



Disk and circumsolar radiances in the presence of ice clouds

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Abstract. The impact of ice clouds on solar-disk and circumsolar radiances is investigated using a Monte Carlo radiative transfer model. The monochromatic direct and diffuse radiances are simulated at angles of 0° to 8° from the center of the Sun. Input data for the model are derived from measurements conducted during the 2010 Small Particles in Cirrus campaign together with state-of-the-art databases of optical properties of ice crystals and aerosols. For selected cases, the simulated radiances are compared with ground-based radiance measurements with the Sun and Aureole Measurement (SAM) instrument.

First, the sensitivity of the radiances to the ice cloud properties and aerosol optical thickness was addressed. The angular dependence of the disk and circumsolar radiances was found to be most sensitive to assumptions about ice crystal roughness (or, more generally, non-ideal features of ice crystals) and size distribution, with ice crystal habit playing a somewhat smaller role. Second, in the comparisons with SAM data, the ice-cloud optical thickness was adjusted for each case so that the simulated radiances agreed closely (i.e., within 3 %) with the measured disk radiances. Circumsolar radiances at angles larger than $\approx 3^\circ$ were systematically underestimated when assuming smooth ice crystals, but the agreement with the measurements was better when rough ice crystals were assumed. Our results suggest that it may well be possible to infer the particle roughness (or more generally, non-ideality) directly from ground-based SAM measurements. In addition, the results show the necessity of correcting the ground-based measurements of direct radiation for the presence of diffuse radiation in the instrument's field of view, in particular in the presence of ice clouds.



20 1 Introduction

The portion of solar radiation that appears to originate from a small disk around the Sun is called circumsolar radiation or solar aureole. This radiation arises from near-forward scattering of direct solar radiation by atmospheric particles with sizes comparable to or larger than the wavelength of sunlight (1 μm to 0.1 mm); the larger the particle is compared to the wavelength of radiation, the more scattering is concentrated at near-forward angles and more peaked the scattering phase function P_{11} is. Consequently, the amount of circumsolar radiation varies widely depending on the geographical, seasonal and diurnal variation of airborne particles (Norrig et al., 1991; Neuman et al., 2002). As ice crystals are typically much larger than aerosol particles or gas molecules, a considerably larger part of the direct solar radiation is scattered into the circumsolar region in the presence of ice clouds.

30 In addition to the phase functions, the amount of circumsolar radiation depends on single-scattering albedos and extinction coefficients of atmospheric gases and particles. All these optical properties depend on the wavelength. Furthermore, the ensemble/volume-averaged optical properties depend on the concentration, composition and size-shape distribution of the particles. Although the role of the ice crystal sizes and shapes on their optical properties has been studied in much detail (Macke et al., 1998; Zhang et al., 1999; McFarquhar et al., 2002; Schlimme et al., 2005; Um and McFarquhar, 2007, 2009, 2011, 2013), there is no detailed information on how ice crystals affect the angular dependence of circumsolar radiances. However, the studies of Segal-Rosenheimer et al. (2013) and Reinhardt et al. (2014) have revealed that differences in the modeled forward scattering of smooth and roughened ice crystals as well as different shape distributions of ice crystals lead to differences

40 in the circumsolar radiation. DeVore et al. (2012) also noted the impact of ice crystals properties (roughness and effective radius) on calculated circumsolar radiances.

Circumsolar radiation is widely detected by instruments measuring the direct radiation (i.e. pyrhemometers) and therefore counted as direct radiation. Such instruments often have a half-opening angle of 2° - 3° , whereas the half-width of the solar disk is only about 0.27° when observed from the

45 Earth. Depending on the ambient atmospheric conditions, the near-forward scattered radiation can be a large portion of the total radiation measured by these instruments, leading to overestimation of the amount of direct solar radiation. Therefore, retrievals of ice cloud optical thickness and other properties from the direct radiation measurements can be biased. There have been some efforts to quantify the amount of circumsolar radiation in the measured direct radiation and to account for

50 its impact on the underestimation of cloud optical thickness (Shiobara and Asano, 1994; Kinne et al., 1997; Segal-Rosenheimer et al., 2013). For example Segal-Rosenheimer et al. (2013) proposed a new approach to derive ice cloud optical thickness and effective diameter from sun photometry measurements by using ice-cloud optical property models.

Since the circumsolar radiance distribution is usually nearly radially symmetric around the Sun,

55 it is reasonable to describe it as a function of the angular position relative to the centre of the Sun (Blanc et al., 2013). This solar radiance profile is also called the sunshape. Wilbert et al. (2012) pre-



sented a method for determining the sunshape using a pair of pyrheliometers with different opening angles. The amount of circumsolar radiance and the radial profile of sunshape can also be measured using a Sun and Aureole Measurement (SAM) instrument. It consists of two solar tracking cameras: 60 one observing the Sun disk and another the aureole. The cameras are filtered into the 670 ± 5 nm wavelength band. SAM measures the disk and circumsolar radiances with a very high dynamic range and produces the disk and aureole radiances as a function of angle from the center of the Sun out to 8° with an angular resolution of 0.0148° . DeVore et al. (2009) demonstrated the ability of SAM measurements to derive the effective radius and optical thickness of ice clouds and DeVore et al. 65 (2012) used MODIS retrievals of thin cirrus to calculate solar disk and aureole measurements that were compared with SAM measurements. Reinhardt et al. (2014) have also developed a method to determine circumsolar radiation from the satellite observations. They noted that the uncertainties in their retrieval due to assumptions on the ice particle shape can sum up to 50 %, and even larger errors are expected if instantaneous values are compared against SAM measurements. The main source of 70 error is, however, the uncertainties in the cloud properties. DeVore et al. (2012) suggested that a collection of SAM measurements might provide a useful template for helping to derive phase functions of ice crystals.

There have been some efforts to account for the impact of circumsolar radiation and sunshape on concentrating solar energy applications (Bui and Monger, 2004; Reinhardt, 2013; Reinhardt et al., 75 2014; Wilbert et al., 2012, 2013). These applications use concentrating solar collectors whose half opening angles are typically less than 1° . Due to the 1° – 2° smaller acceptance angle than that of a pyrheliometer, these collectors are able to use only a fraction of the circumsolar radiation measured with a pyrheliometer. Consequently, if the performance of the solar concentrating system is predicted based on measurements of direct radiation (including circumsolar radiation), the energy contained 80 in the circumsolar region at angles from 1° to 3° can lead to overestimation of the performance. To better estimate and optimize the amount of received energy of the concentrating solar energy systems, the detailed angular distribution of the circumsolar radiation and how it varies in time and location should be known.

In this study, we investigate how circumsolar radiances depend on the ice cloud microphysical 85 properties. In particular, the impacts on circumsolar radiances due to ice crystal size-shape distribution and roughness, ice cloud optical thickness and aerosol optical thickness are simulated. For the purpose, a forward Monte Carlo radiative transfer model is used. Monochromatic downwelling radiances for various ice-cloud scenarios are simulated at a wavelength of $0.670 \mu\text{m}$. These scenarios are based on in-situ-measured size distributions of mid-latitude ice clouds together with either 90 measurement-based shape distributions or idealized single-habit distributions. These size-shape distributions of ice crystals are combined with a database of single-scattering properties of ice crystals (Yang et al., 2013) to produce size-shape-integrated bulk optical properties of the ice clouds as needed for input to the radiative transfer model. The in-situ-based distributions of ice crystals were



obtained from aircraft measurements made over the Atmospheric Radiation Measurement (ARM)
95 program's Southern Great Plains (SGP) site (36.606° N, 97.485° W) during the year 2010. In ad-
dition to probing the sensitivity of the disk and circumsolar radiances to ice cloud properties, the
simulated radiances are compared against selected ground-based solar-disk and circumsolar radi-
ance measurements by the SAM instrument at the SGP site.

2 Radiative transfer model

100 In this study, the angular dependence of solar disk and circumsolar radiances are simulated with a
modified version of the Monte Carlo Model of the University of Kiel (MC-UniK) by Macke et al.
(1999). Even though a plane-parallel horizontally homogeneous atmosphere is assumed in the radi-
ation calculations (see below), the Monte Carlo technique is applied here because of its flexibility.
Specifically, it allows us to consider the finite width of the Sun and to compute radiances at an arbi-
105 trarily high angular resolution in the vicinity of the direction of the Sun, without incurring extreme
computational costs. In fact, we are not aware of any deterministic radiative transfer models that
would satisfy these criteria.

2.1 Technical details

The MC-UniK is a forward Monte Carlo model for efficient calculations of radiances at discrete
110 directions. It employs the Local Estimate Method (e.g., Marshak and Davis, 2005) and has been val-
idated within the Intercomparison of 3-D-Radiation Codes project (Cahalan et al., 2005). The model
simulates the scattering events of photons within the ice cloud/atmosphere using a non-truncated
treatment for the phase functions. The free path length is based on Beer's law and gives the dis-
tance between two successive scattering processes. The scattering direction is derived using a ran-
115 dom number generator so that the scattering angle s corresponding to a given random number $[0,1]$
equals the cumulative phase function from 0 to s , and the azimuth angle is sampled uniformly in the
range $[0, 2\pi]$. Absorption is taken into account by multiplying the photon weight by the local single
scattering albedo. For reasons of variance reduction and computing time, techniques as proposed by
Barker et al. (2003) have been implemented. For calculating the radiance field, the Local Estimate
120 Method is more efficient than the common Monte Carlo photon counting method because no pho-
tons get lost. Thus, in effect, MC-UniK assumes that a fraction of the photon is scattered directly into
each detector. These photons are attenuated along the optical path between the scattering location
and the detector.

2.2 Modifications

125 We have modified the original MC-UniK to account for the finite width of the solar disk, that is
an opening angle of 0.534° . In addition, a phenomenon called limb darkening is accounted for.



The solar radiation that reaches the observer originates in the photosphere of the Sun peaking at an optical depth of roughly unity along the line of sight. On average, this corresponds to a temperature of about 5778 K. However, along a slant line of sight toward the Sun's limb, an optical depth of one
130 is reached at a higher altitude with a lower temperature. Hence the intensity reaching the observer from the limb of the Sun is lower than that from the center (Green and Jones, 2015). In our version of MC-UniK the limb darkening is taken into account by using the formula

$$I(\beta) = I(0,0)[a + b\cos(\beta) + c\cos^2(\beta)] \quad (1)$$

given in Böhn-Vitense (1989), where β is the angular distance from the center of the Sun to the limb
135 (0° – 90°). At the wavelength of $\lambda=0.69 \mu\text{m}$, the coefficients have values of $a=0.4128$, $b=0.7525$, and $c=-0.1761$.

The model output is modified to include the direct and diffuse radiances at the surface (in units of $\text{Wcm}^{-2}\mu\text{m}^{-1}\text{sr}^{-1}$) for specified detector positions. For the mean solar constant at $\lambda=0.670 \mu\text{m}$, values of $0.1509 \text{ Wcm}^{-2}\mu\text{m}^{-1}$ (Guemard, 2004) and $2206 \text{ Wcm}^{-2}\mu\text{m}^{-1}\text{sr}^{-1}$ are used in the calcu-
140 lation of diffuse and direct radiances, respectively. The latter value is obtained by dividing the former by the solid angle of Sun.

2.3 Input

The model domain is separated into grid boxes which are characterized by their bulk optical properties: the volume extinction coefficient K_{ext} , the single-scattering albedo ω , and the scattering phase
145 function $P_{11}(\gamma)$, where γ is the scattering angle. Here the model domain of MC-UniK is divided into 15 vertical layers extending from the ground up to 50 km. Gas absorption and Rayleigh scattering occur in all layers, while aerosols are assumed to be confined to the lowest layer below 2 km. The ice cloud resides in layers 5-11 (8.0-11.5 km) depending on the case (see Sect. 3.2). A plane parallel cloud is assumed due to insufficient information on the cloud horizontal structure. Thus, while the
150 Monte Carlo model can account for 3D effects, the effects related to cloud horizontal inhomogeneity are not accounted for.

Furthermore, the solar zenith angle (θ), detector positions, and surface albedo data are required. A total of 418 detectors pointing to the Sun and its surrounding areas inside the opening angle of 16° are positioned so that they cover both the horizontal and vertical cross sections of the area as
155 illustrated in Fig. 1. For surface albedo, a fixed value of 0.2 is used. To achieve sufficient accuracy for the calculations, 8 million photons are used. At the angles considered here (0° – 8° from the center of Sun), the resulting random errors are mostly below 3 % (6 %) for rough (smooth) crystals, with smaller errors at the smaller angles.



3 Optical properties

160 The optical properties of ice clouds (and atmospheric gases and aerosols) needed as input to the
MC-UniK are based on data collected during the Atmospheric Radiation Measurement program's
2010 Small Particles in Cirrus (SPARTICUS) field campaign (Mishra et al., 2014; Muhlbauer et al.,
2014; Jackson et al., 2015). The aircraft measurements were collected in the vicinity of the ground-
based measurements made at the SGP site. Out of the numerous case days of SPARTICUS, only
165 two were deemed suitable for the present investigation: 23 March (hereafter flight A) and 24 June
(hereafter flight B). During these flights, there was a visually observable cirrus cloud without lower
cloud layers and all the needed in situ and ground-based measurement data had good quality.

3.1 Optical properties of atmospheric gases and aerosols

To account for Rayleigh scattering and gas absorption, the optical properties (ω and K_{ext}) of the
170 atmosphere without cloud and aerosols are calculated using the scheme of Freidenreich and Ra-
maswamy (1999). The spectral band of 0.599–0.685 μm is used for gas absorption, with Rayleigh
scattering optical depth scaled to 0.67 μm . The vertical profiles of temperature and water vapour are
based on radiosondes launched at the SGP site, complemented by ERA-Interim reanalysis data (Dee
et al., 2011) in the middle and upper stratosphere. Ozone profiles are taken from the ERA-Interim
175 data. The phase function for Rayleigh scattering is $P_{11}(\gamma) = (3/4)(1 + \cos^2 \gamma)$.

The ensemble-averaged aerosol ω and $P_{11}(\gamma)$ are taken from the OPAC (Optical Properties of
Aerosols and Clouds) database (Hess et al., 1998), assuming values for continental average aerosols
at $\lambda = 0.650 \mu\text{m}$ computed at a relative humidity of either 70 % (for comparison with SAM mea-
surements during flight B) or 50 % (for all other calculations). The aerosol optical thickness τ_a is
180 estimated from the AERONET level 1.5 τ_a retrieval (at $\lambda = 0.675 \mu\text{m}$) and from the visible Multifil-
ter Rotating Shadowband Radiometer (MFRSR) measurements (at $\lambda = 0.673 \mu\text{m}$) conducted at the
SGP site, which yields $\tau_a = 0.09$ during flight A and $\tau_a = 0.166$ during flight B. The aerosol K_{ext}
is derived from τ_a assuming that the aerosols are confined to the lowest 2 km.

3.2 Ice crystal size-shape distributions

185 During SPARTICUS in situ probes were installed on the Stratton Park Engineering Company (SPEC)
Inc. Learjet 25 aircraft. The Learjet conducted 101 missions sampling several cirrus clouds in the
mid-latitudes of the United States at temperatures between -70° and -20° C. The probes on the Learjet
that were used in this study include the Cloud Particle Imager (CPI) acquiring high 2.3 μm resolution
images of particles, the Fast Forward Scattering Spectrometer Probe (FFSSP) measuring particles
190 with maximum diameter (D_{max}) smaller than 50 μm from the forward scattering of light, the Two-
Dimensional Stereo (2DS) probe nominally measuring particles with $10 < D_{max} < 1280 \mu\text{m}$, and a
2-D Precipitation Probe (2DP) measuring particles with $200 < D_{max} < 6400 \mu\text{m}$ for flight A and a



High Volume Precipitation Sampler (HVPS-3) measuring particles with $150 < D_{max} < 19200 \mu\text{m}$ for flight B.

195 The composite size distribution required to calculate the microphysical and optical properties was determined using the FFSSP to characterize particles with $D_{max} < 50 \mu\text{m}$, the 2DS for $D_{max} < 1200 \mu\text{m}$, and the 2DP or HVPS-3 for larger particles. Concentrations of small ice crystals (defined as those with $D_{max} < 100 \mu\text{m}$) are, however, highly uncertain due to a small and poorly defined sample volume (Baumgardner and Korolev, 1997; McFarquhar et al., 2016) and potential contribu-
200 tions from shattered artifacts (e.g. Gardiner and Hallett, 1985; McFarquhar et al., 2007; Korolev et al., 2011, 2013) in both the 2DS and FFSSP. Therefore, four alternative representations of the concentration of small ice crystals are used to test the sensitivity of the results to these concentrations. In *small*_{100%}, the concentration of crystals with $D_{max} < 100 \mu\text{m}$ is taken directly from the FFSSP and 2DS measurements. In *small*_{0%}, *small*_{50%} and *small*_{200%} the measured concentration is multiplied
205 by 0 (i.e., no small ice crystals), 0.5 and 2, respectively.

For large ice crystals ($D_{max} > 100 \mu\text{m}$), the size dependent shape distributions are based on the CPI images measured in situ. Um and McFarquhar (2011) and Ulanowski et al. (2004) show that the detailed shapes of small ice crystals cannot be identified using the CPI due to its limited image resolution and blurring of images due to diffraction that renders the shape classification of small ice
210 crystals unreliable. Due to the lack of reliable in situ measurements of the shapes of crystals with $D_{max} < 100 \mu\text{m}$, they are assumed to be hollow columns. For large crystals, an automatic ice-cloud particle habit classifier, IC-PCA (Lindqvist et al., 2012) is used to determine the fraction of different habits as a function of particle size from the CPI images. The IC-PCA automatically sorts the crystals into 8 classes: bullet, column, column aggregate, bullet rosette, bullet rosette aggregate, plate, plate
215 aggregate, and irregular. In our study we classify bullets as columns and bullet rosette aggregates as column aggregates due to the lack of information about their single-scattering properties. The final six habit classes listed in Table 1 are named as column, column agg, bullet rosette, plate, plate agg, and irregular. The size-resolved shape distributions are created by combining the size distributions (measured by 2DS and 2DP or HVPS-3) and the relative portions of the size-resolved shape distribu-
220 tions from CPI/IC-PCA at each layer. During flight A the most dominant crystal habits were bullet rosettes and column aggregates, whereas during flight B, column aggregates and plate aggregates dominated. This is seen in Fig 2, where the vertically averaged size-shape distributions of flights A and B are shown as a function of D_{max} . During both flights, column and irregular crystals are only found at small particle sizes with a small fraction of plates also present.

225 Based on the stepwise flight path of the aircraft, the measurements of ice crystal are sorted into 0.5 km vertical layers. In each layer, the particle concentrations and size distributions are averaged over the time the Learjet was in the appropriate layer. During flight A the cloud was present in four of the layers (from 9.5 km to 11.5 km) and during flight B in seven layers (8.0 to 11.5 km) (Table 2).



3.3 Ensemble-averaged ice crystal optical properties

230 To obtain the ensemble-averaged optical properties of the ice clouds during flights A and B, the in-
situ-measured size-shape distributions are combined with single-scattering properties of individual
ice crystals obtained from the database of Yang et al. (2013). In this database, the optical properties
are given as a function of wavelength and size (D_{max}), shape and roughness of the particle. The
three roughness options are: completely smooth (i.e. homogeneous) (CS), moderately rough (MR)
235 and severely rough (SR). The effect of roughness is simulated by randomly distorting the surface
slope for each incident ray, assuming a normal distribution of local slope variations with a standard
deviation of 0.03 and 0.50 for the MR and SR cases, respectively, (Eq. 1. in Yang et al. (2013)). In
fact, this treatment does not represent any specific roughness characteristics but attempts instead to
mimic the effects due to non-ideal crystal characteristics in general (roughness effects, irregularities
240 and inhomogeneities like air bubbles).

For each ice crystal size and shape, the cross-sectional area, A , the extinction efficiency, Q_{ext} ,
the single-scattering albedo, ω , and the phase function $P_{11}(\gamma)$ at $\lambda=0.670 \mu\text{m}$ are obtained from the
database, using the closest D_{max} available in the database. The phase function with 498 scattering
angles (between 0° and 180°) is interpolated to 2011 scattering angles to obtain sufficient angular
245 resolution in the near-forward directions. For single-habit distributions, the in-situ-measured size
distribution $N(D_{max} > 100 \mu\text{m})$ of either flight A or B is combined with the optical properties of
that habit and then integrated over the size distribution to obtain the vertical profiles of ensemble av-
eraged optical properties: K_{ext} , ω , and $P_{11}(\gamma)$. For the IC-PCA based habit distributions, the optical
properties of each habit are weighted by the IC-PCA fractions before size integration. Hereafter, the
250 optical properties based on the IC-PCA size-shape distributions of flight A and B are referred to as
 $large_A$ and $large_B$, respectively. Finally, when studying the sensitivity of disk and circumsolar ra-
diances to the concentration of small ice crystals, $large_A$ and $large_B$ are combined with the optical
properties of the four alternative size distributions of small crystals. Habits used for crystals with
 $D_{max} > 100$ are listed in Table 1 while crystals smaller than that are treated as hollow columns (see
255 Sect. 3.2).

In the radiative transfer simulations, we do not, however, use the cloud optical thickness integrated
from the in situ based size-shape distributions ($\tau_c = \int K_{ext}(z) dz$, where z is altitude). Instead, in
our sensitivity tests, we use the same user-specified τ_c for each size-shape distribution. This is to
overcome the effects related to different area-ratios of the crystal habits and to make the comparison
260 of the size-shape distributions of flights A and B possible. By fixing the cloud optical thickness, we
adjust the in situ concentrations of the size-shape distributions by a uniform factor across all shapes
and sizes. Furthermore, when comparing the modeled radiances with those measured with the SAM
instrument, τ_c is adjusted so that modeled radiances in the disk region agree closely (i.e., within
 $\approx 3\%$) with the measurements. This often leads to value of τ_c that deviate from those retrieved
265 from the SAM (τ_{SAM}) during flights A and B. The values of τ_{SAM} vary from 0.1 to 2.1 during



flight A and from 0.3 to 3.6 during flight B (Fig. 3), indicating that the clouds were not horizontally homogeneous during the flights. This further justifies our approach of using a fixed cloud optical depth because variations in τ_{SAM} over the course of a flight show that exact agreement between retrieved and in-situ-based optical depth should not be expected.

270 3.4 Ice cloud phase functions

Ice crystal phase functions play a key role in determining the angular distribution of disk and circum-solar radiances. Therefore, to aid the interpretation of the radiance comparisons, the impact of ice crystal habit and roughness on P_{11} (integrated over the cloud depth and the size-shape distribution) is considered in Figs. 4 and 5 respectively.

275 In Fig. 4a, P_{11} of the in-situ based $large_A$ and $large_B$ size-shape distributions are compared, assuming SR ice crystals, while in Fig. 4b–c, the relative differences between P_{11} of single-habit distributions and the $large_A$ and $large_B$ distributions are shown, respectively. The general shape of P_{11} is similar for all size-shape distributions, with values of P_{11} decreasing by roughly four orders of magnitude from the exact forward-scattering direction $\gamma = 0^\circ$ to $\gamma = 10^\circ$ for flight A and by
280 nearly five orders of magnitude for flight B. The slope of P_{11} is steeper for flight B than for flight A due to the presence of larger ice crystals (Fig. 2). The differences in P_{11} related to ice crystal habit are relatively subtle compared to the large angular slope of P_{11} in near-forward directions, but not negligible. At scattering angles of 0° to 0.1° , plates yield the strongest forward scattering (over 35 % stronger than that of the observed $large_A$ or $large_B$ habit distributions) and bullet rosettes
285 or plate aggregates the weakest scattering (up to 25 % weaker than that of the $large_A$ or $large_B$ distributions). Furthermore, while the P_{11} of plates is lower than that of most other SR habits at angles of 0.3° – 1° , it is highest among the habits considered at angles of 2° – 10° . At these angles, plates yield up to 60 % and 80 % larger P_{11} than the observed $large_A$ and $large_B$ distributions, respectively, while columns and column aggregates yield ≈ 20 % lower values. The impact of habit
290 depends somewhat on the assumed ice crystal roughness; in particular, for CS crystals, P_{11} of plates exceeds that of the $large_A$ and $large_B$ distributions by over 80 % in the very near-forward directions of 0° – 0.1° .

Figure 5a compares the P_{11} corresponding to the three roughness assumptions for the $large_A$ size-shape distribution, while Figs. 5b–c show the relative differences between the SR and MR ice
295 crystals and the completely smooth (CS) ice crystals for the $large_A$ and $large_B$ distributions. The P_{11} for rough ice crystals is lower than that for CS crystals in very-near-forward scattering directions, but larger at larger angles, starting from $\approx 0.8^\circ$ for MR crystals and from $\approx 1.7^\circ$ for SR crystals. Furthermore, the P_{11} of MR crystals exceeds that for SR crystals up to $\approx 6^\circ$ but at larger angles, SR crystals yield the largest P_{11} . Quantitatively, the impact of roughness is very large and clearly
300 exceeds that of ice crystal habit. The relative difference between MR and CS crystals peaks at 4° – 5° ,



reaching 400 % for $large_A$ and over 700 % for $large_B$, while the difference between SR and CS crystals is largest at 7° – 8° (up to 500 % for $large_A$ and over 600 % for $large_B$).

The phase function differences seen in Fig. 5 are mainly related to rays that are transmitted through an ice crystal, entering and exiting through parallel crystal faces. If the crystal faces are exactly parallel, the phase function contribution by this process is concentrated to very small scattering angles (if finite-size effects are accounted for, as in the Yang et al. (2013) database) or even in the exact forward direction (i.e., delta-transmission), in the limit of geometric optics. However, in the case of MR and SR crystals, the ice crystal surface slopes are distorted randomly for each incident ray, which, in effect, eliminates ray paths that pass through exactly parallel faces. This is why for both MR and SR crystals, P_{11} is lower than that for CS crystals in very-near-forward scattering directions, but larger at larger angles (see Fig. 5). Furthermore, the standard deviation of local slope variations assumed in the case of MR crystals is $\sigma = 0.03$, implying that the scattering angle is typically modified by a few degrees, whereas for SR crystals with $\sigma = 0.50$, the scattered energy is distributed over a much larger range of scattering angles. This explains why the relative difference between MR and CS crystals in Fig. 5 peaks at a smaller scattering angles (4° – 5°) than the difference between SR and CS crystals (at 7° – 8°).

4 Disk and circumsolar radiances: sensitivity tests

In the sensitivity simulations, the size-shape distribution and roughness of ice crystals, ice cloud optical thickness τ_c and aerosol optical thickness τ_a are varied. When not otherwise stated the following parameter settings are used: (1) either the $large_A$ or $large_B$ size-shape distribution of large severely rough ice crystals, with no small crystals with $D_{max} < 100 \mu m$; (2) cloud optical thickness $\tau_c = 1.6$; (3) atmospheric and aerosol properties corresponding to flight A; (4) aerosol optical thickness $\tau_a = 0.09$; (5) solar zenith angle of $\theta = 40^\circ$. The simulated radiances (in $Wcm^{-2}\mu m^{-1}sr^{-1}$) are shown as a function of the angular distance from the center of the Sun (0°) out to 8° when looking towards the Sun from the ground (see Fig. 1).

4.1 Sensitivity of radiances to optical path

To demonstrate the impact of aerosol and cloud optical thicknesses on the radiances, Fig. 6 shows the simulated radiances for a pristine aerosol and cloud-free atmosphere (i.e., gases only) and for cloud-free (with gases and aerosols) and cloudy (gases, aerosol and ice cloud) atmospheres. The $large_A$ size-shape distribution is used for the cloud, and two values are considered both for cloud ($\tau_c=0.2$ and $\tau_c=1.6$) and aerosol ($\tau_a=0.09$ and 0.166) optical thickness. From Fig. 6 it is seen that in the gases only case there is a huge contrast between the very strong radiances in the disk area (1000 – $2400 Wcm^{-2}\mu m^{-1}sr^{-1}$) and the weak and almost constant radiances ($\approx 0.001 Wcm^{-2}\mu m^{-1}sr^{-1}$) in the circumsolar region. In the presence of aerosols with $\tau_a=0.09$ or $\tau_a=0.166$, the disk radiances



335 are 11 % and 18 % smaller and the circumsolar radiances are one to two orders of magnitude greater
than in the gases only simulations. While the circumsolar radiances are ≈ 60 % larger for $\tau_a = 0.166$
than for $\tau_a = 0.09$, the relative difference between these cases decreases to less than 20 % when an
ice cloud is included, even for $\tau_c = 0.2$.

In the presence of a cirrus cloud, the circumsolar radiances are orders of magnitude greater than in
340 the gases only and cloud-free cases as seen from Fig. 6. The most striking effects, both in the absolute
values and in the angular dependence, are seen in the angular region between the limb of the solar
disk and 1° , where in the cloudy cases the radiances are between 100 and $0.8 \text{ W cm}^{-2} \mu\text{m}^{-1} \text{ sr}^{-1}$ as
compared with $\sim 0.1 \text{ W cm}^{-2} \mu\text{m}^{-1} \text{ sr}^{-1}$ for the cloud-free cases and $\sim 0.001 \text{ W cm}^{-2} \mu\text{m}^{-1} \text{ sr}^{-1}$
for the gases only case. The increase in diffuse radiance in the presence of a cirrus cloud is due to
345 the strong forward-scattering peak of ice crystals, whereas the smaller disk radiances are due to the
larger total optical thickness. The disk radiance decreases monotonically with increasing τ_c , being
74 % less for $\tau_c = 1.6$ than $\tau_c = 0.2$. This is due to the decrease in direct solar radiation; the diffuse
radiation in the disk region is, in fact, larger for $\tau_c = 1.6$ than $\tau_c = 0.2$ (see the insert in Fig. 7).
In contrast, the circumsolar radiance is on average 140–170 % larger for $\tau_c = 1.6$ than $\tau_c = 0.2$,
350 depending on the assumed τ_a . However, as demonstrated in Fig. 7, the increase of diffuse radiance
with τ_c is not linear, and when attenuation becomes strong enough, the amount of diffuse radiation
decreases with increasing τ_c , both in the disk and circumsolar regions.

4.2 Sensitivity of the radiances to properties of large ice crystals

Sensitivities of the disk and circumsolar radiances to the size-shape distributions of large ice crys-
355 tals are addressed by comparing results for the six single-habit distributions and the measured habit
distributions of flights A and B. The radiances simulated with *large_A* and *large_B* size-shape dis-
tributions are compared in Fig. 8a. For *large_B*, the total radiance in the disk region is 10 to 20 %
larger than for *large_A*, and the circumsolar radiance is smaller by up to 30 %, even though the same
 τ_c is assumed in both cases. This occurs because the ice crystal population for flight B results in a
360 stronger and narrower forward-scattering peak in P_{11} as noted already from Fig. 4. As the optical
thickness is the same in both cases, the differences in the total radiances arise from differences in the
diffuse component. On average, the amount of diffuse radiance in the disk region is 41 % and 51 %
of the total radiance for *large_A* and *large_B*, respectively. For the angular range of 0° to 3° from the
center of the Sun, the corresponding fractions are 44 % and 53 %.

365 The relative differences between the six single-habit distributions and the *large_A* or *large_B* distri-
butions are shown in Fig. 8b–c for total radiances. The differences in radiances follow the differences
in P_{11} of the habit distributions shown in Fig. 4. In the disk region the difference between different
habit distributions reaches at most 15 %. The impact of habit, however, differs between flights and
therefore depends on the size distribution. Based on the circumsolar radiances, the habits can be
370 divided into two groups; column-like (column, column agg and bullet rosette) and plate-like crystals



(plate, plate agg and irregular). Column-like crystals tend to result in a steeper angular slope in radiances, producing larger diffuse radiances in the disk region and smaller radiances in the circumsolar region than plate-like crystals do. In the circumsolar region, plate and column agg tend to differ most from each other regardless of the size distribution. The relative differences in the circumsolar region
375 between the single-habit distributions and CPI-based habit distributions reach up to 60 % for flight A and up to 80 % for flight B, similarly to the phase functions differences in Fig. 4. The impact of ice crystal habit also depends on the cloud optical thickness. Generally, as τ_c increases and multiple scattering becomes more important, the relative differences in diffuse radiances between different habits are reduced.

380 The impact of ice crystal roughness on the radiances is depicted in Fig. 9. Consistent with the large phase function differences in Fig. 5, the impacts of roughness on the radiances are substantial: rough crystals yield smaller diffuse radiances than smooth crystals at angles smaller than 1° to 2.5° but larger diffuse radiances at angles larger than that. In the disk region, SR and MR crystals produce almost identical radiances, which are within 1 % of each other, but 15 % to 21 % below those of
385 smooth crystals, depending on the flight. In the circumsolar region at angles smaller than 7° , MR crystals produce larger radiances than the SR crystals, the relative differences being largest at angles of 2° to 3° , up to 140 % for flight A and 195 % for flight B. The relative differences between MR and CS crystals are largest at angles of $\sim 4^\circ$, reaching up to 425 % for flight B. Correspondingly, the maximum relative differences between SR and CS crystals occur at angles larger than 6° , reaching 240 %
390 for flight B. These angle-dependent radiance differences between different roughness assumptions follow the P_{11} differences shown in Fig. 5. The relative differences in radiances are, however, not quite as large as those in P_{11} , and they decrease somewhat with increasing τ_c (here, $\tau_c=1.6$), due to the effects of multiple scattering. In any case, roughness has a large impact on both the disk and the circumsolar radiances, and these differences clearly exceed the corresponding differences between
395 different SR habits (compare Figs 8 and 9).

The roughness of the particle also impacts the fractional contribution that diffuse radiation makes to the total radiance in the range of 0° to 3° typically measured by pyrheliometers. For the cases considered here, the contribution of diffuse radiation is $\approx 10\%$ larger for CS than SR or MR ice crystals.

400 4.3 Sensitivity of the radiances to small ice crystals

To probe the impact of uncertainties in the measurements of small ice crystals, the effects of their concentration on the disk and circumsolar radiances are simulated. Simulations are made with the $large_A$ and $large_B$ distributions together with 0–200 % of the measured concentration of small column-shaped ice crystals ($small_{0\%}$, $small_{50\%}$, $small_{100\%}$, and $small_{200\%}$). In these simulations,
405 ice crystals are severely rough and $\tau_c = 1.6$. The angular dependence of the total radiances simulated with 0 and 100 % of the measured small-crystal concentrations are shown in Fig. 10a at angles of



0° to 4° from the center of the Sun. Regardless of the small crystal concentration, the radiances at angles larger than 5° are within 3 % of each other during flights A and B. Because the same cloud optical thickness is assumed for all the size distributions, including small ice crystals necessarily
410 decreases the concentration of large ice crystals. This acts to decrease the near-forward radiances in the disk region and just around it and to increase the circumsolar radiances at angles between 0.5° and 5° from the center of the Sun. This is due to the wider forward-scattering peak of the small ice crystals.

Quantitatively, the impact of the assumed concentration of small ice crystals is substantial and
415 somewhat larger for flight A than flight B (see Fig. 10b–c). Compared to the cases with large ice crystals only, the relative reduction in radiance due to small ice crystals is largest near the edge of the solar disk, amounting up to –47 % for flight A and –22 % for flight B. The largest relative increases occur at 1–2° from the center of the Sun. For flight A, the maximum differences to the case with large ice crystals only are 95 %, 111 % and 123 %, and for flight B, 33 %, 55 % and 84 %, when assuming
420 50 %, 100 % and 200 % of the observed concentration of small ice crystals, respectively. When averaged over the angular range of 0° to 3° covered by a pyrhelimeter, the negative differences in the disk region and positive differences in the circumsolar region partly cancel each other leading to smaller relative differences. For example, when including 100 % of the observed concentration of
425 crystals only for flight A, and 10 % smaller for flight B. The impacts of including small ice crystals are similar regardless of the cloud optical thicknesses.

5 Comparison of the simulated and measured radiances

During the SPARTICUS campaign, disk and circumsolar radiances were measured with the SAM instrument of Visidyne Inc. located at the SGP site. For both flights A and B, three SAM measure-
430 ments are selected for comparison. Our goal is to reproduce these radiances using the in-situ-based size-shape distributions. The simulations are conducted both with and without the contribution of small ice crystals, assuming 100 % of the measured small-crystal concentration in the former case. The atmospheric and aerosol properties of flights A and B are used in the simulations. The cloud optical thickness τ_c was adjusted separately for each case, based on the criterion that the simulated
435 radiance averaged over the solar disk should be within 3 % of the SAM measurements. The resulting values of τ_c are listed in Tables 3 and 4 for flights A and B respectively, along with the θ of the selected SAM measurement times, and the total apparent optical thickness (cloud + aerosols) retrieved from SAM assuming that the disk radiance consists of direct solar radiation only. The derived values of τ_c depend not only on the measurement time but also on the assumptions about ice crystal rough-
440 ness and small ice crystals. In particular, for a given optical thickness, stronger disk radiances are produced by smooth than rough crystals (see Fig. 9), and consequently, larger τ_c is needed to match



the SAM measurements in the case of smooth than rough ice crystals. Further, τ_c tends to be larger than that reported by the SAM. This is in line with DeVore et al. (2012) who found that the τ_{SAM} needs to be corrected upward to account for forward scattering of ice crystals.

445 The simulated radiances are compared with the selected SAM measurements in Figs. 11 and Fig.12 for flights A and B, respectively. Both the simulated and the SAM-measured radiances shown here are horizontal profiles (to the left and right, see Fig. 1) from the center of the Sun out to 8° . For the simulations, the profiles to the left and right are averaged, while for SAM, they are shown separately as "hp" and "hn" curves. We note that the radiance arriving at different sensors comes
450 from different parts of the cloud. To assure that the observed angular dependence of radiance is not due to cloud inhomogeneity, we limit our considerations to cases where "hp" and "hn" curves are similar.

First, it is noted that while (by definition) the average simulated disk radiances agree closely with the SAM measurements, the angular slope measured is not quite consistent with the limb-
455 darkening profile used in the simulations. The reasons for this discrepancy are not clear and should be scrutinized in future work. Second, considering the circumsolar radiances, the simulations with SR ice crystals capture better the measured angular dependence than the simulations for CS crystals do. The use of CS ice crystals overestimates near-disk radiances and underestimates the radiances at angles larger than about 3° . It is further noted from Figs. 11 and 12 that excluding small crystals
460 decreases the radiances at angles smaller than 3° and by doing so, it tends to improve the comparison of radiances at these angles. Overall, it appears that the angular dependence produced by large SR crystals is most similar to the measurements, even though it tends to overestimate the radiances at angles larger than $\approx 6^\circ$ in most cases.

The systematically better performance of SR than CS ice crystals in simulating the measured ra-
465 diances in the circumsolar region suggests that the SR crystals approximate better the phase function of ice crystals present during flights A and B, at least in near-forward directions. Furthermore, the SR crystals are more consistent with the measured radiances than the MR crystals are. The use of MR crystals results in radiances that exceed those for CS and SR crystals and also the measurements between angles of $\approx 1^\circ$ and 6° , even when small ice crystals are not accounted for. Referring to
470 the discussion in Sect. 3.4, the better performance of SR than CS crystals suggests that ray paths passing through smooth, exactly parallel ice crystal faces are less common in nature than they would be for idealized ice crystals. However, there is no reason to expect that the somewhat ad-hoc approach employed in the Yang et al. (2013) database to represent ice crystal "roughness" (or rather, non-ideal features like roughness, irregularities and inhomogeneity in general) would result in a perfect
475 description of P_{11} . Even so, our results add to the growing body of evidence (Cole et al., 2014; Ulanowski et al., 2014) suggesting that the scattering by natural ice crystals most often differs from their idealized counterparts, also in the near-forward directions (DeVore et al., 2012).



6 Conclusions

In this study, we quantified the amount of diffuse radiance in the solar disk region and in the circum-
480 solar region up to angles of 8° from the center of Sun using a modified version of the Monte Carlo
radiative transfer model MC-UniK. The input data for the model were derived from the measured
size-shape distributions of two ice cloud cases observed over the ARM's Southern Great Plains mea-
surement site during the 2010 SPARTICUS campaign. This work extends and supports the previous
studies on the impact of ice crystals' properties on near-forward scattering and circumsolar radiation
485 (Reinhardt et al., 2014; Segal-Rosenheimer et al., 2013) by modelling radiances instead of irradi-
ances and by conducting systematic sensitivity tests using in situ based size-shape distributions of
ice crystals.

In the sensitivity tests, it was found that the disk and circumsolar radiances depend substantially on
the ice crystal properties (roughness and size-shape distribution) through their impact on the phase
490 function, in line with previous research (Reinhardt et al., 2014; Segal-Rosenheimer et al., 2013;
DeVore et al., 2012). Specifically:

- Of all parameters considered, assumptions about ice crystal roughness (or non-ideal features
in general) were found to be most important. The use of moderately or severely rough ice
crystals instead of completely smooth crystals leads to reduced radiances in the solar disk
495 region while substantially increasing radiances in the circumsolar region at angles larger than
 $\approx 1\text{--}2.5^\circ$, with maximum differences as large as 400 % between MR and CS crystals and 200
% between SR and CS crystals.
- A larger portion of small ice crystals results in reduced disk radiances but increased radiances
at angles of $\approx 0.5^\circ\text{--}5^\circ$, with a maximum difference of up to $\approx 100\%$ at $\approx 1^\circ\text{--}2^\circ$ from the center
500 of the Sun, compared to the case with no small ice crystals.
- Column-like crystals tend to yield radiances with a steeper angular slope than plate-like crys-
tals, as they produce more diffuse radiance in the disk region and less in the circumsolar region
than plate-like crystals. The relative differences between all single-habit distributions and the
actually measured habit distributions were less than 10 % in the disk region but up to 80 % at
505 angles larger than 4° from the center of the Sun.

The quantitative results listed above depend on the cloud optical thickness and solar zenith angle.
In general, an increasing path length through the cloud acts to reduce the radiance contrast between
the disk region and the circumsolar region, and the impact of the phase function. Changes in aerosol
optical thickness also affect the absolute values of the radiances in the presence of an ice cloud, but
510 not significantly their angular dependence.

Simulated radiances were compared with ground-based measurements with the SAM instrument
for three measurement times during both flights A and B. It was found that SR ice crystals mimicked



the measured circumsolar radiances better than either the MR crystals (which overestimated the radiances at angles of a few degrees) or the CS crystals (which invariably underestimated the radiances at angles larger than $\approx 3^\circ$). In some cases, the agreement was better when crystals smaller than 100 μm were neglected from the measured size distribution, suggesting that the measurements may have overestimated the concentration of small crystals. These results add to the growing body of evidence suggesting that natural ice crystals tend not to be pristine (Cole et al., 2014; Ulanowski et al., 2014).

Even though we had detailed information about the size-shape distribution of ice crystals of the clouds studied, the observed radiances could not be reproduced perfectly. There are several factors that possibly contribute to this. Part of the discrepancies can be surely attributed to the non-perfect spatiotemporal collocation of the in situ and SAM measurements. It is also quite possible that the simplistic ad hoc scheme employed to mimic the effects of roughness, non-ideality and internal structures on scattering is not entirely realistic or representative of natural ice crystals. Further, the limb darkening parameterization may not be entirely accurate, and some discrepancies might also be due to the aerosol optical properties chosen. Likewise, there may be some remaining inhomogeneities in the clouds that our analysis did not reveal. Finally, it is entirely possible that the clouds sampled had mixtures of ice crystals with varying degrees of deformation, in which case any one crystal roughness model could not be expected to perform perfectly, but a combination of differently deformed crystals should be used.

In the future, the version of MC-UniK modified for the present work could be used for analyzing a wide range of cirrus cloud and aerosol scenarios and their 3D effects on near-forward radiances. The unique modeling results might be of interest for the design of concentrating solar power systems and for the interpretation of data from instruments intended to measure the direct solar radiation. The results could also be utilized for evaluating the contribution of diffuse solar radiation to the disk radiation in SAM measurements, thereby allowing for a more accurate determination of the "true" direct solar radiation, and hence the optical thickness. Furthermore, they might be exploited for developing methods to retrieve ice cloud properties from measurements of disk and circumsolar radiances; in particular, it might be possible to estimate ice crystal non-ideality from SAM measurements. Finally, the combination of SAM with sun photometer measurements (e.g. AERONET) might allow separating the contributions of large and small particles (e.g., ice crystals vs. aerosols) to optical thickness.

Author contributions. TN, GM, PR, MK, AM and PH designed the study. GM provided the airborne in situ data, JD the SAM data and AM the Monte Carlo model MC-UniK. JT was responsible for using the IC-PCA. MK, TN, PR, AM and PH planned the needed modifications of the MC-UniK, which PH then implemented. PR calculated the atmospheric optical properties. PH combined the in situ data and single-scattering properties, conducted all the MC-UniK simulations and made the figures, except for Fig. 2 which was made by PR. PH, PR, GM and TN wrote the manuscript. All authors discussed the results and commented on the manuscript.



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555 **References**

- Barker, H. R., Goldstein, and Stevens, D.: Monte Carlo simulation of solar reflectances for cloudy atmospheres, *J. Atmos. Sci.*, 60, 1881-1894, 2003.
- Baumgardner, D., and Korolev, A. V.: Airspeed corrections for optical array probe sample volumes, *J. Atmos. Ocean. Tech.*, 14, 1224-1229, 1997.
- 560 Blanc, P., Espinar, B., Geuder, N., Gueymard, C., Meyer, R., Pitz-Paal, R., Reinhardt, B., Renne, D., Sengupta, M., Wald, L., and Wilbert, S.: Direct normal irradiance related definitions and applications: The circumsolar issue. *Solar Energy* 110, 561–577, 2013.
- Böhn-Vitense, E: Introduction to stellar astrophysics, Volume 2, Stellar atmospheres, Cambridge University Press, 1989.
- 565 Bui, D., and Monger, A. G.: The effect of circumsolar radiation on a solar concentrating system, *Solar Energy*, 76, 181–185, 2004.
- Cahalan, R. F., Oreopoulos, L., Marshak, A., Evans, K. F., Davis, A. B., Pincus, R., Yetzer, K. H., Mayer, B., Davies, R., Ackerman, T. P., Barker, H. W., Clothiaux, E. E., Ellingson, R. G., Garay, M. J., Kassianov, E., Kinne, S., Macke, A., O'Hirok, W., Partain, P. T., Prigarin, S. M., Rublev, A. N., Stephens, G. L., Szczap, F.,
- 570 Takara, E. E., Varnai, T., Wen, G. and Zhuravleva, T. B.: The International Intercomparison of 3D Radiation Codes (I3RC): Bringing together the most advanced radiative transfer tools for cloudy atmospheres, *Bull. Amer. Meteor. Soc.*, 86 (9), 1275–1293, 2005.
- Cole, B. H., Yang, P., Baum, B. A., Riedi, J., and Labonnote, L. C.: Ice particle habit and surface roughness derived from PARASOL polarization measurements, *Atmos. Chem. Phys.*, 14, 3739-3750, doi:10.5194/acp-14-3739-2014, 2014.
- 575 Dee, D. P., Uppala, S. M., Simmons, A. J., Berrisford, P., Poli, P., Kobayashi, S., Andrae, U., Balmaseda, M. A., Balsamo, G., Bauer, P., Bechtold, P., Beljaars, A. C. M., van de Berg, L., Bidlot, J., Bormann, N., Delsol, C., Dragani, R., Fuentes, M., Geer, A. J., Haimberger, L., Healy, S. B., Hersbach, H., Hólm, E. V., Isaksen, L., Kållberg, P., Köhler, M., Matricardi, M., McNally, A. P., Monge-Sanz, B. M., Morcrette, J.-J., Park, B.
- 580 K., Peubey, C., de Rosnay, C. P., Tavolato, C., Thépaut, J.-N., and Vitart, F.: The ERA-Interim reanalysis: configuration and performance of the data assimilation system, *Q. J. Roy. Meteor. Soc.*, 137, 656, 553–597, doi 10.1002/qj.828, 2011.
- DeVore, J. G., Stair, A. T., LePage, A. J., Rall, D., Atkinson, J., Villanucci, D., Rappaport, S., Joss, P., and McClatchey, R.: Retrieving properties of thin clouds from solar aureole measurements, *J. Atmos. Ocean. Techn.*, 26(12), 2531-2548, 2009.
- DeVore, J. G., Stair, A. T., LePage, A. J., Rall, D., and Villanucci, D.: Using scattering calculations to compare MODIS retrievals of thin cirrus optical properties with SAM solar disk and aureole radiance measurements, *J. Geophys. Res.*, 117, D10204, 2012.
- Freidenreich, S. and Ramaswamy, V.: A new multiple-band solar radiative parameterization for general circulation models, *J. Geophys. Res.*, 104, D24, 31,389-31,409, 1999.
- 590 Gardiner, B.A., and Hallett, J.: Degradation of in-cloud forward scattering probe measurements in the presence of ice particles, *J. Atmos. Ocean. Tech.*, 2, 171-180, 1985.
- Green S. F., and Mark H. Jones: An Introduction to the Sun and Stars, The Open University, 2015.



- Gueymard, C. A.: The sun's total and spectral irradiance for solar energy applications and solar radiation models, *Solar Energy*, 76, 423-453, 2004.
- 595 Hess, M., Koepke, P., and Schult, I: Optical Properties of Aerosols and Clouds: The Software Package OPAC, *Bulletin of the American Meteorological Society*, 79, 5, 831-84, 1998.
- Lindqvist, H. and Muinonen, K., Nousiainen, T., Um, J., McFarquhar, G. M., Haapanala, P., Makkonen, R., and Hakkarainen, H.: Ice-cloud particle habit classification using principal components, *J. Geophys. Res.*
- 600 *Atmos.*, 117, D16, doi:10.1029/2012JD017573, 2012.
- Jackson, R.C., McFarquhar, G.M., Fridlind, A.M., and Atlas, R.: The dependence of cirrus gamma size distributions expressed as volumes in N_0 - λ - μ phase space and bulk cloud properties on environmental conditions: Results from the Small Ice Particles in Cirrus Experiment (SPARTICUS), *J. Geophys. Res. Atmos.*, 120, 10351–10377, doi:10.1002/2015JD023492, 2015.
- 605 Kinne, S., Ackerman, T. P., Shiobara, M., Uchiyama, A., Heymsfield, A. J., Miloshevich, L., Wendell, J., Eloranta, E., Purgold, C., and Bergstrom, R. W.: Cirrus cloud radiative and microphysical properties from ground observations and in situ measurements during FIRE 1991 and their application to exhibit problems in cirrus solar radiative transfer modeling. *J. Atmos. Sci.*, 54, 2320–2344, 1997. doi: 10.1175/1520-0469(1997)054<2320:CCRAMP>2.0.CO;2
- 610 Korolev, A.V., Emery, E.F., Strapp, J.W., Cover, S.G., Isaac, G.A., Wasey, M., and Marcotte, D.: Small ice particles in tropospheric clouds: Fact or artefact?, *Bull. Amer. Meteor. Soc.*, 92, 967-973, 2011.
- Korolev, A.V., Emery, E., and Creelman, K.: Modification and tests of particle probe tips to mitigate effects of ice shattering, *J. Atmos. Ocean. Tech.*, 30, 690-708, 2013.
- Macke A., Francis, P.N., McFarquhar, G. M., and Kinne, S.: The role of particle shapes and size distributions
- 615 in the single scattering properties of cirrus clouds, *J. Atmos. Sci.*, 55, 2874–2883, 1998.
- Macke, A., Mitchell, D., and Bremen, L.: Monte Carlo radiative transfer calculations for inhomogeneous mixed phase clouds. *Phys. Chem. Earth (B)*, 24, 3, 237-241, 1999.
- Marshak, A., and Davis, A. B.: *Radiative Transfer in Cloudy Atmospheres*. Springer Verlag, pp. 701, 2005.
- McFarquhar, G.M., Yang, P., Macke, A., and Baran, A. J.: A new parameterization of single scattering solar
- 620 radiative properties for tropical anvils using observed ice crystal size and shape distributions, *J. Atmos. Sci.*, 59, 2458–2478, 2002.
- McFarquhar, G. M., Um, J., Freer, M., Baumgardner, D., Kok, G. L., and Mace, G.: Importance of small ice crystals to cirrus properties: Observations from the Tropical Warm Pool International Cloud Experiment (TWP-ICE), *Geophys. Res. Letter.*, 34, L13803, doi:10.1029/2007GL029865, 2007.
- 625 McFarquhar, G.M., Um, J., and Jackson, R. C.: Small cloud particle shapes in mixed-phase clouds, *J. Appl. Meteorol. Climatol.*, 52, 1227-1293, 2013.
- McFarquhar, G. M., Baumgardner, D., Bansemer, A., Abel, S., Crosier, J., French, J., Rosenberg, P., Korolev, A., Schwarzenboeck, A., Leroy, D., Um, J., Wu, W., Heymsfield, A. J., Detwiler, A., Field, P., Neumann, A., Stith, J., Axisa, D., Cotton, R., and Dong, J.: Processing of in-situ data collected by bulk water, scattering and cloud imaging probes: Fundamentals, Uncertainties and Efforts towards consistency, *Amer. Meteor. Soc. Monographs*, Under review, 2016.
- 630 Mishra, S. D. L., Mitchell, D. T., and Lawson R. P.: Parameterization of ice fall speeds in midlatitude cirrus: Results from SPARTICUS, *J. Geophys. Res. Atmos.*, 119, 3857-3876, doi:10.1002/2013JD020602, 2014.



- Muhlbauer, A., Ackerman, T. P., Cmostock, J. M., Diskin, G. S., Evans, S. M., Lawson, R.P., and Marchand, R.
635 T.: Impact of large-scale dynamics on the microphysical properties of midlatitude cirrus, *J. Geophys. Res. Atmos.*, 119, 3976–3996, doi:10.1002/2013JD020035, 2014.
- Noring, J.E., Grether, D. F., and Hunt, A. J.: Circumsolar radiation data: the Lawrence Berkeley Laboratory reduced data base. National Renewable Energy Laboratory, NREL/TP-262-4429. URL <http://trredc.nrel.gov/solar/pubs/circumsolar/title.html>.
- 640 Neumann, A., Witzke, A., Jones, S. A., and Schmitt, G.: Representative terrestrial solar brightness profiles, *J. Solar Energy Eng.*, 124, pp. 198–204, 2002.
- Reinhardt, B.: On the Retrieval of Circumsolar Radiation from Satellite Observations and Weather Model Output. Dissertation, LMU München, 2013. <<http://nbn-resolving.de/urn:nbn:de:bvb:19-164380>> (last accessed 26 July 2016).
- 645 Reinhardt, B., Buras, R., Bugliaro, L., Wilbert, S., Mayer, B.: Determination of circumsolar radiation from Meteosat Second Generation. *Atmos. Meas. Tech.*, 7, 823–838, 2014.
- Schlimme, I., Macke, A., and Reichardt, J.: The impact of ice crystal shapes, size distributions, and spatial structures of cirrus clouds on solar radiative fluxes. *J. Atmos. Sci.*, 62, 2274–2283, 2005.
- Segal-Rosenheimer, M., Russell, P. B., Livingston, J. M., Ramachandran, S., Redemann, J., and Baum, B.
650 A.: Retrieval of cirrus properties by Sun photometry: A new perspective on an old issue, *J. Geophys. Res. Atmos.*, 118, 4503–4520, doi:10.1002/jgrd.50185, 2013.
- Shiobara, M., and Asano, S.: Estimation of cirrus optical thickness from sun photometer measurements, *J. Appl. Meteorol.*, 33, 672–681, doi:10.1175/1520-0450, 1997.
- Ulanowski, Z., Connolly, P., Flynn, M., Gallagher, M., Clarke, A. J. M., and Hesse, E.: Using ice crystal analogues to validate cloud ice parameter retrievals from the CPI ice spectrometer data, 14th International Conference on Clouds and Precipitation, Bologna, Italy, 2004.
- 655 Ulanowski, Z., Kaye, P. H., Hirst, E., Greenaway, R. S., Cotton, R. J., Hesse, E., and Collier, C. T.: Incidence of rough and irregular atmospheric ice particles from Small Ice Detector 3 measurements. *Atmos. Chem. Phys.*, 14, 1649–1662, doi:10.5194/acp-14-1649-2014, 2014.
- 660 Um J., and McFarquhar, G. M.: Single-scattering properties of aggregates of bullet rosettes in cirrus. *J. Appl. Meteor. Climatol.*, 46 (6), 757–775, doi:10.1175/JAM2501.1, 2007.
- Um, J. and McFarquhar, G. M.: Single-scattering properties of aggregates of plates. *Q. J. Roy. Meteor. Soc.*, 135, 291–304. doi:10.1002/qj.378, 2009.
- Um, J. and McFarquhar, G. M.: Dependence of the single-scattering properties of small ice crystals on idealized
665 shape models, *Atmos. Chem. Phys.*, 11, 3159–3171, doi:10.5194/acp-11-3159-2011, 2011.
- Um, J., and McFarquhar, G. M.: Optimal numerical methods for determining the orientation averages of single-scattering properties of atmospheric ice crystals. *J. Quant. Spectrosc. Radiat. Transfer*, 127, 207–223, 2013.
- Yang, P., Bi, L., Baum, B. A., Liou, K.-N., Kattawar, G. W., Mishchenko, M. I., and Cole, B.: Spectrally consistent scattering, absorption and polarization of atmospheric ice crystals at wavelengths from 0.2 to 100
670 μm , *J. Atmos. Sci.*, 70, 330–347, 2013.
- Zhang Y., Macke, A., and Albers, F.: Effect of crystal size spectrum and crystal shape on stratiform cirrus radiative forcing, *Atmos. Res.*, 52, 59–75, 1999.



Wilbert, S., Pitz-Paal, R., and Jaus, J.: Circumsolar Radiation and Beam Irradiance Measurements for Focusing Collectors. ES1002: Cost Wire Workshop, May 22-23, Risö, 2012.

- 675 Wilbert, S., Bernhard, R., DeVore, J., Röger, M., Pitz-Paal, R., Gueymard, C. A., and Buras, R.: Measurement of Solar Radiance Profiles with the Sun and Aureole Measurement Systems. *Journal of Solar Energy Engineering*, 135, doi: 10.1115/1.4024244, 2013.



Table 1. The final habit classes of large ice crystals that are created by combining habit classes of the IC-PCA and further interpreted as Yang et al. (2013) habits. In addition to the IC-PCA based habit distributions, $large_A$ and $large_B$, six single-habit distributions are used to describe the shape of large ice crystals.

habit class	habits of Yang et al. (2013)	habit classes of IC-PCA
column	hollow column	columns and bullets
column agg	column aggregate with 8 elements	column aggregates and bullet rosette aggregates
bullet rosette	bullet rosette	bullet rosettes
plate	plate	plate
plate agg	plate aggregate with 5 elements	plate aggregate
irregular	plate aggregate with 10 elements	irregular
large	fractional distribution of habits from in situ data	habits classified using IC-PCA

Table 2. Flight information. θ is the solar zenith angle during the flights A and B.

	Flight A	Flight B
Date	23 March 2010	24 June 2010
Time [UTC]	16:58-17:56	14:35-15:58
θ [°]	36.5-42.1	42.7-52.3
Cloud altitude [km]	9.5-11.5	8.0-11.5
Model layers with cloud	8-11	5-11

Table 3. The values of solar zenith angle θ and optical thickness of cloud (τ_c), aerosols (τ_a), and gases (τ_{gases}) used in the comparison simulations for flight A. The cloud is described with the size-shape distributions $large_A$ and $large_A + small_{100\%}$ of rough (MR and SR) and completely smooth (CS) ice crystals. Values of total optical thickness (cloud+aerosols) retrieved from the Sun and Aureole measurements (SAM) are also shown.

θ [°]	40.5	38.3	38.6
τ_{gases}	0.072	0.072	0.072
τ_a (AERONET, MFRSR)	0.09	0.09	0.09
τ_c , CS, $large_A + small_{100\%}$	0.6	1.05	2.5
τ_c , MR/SR, $large_A + small_{100\%}$	0.6	1.0	2.4
τ_c , CS, $large_A + small_{0\%}$	0.75	1.25	3.1
τ_c , MR/SR, $large_A + small_{0\%}$	0.65	1.15	2.75
τ_{SAM}	0.6	1.0	2.1



Table 4. The values of solar zenith angle θ and optical thickness of cloud (τ_c), aerosol (τ_a) and gases (τ_{gases}) used in the comparison simulations for flight B. The cloud is described with the size-shape distributions $large_B$ and $large_B + small_{100\%}$ of rough (MR and SR) and completely smooth (CS) ice crystals. Values of total optical thickness (cloud+aerosols) retrieved from the Sun and Aureole measurements (SAM) are also shown.

θ [°]	50.4	50.0	44.3
τ_{gases}	0.074	0.074	0.074
τ_a (AERONET, MFRSR)	0.166	0.166	0.166
τ_c , CS, $large_B + small_{100\%}$	0.7	1.3	3.5
τ_c , MR/SR, $large_B + small_{100\%}$	0.6	1.15	3.05
τ_c , CS, $large_B + small_{0\%}$	0.75	1.45	4.0
τ_c , MR/SR, $large_B + small_{0\%}$	0.65	1.25	3.3
τ_{SAM}	0.6	1.0	2.3

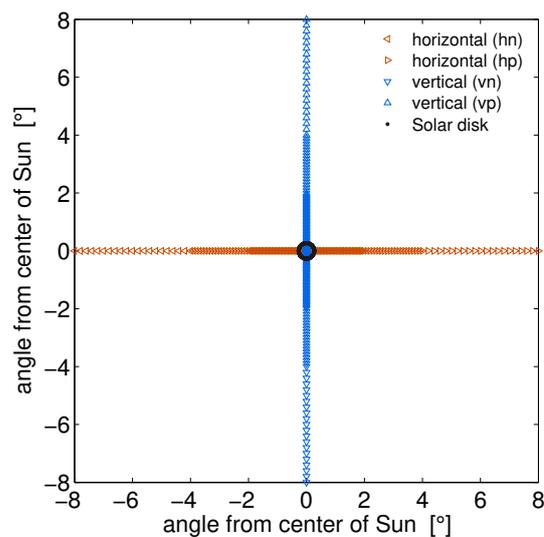


Figure 1. Detector positions in the MC-UniK model cover angles from 0° to -8° and 8° from the center of the Sun (0,0). Both horizontal and vertical cross sections are divided into positive and negative parts (hp; hn; vp; vn). The circle demonstrates the size of the solar disk, with a diameter of 0.534° .

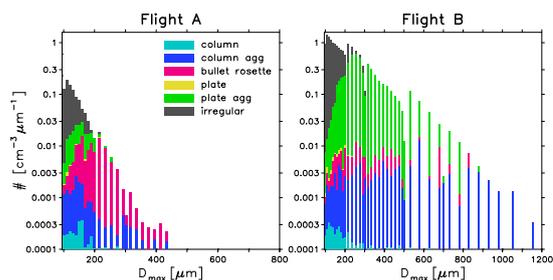


Figure 2. Vertically averaged size-shape distribution of in situ measured large ice crystals ($D_{max} > 100 \mu\text{m}$) during the flights on 23 March 2010 (flight A) and 24 June 2010 (flight B). These distributions were obtained by weighting fractional habit distributions at each vertical layer by the corresponding particle size distribution. The height of each column indicates the total number of particles in each size range (logarithmic scale on the y-axis). The fraction of particles of each habit is shown with different colors (in a linear scale)

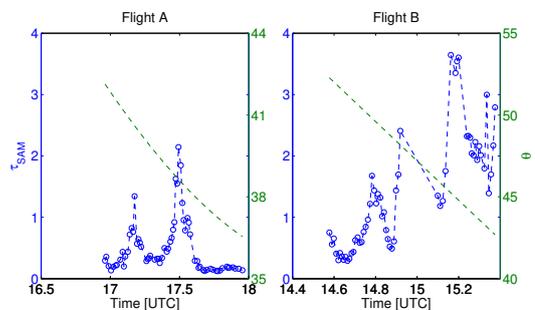


Figure 3. Optical thickness and solar zenith angle (θ) as a function of time during the flights A and B derived from the Sun and Aureole measurements at the SGP site.

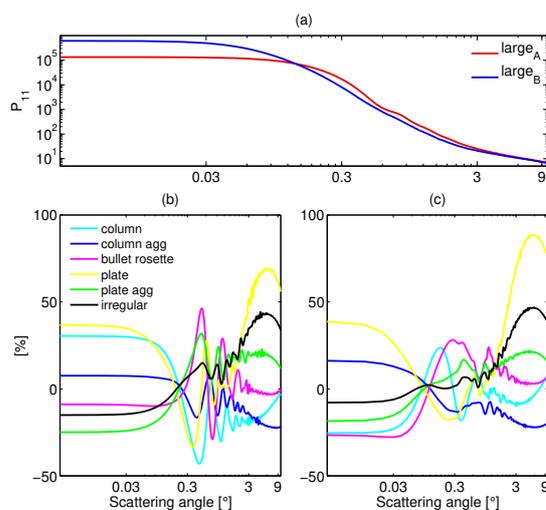


Figure 4. Sensitivity of the size and vertically integrated phase functions to size-shape distribution of large severely rough ice crystals. **(a)** The P_{11} of in-situ-based distributions of flights A and B. **(b)** and **(c)** The relative differences in P_{11} between the six single-habit distributions and the in-situ-based distributions for flight A (left) and B (right).

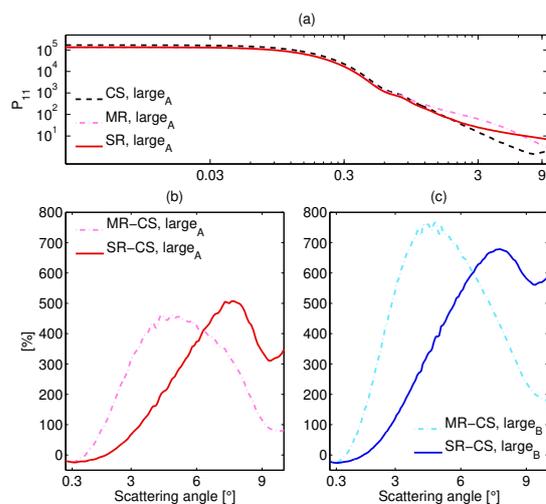


Figure 5. Sensitivity of the size and vertically integrated phase functions to the roughness of large ice crystals. **(a)** The P_{11} of the in-situ-based size-shape distribution of smooth, moderately and severely rough ice crystals of flight A ($large_A$). **(b)** and **(c)** The relative differences in P_{11} between MR and CS ice crystals and between SR and CS ice crystals of flight A and B.

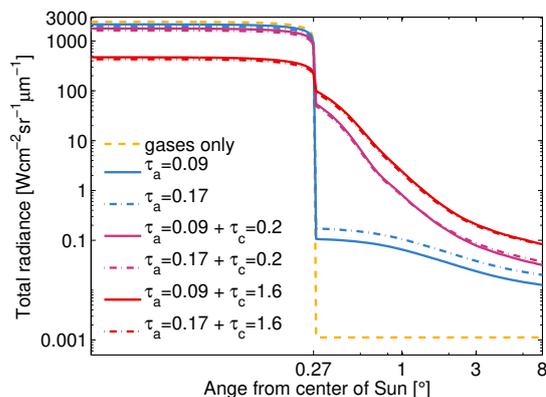


Figure 6. Impacts of the aerosol and cloud optical thicknesses on the simulated radiances as a function of angle from the center of the Sun out to 8° . Atmospheric and aerosol properties are based on flight A with either $\tau_a = 0.09$ or $\tau_a = 0.166$. The cloud is described with the *large_A* distribution of large SR ice crystals using two cloud optical thicknesses, $\tau_c = 0.2$ and 1.6 .

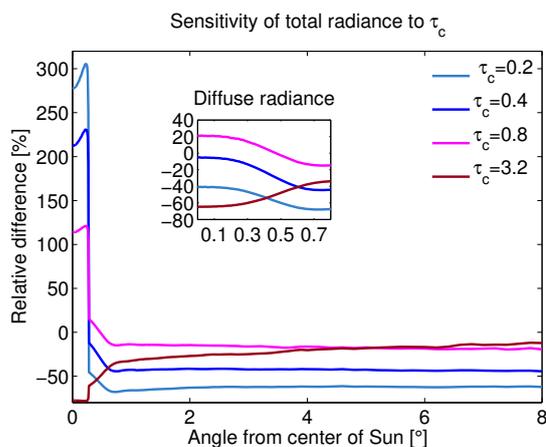


Figure 7. Sensitivity of the disk and circumsolar radiances to cloud optical thickness when the cloud is described using the *large_A* distribution of SR ice crystals. Relative differences between radiances simulated with alternative cloud optical thicknesses (τ_c of 0.2, 0.4, 0.8, and 3.2) and $\tau_c = 1.6$ are displayed. The insert shows the relative differences in diffuse radiance at angles of 0° – 0.8° . In these simulations $\tau_a = 0.09$.

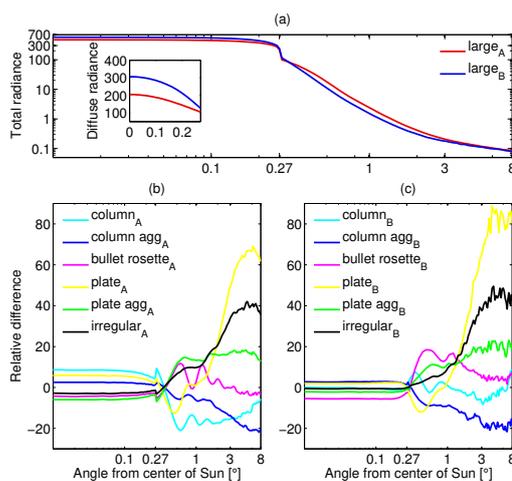


Figure 8. Impact of the shape of large severely rough ice crystals on the disk and circumsolar radiances. **(a)** The total radiances based on the *large_A* and *large_B* distributions. **(b)** and **(c)** The relative differences of the radiances based on the six single-habit distributions of flight A or B and the *large_A* or *large_B*, respectively. All the simulations are conducted with $\tau_a = 0.09$ and $\tau_c = 1.6$.

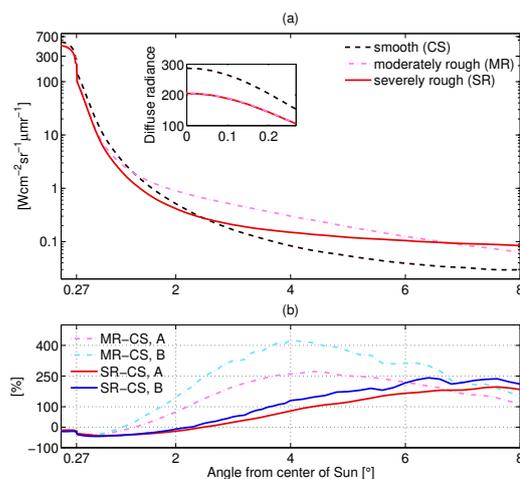


Figure 9. **(a)** Impact of the roughness (smooth, CS, moderately, MR, and severely rough, SR) of large ice crystals on the disk and circumsolar radiances in case of the *large_A* size-shape distribution. **(b)** Relative differences between results based on the MR or SR and CS ice crystals for the *large_A* and *large_B* distributions. In these simulations $\tau_a = 0.09$ and $\tau_c = 1.6$.

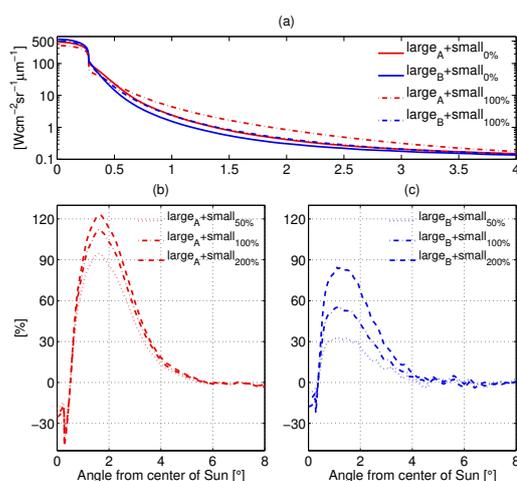


Figure 10. (a) Impact of the concentration of small ice crystals on the disk and circumsolar radiances. The simulations are made with the $large_A$ and $large_B$ distributions of large ice crystals including 0–200 % of the measured concentration of small ice crystals assumed to be columns. (b) and (c) Relative differences to the case with no small ice crystals. In these simulations ice crystals are severely rough, $\tau_a = 0.09$ and $\tau_c = 1.6$.

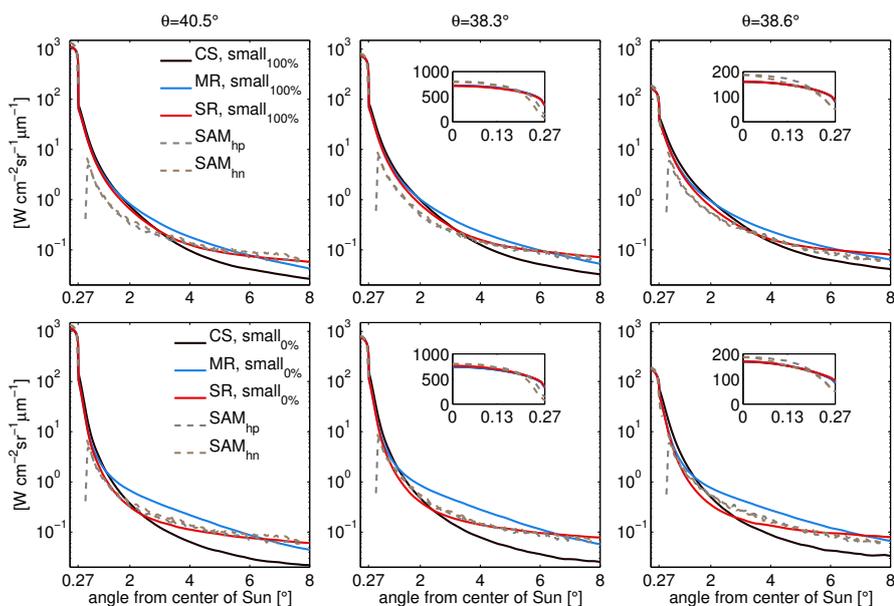


Figure 11. Comparison of the Sun and Aureole measured (SAM; hp and hn for the profiles to the right and left of Sun) and simulated radiances at three measurement times during flight A. For the simulations, the $large_A$ distribution with 100 % and 0 % of measured concentration of small ice crystals is used with τ and θ values listed in Table 3. Smooth (CS) and rough (MR and SR) ice crystals are considered.

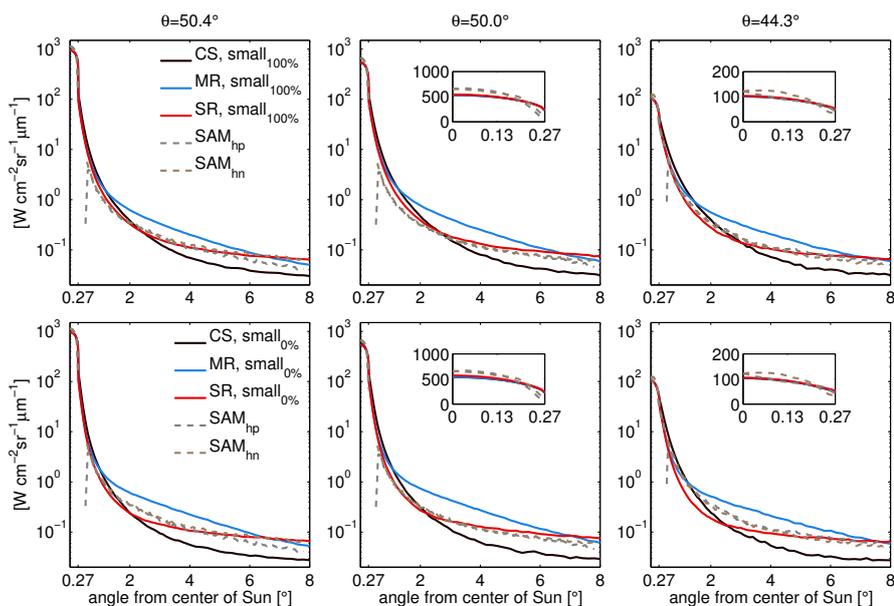


Figure 12. Comparison of the Sun and Aureole measured (SAM; hp and hn for the profiles to the right and left of Sun) and simulated radiances at three measurement times during flight B. For the simulations, the *large_B* distribution with 100 % and 0 % of measured concentration of small ice crystals is used with τ and θ values listed in Table 4. Smooth (CS) and rough (MR and SR) ice crystals are considered.