, and the second-generation products, respectively. Under an assumption of negligible wall losses of gas-phase species, the three differential equations that govern the species concentrations inside the CMFR are as follows:

\[
\frac{d\text{[VOC]}}{dt} = \frac{[\text{VOC}]_0}{\tau} - \frac{[\text{VOC}]}{\tau} - k_1[O_3][\text{VOC}]
\]  

(S2)

\[
\frac{d[G_1]}{dt} = -\frac{[G_1]}{\tau} + k_1[O_3][\text{VOC}] - k_2[O_3][G_1]
\]  

(S3)

\[
\frac{d[G_2]}{dt} = -\frac{[G_2]}{\tau} + k_2[O_3][G_1]
\]  

(S4)

where \( \tau \) is the residence time of the CMFR, \([\text{VOC}]_0 \) is the concentration of β-caryophyllene in the CMFR inflow, \([O_3] \) is the ozone concentration, and \([\text{VOC}], [G_1], \) and \([G_2] \) are the species concentrations in the CMFR outflow.

At steady state, \( \frac{d[\text{VOC}]}{dt} = \frac{d[G_1]}{dt} = \frac{d[G_2]}{dt} = 0 \). The algebraic solution for Equations S2 to S4 are as follows:

\[
[\text{VOC}]_{ss} = \frac{[\text{VOC}]_0}{\tau k_1[O_3]_{ss} + 1}
\]  

(S5)

\[
[G_1]_{ss} = \frac{\tau k_1[O_3]_{ss}[\text{VOC}]_0}{(\tau k_1[O_3]_{ss} + 1)(\tau k_2[O_3]_{ss} + 1)}
\]  

(S6)
The ozone concentration was maintained at steady state in the CMFR for each experiment. The reaction rate constants are $1.16 \times 10^{-14}$ molecule$^{-1}$ cm$^3$ s$^{-1}$ for the ozonolysis of the endo-cyclic double bond ($k_1$) of $\beta$-caryophyllene (Shu and Atkinson, 1995) and $1.1 \times 10^{-16}$ molecule$^{-1}$ cm$^3$ s$^{-1}$ for the ozonolysis of the exo-cyclic double bond ($k_2$) of the first generation products (Winterhalter et al., 2009). The mean residence time of the chamber is 13000 s.

**B. Parameters used in air quality models**

Regional and global chemical transport models have employed parameterizations derived from the data reported by Griffin et al. (1999) to estimate the contribution of sesquiterpenes to the ambient organic particle mass concentrations (Chung and Seinfeld, 2002; Sakulyanontvittaya et al., 2008; Carlton et al., 2010; Zhang and Ying, 2011). Table S2 listed the parameters used in Goddard Institute for Space Studies General Circulation Model II-prime (GISS GCM II-prime) and Community Multiscale Air Quality Model (CMAQ). The mass-based stoichiometric yield $\alpha$ and the product saturation concentration $C^*$ were derived for one-product model (Odum et al., 1996; Kroll and Seinfeld, 2008) as described as follows:

$$Y(M_{\text{org}}) = \alpha \left( 1 + \frac{C^*}{M_{\text{org}}} \right)^{-1}$$  \hspace{1cm} (S8)

where $Y$ is the particle mass yield and $M_{\text{org}}$ is the organic mass concentration. The gas-to-particle partitioning of semivolatile compounds depends on temperature. $C^*$ is therefore defined by the Clausius-Clapeyron equation as follows:
\[ C^*(T) = C^*(T_0) \frac{T_0}{T} \exp \left[ \frac{\Delta H_{\text{vap}}}{R} \left( \frac{1}{T_0} - \frac{1}{T} \right) \right] \]  

where \( \Delta H_{\text{vap}} \) is the vaporization enthalpy, \( R \) is the ideal gas constant, and \( T_0 \) is the reference temperature (i.e., 308 K for \( \beta \)-caryophyllene oxidation in Griffin et al. (1999)).

Recent experimental data suggest that the \( \Delta H_{\text{vap}} \) values used in earlier versions of CMAQ (\( \Delta H_{\text{vap}} = 156 \) or 163 kJ mol\(^{-1}\) in version 4.3 to 4.6) were overestimates (Offenberg et al., 2006). The new \( \Delta H_{\text{vap}} \) value of 40 kJ mol\(^{-1}\) was used in CMAQ version 4.7 (Carlton et al., 2010; Zhang and Ying, 2011). Moreover, the original analysis of Griffin et al. (1999) assumed a density of 1000 kg m\(^{-3}\) for secondary organic material (SOM), which was adapted by Chung and Seinfeld (2002) and Sakulyanontvittaya et al. (2008) in their models. The original CMAQ v4.7 (Zhang and Ying, 2011) scaled the values of \( \alpha \) by 30% to account for recent laboratory measurements of density of 1300 kg m\(^{-3}\) for \( \beta \)-caryophyllene-derived SOM (Bahreini et al., 2005). More accurately, Carlton et al. (2010) derived a new set of \( \alpha \) and \( C^* \) from the original data from Griffin et al. (1999) in which both \( Y \) and \( M_{\text{org}} \) were corrected by the SOM density of 1300 kg m\(^{-3}\) and the data from Hoffmann et al. (1997) were excluded.
<table>
<thead>
<tr>
<th>Excess Ozone (ppbv)</th>
<th>$\alpha_0$</th>
<th>$\alpha_1$</th>
<th>$\alpha_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>50</td>
<td>0.15 ± 0.02</td>
<td>0.16 ± 0.07</td>
<td>0.32 ± 0.13</td>
</tr>
<tr>
<td>100</td>
<td>0.13 ± 0.03</td>
<td>0.22 ± 0.10</td>
<td>0.38 ± 0.15</td>
</tr>
<tr>
<td>200</td>
<td>0.17 ± 0.05</td>
<td>0.11 ± 0.17</td>
<td>1.03 ± 0.30</td>
</tr>
</tbody>
</table>

**Table S1.** Summary of the optimized mass-based stoichiometric yields $\alpha_i$ of product class $i$ for β-caryophyllene ozonolysis. The volatility of product class $i$ is prescribed in decadal units of $10^{-i}$, where $10^{-i}$ is denoted as $C_i^*$. 

<table>
<thead>
<tr>
<th>Reference</th>
<th>Model</th>
<th>$\alpha$</th>
<th>$C^*$ at 298 K (µg m$^{-3}$)</th>
<th>$\Delta H_{vap}$ (kJ mol$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chung et al. (2002)</td>
<td>GISS GCM II-prime</td>
<td>1.000</td>
<td>12.986</td>
<td>42</td>
</tr>
<tr>
<td>Sakulyanontvittaya et al. (2008)</td>
<td>CMAQ v4.5</td>
<td>1.000</td>
<td>2.935</td>
<td>163</td>
</tr>
<tr>
<td>Zhang et al. (2011)</td>
<td>CMAQ original v4.7</td>
<td>1.300</td>
<td>14.710</td>
<td>40</td>
</tr>
<tr>
<td>Carlton et al. (2010)</td>
<td>CMAQ revised v4.7</td>
<td>1.537</td>
<td>29.893</td>
<td>40</td>
</tr>
</tbody>
</table>

**Table S2.** Summary of the mass-based stoichiometric yield $\alpha$, the product saturation concentration $C^*$, and the vaporization enthalpy $\Delta H_{vap}$ used in four different regional and global models for β-caryophyllene oxidation. Parameters were derived for one-product model (Eq. S8) based on the yield data reported by Griffin et al. (1999) for β-caryophyllene photooxidation at 308 K. The parameters for β-caryophyllene oxidation were used for all sesquiterpenes when estimating sesquiterpene-derived particle mass concentrations by Chung and Seinfeld (2002) and Sakulyanontvittaya et al. (2008). In contrast, in CMAQ v4.7 (original and revised), the parameters for both β-caryophyllene and α-humulene oxidation were lumped together to represent the overall sesquiterpene oxidation.
List of Figures

**Figure S1.** Two examples of the mass-diameter distributions recorded by the AMS compared to the distributions calculated from the number-diameter SMPS measurements and an optimized particle effective density $\rho_{\text{eff}}$.

**Figure S2.** Scatter plot of the total particle mass concentrations measured by the AMS and the mass concentrations calculated from the SMPS data using the optimized particle effective densities of each experiment. Error boxes around the data points show the instrument uncertainty of 30% for the AMS (Jimenez et al., 2003) and the SMPS (Wiedensohler et al., 2010).

**Figure S3.** Dependence of the material density $\rho_{\text{org}}$ of the particle-phase organic material on the wall-loss corrected organic particle mass concentration $M_{\text{org,corr}}$. Results are shown for both the DMA-APM and the AMS-SMPS methods.

**Figure S4.** (a) Differential and (b) cumulative number-diameter distributions of the SOM-coated sulfate particles for the experiments of Table 2.

**Figure S5.** Particle mass yield before and after applying wall-loss corrections (Equation 1). Black dots represent a subset of the data collected under typical wall-loss conditions ($\beta = 1.04 \pm 0.11 \text{ h}^{-1}$) (Table 2). Red dots represent data collected for modified wall-loss conditions ($\beta = 0.19 \pm 0.02 \text{ h}^{-1}$ for Exp. #27 in panel a1/a2) and ($\beta = 0.49 \pm 0.03 \text{ h}^{-1}$ for Exp. #10 in panel b1/b2). Solid lines are drawn to guide the eye.

**Figure S6.** Chemical structures associated with product labeling used in the main text and highlighting ozonolytic conversions from first- to second-generation
products. The conversions from first- to second-generation products are presented by arrows. The red label calls attention to a product that appears to have been incorrectly assigned in previous work (Li et al., 2011).
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Figure S1

(a) Exp. #1 (monodisperse seed)

\( \rho_{\text{eff}} = 1780 \text{ kg m}^{-3} \)

(b) Exp. #26 (polydisperse seed)

\( \rho_{\text{eff}} = 1710 \)
Figure S2

AMS Total Particle Mass Concentration [$\mu$g m$^{-3}$]

SMPS Total Particle Mass Concentration [$\mu$g m$^{-3}$]

Fitted Line:
Slope = 0.99 ± 0.02
r = 0.99
Figure S3

Material Density of SOM, $\rho_{\text{org}}$ [kg m$^{-3}$]

Wall-Loss Corrected Particle-Phase Organic Mass Concentration, $M_{\text{org, corr}}$ [µg m$^{-3}$]
Figure S4

(a) Particles having secondary organic material coated on
- 70-nm monodisperse (NH₄)₂SO₄ particles
- 50-nm monodisperse (NH₄)₂SO₄ particles
- Polydisperse (NH₄)₂SO₄ particles x 0.25

(dN/dlog₁₀dₘ) [cm⁻³] at 10⁻⁴ cm⁻³

Cumulative Distribution of Particle Number Concentration

Mobility Diameter, dₘ [nm]
Figure S5

(a1) Original data (50 ppbv O₃)

(a2) Corrected for wall losses

(b1) Original data (100 ppbv O₃)

(b2) Corrected for wall losses

Particle-Phase Organic Mass Concentration, (M_{org})_{outflow} [µg m⁻³]

Initial β-Caryophyllene Concentration [ppbv]
Figure S6