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**Parametric studies of  
contrail ice particle  
formation**

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R. C. Miake-Lye

# Parametric studies of contrail ice particle formation in jet regime using one-dimensional microphysical modeling

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## Abstract

Condensation trails (contrails) formed from water vapor emissions behind aircraft engines are the most uncertain components of the aviation impacts on climate change. To gain improved knowledge of contrail and contrail-induced cirrus cloud formation, understanding of contrail ice particle formation immediately after aircraft engines is needed. Despite many efforts spent in modeling the microphysics of ice crystal formation in jet regime (with a plume age  $<5$  s), systematic understanding of parametric effects of variables affecting contrail ice particle formation is still limited. In this work, we apply a one-dimensional modeling approach to study contrail ice particle formation in near-field aircraft plumes up to 1000 m downstream of an aircraft engine in the soot-rich regime (soot number emission index  $>1 \times 10^{15} \text{ (kg - fuel)}^{-1}$ ) at cruise. The effects of ion-mediated nucleation, ambient relative humidity, fuel sulfur content, and initial soot emissions were investigated. Our simulation results suggest that ice particles are mainly formed by water condensation on emitted soot particles. The growth of ice coated soot particles is driven by water vapor emissions in the first 1000 m and by ambient relative humidity afterwards. The presence of chemi-ions does not significantly contribute to the formation of ice particles, and the effect of fuel sulfur content is small over the range typical of standard jet fuels. The initial properties of soot emissions play the most critical role, and our calculations suggest that higher number concentration and smaller size of contrail particle nuclei may be able to effectively suppress the formation of contrail ice particles, providing a possible approach for contrail mitigation.

## 1 Introduction

Environmental concerns over aviation emissions on the current and projected climate change have increased as air traffic and aviation industry continue to grow (Wuebbles, 2006). Among aviation emissions, condensation trails (contrails) formed from water vapor emissions behind aircraft engines has gained greater attention during recent

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years. Contrails are formed under certain thermodynamic constraints (Schmidt, 1941; Appleman, 1953; Schumann, 2005) and can evolve into cirrus clouds under favorable conditions (Minnis et al., 2004). Both contrails and contrail-induced cirrus clouds could play important roles in the global climate change via affecting the radiation budget. The Intergovernmental Panel on Climate Change (IPCC) identified contrails as the most uncertain components of the aviation impacts on climate with a low level of scientific understanding (Sausen et al., 2005; Lee et al., 2009). Clearly, knowledge of how contrail ice particles are formed from aircraft emissions and how they evolve into contrails and cirrus clouds is critical to understanding climate impacts of contrails and contrail-induced cirrus clouds.

Many field measurements, such as Subsonic Aircraft: Contrail and Cloud Effects Special Study (SUCCESS) (Toon and Miake-Lye, 1998), Pollution from Aircraft Emissions in the North Atlantic Flight Corridor (POLINAT) (Schumann, 2000), and SULFUR series (Schumann et al., 2002), were carried out to elucidate important parameters affecting contrail ice particle formation and contrail evolution. Modeling studies were also performed to understand contrail formation mechanisms and potential impacts of contrails to global climate change (Brown et al., 1996; Kärcher, 1998; Yu and Turco, 1998; Kärcher et al., 2007). The initial properties of ice crystals in the near-field aircraft plumes are of particular interest, since these properties are critical in the representation of emitted aerosols and contrails in large scale models such as global climate models or large eddy simulations (Shirgaonkar and Lele, 2009). This information can only be obtained via modeling due to instrumental limitations in near-field aircraft plumes within five wingspans downstream ( $\sim 1$  s) of an aircraft engine.

Despite many efforts spent in modeling the microphysics of ice crystal formation in jet regime (with a plume age  $< 5$  s), parametric understanding of the roles of chemions, ambient conditions, fuel sulfur content, and soot emissions in the formation and evolution of contrail ice particles immediately after the engine exit plane is still limited. In this work, we apply a one-dimensional modeling approach to study the microphysics of ice particle formation in near-field aircraft plumes up to 1000 m downstream of an

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aircraft engine at cruise. The results from our microphysical calculations are presented.

## 2 Microphysical model for ice particle formation

We apply the one-dimensional microphysical model we developed previously (Brown et al., 1996; Wong et al., 2008) to study ice particle formation in near-field aircraft plumes at cruise. Our model tracks time evolution of a gaseous or a particle species in a jet engine exhaust in terms of contributions of chemistry, plume dilution and mixing, and microphysical processes as (Kärcher, 1998):

$$\frac{dX_i}{dt} = \frac{dX_i}{dt} \Big|_{\text{chemistry}} + \frac{dX_i}{dt} \Big|_{\text{mixing}} + \frac{dX_i}{dt} \Big|_{\text{microphysics}} \quad (1)$$

The contribution of chemistry comes from the chemical molar production rates of gaseous species. In our model, we use a gas-phase reaction mechanism consisting of 35 chemical species and 181 chemical reactions, which was derived from the NO<sub>x</sub> and SO<sub>x</sub> combustion mechanism by Muller et al. (2000) and the H<sub>2</sub>SO<sub>4</sub> formation pathway reported in our previous study (Brown et al., 1996). The contribution of plume dilution and mixing is described as:

$$\frac{dX_i}{dt} \Big|_{\text{mixing}} = (X_i - X_{\text{amb},i}) \cdot \frac{df(t)}{dt} \cdot \frac{1}{f(t)} \quad (2)$$

where  $f(t)$  is the exhaust mass fraction which explains how the plume is diluted by the ambient air. In our model,  $f(t)$  is evaluated using the simple dilution profile reported by Schumann et al. (1998), which was determined from measured plume properties behind aircraft at cruise altitudes for plume ages of seconds to hours.

The contribution of microphysical processes is further divided into contributions of homogeneous nucleation of new particles, coagulation among liquid particles, and ac-

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tivation and condensational growth on soot particles as:

$$\left. \frac{dX_i}{dt} \right|_{\text{microphysics}} = \left. \frac{dX_i}{dt} \right|_{\text{nucleation}} + \left. \frac{dX_i}{dt} \right|_{\text{coagulation}} + \left. \frac{dX_i}{dt} \right|_{\text{soot}} \quad (3)$$

Homogeneous nucleation of new particles is described by the kinetic quasi-unary nucleation (KQUN) theory developed by Yu (2005, 2006a, 2007). In the cases where the role of chemi-ions may be important, the kinetic ion-mediated nucleation (IMN) model developed by Yu (2006b) is used. In both KQUN and IMN, binary nucleation of H<sub>2</sub>SO<sub>4</sub>-H<sub>2</sub>O is treated as unary nucleation of sulfuric acid, and the embryo formation rates due to homogeneous binary nucleation are derived explicitly from the condensation and evaporation rates as:

$$\begin{aligned} \frac{dn_1^0}{dt} = & \gamma_{2,0}^0 n_2^0 - \sum_{j=1}^{j^{\max}-1} (\beta_{j,0}^0 n_j^0 + \beta_{j,+}^+ n_j^+ + \beta_{j,-}^- n_j^-) \\ & + \sum_{j=2}^{j^{\max}} (\gamma_{j,0}^0 n_j^0 + \gamma_{j,+}^+ n_j^+ + \gamma_{j,-}^- n_j^-) \end{aligned} \quad (\text{neutral}, i = 1) \quad (4.1)$$

$$\frac{dn_1^+}{dt} = - \sum_{j=1}^{j^{\max}-1} (\beta_{j,+}^+ n_j^0 + \beta_{j,0}^- n_j^-) + \sum_{j=2}^{j^{\max}} (\gamma_{j,0}^+ n_j^+ + \gamma_{j,-}^0 n_j^0) \quad (\text{positive}, i = 1) \quad (4.2)$$

$$\frac{dn_1^-}{dt} = - \sum_{j=1}^{j^{\max}-1} (\beta_{j,-}^- n_j^0 + \beta_{j,0}^+ n_j^+) + \sum_{j=2}^{j^{\max}} (\gamma_{j,0}^- n_j^- + \gamma_{j,+}^0 n_j^0) \quad (\text{negative}, i = 1) \quad (4.3)$$

$$\begin{aligned} \frac{dn_i^0}{dt} = & \delta i (\beta_{i-1,0}^+ n_{i-1}^+ + \beta_{i-1,0}^- n_{i-1}^- + \beta_{i-1,0}^0 n_{i-1}^0) \\ & - (\gamma_{i,+}^0 + \gamma_{i,-}^0 + \gamma_{i,0}^0) n_i^0 - (\beta_{i,+}^0 + \beta_{i,-}^0 + \beta_{i,0}^0) n_i^0 \\ & + (\gamma_{i+1,0}^+ n_{i+1}^+ + \gamma_{i+1,0}^- n_{i+1}^- + \gamma_{i+1,0}^0 n_{i+1}^0) \end{aligned} \quad (\text{neutral}, i \geq 2) \quad (4.4)$$

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$$\frac{dn_i^+}{dt} = \delta i (\beta_{i-1,+}^+ n_{i-1}^+ + \beta_{i-1,+}^0 n_{i-1}^0) - (\gamma_{i,+}^+ + \gamma_{i,0}^+) n_i^+ - (\beta_{i,+}^+ + \beta_{i,0}^+) n_i^+ + (\gamma_{i+1,+}^+ n_{i+1}^+ + \gamma_{i+1,+}^0 n_{i+1}^0) \quad (\text{positive}, i \geq 2) \quad (4.5)$$

$$\frac{dn_i^-}{dt} = \delta i (\beta_{i-1,-}^- n_{i-1}^- + \beta_{i-1,-}^0 n_{i-1}^0) - (\gamma_{i,-}^- + \gamma_{i,0}^-) n_i^- - (\beta_{i,-}^- + \beta_{i,0}^-) n_i^- + (\gamma_{i+1,-}^- n_{i+1}^- + \gamma_{i+1,-}^0 n_{i+1}^0) \quad (\text{negative}, i \geq 2) \quad (4.6)$$

where  $n_i$  is the number concentration of embryos with  $i$  sulfuric acid molecules, and  $j_{\max}$  is the maximum embryo size tracked in the model.  $\beta_{i,0}$ ,  $\beta_{i,+}$ , and  $\beta_{i,-}$  are condensational growth rate constants for embryos with  $i$  sulfuric acid molecules to form neutral, positively charged, and negatively charged embryos one size larger (i.e.,  $i+1$  sulfuric acid molecules). Similarly,  $\gamma_{i,0}$ ,  $\gamma_{i,+}$ , and  $\gamma_{i,-}$  are evaporation rate constants for embryos with  $i$  sulfuric acid molecules to produce neutral, positively charged, and negatively charged embryos one size smaller (i.e.,  $i-1$  sulfuric acid molecules). The superscripts “0”, “+”, and “-” in concentration and rate constant terms refer to neutral, positively charged, and negatively charged embryos, and  $\delta_i$  is a constant with a value of 0.5 when  $i=2$  and a value of 1.0 otherwise.

Coagulation of different liquid embryos is described using the coagulation kernels in the IMN theory (Yu, 2006b). For liquid particles that are larger than  $j_{\max}$ , we use sectional bin approach (Jacobson et al., 1995) and Brownian coagulation kernels (Fuchs, 1989). In our model, we allow coagulation interactions between all liquid droplets except those between two positively charged or two negatively charged droplets.

Activation and condensational growth of liquid particles on soot is treated the same way as Kärcher et al. (1998) and our previous study (Wong et al., 2008). Activation is described as adsorption of  $\text{H}_2\text{SO}_4$ ,  $\text{SO}_3$ , or  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  embryos on soot particle

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surfaces. For example, the amount of sulfate mass ( $m$ ) adsorbed on soot particles in the  $i$ -th bin can be expressed as:

$$\frac{dm_i}{dt} = \frac{\pi}{4} \cdot \alpha \cdot \bar{c} \cdot d_{p,i}^2 \cdot (1 - \theta_i) \cdot C_a \cdot M_{w,a} \quad (5)$$

where  $\alpha$  is the mass accommodation coefficient of  $\text{H}_2\text{SO}_4$  on the uncovered fraction of soot surface,  $\bar{c}$  is mean particle thermal speed,  $d_{p,i}$  is soot particle diameter,  $\theta$  is the covered (activated) fraction of the soot surface,  $C_a$  is  $\text{H}_2\text{SO}_4$  concentration, and  $M_{w,a}$  is  $\text{H}_2\text{SO}_4$  molecular weight. The resulting change in activation fraction on soot surface by  $\text{H}_2\text{SO}_4$  is described as:

$$\frac{d\theta_i}{dt} = \frac{1}{4} \cdot \alpha \cdot \bar{c} \cdot \frac{N_0}{\sigma_0} \cdot (1 - \theta_i) \cdot C_a \quad (6)$$

where  $N_0$  is Avogadro's number,  $\sigma_0$  is average number of sites (molecules) per unit area of soot surface set at  $5 \times 10^{18} \text{ m}^{-2}$ . In our model, no coagulation between ice coated soot particles is allowed.

To simplify our calculations, the homogeneous  $\text{H}_2\text{SO}_4$ - $\text{H}_2\text{O}$  droplets and the liquid coatings condensed on soot particles are not allowed to freeze until the plume temperature drops below the composition dependent freezing temperature of  $\text{H}_2\text{SO}_4$ - $\text{H}_2\text{O}$  binary solution reported by Gable et al. (1950). As will be discussed later, the homogeneous  $\text{H}_2\text{SO}_4$ - $\text{H}_2\text{O}$  droplets produced in our simulations are too small and too acidic to freeze under our conditions of interest. This is consistent with the slow homogeneous freezing rates calculated by the parameterized classical theory of homogeneous freezing (Tabazadeh et al., 1997). On the other hand, calculations using the modified classical theory of heterogeneous freezing (Kärcher et al., 1996; Pruppacher and Klett, 1997) indicate that coated soot particles with a size of 20 nm and a contact angle of  $50^\circ$  should induce heterogeneous freezing in a time scale of  $10^{-2} \text{ s}$  ( $\sim 2.5$ – $5 \text{ m}$  in distance) after 70 m downstream. Due to this reason and the well-known uncertainties of the classical heterogeneous nucleation theory of freezing, we assume coatings on soot particles freeze instantly below their freezing points determined by sulfate mass

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fraction. Although this approximation gives us an upper bound of size and number concentration of ice particles produced, we do find our representative modeling results, which will be discussed in the next section, consistent with available modeling results (Kärcher, 1998; Kärcher and Yu, 2009) and measurement data (Schumann, 2002).

Enhancement of nucleation rates by organic species has been shown in the laboratory (Zhang et al., 2004). Recent field campaigns measuring aircraft emissions at ground-level also demonstrate that this process may be important especially at low to mid power range where significantly more organic emissions are present in the gas and condensed phases (Knighton et al., 2007; Yelvington et al., 2007). However, knowledge of nucleation or particle growth enhanced by organic species is still limited, as are the species involved and the process by which the organic compounds contribute to the aerosol growth. Due to this reason, we do not explicitly consider the effects of organic species in these calculations. However, we believe that our modeling results will provide valuable information to understand the parametric effects of the contrail ice particle formation from aircraft emissions at cruise even though our model may not capture all the microphysical details. The simulation results are also a good source for interpreting current measurement data. The entrainment of ambient particles is also neglected in this work because the concentration of ambient particles in the soot-rich regime is much smaller than the aircraft emitted particles in near-field aircraft plumes with a downstream distance smaller than 1000 m.

### 3 Results and discussions

We have performed one-dimensional (1-D) detailed microphysical simulations for PW4056 engines equipped on some Boeing 767 aircraft, which have a wingspan of 47.5 m. The parameters used for these simulations are listed in Table 1, which describes the ambient conditions and the engine operating parameters we used for a cruising altitude of 35 000 ft. Effects of ion-mediated nucleation, ambient relative

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humidity, fuel sulfur content, and initial soot emissions are investigated in this work.

Figure 1 shows a set of representative results from a 1-D microphysical simulation with an initial soot particle concentration of  $1 \times 10^7 \text{ cc}^{-1}$  (which corresponds to a number emission index,  $EI_N$ , of  $\sim 4.6 \times 10^{15} (\text{kg} - \text{fuel})^{-1}$ ), an initial soot geometric mean diameter (GMD) of 40 nm, a GMD standard deviation of 1.6, a fuel sulfur content level of 400 ppm by weight, and an ambient relative humidity with respect to ice of 100%. In our model, the growth of the homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles is tracked individually if they contain no more than 40 sulfuric acid molecules (Fig. 1c). For larger homogeneous particles, we use 30 log-normally distributed bins (Jacobson et al., 1995) to track all the particles up to 250 nm (Fig. 1b). For ice coated soot particles (Fig. 1d), we also use 30 log-normally distributed bins to represent particle size distributions at the engine-exit plane and downstream. As illustrated in the figure, the nucleation of the homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles takes place as sulfuric acid and water supersaturation is highest about 30 m downstream. It is known that acidity of homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles increases with decreasing particle size (Yu, 2005), and more acidic particles have lower freezing temperature (Gable et al., 1950). As a result, small volatile particles formed from homogeneous nucleation are too acidic to freeze when water supersaturation is above 100%. After water supersaturation drops below 100%, additional water condensation on liquid particle surface to have significant particle growth becomes thermodynamically unfavorable. In contrast, ice coated soot particles grow to a size of around  $1 \mu\text{m}$  at 1000 m downstream. The growth of these particles is the most rapid in the first 100 m, especially in between 30–50 m, where the particle growth is driven mostly by the supersaturation of water vapor emitted from the engines. The ice particle growth after 100 m is more moderate compared to the first 100 m and is driven by modest supersaturation of water with respect to ice. Our simulation results suggest that ice particles are mainly formed by water condensation on emitted soot particles under this condition, which is consistent with the modeling results in the soot-rich regime ( $EI_N > 1 \times 10^{15} (\text{kg} - \text{fuel})^{-1}$ ) by Kärcher and Yu (2009). Our results are also agreeable with laboratory findings in freezing experiments of soot

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particles immersed in water droplets that heterogeneous freezing on soot surfaces is more favorable than homogeneous freezing of unseeded water droplets (Popovicheva et al., 2008).

Since plume dilution in our model is based on a simple equation (Schumann et al., 1998) that was determined largely from measured plume properties for a plume age greater than 0.2 s ( $\sim 50$  m downstream), the dilution history within the first wing span downstream may not be accurately captured. To study the sensitivity of contrail ice particle formation to plume dilution history immediately after engine-exit plane, we employed a semi-empirical, self-similar approach developed by Davidson and Wang (2002) in addition to the Schumann equation to estimate exhaust dilution. The Davidson and Wang algorithm describes the behavior of a nonbuoyant discharge in a coflowing ambient fluid, and was found to be able to capture the dilution behavior of near-field aircraft plumes at ground-level at 30 m downstream very well (Wong et al., 2008). As shown in Fig. 2a, the exhaust dilution profile estimated from the Davidson and Wang algorithm under the same ambient and engine operating conditions is faster than that is determined from the Schumann equation. The final exhaust mass fraction at 1000 m downstream is also lower ( $\sim 0.5\%$  compared to  $\sim 2\%$ ). To eliminate the effects of different dilution level at the end of 1000 m, we also introduced a hybrid profile of the two, which approximates the fast dilution of the Davidson and Wang profile in the first 500 m but approaches the final dilution level of the Schumann profile at the end of the 1000 m.

The predicted values of geometric mean diameter of the ice coated soot particles using different dilution profiles are shown in Fig. 2b. Although dilution is faster (and thus plume temperature also drops faster) for the Davidson and Wang profile, the rapid particle growth starts earlier when the Schumann profile is used. This is because higher water vapor concentration in the Schumann profile enables the exhaust to reach water vapor supersaturation sooner at a warmer temperature, as illustrated in Fig. 2c. The final particle size is slightly smaller when the Davidson and Wang profile is used. This is because the dilution level at 1000 m downstream is higher in this case and there is less available water vapor for condensation. On the other hand, the final particle size

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for the hybrid profile approaches the prediction for the Schumann equation, suggesting that differences in the dilution trajectories in the first 500 m only affects the onset of particle growth, but final particle size is determined by final dilution levels. This is consistent with the assumption that contrail ice particle formation is a thermodynamically controlled process.

The effects of ion-mediated nucleation have been studied extensively in the literature. It is believed that ions present in the aircraft emissions at cruise have great impacts on homogeneous nucleation and formation on volatile sulfuric acid-water aerosols. However, their contribution to the formation of contrail ice particles is still uncertain. Here, we investigated the effects of ion-mediated nucleation on the formation of ice coated soot particles, as shown in Fig. 3. The ion-mediated nucleation model developed by Yu [2006b] was incorporated, and the same conditions used in Fig. 1 were chosen for Fig. 3. The initial ion concentration was assumed to come from ionization of 1% of the initial sulfuric acid concentration ( $\sim 7.5 \times 10^{17} \text{ (kg - fuel)}^{-1}$  for both positive and negative ions). As shown in the figure, the presence of chemi-ions does speed up the nucleation rates of homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles, as evidenced by significant enhancement of embryo and droplet size and concentration (Fig. 3a, b). However, freezing of these larger liquid  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles formed from ion-mediated nucleation are still unfavorable such that their contribution to ice particle growth is limited. As a result, the growth of ice coated soot particles is not affected, as shown in Fig. 3c, and no significant increase of the ice particle size was observed with the addition of chemi-ions. Our modeling results suggest that the presence of chemi-ions in the soot-rich regime does not significantly contribute to the formation of additional ice nuclei to alter ice particle growth.

Figure 4 shows the effects of ambient relative humidity with respect to ice (RHI) on ice coated soot particle size distributions. Four different levels of ambient RHI were studied in this work: 110, 100, 90, and 80%. As shown in the figure, the growth of ice coated soot particles is most rapid in between 30–50 m downstream regardless ambient RHI levels. In this region, the effect of ambient RHI is negligible because the

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particle growth is driven by water vapor emitted from the aircraft engines. At 1000 m downstream, the ice coated soot particles under higher ambient RHI become slightly larger than those under lower ambient RHI. However, this difference is still quite small because the difference in ice supersaturation in the exhaust plume is within 1% for such a short plume age ( $\sim 4$  s). This further confirms that ice particle growth in the first 1000 m is driven by emitted water vapor condensation whereas ice particle growth afterwards is driven by ambient relative humidity.

Figure 5a shows the effects of fuel sulfur content (FSC) on particle size distributions of ice coated particles as a function of downstream distance. The same conditions in Fig. 1 were modeled, and two additional fuel sulfur levels, 200 ppm and 800 ppm by weight, were studied. Our calculation results show that the growth of ice coated soot particles is initially slower when fuel sulfur is lower at a downstream distance of around 32.5 m. This is because lower fuel sulfur levels give lower initial  $\text{SO}_3$  and  $\text{H}_2\text{SO}_4$  concentrations. As a result, a smaller fraction of the soot surface is activated by  $\text{SO}_3$  and  $\text{H}_2\text{SO}_4$  as illustrated in Fig. 5b and the modeling results by Kärcher (1998). This can be explained by the relationship between soot surface coverage ( $\theta$ ) and  $\text{H}_2\text{SO}_4$  concentration ( $C_a$ ) in Eq. (6). Smaller activated area on soot surface effectively reduces water condensation rate on soot surface when the particles are small. When particles grow to a size that is much larger than the cores, however, the fraction of the activated soot surface becomes relatively unimportant because of much larger available ice surface area. In this case, the growth of ice coated soot particles is faster when fuel sulfur is lower, since binary homogeneous nucleation is not depleting water as effectively without enough  $\text{SO}_3$  and  $\text{H}_2\text{SO}_4$  in the gas phase, resulting in higher water vapor concentration (and hence higher water supersaturation). This difference, however, is very small between FSCs of 200 ppm and 800 ppm (Fig. 5a), since our model predicts that only slightly larger particles are formed for a fuel sulfur level of 200 ppm at a downstream distance of 1000 m. Our modeling results are consistent with experimental findings (Schumann et al., 2002) where no significant effect of fuel sulfur content on contrail formation was observed.

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Studies on the effects of soot emissions on contrail ice particle properties are very limited in the literature. To our knowledge, the recent paper by Kärcher and Yu (2009) is the only modeling work that attempts to perform systematic studies on the roles of soot emissions in the formation and evolution of young contrails. It is suggested in their work that in the soot-rich regime ( $EI_N > 1 \times 10^{15} \text{ (kg - fuel)}^{-1}$ ) ice particles mainly form by freezing of water around the soot cores, whereas in the soot-poor regime ( $EI_N < 1 \times 10^{13} \text{ (kg - fuel)}^{-1}$ ) ice particles mainly originate from liquid particles without soot cores. In this paper, we performed a similar parametric study to investigate the effects of initial number concentration and particle size distribution of soot emissions. We focus our work on the soot-rich regime, since it corresponds to the soot emissions from existing aircraft technology.

Figure 6 shows the effects of initial number concentration of soot particles on ice particle size distributions in the aircraft exhaust up to 1000 m downstream. Three different initial number loadings of soot particles were studied, and our simulation results show that size of ice coated soot particles decreases with increasing initial soot concentration. This is because more soot particles are competing for water vapor and a smaller amount of water is condensed on each soot particle when the initial soot concentration is higher. Note that when the initial soot concentration is  $5 \times 10^7 \text{ cc}^{-1}$  (Fig. 6c), a bimodal particle size distribution is predicted from our calculation after 35 m downstream. The smaller mode of this particle size distribution represents those liquid coated soot particles. Because of the Kelvin effect and the smaller available surface area, the amount of water condensation on these liquid soot particles is smaller, resulting in more acidic coatings on them. Similar to the homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles formed from nucleation, these liquid particles are too acidic to freeze when water supersaturation is above 100%. After water supersaturation drops below 100% (even though RHI is above 100%), water condensation on liquid particle surface becomes thermodynamically unfavorable to grow into larger size. This prediction is consistent with the experimental findings by Popovicheva et al. (2008), where they suggested that hydrophilic coverage (e.g. sulfuric acid) on the hydrophobic soot surface higher than

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a threshold value could inhibit ice nucleation due to effective dissolution of water in the soluble surface coverage, reducing the likelihood of freezing of the solution.

Figure 7 shows the effects of initial soot particle size on the growth of ice coated soot particles in the aircraft exhaust up to 1000 m downstream. Three different particle size distributions of soot cores were initialized for calculations, and our simulation results show that smaller soot cores result in more liquid particles and fewer but larger ice particles. This is because liquid particles in the smaller mode of the bimodal particle size distribution are too acidic to freeze, and fewer soot particles in the large mode can serve as ice nuclei to compete for water vapor condensation. The resulting particle size distribution of ice coated soot particles is also broader for smaller soot cores since the split between the two modes are more marked.

Our above simulation results are generally consistent with the modeling results in the soot-rich regime by Kärcher and Yu (2009). However, the effects of initial soot number concentration and initial soot core size observed in our model also suggest that sufficiently high soot core number concentration and sufficiently small soot core size that were not investigated in Kärcher and Yu (2009) may be able to suppress ice particle growth. To validate this assumption, we performed a one-dimensional micro-physical calculation initialized with a hypothetical soot core number concentration of  $1 \times 10^{10} \text{ cc}^{-1}$  ( $EI_N = 4.6 \times 10^{18} \text{ (kg - fuel)}^{-1}$ ) and a GMD of soot core size distribution of 5 nm. The simulation results are shown in Fig. 8. In this case, no significant ice particle growth is predicted from the model because all the particles are too acidic to freeze and are “trapped” in the liquid phase, limiting significant particle growth. The results shown in Fig. 8 suggest that ice particle growth could be suppressed by a high number concentration of sufficiently small soot cores in the aircraft emissions. Although existing engine technology does not produce such soot particles, our findings suggest that manipulating the number and size of contrail particle nucleation sites can affect contrail properties and offers possibilities for potential mitigation. Further laboratory studies and field measurements are clearly needed to validate the above implication.

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## 4 Conclusions

To gain systematic understanding of parametric effects of variables affecting contrail ice particle formation, we apply a one-dimensional modeling approach to study micro-physics of contrail ice particle formation in near-field aircraft plumes in the soot-rich regime (soot number emission index  $> 1 \times 10^{15}$  (kg – fuel) $^{-1}$ ) at cruise. Our calculations suggest that ice particles are mainly formed by water condensation on emitted soot particles in this regime. The growth of ice coated soot particles is more rapid in the 100 m downstream of an engine and is driven by water emissions. After 100 m downstream, the size of ice particles is mostly affected by ambient relative humidity with respect to ice but the effect of ambient relative humidity in the first 1000 m downstream remains insignificant. The presence of chemi-ions speeds up the nucleation rates of homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  particles, but the growth of ice coated soot particles is not affected since these homogeneous particles are too acidic to freeze and do not serve as ice nuclei. The effect of fuel sulfur content is small, and our calculations show that only slightly larger particles at 1000 m downstream are formed for a lower fuel sulfur level at 200 ppm by weight. The initial properties of soot emissions play the most critical role, and our calculations show that higher initial number concentrations of soot cores result in smaller ice particles. In addition, a bimodal particle size distribution consisting of smaller liquid particles and larger ice particles is predicted when initial number concentration of soot cores is sufficiently high. Initializing with smaller soot particles also results in more liquid particles in the smaller mode of the bimodal distribution, suggesting that ice particle growth could be suppressed by a high number concentration of sufficiently small contrail particle nuclei in aircraft emissions, providing a possible approach for contrail mitigation.

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**Table 1.** Parameters used for the 1-D microphysical simulations in this work.

Cruise altitude	35 000 ft
Ambient temperature	218.80 K
Ambient pressure	23.84 kPa
Ambient air density	0.38 kg/m <sup>3</sup>
Cruise speed	236.79 m/s (0.8 M)
Net Thrust	42.18 kN
Core mass flow rate	52.72 kg/s
Bypass mass flow rate	247.03 kg/s
Fuel mass flow rate	0.69 kg/s
Bypass ratio	4.69
Core total temperature at engine exit	590.23 K
Bypass total temperature at engine exit	288.36 K
Core flow velocity at engine exit	444.60 m/s
Bypass flow velocity at engine exit	310.76 m/s

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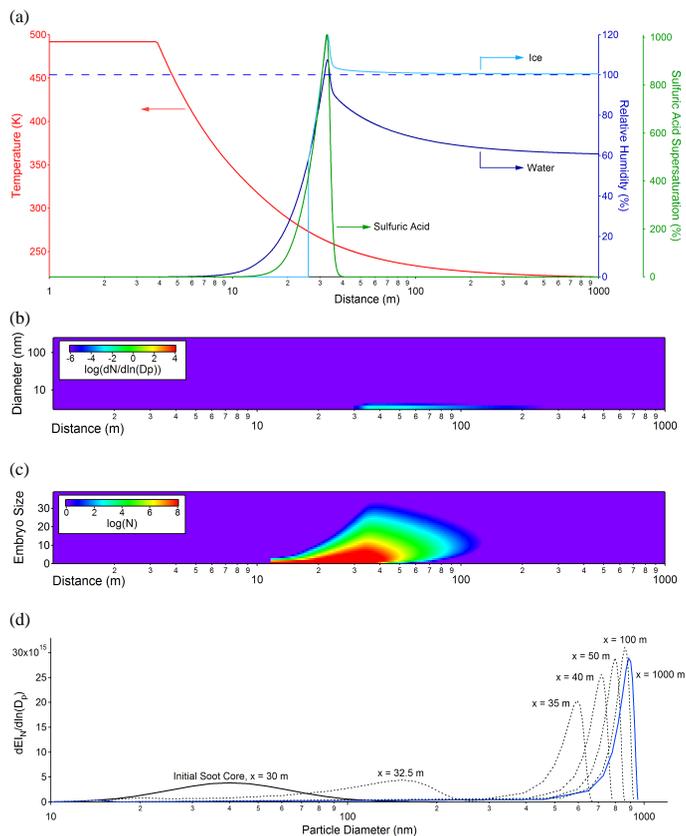
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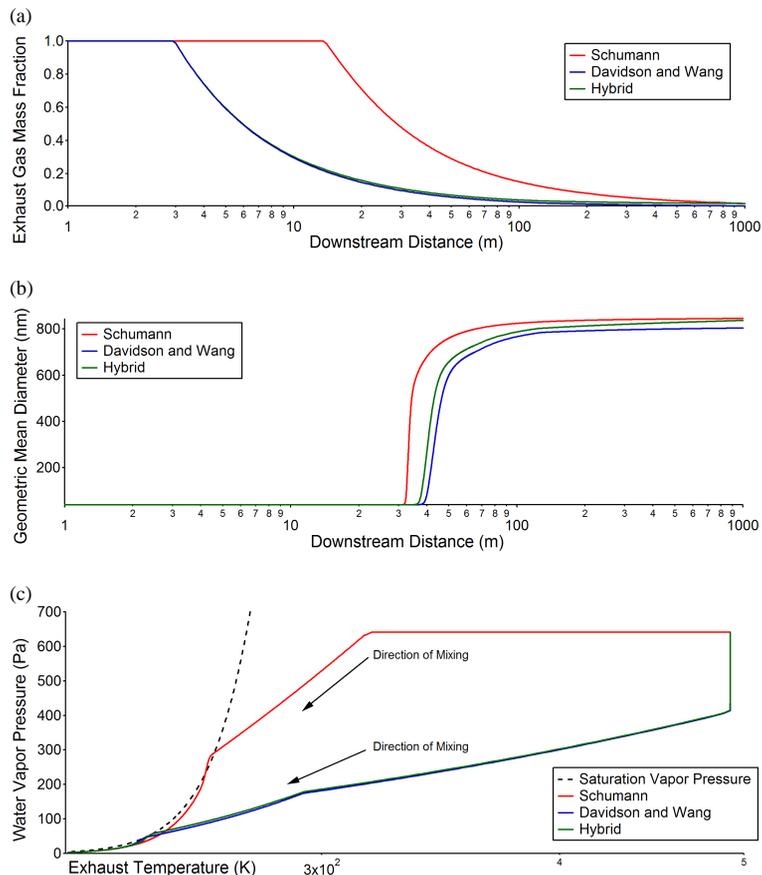
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**Fig. 1.** Representative simulation results following the plume centerline trajectory up to 1000 m downstream: **(a)** trajectories of plume temperature, and ice, water, and acid supersaturation as a function of downstream distance; **(b)** concentration and size evolution of volatile  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  droplets; **(c)** concentration and size evolution of volatile  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  embryos smaller than 40 acid molecules; **(d)** size evolution of ice coated soot particles.

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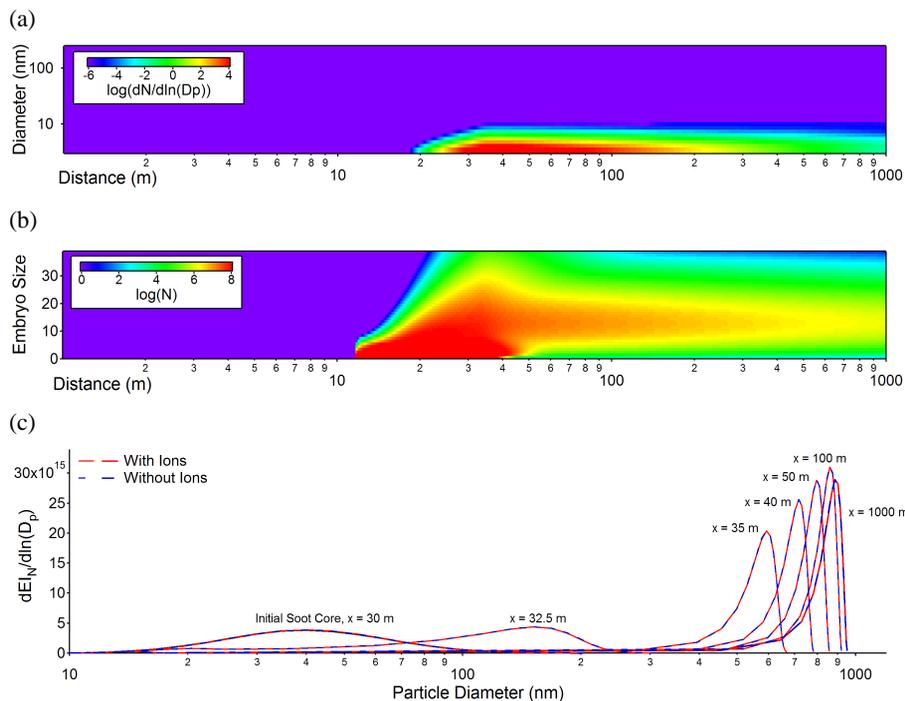
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**Fig. 2.** (a) Exhaust mass fraction determined from the Schumann equation, the Davidson and Wang algorithm, and the hybrid of the two; (b) the predicted values of geometric mean diameter of the ice coated soot particles using different dilution profiles; (c) the water vapor pressure following different mixing trajectories and its relevance to saturation vapor pressure.

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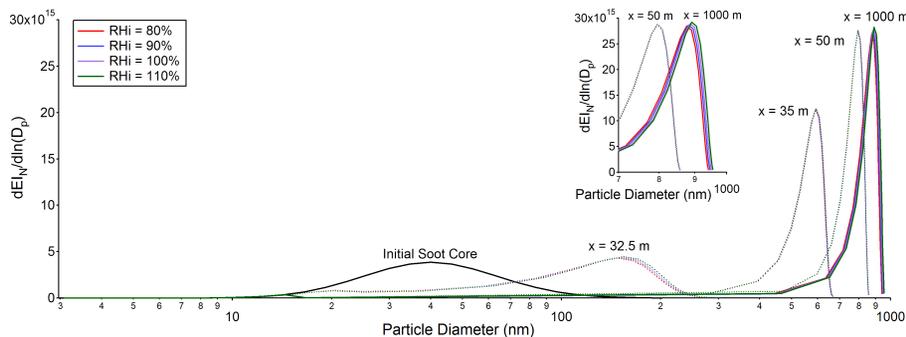


**Fig. 3.** Simulation results for ion-mediated homogeneous  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  nucleation under the same condition as Fig. 1: **(a)** concentration and size evolution of volatile  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  droplets; **(b)** concentration and size evolution of volatile  $\text{H}_2\text{SO}_4\text{-H}_2\text{O}$  embryos smaller than 40 acid molecules; **(c)** ice coated soot particle size distributions as a function of downstream distance with or without ion-mediated nucleation.

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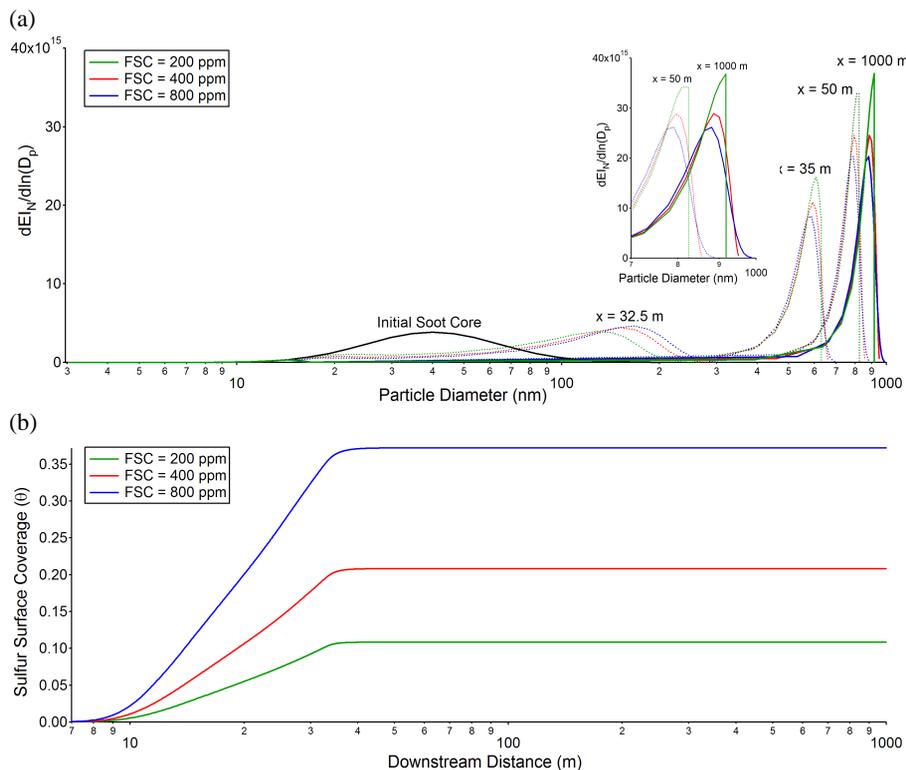
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**Fig. 4.** Effects of ambient relative humidity with respect to ice (RHI) on ice particle size distributions at downstream distances of 32.5, 35, 50, and 1000 m.

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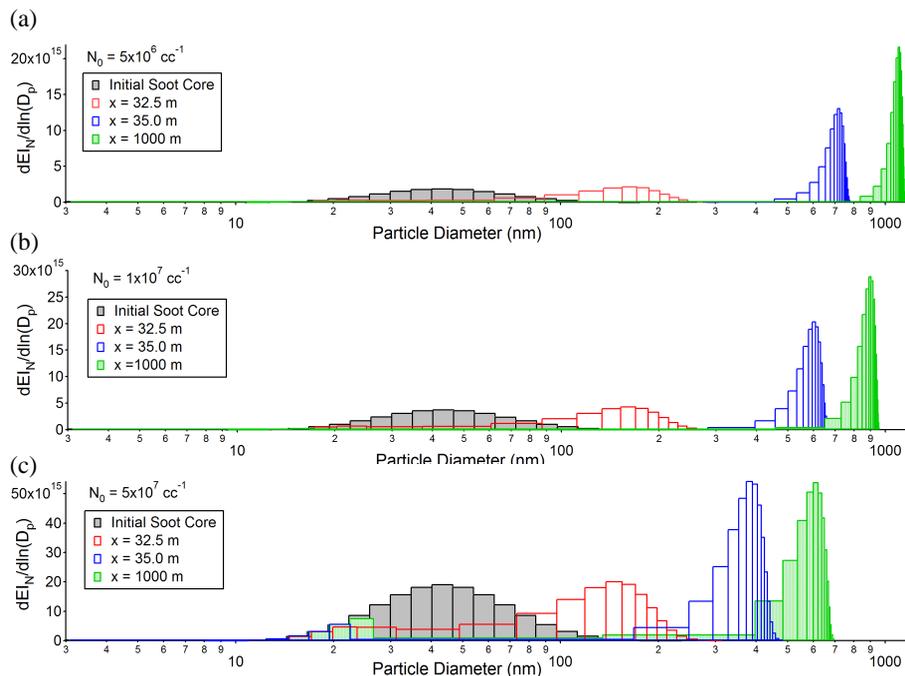
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**Fig. 5.** Effects of fuel sulfur content (FSC) on: **(a)** ice particle size distributions at downstream distances of 32.5, 35, 50, and 1000 m; **(b)** sulfur activated fraction on soot surface.

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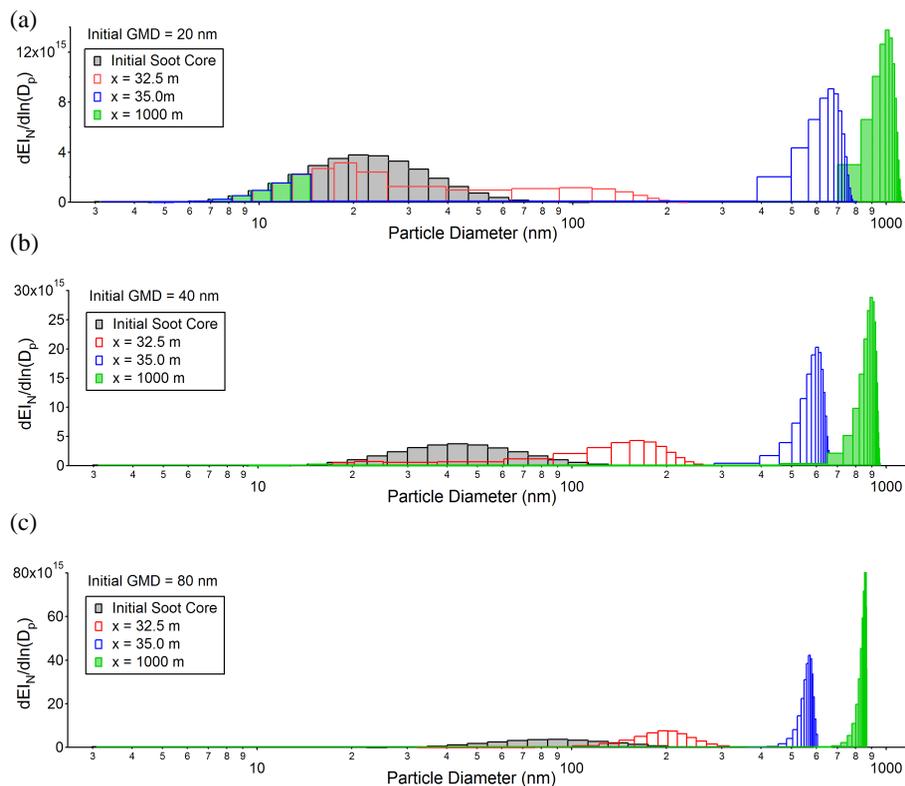
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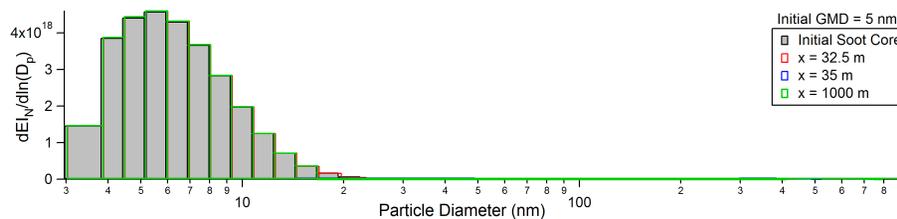
**Fig. 6.** Effects of initial soot core number concentration ( $N_0$ ) on size distributions of ice coated soot particles as a function of downstream distance ( $x$ ) when  $N_0$  is: **(a)**  $5 \times 10^6 \text{ cc}^{-1}$  ( $EI_N \sim 2.3 \times 10^{15} \text{ (kg - fuel)}^{-1}$ ); **(b)**  $1 \times 10^7 \text{ cc}^{-1}$  ( $EI_N \sim 4.6 \times 10^{15} \text{ (kg - fuel)}^{-1}$ ); **(c)**  $5 \times 10^7 \text{ cc}^{-1}$  ( $EI_N \sim 2.3 \times 10^{16} \text{ (kg - fuel)}^{-1}$ ).

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**Fig. 7.** Effects of initial soot core size on size distributions of ice coated soot particles as a function of downstream distance ( $x$ ) when geometric mean diameter (GMD) of initial particle size distribution of soot cores is: **(a)** 20 nm; **(b)** 40 nm; **(c)** 80 nm.

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**Fig. 8.** Simulation results show no significant ice coated soot particle growth when initial soot core concentration is  $1 \times 10^{10} \text{ cc}^{-1}$  and GMD of initial soot particle size distribution is 5 nm.

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