

Asymmetric and axisymmetric dynamics of tropical cyclones

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Abstract

We present the results of idealized numerical experiments to examine the difference between tropical cyclone evolution in three-dimensional (3-D) and axisymmetric (AX) model configurations. We focus on the prototype problem for intensification, which considers the evolution of an initially unsaturated AX vortex in gradient-wind balance on an f -plane. Consistent with findings of previous work, the mature intensity in the 3-D model is reduced relative to that in the AX model. In contrast with previous interpretations invoking barotropic instability and related horizontal mixing processes as a mechanism detrimental to the spin-up process, the results indicate that 3-D eddy processes associated with vortical plume structures can assist the intensification process by contributing to a radial contraction of the maximum tangential velocity and to a vertical extension of tangential winds through the depth of the troposphere. These plumes contribute significantly also to the azimuthally-averaged heating rate and the corresponding azimuthal-mean overturning circulation.

The comparisons show that the resolved 3-D eddy momentum fluxes above the boundary layer exhibit counter-gradient characteristics and are generally not represented properly by the subgrid-scale parameterizations in the AX configuration. The resolved eddy fluxes act to support the contraction and intensification of the maximum tangential winds. The comparisons indicate fundamental differences between convective organization in the 3-D and AX configurations for meteorologically relevant forecast time scales. While the radial and vertical gradients of the system-scale angular rotation provide a hostile environment for deep convection in the 3-D model, with a corresponding tendency to strain the convective elements in the tangential direction, deep convection in the AX model does not suffer this tendency. Also, since during the 3-D intensification process the convection has not yet organized into annular rings, the azimuthally-averaged heating rate and radial gradient thereof is considerably less than that in the AX model. This lack of organization results broadly in a slower intensification rate in the 3-D model and leads ultimately to a weaker mature vortex after 12 days

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alent potential temperature (θ_e) through the high straining motions that it generates within and above the boundary layer. Both of these processes create an environment less favourable for future convective episodes until the boundary layer re-establishes some ambient level of instability as a result of sea-air moisture fluxes (Nguyen et al., 2011).

When buoyant convection occurs in a environment with non-zero vertical vorticity, updraughts will amplify the vorticity by the process of vortex-tube stretching (e.g., Julian et al., 1996; Sprague et al., 2006; Wissmeier and Smith, 2011).

There is accumulating observational and numerical modelling evidence affirming the hypothesis that deep convection in pre-depression disturbances and tropical cyclones acts to spin up localized cyclonic vorticity anomalies in the lower troposphere (Reasor et al., 2005; Bell and Montgomery, 2010; Sippel et al., 2006; Raymond and Lopez, 2011; Sanger et al., 2013; Kilroy and Smith, 2012). The role of these rotating deep convective clouds and their aggregation in the amplification of the larger-scale vortex has been the subject of recent numerical and theoretical investigations (Hendricks et al., 2004; Montgomery et al., 2006; Nguyen et al., 2008; Shin and Smith, 2008; Fang and Zhang, 2010; Braun et al., 2010; Gopalakrishnan et al., 2011; Schecter, 2011) and is reviewed briefly below.

1.1 Role of vortical deep convection in tropical cyclones

The studies referred to above suggest that vortical updraughts have typical horizontal length scales of 10 to 20 km and lifespans of an hour or more. The magnitude of the vorticity amplification above its ambient value is up to 1–2 orders in the lowest 5 km of the troposphere. This vorticity outlives the convection that produced it and the like-signed vortical remnants tend to aggregate in a quasi two-dimensional manner with a corresponding upscale vorticity cascade together with a segregation and weakening of the convectively-generated anticyclonic vorticity, at least above the boundary layer. Some of the positive remnants are intensified further by subsequent convective episodes.

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When the system-scale circulation becomes sufficiently strong, vorticity remnants tend to become axisymmetrized by the associated angular shear flow. In addition, system-scale inflow forced by the aggregate latent heating from the convective elements leads to an inward advection of both system-scale absolute vorticity and convectively-enhanced vorticity. Stokes' theorem applied to a fixed area surrounding the convection implies that there will be an accompanying increase in strength of the system-scale circulation on account of the import of net ambient absolute vorticity into it. When applied to a fixed area within the convective region, the import¹ also of net convectively-enhanced cyclonic vorticity into the area will lead to an increase in the circulation within the convective region. As the near-surface circulation increases progressively in strength, there is some increase in the surface moisture fluxes (Montgomery et al., 2009), which will accelerate the replenishment of ambient CAPE. However, Montgomery et al. (2009) showed that it is not necessary that the moisture fluxes continue to increase with surface wind speed, hitherto believed to be an essential element in the intensification process (Rotunno and Emanuel, 1987; Emanuel et al., 1994).

The emerging paradigm of tropical cyclone spin-up as articulated above recognizes the intrinsic fluid dynamics and thermodynamics of rotating deep convection as well as its collective effects in producing system-scale inflow. It recognizes also the potential role of vortex Rossby waves (VRWs²) and their wave-mean and wave-wave interaction as well as their coupling to the boundary layer and convection (Chen and Yau, 2001; Wang, 2002a, b; Chen et al., 2003; Martinez, 2008; Martinez et al., 2010, 2011). In

¹The stretching and thereby amplification of ambient (or system-scale) vorticity by convection by itself does not lead to an increase in the circulation so defined, because stretching leads to a contraction in the areal extent of the amplified vorticity (see Haynes and McIntyre, 1987).

²VRWs are analogues of planetary Rossby waves (e.g., Holton, 2004), but propagate on the potential vorticity gradient of the system-scale vortex and are affected by the corresponding differential rotation in the radial and vertical direction (Shapiro and Montgomery, 1993; Guinn and Schubert, 1993; Montgomery and Kallenbach, 1997; Schubert et al., 1999; Möller and Montgomery, 2000; McWilliams et al., 2003).

other words, the tropical cyclone intensification process generally comprises a turbulent system of rotating, deep moist convection and vortex Rossby waves. A recent review of the new paradigm and its relationship to previous ones is given by Montgomery and Smith (2013).

5 1.2 An axisymmetric perspective

There is an extensive literature describing the axisymmetric dynamics of tropical cyclone intensification (Ooyama, 1969, 1982; Carrier, 1971; Anthes, 1982; Shapiro and Willoughby, 1982; Hack and Schubert 1986; Rotunno and Emanuel, 1987; Emanuel, 1989, 1995, 1997, 2012; Willoughby, 1990; Nguyen et al., 2002; Smith et al., 2011) and maximum possible intensity for a given thermodynamic environment (Miller, 1958; Malkus and Riehl, 1960; Carrier et al., 1971; Emanuel, 1986, 2012; Bister and Emanuel, 1998; Camp and Montgomery, 2001; Emanuel et al., 2004; Bryan and Rotunno, 2009a, b; Emanuel and Rotunno, 2011).

In axisymmetric models, all effects of the flow asymmetries must be parameterized in terms of azimuthally-averaged variables. Previous studies have suggested that flow asymmetries generally contribute adversely to the intensification rate and the mature hurricane intensity (e.g., Yang et al., 2007; Bryan et al., 2010). One type of flow asymmetry results from the barotropic breakdown of an unstable ring vortex (e.g., Michalke and Timme, 1967; Rotunno, 1979; Vladimirov and Tarasov, 1979; Schubert et al., 1999). The ensuing potential vorticity redistribution process has been shown to weaken the maximum tangential wind while simultaneously spinning up the flow within the eye towards solid body rotation (Schubert et al., 1999). On the basis of these findings, the net effect of the asymmetries has been assumed to be the down-gradient mixing of momentum and (local) buoyancy. This diffusive-like mixing process has been hypothesized to yield a reduction of the intensification rate and a weakening of the intensity of the storm at maturity relative to its axisymmetric counterpart (Bryan et al., 2010).

In the azimuthal-mean perspective, deep convection contributes in the aggregate to a system-scale radial gradient of positive latent heating that spans the troposphere

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and is maximized slightly above the mid-troposphere. This heating gradient leads to an azimuthally-averaged inflow in the lower half of the troposphere and outflow above. The deep convection contributes collectively to spinning up the tropical cyclone vortex through the radial convergence of azimuthally-averaged absolute angular momentum

5 $M = rV + \frac{1}{2}fr^2$, where r is the radius, V is the azimuthally-averaged tangential wind speed, and f is the Coriolis parameter. Above the frictional boundary layer, M is materially conserved, assuming that eddy processes are unimportant. Since M is proportional to the absolute circulation for a circular loop around the vortex, the material conservation of M implies a concomitant increase of areally-averaged absolute vorticity

10 within a closed circuit moving with the azimuthally-averaged radial flow. This mechanism has been articulated previously by many authors (e.g., Willoughby, 1979; Shapiro and Willoughby, 1982). It explains why the vortex expands in radial extent as measured by an increase in tangential winds beyond the radius of maximum winds and may be interpreted in terms of axisymmetric balance dynamics (Bui et al., 2009; Smith et al.,

15 2011).

Although M is not materially conserved in the boundary layer, large tangential wind speeds can be achieved there if the radial inflow is sufficiently large to bring the air parcels to small radii with minimal loss of M . This spin-up mechanism, while coupled to the interior flow via the radial pressure gradient at the top of the boundary layer, is tied

20 fundamentally to the dynamics of the boundary layer, where the flow is not in gradient wind balance over a substantial radial span (Smith et al., 2009).

1.3 How different is tropical cyclone dynamics in three-dimensional and axisymmetric models?

Apart from the assumed downgradient role of all asymmetric motions (including vortical convection and VRWs), the apparent success of AX models has supported a view that,

25 in the absence of vertical shear and vortex translation, the structure and evolution of the azimuthally-averaged fields in the 3-D model are captured by a strictly AX model (Anthes et al., 1971; Emanuel, 1991, 1999; Bryan et al., 2010).

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An open question remains as to whether there are other important differences between 3-D tropical cyclones and their purely AX counterparts. An indication, by analogy, of a deficiency in a symmetric depiction of convection, itself, is the excessive convective entrainment rate in a two-dimensional planetary boundary layer with vertical shear relative to a 3-D model (Moeng et al., 2004). These findings suggest a hypothesis that axisymmetric convection occurring in concentric sheets is overly efficient in generating buoyancy fluxes compared to 3-D convection in isolated plumes, leading in the hurricane context to excessive condensation heating and an overly rapid spin up; we will see that this hypothesis is broadly supported by our 3-D and AX comparisons.

Two notable studies attempting to address the foregoing question in the tropical cyclone context are those of Nolan and Grasso (2003) and Nolan et al. (2007) who developed a linear theory of heat forcing on an axisymmetric tropical cyclone-like vortex without a secondary circulation. When a balanced vortex is forced by small-amplitude temperature perturbations with 3-D structure motivated by satellite observations and numerical simulations of tropical cyclones, the results indicate that purely asymmetric heat forcing caused weakening of the vortex circulation. They found also that the evolution of the mean vortex with both symmetric and asymmetric components of diabatic forcing is closely approximated by the symmetric response to the azimuthally-averaged heating rate. The weakening of the symmetric vortex associated with the asymmetric temperature perturbations occurs on account of a “. . . transient growth of the perturbations by downgradient transport of momentum across the radial and vertical shears of the symmetric wind field.” While much of this energy is returned to the mean vortex at long times, there appears to be a net loss of mean energy due to the axisymmetrization and downscale enstrophy cascade as the potential vorticity anomalies of the perturbations undergo spiral wind-up around the mean vortex. These findings are limited to small-amplitude perturbations and also by the choice to consider only the temperature part of the convective elements. Nevertheless, they motivate an examination of the differences in the mean heating rate of the 3-D and AX models within the context

of rotating-convective structures of finite amplitude that possess both temperature and vorticity anomalies.

Another prominent study examining the foregoing question is that of Yang et al. (2007) who used a numerical model configuration that was nearly identical in the 3-D and AX versions. They suggested three effects that contribute to making the mature vortex in the 3-D model roughly 10 % weaker than that in the AX model. The first is that the intensity is controlled principally through a modified entropy imbalance in the sub-cloud layer of the vortex at the radius of maximum tangential wind. The diagnostic model for the entropy imbalance and its connection to the maximum gradient wind is via the energetically-based steady-state potential intensity theory of Emanuel (1995) without dissipative heating. The second is that the eyewall in the 3-D model is less tilted than that in the AX model, which they argued leads to less evaporation/modification of the inflowing air and a reduced entropy imbalance at the surface in the 3-D model. The third is similar to the simple view of “down-gradient” momentum mixing described above and argues that the eddies lead to a direct spin-down of tangential winds at the RMW.

We have several concerns about Yang et al.’s explanation. First, Emanuel’s potential intensity theory is only a theory for maximum gradient wind (Emanuel, 1986), and recent work has identified a fundamental weakness by not representing the intrinsically unbalanced dynamics of the underlying boundary layer and the resulting implications for the maximum radial and tangential velocity of the vortex (Smith et al., 2008; Bryan and Rotunno, 2009a, b). A second weakness has been pointed out by Emanuel (2012), himself, who noted that the assumption of a constant outflow temperature in the steady-state theory of Emanuel (1986) is poor, requiring a major revision (Emanuel and Rotunno, 2011). Thus the first leg of the Yang et al., model appears to be fundamentally challenged. Second, in our view, the authors do not provide a satisfactory explanation why an eyewall in the 3-D model should be less-tilted than in the equivalent AX model. Finally, the authors gave no apparent attention to the differences in the convective or-

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ganization (convection and vorticity aggregation, upscale cascade of vorticity, etc.) in the two models.

1.4 The present study

In this paper we address the question posed in the title of Sect. 1.3. In particular, we compare selected azimuthally-averaged fields of the 3-D model with the corresponding fields in the AX model, both during intensification and in the mature stage for the prototype intensification problem studied by Nguyen et al. (2008). This problem considers the evolution of a prescribed, initially cloud-free, axisymmetric, baroclinic vortex in a quiescent environment over a warm ocean on an f -plane. Specific fields to be examined include all three velocity components, the heating rate, terms in the tangential momentum equation, a forcing function controlling the balanced spin-up of the bulk vortex, subgrid-scale and resolved Reynolds stresses, and horizontal and vertical eddy diffusivities. Another field examined is a gradient Richardson number, which has been hypothesized recently to be a critical component of tropical cyclone intensification. In addition to presenting these comparisons, we explore and discuss the implications of the results.

The remainder of the paper is structured as follows. Section 2 summarizes the model setup and defines the initial vortex structure, together with the temperature and moisture profiles used for the numerical experiments. Section 3 gives an overview of the simulation results. Section 4 presents an analysis of the balanced spin-up of the bulk vortex (outside of the boundary layer and outflow layer). Section 5 examines the tangential momentum equation for both 3-D and AX systems. Section 6 takes a closer look at the subgrid scale and Reynolds stresses in the two model configurations. Some consequences of the differences in 3-D and AX systems found above are illustrated in Sect. 7 with a specific series of numerical experiments in which the surface drag coefficient is varied. Section 8 presents our conclusions.

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2 The numerical model

The experiments are performed using the numerical model CM1 version 14, a non-hydrostatic and fully compressible cloud model (Bryan and Fritsch, 2002)³. Over the sea, as is the case here, the terrain-following coordinate system simplifies to regular Cartesian coordinates. An attractive feature of this model is that it has options for being executed in AX or 3-D configurations.

In the 3-D configuration there are prediction equations for the three components of the velocity vector \mathbf{u} , water vapour q_v , suspended liquid q_l , perturbation Exner function $\pi' = (p'/p_0)^{R/c_p}$, and perturbation potential temperature θ' , where perturbation quantities are defined relative to a prescribed hydrostatic basic state. Here c_p is the specific heat of dry air at constant pressure p , R is the gas law constant for dry air, and $p_0 = 10^5$ Pa is a reference pressure. For simplicity, ice microphysical processes are neglected. The reference sounding is a nearly moist-neutral sounding generated from the axisymmetric Rotunno–Emanuel (1987) model. Near-neutral (very low CAPE) soundings have served as a prototype in idealized studies since Emanuel (1986) demonstrated that ambient CAPE is unnecessary for tropical cyclone maintenance and since many numerical simulations (e.g. Rotunno and Emanuel, 1987; Montgomery et al., 2009) are able to simulate intensification with very little environmental CAPE. Persing and Montgomery (2005) presented a suite of axisymmetric simulations where approximately the same intensity was found for a wide range of environmental soundings with varying CAPE.

On the numerical side the advection terms are calculated in flux form. The pressure gradient force per unit mass takes the form $F_p = -c_p \theta_\rho \nabla \pi$, where the pertinent density potential temperature θ_ρ is defined as: $\theta_\rho = \theta(1 + q_v/\epsilon)/(1 + q_v + q_l)$, with $\epsilon = R/R_v$,

³For a complete description of the three-dimensional model and variable definitions see the technical document “The governing equations for CM1”, available for download at <http://www.mmm.ucar.edu/people/bryan/cm1> and also available from G. Bryan. For a complete description of the axisymmetric version of CM1, see the paper by Bryan and Rotunno (2009a).

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where R_v is the gas constant for water vapor. The vertical momentum equation includes a buoyancy force per unit mass $B = g(\theta_p - \theta_{p0})/(\theta_{p0})$, where $\theta_{p0}(z)$ is the basic state profile of θ_p , and g is the gravitational acceleration. The tendencies of θ' and π' are calculated using the mass- and energy-conserving equations derived by Bryan and Fritsch (2002). For simplicity, dissipative heating is not included (cf. Bister and Emanuel, 1998) and should not alter any of the conclusions or interpretations herein. The calculations are carried out on an f -plane with the Coriolis parameter $f = 5 \times 10^{-5} \text{ s}^{-1}$, corresponding to 20° N .

Radiative effects are represented by adopting a simple Newtonian cooling approximation capped at 2 K per day, following Rotunno and Emanuel (1987). This approximation serves as a simple expedient to parameterize the radiative-convective equilibrium process, which operates to maintain the ambient tropical sounding over realistic forecast time scales of several days. In choosing this particular setup, we purposely omit (1) the more complex cloud-radiative feedback processes in the infrared wavelengths that have been suggested to accelerate the intensification process (e.g., Hakim, 2011; Nicholls and Montgomery, 2012) and (2) the negative ocean feedback associated with storm-induced upwelling of colder ocean water below the storm that tends to retard the intensification process (e.g., Emanuel et al., 2004). To some extent, these two effects act in opposition and it is reasonable to omit both in our first step in developing a basic fluid dynamical understanding of the differences between 3-D and AX tropical cyclones.

The outer lateral boundaries are open with a radiative boundary condition (Durrant and Klemp, 1983). In order to mitigate the reflection of internal gravity waves from the upper boundary, a Rayleigh damping layer is added at heights above 20 km. The surface temperature is 299.3 K (based on the value used in the study by Rotunno and Emanuel, 1987). A simple rainfall scheme is used in which rain has a fixed fall speed of 7 m s^{-1} .

Subgrid-scale turbulence is represented by choosing the available option (“iturb=3”) in the model, which is designed for problems that do not resolve any part of the turbu-

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lent Kolmogorov inertial range. This option requires the external specification of horizontal and vertical mixing lengths l_h and l_v , which for simplicity are assumed constant in both space and time. The scheme follows Smagorinsky (1963) and Lilly (1962), except that different eddy viscosities must be used for the horizontal and vertical directions.

The flow-dependent momentum diffusivities in the horizontal and vertical directions are specified as follows: $K_{m,h} = l_h^2 S_h$ and $K_{m,v} = l_v^2 S_v \sqrt{1 - \text{Ri}/\text{Pr}}$, where the m subscript refers to momentum, and the second subscript h or v refer to the horizontal and vertical directions, S_h and S_v denote the terms found in the total deformation, S , that involve the horizontal and vertical flow components, $\text{Ri} = N_m^2 / S^2$ is the moist Richardson number, N_m^2 is the moist Brunt–Väisälä frequency, and Pr is the Prandtl number (set to unity in this option). In this scheme, the vertical eddy diffusivity is proportionally reduced in regions with positive moist Richardson number and the heat and momentum diffusivities are taken to be identical, $K_h = K_m$. Whenever Ri exceeds unity, the vertical momentum and vertical heat diffusivities are set to zero.

In our experiments, we adopt a configuration of the 3-D and AX models that share the same corresponding values of horizontal mixing lengths and of vertical mixing lengths. The respective mixing lengths are assumed to apply equally to the parameterized mixing of heat and momentum (e.g., as in Bryan et al., 2010; Bryan, 2012a). The choice of the same horizontal mixing lengths in the two models is contrary to that advocated recently by Bryan (2012a). He suggests that in order to match the observed intensity of category four and five tropical cyclones, one should use an enhanced *horizontal* eddy-diffusivity in the AX model to represent the total effects of diffusion and eddy processes. For the following two reasons we have some concerns with this argument. First, the underlying physical basis for the “blunt tuning” of the horizontal diffusivity in the AX model is unclear to us. Second, we see the need to use the information about the resolved eddy structures from the 3-D model (i.e., radial and vertical structure and magnitude of resolved Reynolds stresses, and their possible relation to the gradients of the mean fields, etc.) to determine if such a tuning procedure is justified. In this study, we choose to compare the resolved fluid dynamics of the AX and 3-D models using the

same formulae for the subgrid-scale processes to ascertain how these systems differ. We see this comparison as a necessary first step to considering how one should revise the AX model to better mimic the dynamics of the 3-D model.

The mixing lengths required in the formulation of the subgrid-scale processes are set to be consistent with recent observations of intense hurricanes at the base of the eyewall region for horizontal wind speeds $\approx 50 \text{ ms}^{-1}$ (Zhang and Montgomery, 2012; Zhang et al., 2011): $l_h = 700 \text{ m}$ and $l_v = 50 \text{ m}$. For reasons given in the foregoing paragraph, the horizontal mixing length in the AX model is taken to be the same as in the 3-D model⁴. For the horizontal grid spacing used herein, at least some of the horizontal mixing noted in observations must be resolvable on the 3-D grid mesh.

The parameters determining the exchange of heat and momentum at the air-sea interface are set as follows. The surface exchange coefficients of heat and momentum are taken to be constant in both space and time. The moist enthalpy transfer coefficient C_k is set equal to 1.29×10^{-3} . This value is close to the mean value (1.2×10^{-3}) derived from the Coupled Boundary Layers/Air-Sea Transfer (CBLAST) experiment (Fig. 6 of Black et al., 2007; Fig. 4 of Zhang et al., 2007), a recent laboratory study (Fig. 1 of Haus et al., 2010) near and slightly above marginal hurricane wind speeds, and an energy and momentum budget analysis of the lower-tropospheric eyewall region at major hurricane wind speeds (Bell et al., 2012). The drag coefficient is set to be twice the enthalpy exchange coefficient $C_D = 2 \times C_k = 2.58 \times 10^{-3}$, and is close to the estimated

⁴Although the chosen value of $l_v = 50 \text{ m}$ is somewhat below the average mixing length reported by Zhang et al. (2011), it is well within the range of scatter in the observational data. The value of $l_v = 50 \text{ m}$ was chosen also by Bryan (2012a) to give more “realistic”-looking hurricane winds and, in particular, more realistic inflow angles in the boundary layer of his simulated hurricanes in comparison to the observations of Powell et al. (2009). This value of the vertical mixing length (and corresponding vertical eddy momentum diffusivity of approximately $50 \text{ m}^2 \text{ s}^{-1}$ in the boundary layer region, see Sect. 6 for more) is consistent with recent results reported by Zhang and Drennan (2012) using flux-profile data in the rainband regions of Hurricanes Fabian (2003), Isabel (2003), Frances (2004), and Jeanne (2004).

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mean value of $C_D = 2.4 \times 10^{-3}$ from CBLAST-derived observations for major hurricane wind speeds by (Bell et al., 2012).

The same initial vortex is used for all simulations. The initial radial and vertical velocity are set to zero. The initial tangential velocity is taken to be in gradient wind balance with a maximum of 13 ms^{-1} at the surface and occurs at a 100 km radius from the centre of circulation. The tangential velocity varies smoothly in space and tends to zero at large radii: it is effectively zero beyond 400 km radius and above $z = 20 \text{ km}$. The 3-D experiments are conducted with a 3 km horizontal grid spacing on an interior domain. Further details of the domain sizes and grid stretching are given in the Appendix.

There are two principal numerical simulations: (1) a three-dimensional simulation at 3 km horizontal grid spacing on the interior grid mesh (hereafter called “3D3k”) and (2) a corresponding axisymmetric simulation at 3 km radial grid spacing (hereafter called “AX3k”). Other sensitivity experiments are detailed in Sects. 3 and 7.

Before presenting specific solutions using a particular model configuration, it should be recalled from the Introduction that tropical cyclone intensification is a turbulent process in which deep convection is a prominent stochastic feature. As a result, one should think of a particular simulation as being just one realization of an ensemble of simulations in which the convection is perturbed. One way that the convection can be perturbed is by adding a stochastic component to the initial moisture in the boundary layer, the amplitude of which is comparable with the errors in observing moisture with current observational platforms (Nguyen et al., 2008; Shin and Smith, 2008). A simpler approach is used here to create a second simulation that is identical to the AX3k simulation, except for the inclusion of a $20 \mu\text{g kg}^{-1}$ increase in the initial basic state moisture profile over the lowest levels of the simulation. This simulation is denoted as “AX3k*”.

Another way that the stochastic nature of convection may materialize is by running the model on a different computational platform. In this case the stochastic nature of truncation error leads to a random component of the convection in comparison with that from the original platform. This sensitivity became apparent when our 3-D calculations were performed on a newer computer, but using the same Fortran code. We

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have taken the newer 3-D experiments to be our principal experiments, but for comparison purposes we have retained one of our older 3-D experiments and denoted this experiment subsequently as “3D3k*”⁵.

3 Overview of simulated development in the AX and 3-D models

3.1 Vortex evolution

Figure 1 shows a time series of the maximum tangential velocity (V_{\max}) and corresponding radius of maximum tangential wind (RMW) simulated in the AX and 3-D model simulations AX3k, AX3k*, 3D3k and 3D3k* out to 288 h (12 d). In the 3-D configuration, the maximum velocity plotted is that of the azimuthally-averaged tangential velocity anywhere in the domain and the RMW corresponds to the radius of this wind maximum. During both spin-up and maturity the velocity maximum in both 3-D and AX configurations occurs in the height range between 500 m to 750 m, which is within, but near the top of, the frictional boundary layer of the vortex as defined by the layer of strong radial inflow (Smith and Montgomery, 2010; Zhang et al., 2011). Comparing the two AX runs (with identical initializations save for a very small moisture perturbation as described above) the differences are relatively small (only occasionally more than 5 ms^{-1}) after accounting for a small time offset during rapid intensification. A quasi-steady maximum intensity is maintained between 130 h and 190 h (for approximately 60 h) until a slow weakening is evident in both AX runs. Comparing the two 3-D runs (with identical initializations, but carried out on different computer platforms), the differences in V_{\max} are comparatively small during the first 90 h of integration, which encompasses the first intensification period. After 90 h, there are differences in V_{\max} of up to about 10 ms^{-1} ,

⁵Computational expense and the limited availability of the alternate computation platform dictated the differing treatments, 3-D versus AX. The point of both is that miniscule initial differences result in distinct realizations 3-D within an envelope of permissible solutions.

and these differences are typically coherent over longer time periods than in the AX configuration.

We focus attention now on the differences between the AX3k and the 3D3k simulations⁶. For subsequent analyses and interpretation, we will define the intensification period as a time interval spanning the most rapid rate of increase of the maximum tangential velocity. In experiment AX3k, we take this time interval to be the period between 75 h and 85 h, and in experiment 3D3k, the period between 60 h and 70 h. Since the intensification process in the 3-D experiments spans a comparatively longer time interval, we will consider also a second rapid intensification period in the 3D3k run between 151 and 155 h.

While there is a degree of arbitrariness in defining when the vortex has reached a mature intensity, in forthcoming analyses we focus on a less ambiguous metric, namely, a one-day interval encompassing the maximum intensity of each simulation.

A peak intensity of 69.7 m s^{-1} is found in the AX3k model at 198 h and of 60.0 m s^{-1} in the 3D3k model. Inspection of Fig. 1 shows that the substantial portion of intensification is complete in the AX3k model around 105 h and in the 3D3k model around 170 h; after which time a fluctuating quasi-steady mature stage is found, for the chosen simulation time interval. Between 200 h and 250 h, the intensity in the AX model declines slowly to approximately the maximum intensity found in the 3-D model and then continues a gradual decline. In the 3-D model, the intensity declines after 250 h. Longer versions of these simulations (not shown) suggest that the weakening trend continues for many days after the end of these simulations. We have not studied the near coincidence in the

⁶Strictly speaking, comparing just two simulations can be problematic because of the intrinsic variability associated with deep convection as discussed in the foregoing subsection. It is for this reason that small differences between the two classes of simulations are not emphasized. The detailed dynamics and thermodynamics governing the fluctuations in tangential wind speed is certainly an interesting topic (cf. Nguyen et al., 2011), but for the present purpose we will focus only on the broad aspects determining the basic differences in intensification and intensity between AX and 3-D simulations.

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intensity in the 3-D and AX simulations starting near 250 h or the continued weakening trend.

The maximum intensity of the 3-D simulations for the 12 d simulation is approximately 15 % weaker than that of the AX configurations. In addition, the AX simulations exhibit their peak intensification rate for a longer period of time than the 3-D simulations, although these rates are roughly the same in the two models. Both of these aspects are broadly consistent with prior findings comparing three-dimensional and axisymmetric tropical cyclone simulations (e.g., Yang et al., 2007; Montgomery et al., 2009; Bryan et al., 2010). At early times in both AX and 3-D configurations, the RMW (Fig. 1b) exhibits modest (in 3D3k) and large (in AX3k) fluctuations with time before a more systematic contraction ensues. In the case of the AX simulations, the RMW fluctuates wildly in the early spin-up period, sometimes by more than 100 km. The rapid increase of V_{\max} with time in the AX3k simulation is coincident with a period in which the RMW contracts inwards from 40 to 20 km. Unlike the AX3k simulation, the first rapid intensification period in the 3D3k simulation occurs towards the end of the contraction of the RMW corresponding to the mean tangential wind. The final contraction phase of the RMW in the 3D3k simulation is coincident with the second rapid intensification period identified above. By 250 h, the RMWs for each simulation approach the same radius of approximately 20 km.

It may be worth pointing out that there is a short period of time (near 66 h) during the early spin-up period when the rate of spin-up is largest in the 3-D model. We will show later that at about this time, the local heating rate exceeds that found in the AX model and there is degree of ring-like organization in the deep convection.

3.2 Evolution of relative vorticity

In the foregoing 3-D simulations, the evolution of relative vorticity and vertical velocity is similar to that described in previous work (Hendricks et al., 2004; Montgomery et al., 2006, 2009; Nguyen et al., 2008; Shin and Smith, 2008; Gopalakrishnan et al., 2011; Nguyen et al., 2011). Specifically, there is a brief gestation period in which the

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boundary layer is moistened by sea-to-air moisture fluxes and during which the vortex intensity weakens by frictional spin-down until some air parcels are lifted to their level of free convection. The ensuing deep convection leads to the vertical stretching of local vortex tubes. The presence of a cyclonically-rotating background vortex would suggest a tendency for cyclonic vorticity to amplify more rapidly than any anticyclonic vorticity. The cyclonic vorticity so generated tends to aggregate by both vortex mergers and system-scale convergence driven by the collective buoyancy of deep convective clouds⁷. Figures 2 and 3 summarize the evolution in relative vorticity structure at a height of 1 km in the 3-D simulation and compare it with that in the AX simulation during the intensification phase, a level near the top of the strong inflow layer associated with surface friction. The depictions of Fig. 2 span time periods that contain intervals of peak intensification in each simulation.

The tangential velocities for the 3D3k simulation (left column) and AX3k simulation (right column) are roughly comparable (within 10 ms^{-1} of each other) at the corresponding stages of evolution.

During the first intensification period, the vorticity in the 3-D simulation is an amorphous mass of cyclonic values in the interior, punctuated by several regions of localized intense cyclonic vorticity (Fig. 2a). On the edge of this mass are curved banded features which tend at later times to spiral cyclonically inwards. This cyclonic vorticity region is immersed in a sea of weak cyclonic/anticyclonic vorticity. During the second intensification period (middle column), a contraction of a ring of vorticity associated with the eyewall is evident, with asymmetries still present in the vorticity ring corresponding

⁷The present overview neglects the contribution to the material rate of change of vertical vorticity due to vortex-tube tilting, solenoidal generation and sub-grid scale diffusion. As discussed elsewhere (e.g., Montgomery et al. (2006 and references therein), one of the more significant of these is the vortex-tube tilting term, which generally contributes small-scale vortex dipole structures on the horizontal scale of the updraughts/downdraughts. The tilting effect must be accounted for in a complete explanation of the material change of vorticity and can alter the simple picture sketched here.

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with localized enhancements in the eyewall and in the vorticity bands extending out from the eyewall. In the AX simulation (Fig. 2b), the evolution of the relative vertical vorticity is strikingly different with the vorticity pattern consisting of annular bands of alternating positive and negative values. As in the 3-D simulation, the magnitude of maximum positive relative vorticity in the central disk greatly exceeds the magnitude of the negative vorticity in neighboring rings. The pattern of vorticity rings reflects that of the vertical velocity associated with deep convection in the AX model.

Figure 3 shows a radius-time plot of the relative vorticity at a height of 1 km for both the 3D3k and AX3k simulations, the vorticity being azimuthally averaged in the 3-D case. In broad terms, both plots exhibit a consolidation of cyclonic vorticity with time, with an elevated maximum near the RMW, whose values are greater there than near the centre of the vortex. The consolidated vortices exhibit a ring-like radial distribution of vertical vorticity as opposed to a monopolar distribution with radius.

The azimuthal-mean vorticity in the 3-D simulation exhibits considerably less spatio-temporal variability than the corresponding AX simulation. This difference can be explained in part by the fact that the convective elements and the vorticity that they generate are averaged azimuthally in the 3-D simulation, whereas the convection and vorticity in the AX model is unfiltered. Another difference between the two simulations is that radial and vertical gradients of the system-scale angular rotation provide a hostile environment for deep convection in the 3-D model, with a corresponding tendency to strain the convective elements in the tangential direction. This process tends to damp the small-scale fluctuations over the larger-scale motions (Melander et al., 1987; Carr and Williams, 1989; Sutyrin, 1990; Smith and Montgomery, 1995; Rozoff et al., 2006). In contrast, convection in the AX model is not damped by such a process and consequently retains a high degree of noisiness with time. Indeed, there is considerable noise in the vorticity field during the intensification process, which appears to be a consequence of the unrealistic “ring-like” nature of the convection that produces the vorticity.

3.3 Comparison of surface enthalpy fluxes

A widely accepted paradigm for tropical cyclone intensification and mature intensity focuses on the role of the ocean energy source via sea-to-air enthalpy fluxes (Emanuel, 2003). Indeed, in their comparison between axisymmetric and three-dimensional simulations, Yang et al. (2007) attributed the differences in the mature intensity to the differences in the air-sea disequilibrium and the corresponding total heat flux. For this reason we show in Fig. 4 the radial profile of the azimuthally-averaged moist enthalpy flux during the rapid intensification stage and during the mature stage. At each time the radial profile of surface enthalpy flux is maximized near the RMW and increases roughly with the tangential wind speed. The selected times shown for rapid intensification have a similar intensity in both the 3D3k and AX3k experiments, but at peak intensity the azimuthally-averaged enthalpy flux for the AX3k experiment is a little stronger. However, unlike Yang et al., we do not attribute much physical significance to this result because the commonly assumed connection between surface fluxes and intensification is tenuous and involves a number of assumptions that are difficult to substantiate (Montgomery et al., 2009). In view of these issues, we believe that a perspective based on both dynamics and thermodynamics is called for. This need provides the motivation for the next section.

3.4 Comparison of convective heating rates

One measure for comparing the 3-D and AX simulations is the heating rate associated with deep convection, which is roughly proportional to the vertical velocity (e.g., Holton, 2004). For reasons given later in Sect. 5, the vertical structure and magnitude of the heating rate, as well as its horizontal distribution in relation to the vorticity field of the mean vortex, are pertinent quantities in forcing the spin-up of the bulk vortex. Figure 5 shows radius-height contour plots of the heating rate in the AX3k simulation and the corresponding azimuthally-averaged heating rate in the 3D3k simulation. Shown also is a horizontal cross section of the heating rate in this simulation at the height of max-

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imum heating rate ($z \approx 7$ km). As in the foregoing subsection, these heating rates are shown at times of peak intensification and peak intensity, respectively, in each simulation. For simplicity, we restrict the quantitative comparison of the convective heating rates between the two configurations to the first intensification interval in the 3D3k experiment. (Similar results are found during the second intensification interval.) Again, the intensities as measured by the maximum azimuthally-averaged tangential velocity are not identical at these comparison times, although they are roughly comparable (within 10 m s^{-1}) with one another in the 3-D and AX simulations.

It is evident from Fig. 5 that the AX simulation has a larger maximum heating rate than the maximum azimuthally-averaged heating rate in the 3-D simulation. Peak heating rates occur in the eyewall, typically at a height of around 7 km. The peak heating rate in the AX simulation is two to three times as large as the azimuthally-averaged heating rate in the corresponding 3-D simulation (see Fig. 5a and b) both during intensification and the mature stage⁸.

During intensification in the 3-D simulation, the pattern of convective heating comprises several strong cells loosely organized in bands outside the radius of maximum azimuthally-averaged heating rate, and a ring-like organization in the deep convection indicating a developing eyewall updraught (Fig. 5c). Isolated centres in the 3-D simulation exceed the heating rate found in the AX simulation. The fact that only the peak heating rates are comparable to those in the AX simulation explains why the azimuthally-averaged heating rates are markedly less than those in the AX simulation. In the mature stage, the heating field in the 3-D simulation is dominated by both an

⁸A factor of two difference between the maximum heating rate in the AX and 3-D models was noted also for the mature stage by Yang et al. (2007), their Fig. 4a and b and p1172, "... The maximum heating rate in the eyewall in SYM (the AX model) is almost twice as twice large as that in CTL (the 3-D model) ..." However, the interpretation offered therein focused on the effects of downdrafts and the enhanced air-sea disequilibrium in the AX simulation that was suggested to render the AX simulation more intense than the 3-D model. For reasons already noted, the commonly assumed connection between surface fluxes and system-scale intensification is tenuous and involves a number of assumptions that are difficult to substantiate.

approximately circular inner edge and banded structures, but isolated strong centres of heating are still present (Fig. 5f).

To assess the generality of the above results at different times during the vortex evolution, several time series involving the heating rate are plotted in Fig. 6. The green curve is the maximum heating rate obtained from the AX3k experiment, output every hour. The red curve is the azimuthally-averaged maximum heating rate from the 3D3k simulation, output every hour. The purple curve is the corresponding local maximum heating rate in the 3D3k simulation. The heating rate in the AX simulation is comparatively strong at early times ($> 100 \text{ Kh}^{-1}$) before settling down once the peak intensity has been achieved. In the 3-D simulation, the averaged heating rate gradually increases with the intensity. Of course, the local maximum value of the heating rate in the 3-D simulation greatly exceeds the maximum of the corresponding mean heating rate, but the local maximum exceeds also the maximum value in the AX model. The extreme heating rates in the 3-D simulation are associated with highly localized convective cells whose areas occupy only a small fraction of the annular ring of strong heating (Fig. 5).

One might inquire now whether the differences in the heating rates between the two models suggest a relationship between the maximum mean heating rate and the instantaneous intensity of the simulated storms. Given that the heating rate is an approximate measure of the convective mass flux, one might naively suppose that the strength of the system-scale overturning circulation is related to the heating rate. A larger heating rate would thus imply a stronger overturning circulation and a greater likelihood for a stronger swirling circulation via the conventional spin-up mechanism as discussed in the Introduction. For example, one might ask whether the temporary maximum in the mean heating rate at 80 h in the 3D3k simulation (Fig. 6) is associated with a period of enhanced mean tangential wind speed (Fig. 1)? To explore this question we show in Fig. 7 a scatter plot of the maximum mean heating rate against the instantaneous vortex intensity (Fig. 7). We see that although there is some scatter, the mean heating rate data comprise a cluster that suggest a monotonic, but non-linear relationship

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between mean heating rate and intensity. Although the AX simulation exhibits more scatter in this plot (especially early in the intensification period, when the mean intensity is low), the AX simulation follows a similar non-linear relationship. However, for the same intensity, the AX simulation has a larger maximum heating rate than the 3-D simulation. Of course, the foregoing ideas are overly simplistic because one may expect a time delay between an increase in the strength of the secondary circulation and the increase of the maximum tangential winds. This concern motivates a shift in focus to an examination of the link between the *heating rate*, its spatial distribution, and the *rate of spin-up*.

As noted earlier, it is near the 66 h time (within the early spin-up period) when the rate of spin-up of the mean tangential wind in the 3-D model exceeds the maximum spin-up rate of the AX model (cf. Fig. 1a, compare red and green curves). In Sect. 6 a plausible explanation will be offered to explain how the intensification rate in the 3-D model can locally surpass the maximum intensification rate in the AX model despite the smaller azimuthally-averaged heating rates and updraughts in the 3-D model.

At this point, the question arises whether the foregoing differences in evolution between the 3-D and AX systems are principally due to an intrinsic difference in the system-scale heating rates and spatial gradients thereof or because of the previously postulated idea by Bryan et al. (2010 and references therein) that the “eddies” mix momentum, buoyancy and equivalent potential temperature down the local gradient of the corresponding mean scalar field? The above results hint that the effects of “eddies” in real tropical cyclones may be subtle, but important. They hint also that the azimuthally-averaged and local heating rates may be at least as important in a complete explanation of the essential differences between the two systems. As a step towards examining the link between the heating rate gradient and evolution of the system-scale vortex, the next section considers axisymmetric balance aspects of spin-up in both systems.

4 Insights from axisymmetric balance theory

Recall that the conventional spin-up mechanism for the system-scale circulation discussed in the Introduction can be captured approximately by axisymmetric balance dynamics in association with the radial gradient of the aggregate latent heating rate of deep convection and the mean inflow above the boundary layer. In particular, the balance framework captures the connection between the heating rate and the spin-up of the mass field of the bulk vortex. However, the balance assumption is poor in the boundary layer and the balance theory does not capture the boundary layer spin-up mechanism discussed in the Introduction. This deficiency has ramifications for the entire vortex because the radial distribution of absolute angular momentum that develops in the boundary layer is communicated to the vortex aloft by vertical advection. Since the tangential wind tends to be supergradient in the inner-core boundary layer, air that ascends from this region contributes to the spin-up of the bulk vortex as part of an adjustment process to a new balanced state as illustrated later in Sect. 5.2 (Zhang et al., 2001; Smith and Montgomery, 2010). For the remainder of this section we neglect the unbalanced aspects of the boundary layer and consider only the conventional spin-up mechanism.

Previous studies of the conventional spin-up process have tended to use an approach based on the Sawyer-Eliassen equation for the balanced overturning circulation forced by heat and momentum sources (Willoughby, 1979; Bui et al., 2009). Here we follow Shapiro and Montgomery (1993) and Vigh and Schubert (2009) and adopt an alternative approach based on the geopotential tendency equation. The use of the geopotential tendency equation for describing the balanced evolution of a vortex has a number of advantages over the use of the Sawyer-Eliassen equation. To begin with, unlike the Sawyer-Eliassen equation, the derivation is not degenerate for the steady state. A mathematical advantage of using the geopotential tendency equation is that it avoids the need to first invert for the overturning circulation, then advect the tangential wind component by the radial and vertical flow, and finally to link the changes

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centre, t denotes time and the azimuthal mean of some quantity Q , denoted by the bracket symbol, is defined as:

$$\langle Q \rangle(r, z, t) = \frac{1}{2\pi} \int_0^{2\pi} Q(r, \lambda, z, t) d\lambda \quad (3)$$

A closed evolution equation for the perturbation geopotential ϕ' may be obtained from Equation (3.10) of Shapiro and Montgomery (1993) after simplification to the limit of azimuthal wavenumber zero (i.e., axisymmetric dynamics):

$$\begin{aligned} & \frac{\partial}{\partial t} \left\{ \frac{1}{r} \frac{\partial}{\partial r} \left[\frac{r N^2}{\langle q \rangle \langle \xi \rangle} \frac{\partial \phi'}{\partial r} \right] + \frac{\partial}{\partial z} \left[\frac{\langle \eta \rangle}{\langle q \rangle} \frac{\partial \phi'}{\partial z} \right] \right. \\ & \left. - \frac{1}{r} \frac{\partial}{\partial r} \left[\frac{r}{\langle q \rangle} \frac{\partial \langle v \rangle}{\partial z} \frac{\partial \phi'}{\partial z} \right] - \frac{1}{r} \frac{\partial}{\partial z} \left[\frac{r}{\langle q \rangle} \frac{\partial \langle v \rangle}{\partial z} \frac{\partial \phi'}{\partial r} \right] \right\} \\ & = \frac{\partial}{\partial z} \left(\frac{\langle \eta \rangle}{\langle q \rangle} Q \right) - \frac{1}{r} \frac{\partial}{\partial r} \left(\frac{r}{\langle q \rangle} \frac{\partial \langle v \rangle}{\partial z} Q \right) \end{aligned} \quad (4)$$

where the coefficient variables in the differential operator are defined as follows: $N^2 = (g/\theta_0)\partial(\theta)/\partial z$ is the static stability of the mean vortex and environment, $\langle \eta \rangle = f + 1/r\partial(rv)/\partial r$ is the absolute vertical vorticity of the mean vortex, $\langle \xi \rangle = f + 2\langle v \rangle/r$ is twice the absolute angular velocity, $Q = (g/\theta_0)D\langle \theta \rangle/Dt$ is the normalized azimuthally-averaged diabatic heating rate, D/Dt is the substantial derivative following the azimuthal mean circulation in (r, z) coordinates,

$$\langle q \rangle = \langle \eta \rangle N^2 - \langle \xi \rangle \left(\frac{\partial \langle v \rangle}{\partial z} \right)^2 \quad (5)$$

is the potential vorticity (PV) of the azimuthal mean vortex in the Boussinesq approximation and t is the time. Here the variable ϕ' denotes the incremental change in the

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azimuthal mean geopotential forced by latent heating associated with the aggregate of deep convection over a small time interval. After some rearrangement, the right-hand-side forcing term can be re-written as follows:

$$\mathcal{L} \left(\frac{\partial \phi}{\partial t} \right) = \eta \cdot \nabla \left(\frac{Q}{\langle q \rangle} \right) \equiv S \quad (6)$$

where \mathcal{L} is the $r - z$ differential operator acting on the geopotential tendency of the foregoing equation and η denotes the azimuthally-averaged absolute vorticity vector.

As shown by Shapiro and Montgomery (1993; their Eq. 4.10), the geopotential tendency equation is a compact form of the balanced perturbation potential vorticity equation in which the radial and vertical advection of the basic state PV is implicit. Apart from the Boussinesq approximation in pseudo-height coordinates, this geopotential tendency equation is essentially the same as that derived by Vigh and Schubert (2009; their Eqs. 2.20 and 2.21). Vigh and Schubert (2009) refer to the right-hand-side of the geopotential tendency equation as the “cyclogenesis function.” Since observations show clearly that tropical cyclogenesis is not an axisymmetric process (e.g., Dunkerton et al., 2009; Montgomery et al., 2012), we believe a more appropriate term for this quantity is the “spin-up function” (S). For the remainder of this paper we will adhere to this latter terminology.

4.2 Deductions from the spin-up function

In the absence of frictional effects (focusing the discussion here on the conventional spin-up mechanism), it is clear that there will be no new generation of PV in the interior of the vortex by condensation heating (and hence no change to the mass field of the bulk vortex) unless the gradient of the mean heating rate divided by the mean PV projects non-trivially onto the absolute vorticity vector in the radius-height plane. Taking the ocean surface and tropopause to be approximately isothermal boundaries, the boundary conditions on the top and bottom of the vortex require a vanishing vertical

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derivative of the geopotential tendency, i.e., $\partial\phi_t/\partial z = 0$, where ϕ_t denotes short hand for the time tendency of the mean geopotential perturbation as defined above, $\partial\phi'/\partial t$.

Symmetry at the axis of rotation implies that $\partial\phi_t/\partial r = 0$ at $r = 0$. Boundedness of the solution requires that $\phi_t \rightarrow 0$ at large r . If the discriminant of the mean vortex is everywhere positive (i.e., $\langle\xi\rangle\langle q\rangle > 0$), and if the spin-up function vanishes throughout the domain, we conclude from the geopotential tendency equation, with the aid of the boundary conditions discussed above, that $\phi_t = 0$ everywhere and the flow is in a steady state. This is the “non-acceleration theorem” for inviscid, axisymmetric balance vortex dynamics (cf. McWilliams et al., 2003).

If, for the sake of argument, during the early stage of intensification, the mean vortex is approximately barotropic, the largest term in the spin-up function $S = \eta \cdot \nabla (\langle Q\rangle/\langle q\rangle)$ results from the vertical gradient of $\langle Q\rangle$. In this situation, assuming that deep convection has a simple heating profile with a maximum in the middle troposphere (à la Gill, 1982), the magnitude of the mean heating rate (and its location with respect to the maximum mean vertical vorticity) controls principally the intensification rate (see Vigh and Schubert (2009)’s Eqn. (2.25) and accompanying discussion). However, as the hurricane reaches maturity and the baroclinicity of the mean vortex becomes significant, the mean vorticity vector $(-\langle\partial\langle v\rangle/\partial z\rangle, 0, f + \langle\xi\rangle)$ rotates clockwise in the $r - z$ plane and becomes locally perpendicular to the vector gradient of $(\langle Q\rangle/\langle q\rangle)$. The result is that the spin-up function approaches zero and the balanced flow tends towards a steady state⁹.

⁹The vanishing of the spin-up function provides a constraint on the secondary circulation in terms of the primary circulation and the diabatic heating (and, in general, other forcing terms). Although the requirement of continuity imposes a further constraint, this together with the vanishing of the spin-up function does not provide a means to determine the steady-state primary circulation and mass field. Indeed, it is unclear whether a global steady-state solution exists (Smith et al., 2012; Sect. 5.2). In the absence of friction and/or eddy fluxes of tangential momentum and moist entropy, the steady tangential momentum and moist-entropy equations imply that the azimuthally-averaged secondary circulation above the boundary layer must be along

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In general, the intensification rate in the axisymmetric balance model is controlled by the structure of the spin-up function and its radial distribution relative to the vorticity distribution (Vigh and Schubert, 2009). On the basis of the foregoing discussion, in lieu of a full inversion of the geopotential tendency equation (as employed for the Sawyer-Eliassen equation by Bui et al., 2009 or using coarse resolution data with a cumulus parameterization derived from the Geophysical Fluid Dynamics Laboratory Hurricane model by Möller and Shapiro, 2002), we will use a bulk measure of the spin-up function in order to assess the balanced contribution of the mean heating rate to the change in the mass field in the 3-D and AX simulations.

In preparation for the analysis foreshadowed above, we show in Fig. 8 radius-height cross sections of selected azimuthally-averaged quantities averaged between 65 and 69 h during the rapid intensification of the 3D3k simulation. These quantities include: the axisymmetric mean gradient wind ($\langle v_g \rangle$), panel (a) defined by

$$\langle v_g \rangle = -\frac{fr}{2} \left(1 - \sqrt{1 + \frac{4}{\langle \rho \rangle f^2 r} \frac{\partial \langle \rho \rangle}{\partial r}} \right); \quad (7)$$

both absolute angular momentum surfaces and moist isentropic surfaces. In other words, these two sets of surfaces must be congruent. Moreover, in the subsiding branch of the overturning circulation, the absolute angular momentum surfaces must have a negative radial gradient, implying that the flow there is inertially unstable and therefore no longer steady and invertible. Notwithstanding this local region of instability, the tangential flow at large radius in the outflow must become anticyclonic. Since cyclonic angular momentum is continuously removed at the surface by friction, a global steady state would require that the angular momentum of the vortex be replenished at the same rate. If sufficient angular momentum is not replenished at the lateral boundary by some means, the upper anticyclone must extend to the surface where cyclonic angular momentum would be diffused into the system. While it might be argued that some replenishment could occur as a result of horizontal eddy fluxes at the lateral boundary, it would be fortuitous if these fluxes were just sufficient to maintain a global steady state.

axisymmetric mean potential vorticity (panel (b)),

$$\langle q_g \rangle = \langle \eta \rangle N^2 - \langle \xi \rangle \left(\frac{\partial \langle v_g \rangle}{\partial z} \right)^2, \quad (8)$$

where $\langle \rho \rangle$ and $\langle p \rangle$ are the axisymmetric mean air density and pressure, respectively, and the subscript “g” denotes evaluation using the axisymmetric mean gradient wind; axisymmetric mean diabatic heating rate ($\langle \dot{\theta} \rangle$) divided by the mean potential vorticity ($\langle q_g \rangle$) (panel (c)); the radial and vertical derivative thereof (panels (d) and (e), respectively); and finally, the spin-up function $S = \zeta \cdot \nabla (\langle Q \rangle / \langle q_g \rangle)$ (panel (f)).

An examination of panels (d) and (e) shows that the spin up function is dominated by the radial derivative term (panel (d)). The radius of maximum gradient wind is slightly larger than the time mean of $\langle v \rangle$ between 65 and 69 h and the maximum of $\langle v_g \rangle$ is a little smaller than that of $\langle v \rangle$ (26 m s⁻¹ compared with 29 m s⁻¹).

The $\langle q_g \rangle$ -field (panel (b) of Fig. 8) shows a weak ring-like structure with a maximum at a finite radius just inside the RMW, the strength decreasing rapidly with radius outside the eyewall. The mean diabatic heating rate at this time (see Fig. 5b), shows two column-like structures, the innermost and strongest marking the developing eyewall. (Note that the radial domain of mean diabatic heating rate $\langle \dot{\theta} \rangle$ shown in Fig. 5 is a little more than half of the domain shown in Fig. 8.) As a result of $\langle q_g \rangle$ becoming small outside the eyewall, the structures of $\langle \dot{\theta} \rangle$ there are accentuated in the $\langle \dot{\theta} \rangle / \langle q_g \rangle$ field (Fig. 8c).

The radial gradient of $\langle \dot{\theta} \rangle / \langle q_g \rangle$ (panel (d)), exhibits strong dipole structures on the periphery of the features in panel (c).

Figure 8f shows the spin-up function, S . Of interest is the coherent region of positive values extending vertically in the main eyewall region in association with the peak eyewall heating rate near 7 km altitude. This region is unlike that found in the rest of the mean vortex, which is dominated by larger-in-amplitude, but smaller-in-scale positive and negative dipole structures. However, as far as axisymmetric balanced spin-

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up of the inner-core tangential winds is concerned, the small-scale positive-negative dipoles in S would tend to be filtered in an inversion of the geopotential tendency equation (Eq. 4) on scales less than the local axisymmetric Rossby radius of deformation $L_R = NH / \sqrt{\langle \eta \rangle \langle \xi \rangle}$ (Shapiro and Montgomery, 1993), where N denotes the static stability, H denotes the vertical scale of a particular dipole feature and $\langle \eta \rangle \langle \xi \rangle$ is the local centrifugal (inertial) stability parameter of the swirling flow. The local Rossby radius is roughly 60 km in the developing eyewall. Since the local Rossby radius of the coarse-grained flow tends to increase with radius outside the eyewall region, we would expect the small-scale positive-negative dipoles in S to make a negligible contribution to the spin-up of the inner-core winds. It is for these reasons that we now focus our attention primarily on the properties of the spin-up function near and interior to the developing eyewall region.

A layer-averaging and volume-averaging of the spin-up function is computed and compared to similar properties of the gradient wind intensification rate. We define the layer average of some axisymmetric quantity $\langle Q(r, z, t) \rangle$ by

$$\bar{Q}(r, t) \equiv \frac{\int_{z_0}^{z_1} \langle Q \rangle \langle \rho \rangle dz}{\int_{z_0}^{z_1} \langle \rho \rangle dz} \quad (9)$$

with bounding heights $z_0 = 1.5$ km, $z_1 = 12$ km and air density ρ . The volume average is defined

$$\hat{Q}(t) \equiv \frac{\int_0^R \int_{z_0}^{z_1} \langle Q \rangle r \langle \rho \rangle dz dr}{\int_0^R \int_{z_0}^{z_1} r \langle \rho \rangle dz dr} \quad (10)$$

where the outer limit of the integrating cylinder $R(t)$ is the radius of maximum \bar{v}_g .

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Figure 9a shows a radius-time plot of layer-averaged spin-up function, \bar{S} , for the simulation 3D3k and Fig. 9b shows time series of the volume-averaged spin-up function, \hat{S} , (dotted) and volume-averaged gradient wind tendency (solid). The layer average used here comprises a height spanning the bulk of the troposphere ($1.5 < z < 12$ km), but purposefully omits the frictional boundary layer, the adjacent transition region ($0 < z < 1.5$ km), and the outflow layer ($z > 12$ km) of the developing storm, where axisymmetric balance dynamics formally breaks down. Before 50 h, the layer-averaged spin-up function displays little coherent structure¹⁰. This is broadly consistent with panel b, which shows little tendency for spin-up of the volume-averaged gradient wind until a little after 50 h. Subsequently, the layer-averaged spin-up function is mostly positive inside the radius of maximum gradient wind. An extended period of intensification from 50 to 80 h corresponds to the first prolonged period of positive spin-up function. A short period of bulk weakening at 90 h corresponds to a pronounced minimum in spin-up function. A second prolonged intensification period shows a period where the spin-up function has large positive values. Within this period, short weakening episodes are commonly found with relatively small values of spin-up function, or alternately the RMW being unfavourably placed in relation to the peak radius of spin-up function. In the mature period (after 180 h) the intensity does not change systematically, yet the spin-up function remains slightly positive. This behaviour is consistent with the general increase of the maximum azimuthally-averaged tangential winds shown in Fig. 1.

Figure 9c and d show the corresponding diagrams for the axisymmetric simulation AX3k. The time series for the RMW shows a non-systematic evolutionary behaviour for the first 80 h of integration with an erratic inward/outward movement evident around 30 h and 70 h, followed by a systematic inward contraction beginning at about 75 h

¹⁰A Gaussian time filter is applied for the data shown and the filter is defined as follows. For a quantity $Q(r, z, t)$ and for time $t_1 \leq t \leq t_2$, the smoothed quantity $Q_s(r, z, t)$ is found over a time scale t_G ($= 5$ h) by $Q_s(r, z, t) = \int_{t_1}^{t_2} Q(r, z, t') G(t, t'; t_G) dt' / \int_{t_1}^{t_2} G(t, t'; t_G) dt'$ where $G(t, t'; t_G) = \exp\left(\frac{-(t-t')^2}{(t_G/2)^2}\right)$.

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until about 120 h. The second interval of RMW contraction and subsequent expansion between 55 h and 70 h suggests some similarity to an eyewall replacement cycle. However, inspection of radius-time diagrams of the vertical motion and radial inflow fields (not shown) demonstrates that this is not the case. The behaviour is rather a reflection of the chaotic nature of the (ring-like) convection which is highly disorganized at early times in the simulation.

The spin-up function in the AX simulation is generally less coherent with time than that found in the 3D3k simulation, showing also large negative as well as positive values near and away from the RMW. The principal spin-up episode (80 to 100 h) does exhibit a persistently positive signature near and just inside the RMW (with the AX spin-up function approximately twice as large as the corresponding spin up function in the 3-D simulation during its first period of rapid spin up (50–80 h)). However, small-scale positive and negative values of the spin-up function extend radially inwards and outwards of the RMW and the most extended period of positive values of spin-up function (190 to 240 h) corresponds to a long, slow weakening period of the AX simulation (cf. Fig. 1). From the perspective of balance dynamics, these findings suggest a qualitative and quantitative difference between the AX and 3-D intensification process.

We turn now to consider more general aspects of spin-up, including the unbalanced aspects thereof. In particular, we determine the quantitative contribution of “mean” and “eddy” processes in the tangential momentum equation for the mean vortex.

5 Tangential momentum equation

This section presents an analysis of the azimuthally-averaged tangential momentum equation, which serves as a first step in understanding the role of “mean” and “eddy” processes in the evolution of the mean vortex in the 3D3k simulation. This analysis will be compared with a similar one for the corresponding AX3k simulation¹¹.

¹¹Although, as discussed in the Introduction, the absolute angular momentum (circulation) equation provides a useful framework for interpreting certain features of vortex evolution, we

In cylindrical-polar coordinates, the tangential momentum equation in the CM1 model has the form

$$\frac{\partial v}{\partial t} = -u \frac{\partial v}{\partial r} - \frac{v}{r} \frac{\partial v}{\partial \lambda} - w \frac{\partial v}{\partial z} - \left(f + \frac{v}{r}\right) u - \frac{c_p \theta_\rho}{r} \frac{\partial \pi}{\partial \lambda} + D_v \quad (11)$$

where (u, v, w) are the velocity components in the cylindrical coordinate system (r, λ, z) and D_v is the subgrid-scale forcing of v (including diffusive tendencies in the interior flow and the boundary layer). In the diagnosis of the 3D3k experiment, the origin of the cylindrical coordinate system is defined as the minimum of the time-averaged surface pressure. The averaging interval for the surface pressure field on the high resolution subdomain is the nominal time ± 3 h.

Applying the azimuthal average operator to the tangential velocity Eq. (11), the equation for the azimuthally-averaged tangential wind tendency is:

$$\begin{aligned} \frac{\partial \langle v \rangle}{\partial t} = & \underbrace{-\langle u \rangle \langle f + \zeta \rangle}_{V_{m\zeta}} - \underbrace{\langle w \rangle \frac{\partial \langle v \rangle}{\partial z}}_{V_{mv}} - \underbrace{\langle u' \zeta' \rangle}_{V_{e\zeta}} - \underbrace{\left\langle w' \frac{\partial v'}{\partial z} \right\rangle}_{V_{ev}} \\ & - \underbrace{c_p \left\langle \frac{\theta'_\rho}{r} \frac{\partial \pi'}{\partial \lambda} \right\rangle}_{V_{ppg}} + \underbrace{\langle D_v \rangle}_{V_d}. \end{aligned} \quad (12)$$

Here and elsewhere, the prime denotes a departure from the azimuthal mean (or “eddy”). The vertical component of relative vorticity is denoted by ζ . The terms on the

prefer to use the tangential momentum equation here because the model is formulated to solve Newton’s second law of motion and horizontal and vertical momentum are the diffused quantities on the subgrid scale. While the two equations are physically equivalent, the tangential momentum equation has advantages when discussing subgrid scale processes. For example, down-gradient transfer of tangential momentum is not necessarily equivalent to the down-gradient diffusion of absolute angular momentum.

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right hand side are, respectively, the mean radial influx of mean absolute vertical vorticity ($V_{m\zeta}$), the mean vertical advection of mean tangential momentum (V_{mv}), the eddy radial vorticity flux ($V_{e\zeta}$), the vertical advection of eddy tangential momentum (V_{ev}), the azimuthal perturbation pressure gradient per unit mass (V_{ppg}), and the combined diffusive and planetary boundary layer tendency (V_d). This methodology represents the traditional Eulerian approach to “eddy-mean” partitioning in the tangential wind equation (e.g., Hendricks et al., 2004; Montgomery et al., 2006; Yang et al., 2007). Although we do not depart from this approach here, it should be pointed out that, in principle, highly localized asymmetric features can project upon what are termed here as “mean” terms. For example, if we suppose an otherwise axisymmetric vortex with an imposed, single, large-amplitude, positive anomaly in vertical motion, this anomaly will project onto both the vertical eddy and mean terms.

To quantify the effect of the subgrid-scale processes on the vortex development, it proves convenient to separate the subgrid-scale diffusive tendency of the tangential wind component into radial (V_{dr}) and vertical (V_{dz}) contributions to the divergence of the subgrid-scale momentum fluxes

$$\langle D_v \rangle = \underbrace{\frac{1}{r^2} \frac{\partial \langle r^2 \tau_{r\lambda} \rangle}{\partial r}}_{V_{dr}} + \underbrace{\frac{1}{\rho_0} \frac{\partial \langle \rho_0 \tau_{\lambda z} \rangle}{\partial z}}_{V_{dz}} \quad (13)$$

where the subgrid-scale momentum fluxes are related to the mean strain-rate tensor in cylindrical coordinates by

$$\langle \tau_{r\lambda} \rangle = \left\langle K_{m,h} \left(\frac{1}{r} \frac{\partial u}{\partial \lambda} + r \frac{\partial v/r}{\partial r} \right) \right\rangle \quad (14)$$

$$\langle \tau_{\lambda z} \rangle = \left\langle K_{m,v} \left(\frac{1}{r} \frac{\partial w}{\partial \lambda} + \frac{\partial v}{\partial z} \right) \right\rangle \quad (15)$$

and $\rho_0(z)$ is the basic state density profile.

To achieve an accurate representation of the subgrid scale diffusion in the tangential momentum budget of the 3-D model, we found it necessary first to calculate the subgrid scale diffusion of horizontal momentum on the stretched Cartesian grid and then transform to cylindrical coordinates. In brief, the diffusive tendency of horizontal momentum per unit mass F is derived from two vectors, the effect of horizontal diffusion on the horizontal wind $F_h = F_{x,h}\hat{x} + F_{y,h}\hat{y}$ and the effect of vertical diffusion on the horizontal wind $F_v = F_{x,v}\hat{x} + F_{y,v}\hat{y}$, where the coefficient functions are the projections onto the horizontal Cartesian coordinate unit vector directions, \hat{x} and \hat{y} , respectively. Outside of the lowest model level, the stress tensor τ is computed using the model output diffusivities $K_{m,h}$ and $K_{m,v}$ and the proper spatial derivatives of the Cartesian velocity field $\mathbf{u} = u_x\hat{x} + u_y\hat{y} + w\hat{z}$ (where \hat{z} is the vertical Cartesian coordinate unit vector). At the lowest model grid level ($z = 25$ m), the shear stresses are computed using the model's bulk-aerodynamic formula: $\tau_{xz} = \rho_0 C_D u_x c$ and $\tau_{yz} = \rho_0 C_D u_y c$, with the near-surface wind speed denoted by $c = \sqrt{u_x^2 + u_y^2}$. The x and y components of the diffusive tendency are obtained from $F_{x,h} = \rho_0^{-1} \left(\frac{\partial \tau_{xx}}{\partial x} + \frac{\partial \tau_{xy}}{\partial y} \right)$, $F_{y,h} = \rho_0^{-1} \left(\frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \tau_{yy}}{\partial y} \right)$, $F_{x,v} = \rho_0^{-1} \frac{\partial \tau_{xz}}{\partial z}$, and $F_{y,v} = \rho_0^{-1} \frac{\partial \tau_{yz}}{\partial z}$. The desired diffusive tendency D_v for the tangential velocity v is then $D_v = \mathbf{F} \cdot \hat{\lambda} = F_y \cos \lambda - F_x \sin \lambda$, where $\hat{\lambda}$ is the azimuthal unit vector.

5.1 The 3D3k simulation

Figure 10 shows, *inter alia*, time averages of the three velocity components and all but one term in the azimuthally-averaged tangential momentum equation during the period of rapid intensification (between 65 and 69 h). The term not shown is the azimuthal average of the azimuthal perturbation pressure gradient force per unit mass (term V_{ppg} in Eq. 3), which is much smaller than the other terms because the azimuthal variation in virtual potential temperature is small. The main features of the azimuthal-mean vortex during this period are as follows. The radial velocity field is dominated by a shallow

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layer of strong inflow below 1 km associated with the frictional boundary layer, a deeper layer of outflow in the upper troposphere and weak inflow through the mid-troposphere outside the eyewall. The maximum tangential wind component is found at low-levels, near the top of the strong inflow layer. The dominant feature of the vertical velocity component is an annular region of strong upward motion with the principal maximum in the upper troposphere at $z = 10$ km, extending downward to a slight extremum at the top of boundary layer. As indicated in Fig. 5, the updraught at this time encircles much, but not all of the circulation centre. The secondary maximum of the vertical velocity near the top of the boundary layer at this time, during the second intensification period (not shown), and during the mature period (shown below) is associated with the inertial turning of the boundary layer inflow into the updraught (Smith et al., 2008, 2009). There is a small region of weak subsidence inside the main updraught annulus near the axis in the upper troposphere, an indication of a developing eye region. All of these features are similar to ones found in Zhang et al. (2001) for the specific “real case” study case of Hurricane Andrew 1992 and Smith et al. (2009) using an idealized model formulation.

We consider next the contributions to the azimuthal-mean tangential wind tendency from the sum of the mean vorticity influx and mean vertical advection shown in Fig. 10d, and the radial and vertical subgrid-scale terms shown in Fig. 10e and f. The main contribution to the spin-up of the maximum tangential wind is associated with the import of mean cyclonic absolute vorticity in the boundary layer and its vertical advection into the eyewall updraught. This result corroborates that of Bui et al. (2009; Fig. 9, panels (a), (c), (g) and (e)). The boundary layer import of absolute vorticity is largely opposed by the loss of tangential momentum to the surface by friction (compare panels (d) and (f)). Note that the radial diffusion (panel (e)) shows a positive tendency in the eye region (particularly between $5 < r < 20$ km), implying that the eye is being spun up primarily by the downgradient diffusion of azimuthal-mean angular velocity. This mechanical spin-up of the eye is accompanied by a diffusive spin-down tendency of the maximum tangential winds (Malkus, 1958; Kurihara and Bender, 1982; Emanuel,

1997; Schubert et al., 1999). However, as shown below and in Sect. 6, the spin-up of the eye is more than simply a diffusive process.

Figure 10g shows the sum of the resolved radial eddy vorticity flux and eddy vertical advection tendencies. In the upper troposphere, the eddies contribute to a positive tendency of the mean tangential wind. In the middle troposphere, the positive tendency of the mean tangential wind from the mean terms (mainly vertical advection) is partly compensated by the negative tendency from the combined eddy terms. There is some compensation also between the mean and eddy tendencies in the lower troposphere. Although not shown here, an examination of the individual eddy terms in the lower troposphere just above the boundary layer inflow indicates that the horizontal eddy vorticity influx can be negative at times and positive at other times, while the vertical eddy momentum advection term is generally positive there and exceeds the horizontal contribution. (A summary of two intensification periods for 3D3k and a full time series for the 1–2 km layer above the boundary layer inflow is shown in Sect. 6b.) While the combined mean term tends to be larger than the combined eddy term in the middle and upper troposphere, the eddies contribute almost equally in spinning up the lower troposphere above the boundary layer as the mean terms contribute to spinning down the same layer. The foregoing results may be interpreted physically to mean that there is azimuthal variability of the boundary layer inflow and outflow associated with the rotating deep convection along the eyewall.

Figure 10h shows the azimuthal-mean tangential wind tendency from model output (the left hand side of Eq. (12)), while Fig. 10i shows the corresponding tendency diagnosed from the sum of mean and eddy terms plus the subgrid scale (boundary layer and diffusion) processes (the right hand side of Eq.(12)). The two panels agree reasonably well quantitatively. For the time interval shown in Fig. 10, the maximum tangential winds are found to reside in the eyewall region near the top of the boundary layer, where the radial spin-up mechanism associated with the sum of the vorticity influx and vertical diffusion terms is a maximum. This spin-up is conveyed up the eyewall by the

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combined mean terms, primarily through the vertical advection of tangential momentum.

The foregoing diagnoses suggest that the presence of the eddies, while quantitatively non-negligible and contributing positively to the spin-up of the system-scale swirling wind above the boundary layer, does not fundamentally alter the view that the maximum tangential wind tendency occurs in the boundary layer. The results strongly support the findings of Zhang et al. (2001), Smith et al. (2009), Smith and Thomsen (2010), and Sanger et al. (2013) that the maximum tangential wind occurs within the boundary layer inflow during the spin-up process.

Figure 11 shows radius-height cross sections corresponding to those in Fig. 10 during the quasi-steady stage of the 3D3k simulation (214–222 h). (As a reminder, the quasi-steady characterization is based on the time evolution of V_{\max} and does not imply that the vortex as a whole is close to a steady state.) As foreshadowed above, it is of interest to note the double maximum of the mean tangential wind field. The region between these two maxima coincides with the region of strong outflow just above the low-level inflow maximum. This outflow, in conjunction with the approximate material conservation of absolute angular momentum, leads to a reduction of the tangential wind speed to the extent that the flow becomes subgradient as it ascends into the eye-wall. The imbalance between the radial pressure gradient and the sum of Coriolis and centrifugal forces leads again to a shallow layer of inflow, and thereby to a secondary acceleration of the tangential wind. This “inertial recoil” effect is in essence a standing centrifugal wave, which is damped as the air ascends and the tangential wind and radial pressure gradient come into balance above the boundary layer. The pattern of inflow and outflow is similar to that during the first intensification period, but the boundary layer inflow and upper-tropospheric outflow have approximately doubled in strength and the deep inflow above the boundary layer has collapsed and has been replaced by weak outflow below 6 km, at least to a radius of 100 km. Also, the region of inflow below the upper-tropospheric outflow layer has expanded in areal extent and strengthened. A prominent feature of the vertical velocity field is more pronounced descent through

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the eye than during the first intensification period. At this stage, the eyewall updraught fully encircles the centre of circulation.

The individual tendency terms exhibit a broadly similar structure to those found during the intensification period, but the net tendency is small near the RMW by definition of the quasi-steady state. However, there is a continued weak spin-up of the eye during this period. Unlike during the first intensification phase, the tendency of the radial diffusion component in the inner-core region is now negative so that the spin-up of the low-to-midtropospheric eye region is the result of the combined eddy and mean tendencies.

5.2 The AX3k simulation

Figure 12 shows radius-height cross sections of both the vortex structure and the contributions to the tangential wind tendency during the period of maximum intensification (77–83 h). As noted in Sect. 3.1, some of the fields are noisier than their counterpart in the azimuthally-averaged fields from the 3-D model.

The maximum radial inflow near the surface occurs at about 30 km radius and has a magnitude comparable to that of the 3-D simulation (-8.2 m s^{-1} versus -9.4 m s^{-1}) during the period of maximum intensification. However, the boundary layer inflow structure shows a secondary maxima near 65 km radius and this maximum appears to be associated with a secondary updraught complex near 50 km radius. From a phenomenological viewpoint, this outer convective complex resembles a secondary eyewall, although all convection in the AX model has a ring-like structure and an enhanced inflow maximum driven presumably by the convection. The role of boundary-layer dynamics in the formation of secondary eyewall features has been articulated recently by Huang et al. (2012).

The flow fields in Fig. 12 show many similarities to those in the 3-D simulation, except that the eyewall updraught is narrower radially and strong tangential winds ($\approx 15 \text{ m s}^{-1}$) extend to a greater height. The contributions to the tangential wind tendency from the sum of the vorticity influx and vertical advection are shown in Fig. 12d, and the radial

6 Eddy momentum fluxes

In the previous section it was found that, while the mean vorticity influx and vertical advection comprise the leading terms of the tangential wind tendency, the resolved and parameterized (subgrid) eddy processes contribute non-negligibly to the mean spin-up tendency around the eyewall and wind maximum throughout the troposphere. Here we examine the structure of these eddy fluxes comparing the 3-D and AX simulations during both spin-up and maturity.

6.1 Flux form of the tangential momentum equation

To establish the framework for comparing resolved and subgrid momentum fluxes, we first re-write the tangential momentum equation of Sect. 5 in flux divergence form. For simplicity, we again adopt a Boussinesq approximation similar to that employed in Sect. 4¹². With the same nomenclature as Sect. 5, the flux form of the azimuthally-averaged tangential momentum tendency equation in cylindrical coordinates is

$$\begin{aligned} \frac{\partial \langle v \rangle}{\partial t} = & \frac{1}{r^2} \frac{\partial (-r^2 \langle u \rangle \langle v \rangle)}{\partial r} + \frac{\partial (-\langle w \rangle \langle v \rangle)}{\partial z} - f \langle u \rangle \\ & + \frac{1}{r^2} \frac{\partial (-r^2 \langle u' v' \rangle)}{\partial r} + \frac{\partial (-\langle v' w' \rangle)}{\partial z} \\ & - c_p \left\langle \frac{\theta'_\rho}{r} \frac{\partial \pi'}{\partial \lambda} \right\rangle + \langle D_v \rangle. \end{aligned} \quad (16)$$

¹²The simplified diagnosis can be justified on the grounds that more elaborate diagnoses using more cumbersome equations including triple correlations involving eddy momentum flux and perturbation density, as well as horizontal and vertical variation of azimuthal mean density yield virtually identical results to the simpler set (not shown). In other words, physical insight gleaned from the approximate tangential momentum equation is essentially the same as found using the less approximate anelastic or fully compressible formulations.

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Again, D_v is the subgrid-scale tendency expressed as a radius-height divergence of the subgrid momentum fluxes τ :

$$\langle D_v \rangle = \frac{1}{r^2} \frac{\partial r^2 \langle \tau_{r\lambda} \rangle}{\partial r} + \frac{\partial \langle \tau_{\lambda z} \rangle}{\partial z} \quad (17)$$

where, for consistency with the Boussineq-type of approximation here, the vertical variation of the basic state density has been neglected in the vertical derivative term in Eq. (17). The comparison of Eqs. (16) and (17) shows the direct analogy of resolved $-\langle u'v' \rangle$ and $-\langle v'w' \rangle$ with subgrid $\tau_{r\lambda}$ and $\tau_{\lambda z}$. In addition, in the mean radial and vertical momentum tendency equations (not written), the resolved $-\langle u'w' \rangle$ is the analog of subgrid τ_{rz} . In the CM1 model (Sect. 2), the subgrid momentum fluxes are specified by local eddy diffusion relations (written here in cylindrical-polar coordinates),

$$\langle \tau_{r\lambda} \rangle = \left\langle K_{m,h} \left(\frac{1}{r} \frac{\partial u}{\partial \lambda} + r \frac{\partial v/r}{\partial r} \right) \right\rangle \quad (18)$$

$$\langle \tau_{\lambda z} \rangle = \left\langle K_{m,v} \left(\frac{1}{r} \frac{\partial w}{\partial \lambda} + \frac{\partial v}{\partial z} \right) \right\rangle \quad (19)$$

with parameterization formulae for horizontal and vertical eddy diffusivities, $K_{m,h}$ and $K_{m,v}$. An analogous specification is made for τ_{rz} using $K_{m,v}$.

6.2 Eddy flux analysis

Figures 14 and 15 show the (r, z) structure of resolved eddy fluxes, subgrid fluxes and their eddy diffusivities, and a local, moist Richardson number (defined below) for the two spin-up periods in the 3-D simulation indicated in Fig. 1a. As noted in Sect. 3, a second intensification interval (151–155 h) is chosen for analysis in the 3-D model because the intensification period spans a comparatively longer time interval than in the AX model. The two periods for the 3-D model provide a representative sample of

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the radius-height eddy structure during the extended spin-up period. Figure 16 shows the corresponding fields for the AX simulation during the primary spin-up period indicated in Fig. 1a. *By definition, there are no resolved eddy fluxes in the AX model.* The selected spin-up times are centred on the times $t = 67$ h and $t = 153$ h for the 3-D simulation and $t = 79$ h for the AX simulation. Figures 17 and 18 show the analogous fields for the mature vortex phase in the 3-D and AX simulations, respectively. Each figure has the same multi-panel format as detailed in the captions. For the reader's convenience, we include in panels (a)–(c) of each figure the azimuthally-averaged velocity component shown in the previous section, except for the second intensification phase.

In the analyses that follow a general conclusion is that the analogous resolved and subgrid fluxes are quite different from each other in pattern and usually in magnitude. It follows that the parameterization of eddy momentum flux in the AX model is inconsistent with the resolved fluxes determined by the 3-D model.¹³

In addition, the differences between the resolved and subgrid flux within each of these figures are generally greater than the subgrid τ differences between the 3-D and AX models and greater than the time period differences. Readers who prefer to skip the detailed description of the results leading to these conclusions may wish to jump to Sect. 6.5 below.

The quantities plotted in Figs. 14–18 are time averages over a specific interval. In the 3-D model, an averaging period of 4 h is used for the two intensification periods in Figs. 14 and 15, whereas the averaging period for mature phase is 12 h in Fig. 17. In the AX model, an averaging period of 6 h is used for the primary intensification period in Fig. 16, whereas the averaging period for the mature phase is 24 h in Fig. 18. A longer averaging period was chosen for the AX model because of the noisier fields compared to the 3-D model. The averages are constructed from data output at 2 min intervals (except Fig. 17 that uses a 10 min interval) to provide an adequate resolution of

¹³This remark does not apply to the boundary layer where subgrid τ_{rz} and $\tau_{\lambda z}$ are dominant in both 3-D and AX models, as expected. Because the boundary layer story is addressed in Sects. 5 and 7, we focus in this section above the frictional boundary layer ($z \geq 1$ km).

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the time variability of the different fields during the averaging period (i.e., the snapshot decorrelation time is much shorter than the averaging period). Because the standard deviation of each respective time series is found to be comparable or less than their time-mean counterpart¹⁴, we conclude that these time-averaged quantities are adequate to characterize the qualitative structure of the plotted fields, although residual intrinsic (sampling) variability is evident as smaller-scale noise in the spatial patterns. This variability could be eliminated only by simulation ensembles with perturbed initial conditions, which is beyond the scope of this study. We show an extended time series of two momentum flux quantities and their associated tangential momentum tendencies in Fig. 19 to illustrate the time evolution of the eddy–mean interaction.

6.3 Radial eddy momentum and vorticity flux

During spin-up in the 3-D simulation, the resolved-eddy radial momentum flux, $-\langle u'v' \rangle$ (Figs. 14d and 15d), exhibits a coherent region of positive values around the RMW within and just above the boundary layer and extending upwards and outwards in the mean updraught to the middle troposphere. In the absence of an asymmetric secondary circulation, this inward-directed flux of cyclonic eddy momentum would contribute to a sharpening of the near eye-wall horizontal shear and an increase of $\langle v \rangle$ inside the RMW¹⁵.

¹⁴An exception occurs with $-\langle u'v' \rangle$, which has a standard deviation above the boundary layer that is consistently larger than the mean of the time series. Its spatial noise is also noticeably larger in Figs. 14d, 15d, and 17d than in other fields. However, individual snapshots recurrently show its dominant pattern near the RMW consisting of a positive outward-tilted feature below approximately 5 km and a negative outward-tilted feature above 6 km altitude.

¹⁵Since there is a locally strong secondary circulation component associated with vortical convection, the mean radial eddy vorticity flux is not simply equal to the mean radial divergence of the horizontal eddy momentum flux and an interpretation of the horizontal eddy dynamics is more challenging.

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The evolutionary behaviour of the resolved eddy contribution is illustrated in Fig. 19 by a radius-time Hovmöller diagram of the eddy momentum flux, $-\langle u'v' \rangle$ and the vertical eddy tangential momentum flux, $-\langle w'v' \rangle$. Shown also are the eddy vorticity flux, $V_{e\zeta}$ and the vertical advection of eddy tangential momentum, V_{ev} , which appear in the material form of the mean tangential momentum Eq. (12). Since the maximum tangential wind during spin-up occurs near the top of the boundary layer, we have chosen to average all of these quantities in a layer near this altitude, between 1 and 2 km altitude.

Outside the RMW, $V_{e\zeta}$ is generally negative throughout the simulation, implying a deceleration of $\langle v \rangle$ there. During the first intensification interval (65–69 h) and extending to approximately $t = 140$ h, $-\langle u'v' \rangle$ is mainly positive in a region straddling the RMW, and $V_{e\zeta}$ is negative around the RMW and weakly positive ($\sim 0.3 \text{ m s}^{-1} \text{ h}^{-1}$) further inside the RMW. These patterns broadly resemble a diffusive-like process in which the maximum tangential wind tends to be reduced while there is a spin-up tendency inside this radius. Between approximately $t = 140$ h and $t = 165$ h (including the second intensification interval highlighted above), $-\langle u'v' \rangle$ remains mostly positive in a region straddling the RMW, and $V_{e\zeta}$ is recurrently positive and stronger in magnitude ($\sim 1 \text{ m s}^{-1} \text{ h}^{-1}$) inside the RMW and negative outside the RMW. Unlike the earlier period, however, $V_{e\zeta}$ is close to zero near the RMW. The fact the eddy vorticity flux is recurrently positive on the inside of the RMW and negative on the outside, implies that the eddies are not acting strictly diffusively and contribute to decreasing the RMW from approximately 30 km to 25 km.

Figures 14 and 15 show that the subgrid radial momentum flux in the 3-D simulation is predominantly negative and much weaker in magnitude than the resolved-eddy flux near the RMW and within the mean updraught. Thus the resolved flux in the lower troposphere acts in a direction opposite to the local velocity gradient presumed by the subgrid scale model, i.e., it is counter-gradient. In the AX simulation, the subgrid flux (Fig. 16d) becomes comparable with that found in the 3-D simulation during the second intensification phase (Fig. 15g), but its dipole pattern in the low to mid-troposphere

updraught region is essentially the reverse of the 3-D resolved-eddy pattern. This difference indicates an intrinsic limitation of the AX model.

The subgrid radial momentum fluxes in both simulations do not show any indication of the upper-troposphere broadening tendency of the resolved eddies. In the upper troposphere, the resolved-eddy flux is broadly negative, which implies a tendency to broaden the radial profile of $\langle v \rangle$ in the upper-tropospheric outflow region, and we see that it is broader in the 3-D simulation. This deficiency may have consequences for understanding the dynamics of the outflow layer.

In the mature phase (Figs. 17–18), all of the fluxes are larger than during spin-up. The resolved-eddy flux (Fig. 17d) is noisier than during spin-up (some of this noise is sampling variability, see above; and some is identified with the inertial recoil effect extending above the boundary layer as discussed in Sect. 5.2), but it is broadly negative near the RMW and in the upper-tropospheric outflow. The subgrid flux in the 3-D simulation (Fig. 17g) is uniformly negative near the RMW and is significant in magnitude. In contrast to this simulation, the subgrid counterpart in the AX simulation (Fig. 18d) has essentially the same eddy-diffusive dipole pattern as during spin-up. Thus, as the system matures the resolved-eddy and subgrid scale fluxes have differences similar to those during spin-up, although they are perhaps less striking.

6.4 Vertical momentum fluxes and eddy vertical advection

The patterns of the 3-D resolved-eddy vertical fluxes (i.e., $-\langle u'w' \rangle$ and $-\langle v'w' \rangle$ in Figs. 14e,f, 15e,f and 17e, f) are tall, negative, outward-sloping columns concentrated around the RMW and mean updraught, both during spin-up and maturity. This location is where the vortical convective plumes are most active, and presumably they are the agents of these flux columns. The tendency of these flux columns is to extend the region of strong tangential wind higher in the troposphere. As indicated by the vertical profile of $\langle v \rangle$, the mean tangential wind is more uniformly spread through the troposphere in the 3-D simulation, and the vertical shear of this wind is more concentrated

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aloft (Figs. 14b and 17b vs. 16b, 15b and 18b); this difference is larger during spin-up than maturity.

In the layer average between 1 and 2 km (Fig. 19d), $-\langle w'v' \rangle$ is negative just inside the RMW and V_{ev} implies a positive tendency in this layer for $\langle v \rangle$ spanning the RMW, especially just inside it, which is an acceleration tendency (cf. Fig. 13g). Both features persist throughout the spin-up period and maturity. The positive spin-up tendency associated with $V_{e\zeta}$ near and inside the RMW increases from the approximate range $1-3\text{ms}^{-1}\text{h}^{-1}$ early in the intensification period (50 to 70 h) (cf. Fig. 13g) to the approximate range $3-10\text{ms}^{-1}\text{h}^{-1}$ later in the intensification period (145 to 165 h). Thus, comparatively speaking, the spin-up tendency from eddy vertical advection is roughly three times larger than that for the radial eddy vorticity flux (cf. Fig. 19b).

Recall from Sect. 3, it is during the period around 66 h when the rate of spin-up of the mean tangential wind in the 3-D model exceeds the maximum spin-up rate of the AX model (cf. Fig. 1a). We showed also in Fig. 5c that at this time there were isolated regions of strong convective heating rate organized in a ring-like developing eyewall. These regions of strong heating will correspond with a strong positive signature in the V_{ev} field and would provide a plausible explanation for the enhanced spin-up rate in the 3-D model despite the relative weakness of the azimuthal mean heating rate in this model.

Recall that the tendency in $\langle u \rangle$ by the resolved flux, $-\langle u'w' \rangle$, is obtained via a vertical partial derivative of this flux. An examination of Figs. 14 and 15 reveals that the indicated tendency in $\langle u \rangle$ is to strengthen both lower-tropospheric inflow and upper-tropospheric outflow, i.e., to accelerate the mean overturning circulation. Thus the resolved-eddy flux, $-\langle u'w' \rangle$, does not act like eddy diffusion, but represents a vertical non-local flux by the troposphere-filling vortical plumes.

During both the spin-up and mature phases the subgrid vertical fluxes in the 3-D and AX simulations (Figs. 14h, i; 16e, f; 17h, i; 18e, f) have the expected large extrema in the boundary layer, but they show nothing in the tropospheric eyewall-updraught region where the resolved-eddy fluxes are active. There is some pattern similarity in

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the negative $-\langle v'w' \rangle$ and $\langle \tau_{rz} \rangle$ in the upper-troposphere updraught region in the 3-D simulation, but the latter is much smaller, and in the AX simulation this feature is entirely absent. For the 3-D configuration, τ_{rz} has a weak vertical dipole pattern in the upper-tropospheric outflow region. Using the same argument as in the previous paragraph, this pattern implies a weak tendency in the vertical profile of $\langle u \rangle$ to decrease the outflow altitude. The associated $K_{m,v}$ have local maxima in the outflow region (Figs. 14k, 15k, 16h, 17k, 18h). However, in the 3-D simulation, there is not support for this effect in the resolved flux patterns in the upper-tropospheric outflow.

In summary, both radial and vertical resolved-eddy fluxes have qualitatively different patterns above the boundary layer in the 3-D simulation compared to the subgrid eddy-diffusive fluxes in either the 3-D or AX simulations, and the resolved-eddy fluxes are generally larger in magnitude, especially the vertical fluxes. The largest resolved-eddy fluxes occur in the eyewall-updraught region where vortical plumes are active. Their disparity with the subgrid patterns belies a simple interpretation as local momentum mixing.

6.5 Discussion of eddy dynamics

Having summarized the main features of the resolved- and subgrid-eddy fluxes in the 3-D and AX models, we examine now some additional physical characteristics of the horizontal and vertical eddies and illustrate their structure during a sample interval within the second intensification period.

First we recall that because the subgrid flux is based on the assumption of an “eddy-diffusion process” by definition, with $K_{m,h}$ a maximum in the RMW region (Figs. 14j, 15j, and 16g), it acts to weaken and spread the peak in $\langle v \rangle$ as in a pure barotropic instability process (e.g., Schubert et al., 1999, their Fig. 4b). Although the foregoing results already indicate that the horizontal eddy dynamics are not acting strictly diffusively on the tangential wind, a natural question arises whether the resolved horizontal eddy vorticity flux in the 3D3k simulation supports the barotropic instability paradigm. Although Fig. 8b suggests that a ring-like potential vorticity structure is evident during the first

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intensification period, animations of the vorticity field on level surfaces show that the vorticity field is highly disorganized and not ring-like during this time (cf. also Fig. 2). The ring-like structure in Fig. 8b is rather an artifact of azimuthally-averaging highly localized cyclonic vorticity anomalies just inside the RMW. Thus one of the necessary conditions for (linear) barotropic-baroclinic instability in a rapidly rotating baroclinic vortex is not satisfied during the first intensification period (Montgomery and Shapiro, 1995). At later times ($t > 80$ h), a more ring-like vorticity structure does emerge (cf. Fig. 2), but a significant limitation of applying purely adiabatic shear instability theory is that the eyewall region is being persistently forced by convection on time scales that are typically short (tens of minutes) compared to barotropic instability e-folding times (hours to 10 h, Schubert et al., 1999; Nguyen et al., 2011). Even if the necessary conditions for (linear) instability are satisfied, Schechter and Montgomery (2007) indicated that, when the effects of cloudiness are accounted for, the predicted e-folding times may be increased significantly (by a factor of three for a hurricane-like vortex example), depending on the extent of cloudiness. For these reasons, Nguyen et al. (2011) proposed the idea of a mixed barotropic-convective instability to explain a transition from a more symmetric to a more asymmetric phase during the intensification phase of their simulation of Hurricane Katrina (2005). However, the disparity in time scales between the convective instability and moist barotropic instability remains a significant issue.

The moist barotropic instability paradigm for ring-like potential vorticity distributions corresponding to a developed eyewall updraught does offer a plausible interpretation for the negative eddy vorticity flux forcing found near and inside the RMW during the early intensification period (Fig. 19b). However, the foregoing discussion is a reminder that one must be cautious of such a simple interpretation for a flow situation in which deep precipitating convection and frictional forcing are important processes in the eyewall vorticity balance. As an example, Fig. 19b shows that the associated radial eddy vorticity flux promotes the spin-up of the mean vortex just inside the RMW, but often leaves the maximum tangential wind approximately unchanged. Although this spin-up contribution inside the RMW is consistent with pure moist barotropic instability of an

elevated annulus of relative vorticity, as discussed above the near-zero eddy tendency at the RMW is not consistent with a diffusive weakening of the maximum tangential wind.

As noted in the foregoing section, as the vortex progressively strengthens, there is a period in which the eddy vorticity flux forcing becomes significantly positive inside the RMW ($140 \text{ h} < t < 165 \text{ h}$) and the RMW continues to contract inwards. An alternative explanation to the barotropic instability model is suggested upon examining animations of the simulated vorticity field in the lower troposphere of the vortex. During sub-periods of positive spin-up tendency, the animations suggest a sequence of local cyclonic vorticity generation, followed by a tendency of vortex axisymmetrization and trailing-spiral vorticity bands, which partially encircle the cyclonic mesoscale vorticity region near the RMW. These banded features appear plausibly consistent with convectively-coupled sheared vortex Rossby waves that would act to strengthen the mean vortex at radii interior to their excitation radius (Montgomery and Kallenbach, 1997; Montgomery and Enagonio, 1998; Wang, 2002a, b; Chen et al., 2003; McWilliams et al., 2003). We pause now to elucidate further the physical nature of the horizontal and vertical eddies in the 3D3k simulation during the second period of intensification.

To identify the physical nature of the eddy spin-up contribution, the left column of Fig. 20 shows the vertical vorticity ζ and vertical velocity w at the $z = 1.5 \text{ km}$ level for a sequence of times, spaced 6 min apart. The RMW during this analysis interval is highlighted by the spotted circle at $r = 24 \text{ km}$. The chosen time interval isolates a particularly positive period of radial eddy vorticity flux forcing near the RMW (i.e., $V_{e\zeta} > 0$) during the second intensification period¹⁶. During this period, several banded features

¹⁶Identification was made with a version of Fig. 19 refined to the second intensification period. While the feature illustrated here is not representative of the entire time period, as negative forcing inside the RMW occupies much of the time period, this episode is found to be typical of this and four other episodes (i.e. a total of five such positive episodes over an extended eight hour period) during which the azimuthally-averaged tangential wind intensifies by about 5 m s^{-1} and the RMW contracts by about 5 km (from 30 to 25 km, averaged over this layer).

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tendency also where $w' < 0$ and $\partial v' / \partial z > 0$. According to Fig. 19, the anticorrelation between w' and $\partial v' / \partial z$ typifies the vertical eddy contribution to the tangential wind tendency in the eyewall region. Recalling the boundary layer spin-up mechanism discussed in the Introduction and illustrated in Sect. 5, the eddy vertical velocity is highly correlated with eddy tangential velocity, because of the convective transport of tangential momentum from low levels. In the vicinity of the eyewall, the flow above the boundary layer and the asymmetries thereof tilt radially outwards with height. The outward tilt of these features with height between 20 and 40 km radius implies that positive or negative asymmetries of tangential velocity will be anticorrelated with the vertical derivative of the tangential wind asymmetry, i.e., $-w' \partial v' / \partial z > 0$.

Outside the eyewall, vorticity bands (whether positive or negative) frequently exhibit positive or negative tendency in $-u' \zeta'$. Isolated convection outside the eyewall leads to cellular enhancements of vorticity and for reasons offered in the prior subsection, these vorticity anomalies may be associated with a spin-up or spin-down signal in $-u' \zeta'$. The eddy radial velocity exhibits larger spatial scales of variability and the smaller-scale convective signals in vorticity appear to be generated within eddy outflow or eddy inflow, more-or-less evenly.

In summary, the principal explanation of the net positive tendency in the radial eddy vorticity flux in the eyewall (just inside the RMW) is the horizontal flow signatures resulting from convective-vorticity asymmetries found near and inside the eyewall. An asymmetry in the inflow is found to support the convective asymmetry that, together with the induced vorticity asymmetry, yields a negative correlation between the eddy radial wind and the eddy vorticity and thus a positive acceleration of the mean tangential wind there. These results are suggestive that the alternative explanation of convectively-generated vorticity and its subsequent tendency to axisymmetrize is the most plausible during periods of positive eddy-vorticity-flux forcing during the second intensification interval. The above analyses show also that the phenomena of vertical eddy acceleration of both the tangential and secondary circulations by convective vor-

tices is quantitatively larger than that of the horizontal eddy acceleration. At the present time we lack a full thermo-mechanical explanation of the eddy dynamics.

6.6 Richardson number

The gradient-Richardson number (panels (l) for the 3-D simulation or (i) for the AX simulation), in conjunction with the time-averaged vertical eddy diffusivity (panels (k) or (h) for the two calculations, respectively), serves as an indicator for the possible occurrence of moist Kelvin–Helmholtz (stratified-shear) instability and parameterized small-scale vertical mixing processes above the boundary layer. An investigation of both quantities allows also a first-assessment of a newly proposed theory of tropical cyclone intensification by Emanuel (2012). The “self-stratification” hypothesis posits that small-scale mixing processes associated with stratified-shear instabilities in the upper-level eyewall and outflow region control the intensifying vortex by limiting the Richardson number to a critical value near unity in the upper-tropospheric outflow layer. The idea is that the mixing sets the thermal stratification of the outflow region of the storm. The Richardson number plotted here is the azimuthal and time average of the *local* Richardson number Ri_{cm1} used in the CM1 model for determining where small-scale vertical mixing associated with shear-stratified turbulence occurs:

$$Ri_{cm1} = \frac{N_{m2}}{\left(\frac{\partial u}{\partial z}\right)^2 + \left(\frac{\partial v}{\partial z}\right)^2}, \quad (20)$$

where N_{m2} is the *local* moist static stability as defined exactly in the CM1 model. When this Richardson number is non-negative and falls below unity, the shear-stratified turbulence parameterization is activated and the vertical eddy diffusivity is nonzero. During the spin-up phases in the 3-D model, Figs. 14l and 15l show a widespread region in the upper-level eyewall and outflow region where the mean gradient Richardson number varies typically between 10 and 30, well above the posited critical value of unity. Of course, given the variability of the solution illustrated by Fig. 1, we would expect some

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deviation above and below these average values during the spin-up period. However, for a given radius and height, the azimuth-time percentage of realizations in which the Richardson number drops below unity is found to be no more than 30 %. In other words, the instances when this local Richardson number is small enough to contribute to a nonzero vertical eddy diffusivity in the model is a small subset of the total time series of values¹⁷. These statements are consistent with plots of the corresponding mean vertical eddy diffusivity during spin-up (Figs. 14k and 15k). The mean diffusivity in the upper eyewall and outflow regions has a maximum between 8 and 20 m² s⁻¹ during the first and second intensification periods, respectively, and is relatively small in comparison to the boundary layer values. Although regions do emerge at the top of the eyewall and top and bottom of the upper-level outflow layer during the mature stage with gradient Richardson numbers near 3, only a thin and radially confined pancake-like region at the bottom of the upper-level outflow possesses gradient Richardson numbers less than unity.

The foregoing pattern of the gradient Richardson number and the lack of strong vertical mixing at upper-levels in the 3-D configuration stand in contrast to those found in the AX configuration (cf. Figs. 17i and 18i). During maturity, the regions of gradient Richardson number in the range between 1 and 3 in the upper-level eyewall and outflow layer are more extensive than in the 3-D model. Moreover, the vertical diffusivity in this region is larger-in-value and the large values cover a larger range of radii than that in the 3-D model.

We conclude that for the realistic model set up used here, the 3-D configuration during spin-up is generally far from criticality with correspondingly little vertical mixing in

¹⁷We have verified these conclusions for smaller values of the horizontal and vertical sub-grid mixing length parameters: ($l_v = 20$ m, $l_h = 500$ m). In this case, we find no more than 10 % realizations of sub-critical Richardson number in the azimuth-time domain and the 3-D vortex intensifies in essentially the same manner as the pathway shown here. Further simulations where vertical diffusion is completely suppressed above 1 km height are essentially similar to the results shown here.

within the predictability envelope for intensity associated with the convective structures that operate in and around the eyewall region of the storm (Nguyen et al., 2008).

While it may be objected that the use of a constant drag coefficient is unrealistic and that the results may be prejudiced by the choice of the bulk-aerodynamic boundary layer scheme in the MM5 model, Smith et al. (2013) carried out simulations with a more realistic formulation of the drag coefficient and a range of boundary-layer parameterization schemes and showed that the results and supporting interpretations presented by Montgomery et al. (2010) are robust¹⁸. The implication is that there is a quantitative difference in the role of the frictional boundary layer in the 3-D and AX configurations. Indeed, it will be shown below that this difference is very striking in these configurations and is a further challenge to the notion that the axisymmetric model, as traditionally configured with explicit convection occurring as concentric rings, is a satisfactory approximation for understanding tropical cyclone intensification and mature intensity in the prototype problem for intensification on meteorologically relevant forecast time scales of 4 to 5 d. These differences are shown to hold true also on the long range forecast time scale of 12 d, even in a quiescent environment.

For the foregoing reasons a series of simulations is performed here using both the AX and 3-D models to examine the sensitivity of intensification and mature intensity to values of the drag coefficient C_D . Recall that in the AX and 3-D control experiments, $C_k = 1.29 \times 10^{-3}$ and $C_D = 2 \times C_k$. The additional calculations are carried out using values of the drag coefficient that are multiples of the baseline enthalpy transfer coefficient

¹⁸In a very recent paper, the results found by Montgomery et al. (2010) were criticized by Bryan (2012b) on the grounds that the calculations were not run long enough to achieve a steady-state solution. As discussed in footnote 7, we believe it is questionable whether a steady-state solution exists. Nevertheless, the calculations carried out here using the CM1 model are for a significantly longer time period (12 d, the same length of time as in Bryan's calculations) and will be shown to support further the results and interpretations of Montgomery et al. (2010) and Smith et al. (2013). In particular, the 3-D results to be shown here are counter examples to Bryan's conclusion that "the maximum intensity is inversely proportional to C_D " (see Fig. 21a).

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cient C_k : $C_D = (0.5, 1.0, 4.0) \times C_k$. The enthalpy transfer coefficient is held constant, and a multiple of 2.0 for the drag coefficient corresponds to the control experiment. The four 3-D simulations, in order of increasing C_D , are referred to as “3D3k-B”, “3D3k-C”, “3D3k”, and “3D3k-E”, with 3D3k being the control. Likewise, the four AX simulations, in order of increasing C_D , are referred to as “AX3k-B”, “AX3k-C”, “AX3k”, and “AX3k-E”, with the AX3k being the control.

The time-series of maximum azimuthally-averaged tangential velocity are shown in Fig. 21. For both the 3-D and AX configurations, simulations with a large drag coefficient (e.g., blue dotted lines) intensify sooner than those with a small drag coefficient (e.g., red solid lines). In the AX simulations, the mature state intensity appears to be strongly dependent on the value of C_D , with the vortex in the lowest drag simulation being much more intense than that in the strongest drag simulation (i.e., 120 ms^{-1} compared with 55 ms^{-1} !). However, in the 3-D configuration, the most intense vortex over the standard forecast time scale of 4 to 5 d occurs with a moderately strong (and realistic) level of surface drag (our control configuration).

With the range of variability of maximum intensity found by Montgomery et al. (2010), Smith et al. (2013) and Thomsen et al. (2013) using the MM5 model, the range shown by the control and 3D3k-E simulations up to 5 d lie close to the range of the variability of the 3-D simulations shown earlier in Fig. 1. In this sense, the control and double-the-control drag simulations do not predict a significantly different mature intensity for a 5 d simulation time, broadly consistent with the foregoing studies. On the time scale of 4–5 d, the vortex in the half-the-control drag simulation, 3D3k-C, is again weaker than that in the control simulation. At longer times, however, the vortex in the 3D3k-C simulation “catches up” to the slowly intensifying vortex in the control simulation, while the vortex in the double-the-control drag simulation, 3D3k-E, stays at approximately the same intensity. At very long times (~ 10 d) vortices in both the 3D3k and 3D3k-E simulations weaken with time. By 12 d, the vortex in the strongest drag simulation is about 20 ms^{-1} weaker than that in the control configuration. However, in the weakest drag simulation, 3D3k-B, the vortex struggles to intensify throughout the entire 12 d

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integration time. Needless to say, the 3D3k-B solution is considerably weaker than that of the corresponding AX3k-B solution after approximately 210 h (8.75 d) (29 ms^{-1} versus 120 ms^{-1})¹⁹.

The interpretations given in Smith et al. (2013) for the vortex behaviour as a result of changing the boundary-layer scheme, or changing the drag coefficient within a boundary-layer scheme, go some way to providing basic understanding of the issues discussed above. However, they fall short of providing a complete theory, which would require consideration of processes above the boundary layer as well as in the boundary layer. In particular, the magnitude and radial distribution of the heating rate may change as the drag coefficient changes. While the lack of such a theory presents an obstacle to interpreting the behaviour shown in Fig. 21 *in both* the 3-D and AX configurations, we attempt to articulate some of the key elements required to elucidate these differences.

To explain the behaviour of the 3-D model to changes in C_D , Smith et al. (2013) invoked the frictional disruption of gradient wind balance in the boundary layer, which increases with C_D . Their arguments were applied to the azimuthally-averaged flow fields. It was shown in Montgomery et al. (2010) and Smith et al. (2013) that a decrease in C_D leads to a weaker inflow in the boundary layer, to a smaller inward displacement of M surfaces, and therefore lower tangential wind speeds in the mature vortex. This argument would explain why a decrease in C_D in both models leads to a slower spin-up at early times. Nevertheless, unlike the behaviour in the 3-D simulation, a stronger mature vortex arises in the AX simulation when the drag coefficient is reduced. Since the above arguments relate to the azimuthally-averaged flow, why then do they apparently fail to explain the radically different behaviour between the AX and 3-D model as the mature stage is approached? Implicit in the foregoing explanation is the presumption

¹⁹Because of the scatter in the observational data used to set the vertical mixing length discussed in Sect. 2, we have conducted an independent numerical experiment and verified the large tangential wind speed obtained in the AX model using a value of $l_v = 100 \text{ m}$ instead of $l_v = 50 \text{ m}$ (not shown).

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radial distribution of the azimuthally-averaged heating rate do not change appreciably. In fact, the time-radius plot of Fig. 23b shows that the azimuthally-averaged heating rate at a height of 6 km in the 3-D simulation with reduced drag is appreciably less than that in the standard drag configuration, Fig. 23a. This difference has a significant impact on the radial displacement of the M surfaces during the vortex evolution and, in particular, the ability to bring some M surfaces to small radii. In Fig. 23, the M surfaces are shown at a height of 1 km, a height that is slightly above the height of maximum tangential wind during the evolution. For reference, Fig. 23 displays also the time evolution of the RMW and that of the M contour coinciding with the RMW in the mature stage.

For the case of standard drag (panel a), the M surfaces begin to move inwards when the heating rate becomes appreciable in the inner region. In particular, the M surface that marks the RMW at 1 km height in the mature stage starts at an initial radius of 80 km and moves in to a small RMW of about 20 km. In contrast, the corresponding M surface in the reduced drag case (panel b) begins at a radius of 160 km and moves in only to a radius of 80 km. However, for this case the arguments in terms of M surfaces are less appropriate because the vortex is highly asymmetric even in the mature stage (see Fig. 22a), a situation in which the simple explanation of the approximate material conservation of the azimuthally-averaged M is not expected.

The situation in the AX simulations is dramatically different in several ways. First, consistent with the findings of Sect. 3, the heating rates in the AX simulations are significantly larger in magnitude than in the 3-D simulations. Second, the heating rate at 6 km height in the AX simulation with reduced drag (Fig. 23d) is appreciably larger than for the AX simulation with standard drag (Fig. 23c). Third, in both AX simulations, the heating rate exhibits considerably more variability than that in the 3-D simulations. Fourth, in both AX simulation at early times, the RMW shows large radial fluctuations (sometimes more than 100 km) and these fluctuations persist for a longer period in the low drag simulation. Fifth, in the low drag simulation, large values of heating rate extend to significant radii (~ 200 km) for much of the simulation.

of M exceeds the frictional depletion of M , leading to a faster spin-up. For reasons discussed above, the foregoing discussion may be less applicable to the lowest drag case in the 3-D configuration.

The difficulty of anticipating a priori which of the foregoing effects dominates is compounded by the coupling of the boundary-layer dynamics and thermodynamics to the flow above, particularly the azimuthally-averaged radial and vertical distribution of the diabatic heating rate. Based on the results shown in Sect. 6, the eddy fluxes of momentum may play an important role also. The final outcome on the mature intensity depends in principle on all of these factors. At this point, we are unable to foresee the outcome without performing explicit calculations.

8 Conclusions

We have carried out idealized numerical experiments to examine the differences between tropical cyclone evolution in three-dimensional and axisymmetric configurations for the prototype intensification problem. The choice of subgrid-scale horizontal and vertical mixing length parameters, as well as air-sea momentum and enthalpy exchange coefficients, is guided by recent observational work.

This study has identified a number of important differences between the two configurations. Many of these differences may be attributed to the dissimilarity of deep cumulus convection in the two models. For example, there are fundamental differences in convective organization. Deep convection in the three-dimensional model is sheared tangentially by the differential angular rotation of the system-scale circulation in the radial and vertical directions, unlike that in the axisymmetric configuration. Because convection is not organized into concentric rings during the spin-up process, the azimuthally-averaged heating rate and radial gradient thereof is considerably less than that in the axisymmetric model. For most of the time this lack of organization results in slower spin-up and leads ultimately to a weaker mature vortex. There is a short period of time, however, when the rate of spin-up in the 3-D model exceeds that of the maximum spin-

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up rate in the AX model. During this period the convection is locally more intense than in the axisymmetric model and the convection is organized in a quasi ring-like structure resembling a developing eyewall. These regions of relatively strong updraughts have an associated vertical eddy momentum flux that contribute significantly to the spin-up of the azimuthal mean vortex and provide an explanation for the enhanced spin-up rate in the 3-D model despite the relative weakness of the azimuthal mean heating rate and its radial derivative in the 3-D model.

Consistent with findings of previous work, the mature intensity in the 3-D model is lower than that in the AX model. In contrast with previous interpretations invoking barotropic instability and related mixing processes as a mechanism detrimental to the spin-up process, the results herein suggest that eddy processes associated with vortical plume structures can assist the intensification process via up-gradient momentum fluxes in the radial direction. These plumes contribute also to the azimuthally-averaged heating rate and the corresponding azimuthal-mean overturning circulation. Our analysis has unveiled a potentially important issue in the representation of subgrid scale parameterizations of eddy momentum fluxes in hurricane models. Comparisons between the two model configurations indicate that the structure of the resolved eddy momentum fluxes above the boundary layer differs from that prescribed by the subgrid-scale parameterizations in either the three-dimensional or axisymmetric configurations, with the exception perhaps of the resolved horizontal eddy momentum flux during the mature stages.

Another important difference between the two configurations is that the flow fields in the axisymmetric model tend to be much noisier than in the three-dimensional model. The larger flow variability is because the deep convection generates azimuthally-coherent, large-amplitude, inertia-gravity waves. Although deep convection in the three-dimensional model generates inertia-gravity waves also, the convection is typically confined to small ranges of azimuth and tends to be strained by the azimuthal shear. These effects lead to a reduced amplitude of variability in the azimuthally-averaged flow fields.

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An analysis of the spin-up function was carried out to determine the extent to which the conventional spin-up mechanism, discussed in the Introduction, provides a useful interpretation for the intensification of the bulk vortex. In the 3-D model, a coherent region with positive values of spin-up function is found just inside the radius of maximum tangential wind and extends vertically in the main eyewall region in association with the peak eyewall heating rate near 7 km altitude, the signal identified by Vigh and Schubert (2009) for intensification. This region is unlike that found at larger radii, which is dominated by larger-in-amplitude, but smaller-in scale positive and negative dipole structures that would tend to be filtered in a balanced inversion of the geopotential tendency equation. The results for the 3-D model show that during spin-up, the time variation of the volume-averaged gradient wind tendency inside the radius of maximum gradient wind mimics closely that of the volume-averaged spin-up function. Although a correspondence between these two quantities persists in the AX model during the primary intensification period (with the spin up function approximately double that of the corresponding 3-D simulation), the higher degree of variability associated with inertia-gravity waves is a pervading feature, even inside the RMW, and at later times compounds the interpretation of the spin-up in this model in terms of balance dynamics.

An analysis of terms in the tangential velocity tendency equation showed that the spin-up of the azimuthally-averaged maximum tangential wind speed in both models takes place within the frictional boundary layer confirming recent predictions and observations. In the 3-D model, surface drag plays a particularly important role in the spin-up process by tending to organize the convection in azimuth. There is a radical difference in behaviour of the 3-D and AX models when the surface drag is reduced or increased from realistic values. Borrowing from ideas developed in a recent paper, we have sought to give a partial explanation for this difference in behaviour.

Analyses of the gradient Richardson number in the three-dimensional model do not support a recent hypothesis concerning the role of small-scale vertical mixing processes in the upper-tropospheric outflow in controlling the spin-up process.

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Our results provide new qualitative and quantitative insight into the asymmetric and symmetric dynamics of tropical cyclones and we believe they are relevant to the formulation of a more satisfactory theory of tropical cyclone intensification and mature intensity. In particular, the results point to some fundamental limitations of strict axisymmetric theory and modeling for representing the azimuthally-averaged behaviour of tropical cyclones in three dimensions. Specifically, the results herein suggest that the representation of convection as concentric rings in the AX model and the assumption of down-gradient eddy momentum fluxes to represent asymmetric eddy transport processes in both 3-D and AX models are flaws in the formulation and interpretation of tropical cyclone models.

Appendix A

In the three-dimensional simulations, the x and y coordinates are treated identically with a stretched grid configuration. Throughout the inner-most 405 km, there is a fixed grid spacing of 3 km, which is then stretched gradually to a grid spacing of 97.98 km at the outer edge of the domain. The entire domain spans 2880 km with 185 grid points. The vertical coordinate is stretched also with a grid spacing near the surface of 50 m and one of 1200 m near the domain top at 25 km. The lowest grid level where horizontal winds and thermodynamic variables are defined is at 25 m. The entire vertical domain is spanned with 40 grid points (Table 1). The total number of computational points is therefore $185 \times 185 \times 40 = 1\,369\,000$ grid points. The number of computational points in the uniform inner-grid domain is $136 \times 136 \times 40 = 739\,840$ grid points. The axisymmetric simulations employ a fixed radial grid spacing of 3 km, but use the same stretched vertical grid as described above.

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Table A1. Vertical grid mesh (km).

0.025	0.090	0.184	0.308
0.461	0.644	0.856	1.097
1.369	1.669	1.999	2.359
2.748	3.167	3.615	4.092
4.599	5.136	5.702	6.297
6.922	7.577	8.261	8.974
9.717	10.49	11.29	12.12
12.98	13.87	14.79	15.74
16.72	17.73	18.77	19.84
20.93	22.06	23.21	24.40

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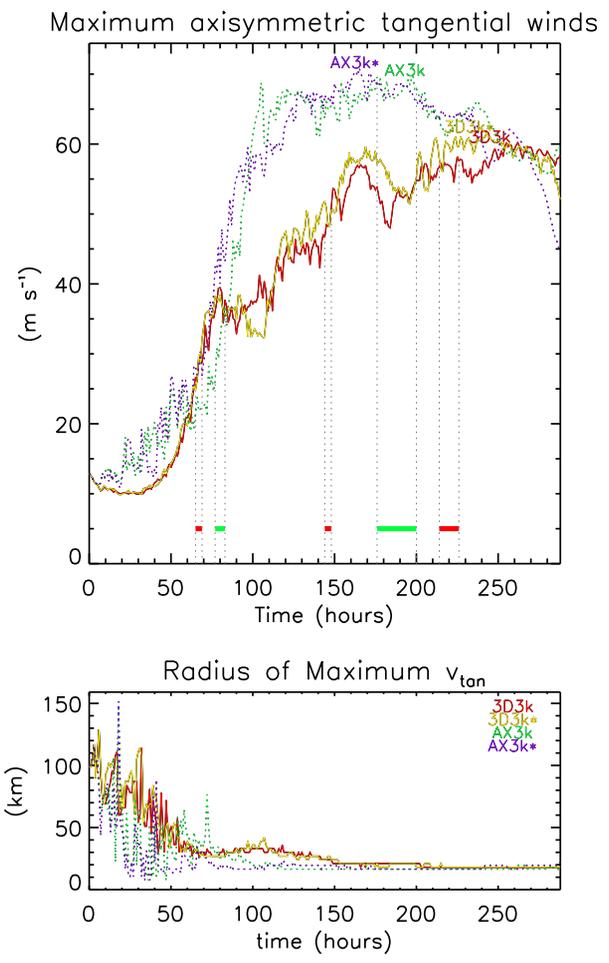


Fig. 1. Please see caption on next page.



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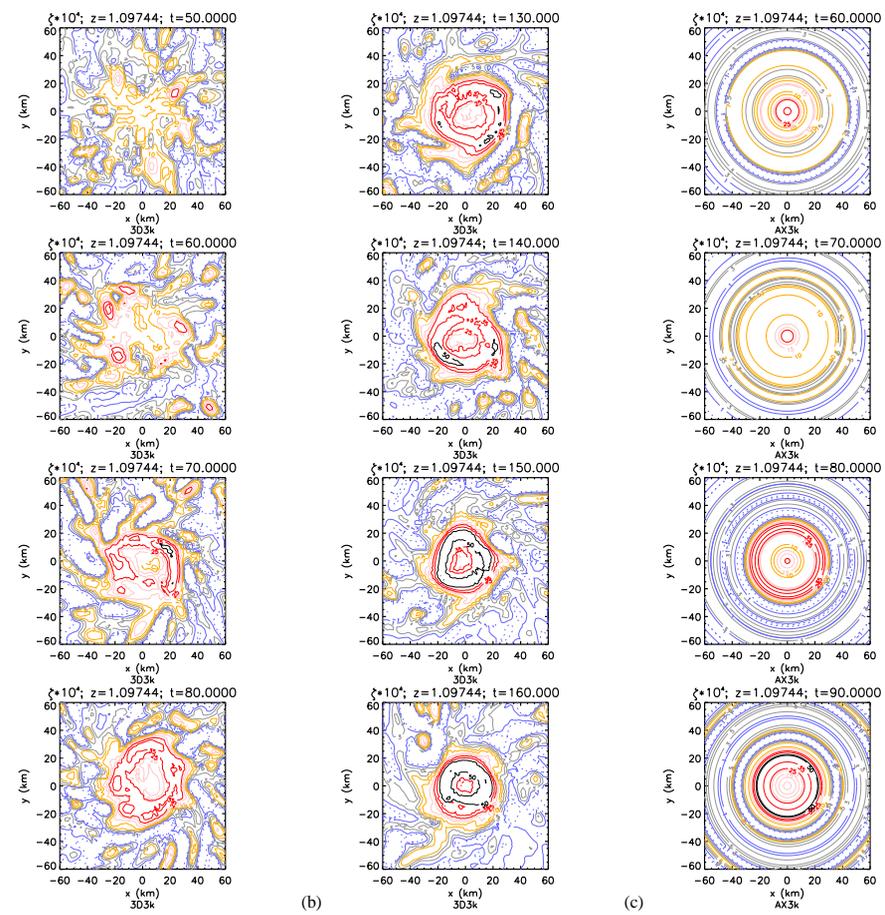


Fig. 2. Please see caption on next page.



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Fig. 2. Contour plots of relative vorticity ζ times 10^4 at $z = 1$ km at a sequence of times **(a)** and **(b)** (left-middle) from the simulation 3D3k and **(c)** (right) from simulation AX3k spanning periods of rapid intensification. The time period shown is between **(a)** 50–80 h and **(b)** 130–160 h for the 3D3k experiment and **(c)** 60–90 h in the AX3k experiment. Contours (s^{-1}) are -1 and 1 (blue); 3 and 5 (gray); 7 and 10 (orange); 15 and 20 (pink); 25 and 35 (red); and 50 and 75 (black).

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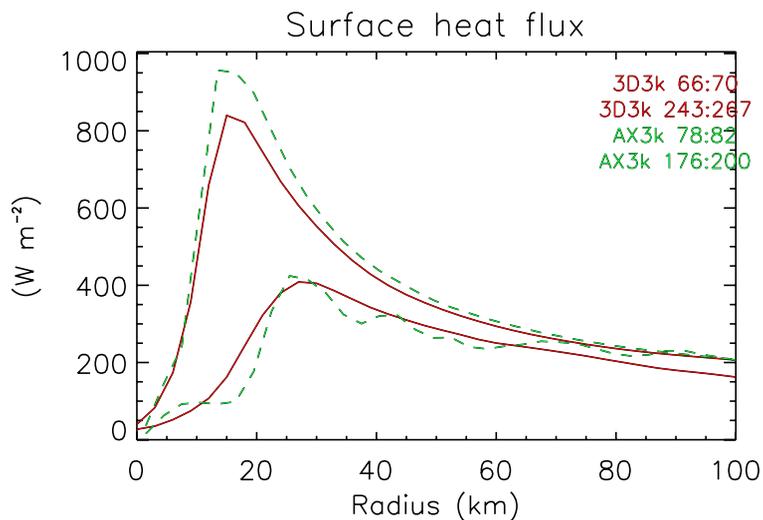


Fig. 4. Radial profile of surface enthalpy flux for the AX3k (green dotted) and 3D3k (red solid) experiments at a time of maximum intensification rate (lower pair of curves) and when the simulated hurricane has reached mature intensity (higher pair of curves).

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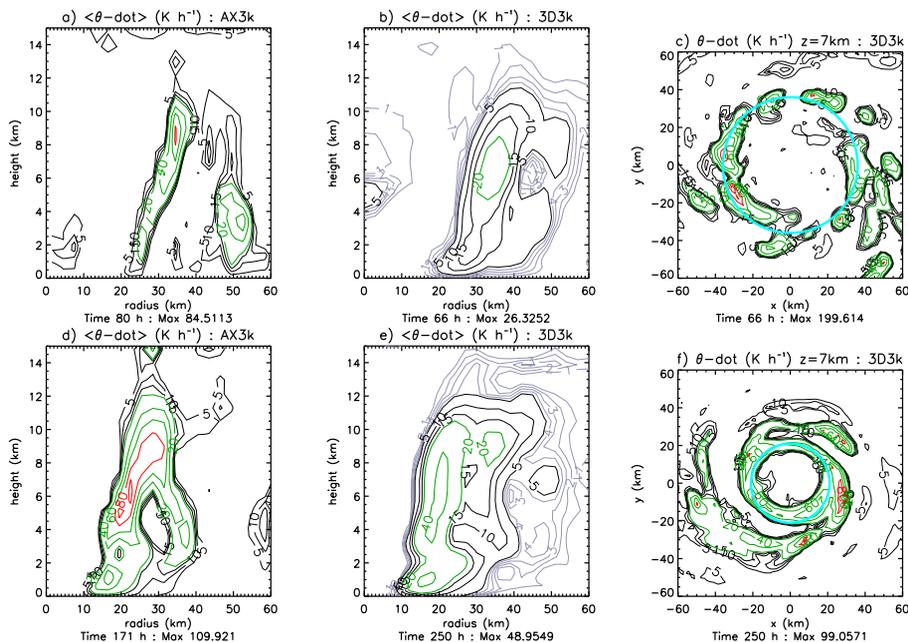


Fig. 5. Diagnosed heating rates during the periods of peak intensification and maximum quasi-steady intensity. **(a)** and **(b)** are radius-height cross sections of the axisymmetric mean heating rate from the AX3k and 3D3k simulations, respectively, at a time of rapid intensification; **(d)** and **(e)** present, respectively, the same at a time of maximum intensity. **(c)** and **(f)** are plan-view plots of heating rate at $z = 7\text{ km}$ from the 3D3k simulation during intensification and maximum intensity; the blue circle depicts the radius of maximum heating rate at this height. Thin, black contours are 5, 10, and 15 K h^{-1} . Thick, green contours are 20, 40, and 60 K h^{-1} . Thick, red contours are 80 and 100 K h^{-1} .

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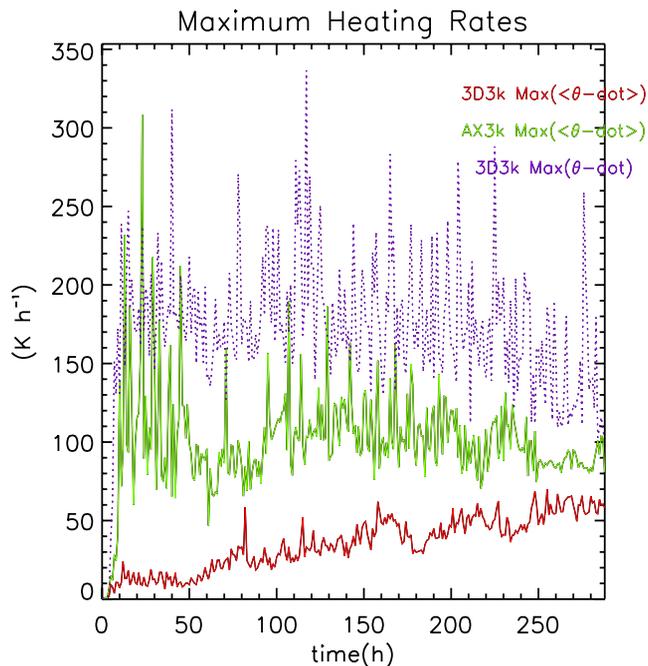


Fig. 6. Time-series of maximum azimuthally-averaged (mean) heating rates in the 3D3k simulation (red solid curve) and the corresponding heating rate in the AX3k simulation (green solid curve). The extreme value of the heating rate found at each time in the 3D3k simulation is shown by the blue-dotted curve.

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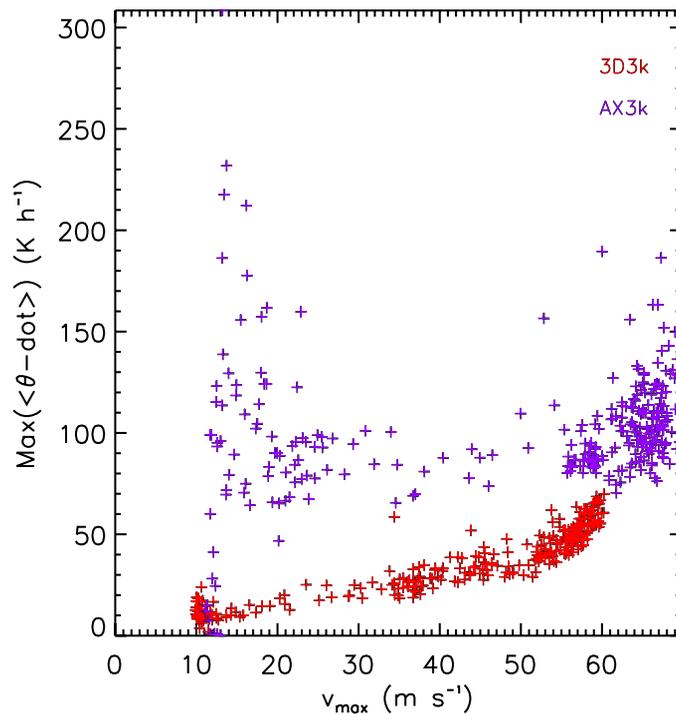


Fig. 7. The maximum azimuthally-averaged heating rate from the 3D3k (red) and AX3k (blue) simulations plotted against instantaneous intensity (e.g., Fig. 1).

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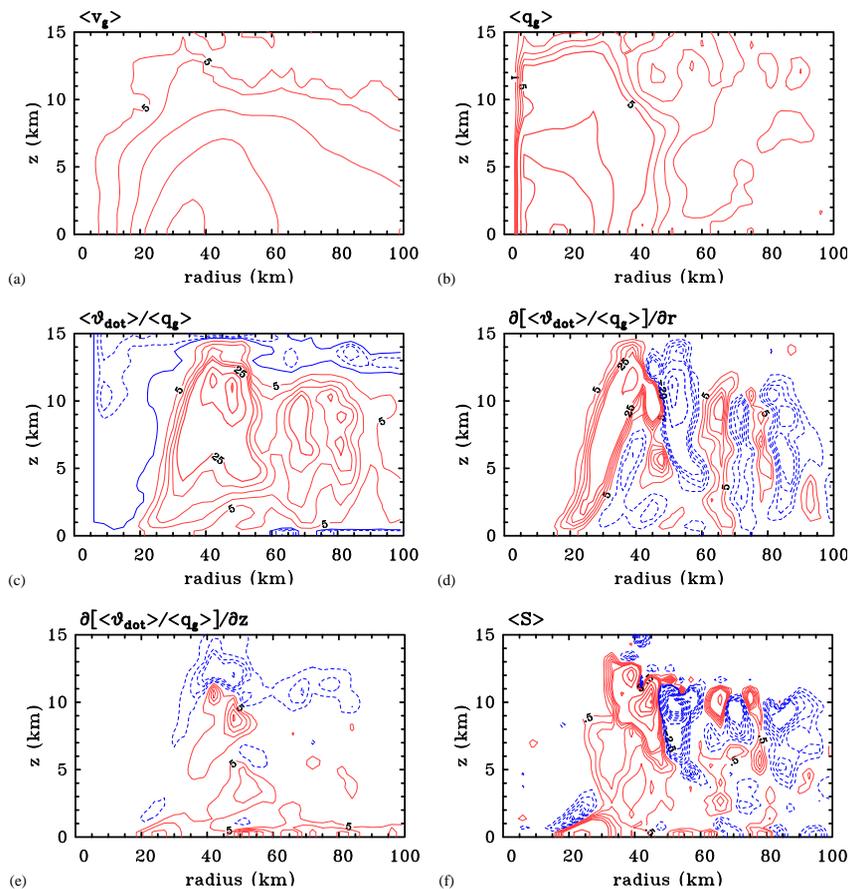


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Fig. 8. Terms used in computing the spin-up function S for the simulation 3D3k at a time of rapid intensification (average between 65 and 69 h). **(a)** The axisymmetric-mean gradient wind, $\langle v_g \rangle$ (Contour interval 5 m s^{-1}). **(b)** Axisymmetric-mean (Boussinesq) potential vorticity, $\langle q_g \rangle$, where the subscript “g” denotes evaluation using the gradient wind (Contour interval: thin contours $\{ 1, 2, 3, 4 \} \times 10^{-7} \text{ s}^{-3}$; thick contours $\{ 5, 10, 15, 20 \} \times 10^{-7} \text{ s}^{-3}$). **(c)** Axisymmetric-mean diabatic heating rate divided by mean potential vorticity, i.e., $\langle \dot{\theta} \rangle / \langle q_g \rangle$. (Contour interval: blue dashed contours $\{ -2, -1 \} \times 10^{-3} \text{ K s}^2$; thin red contours $\{ 5, 10, 15, 20 \} \times 10^{-3} \text{ K s}^2$; thick red contours $\{ 25, 50, 75, 100 \} \times 10^{-3} \text{ K s}^2$). **(d)** Radial derivative of $\langle \dot{\theta} \rangle / \langle q_g \rangle$ (Contour interval: thin contours go from -2.5 to 2.5 in steps of $0.5 \text{ K s}^2 \text{ m}^{-1}$; thick contours $\pm \{ 25, 75, 125, \dots \} \text{ K s}^2 \text{ m}^{-1}$). **(e)** Vertical derivative of $\langle \dot{\theta} \rangle / \langle q_g \rangle$ (Contour interval: thin contours go from -2.5 to 2.5 in steps of $0.5 \text{ K s}^2 \text{ m}^{-1}$; thick contours $\pm \{ 25, 75, 125, \dots \} \text{ K s}^2 \text{ m}^{-1}$). **(f)** Spin-up function S , with the restriction that $\langle q_g \rangle \geq \max \langle q_g \rangle / 100$ (Contour intervals: thin 0.5×10^{-5} up to $\pm 4.5 \times 10^{-5}$; thick $\pm \{ 3, 8, 13, \dots \} \times 10^{-5} \text{ s}^{-1}$).

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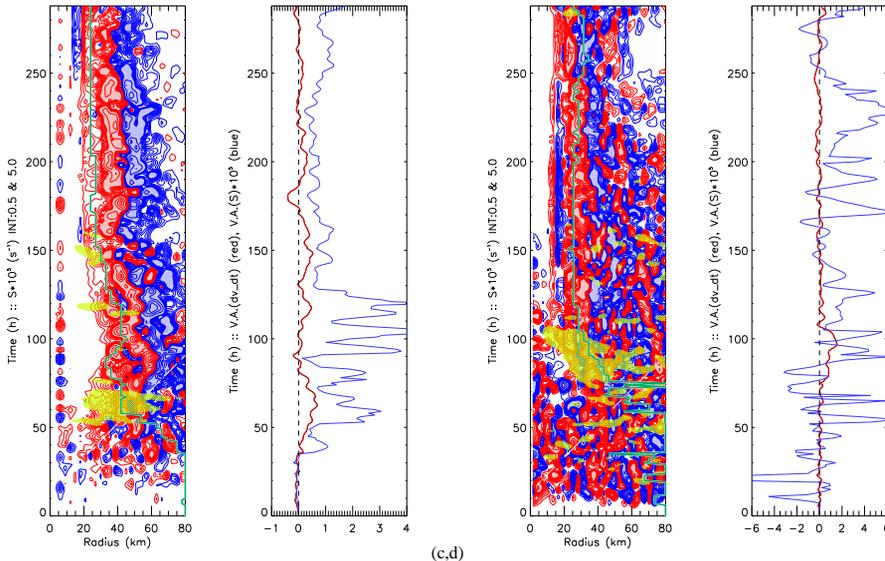


Fig. 9. Please see caption on next page.

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Fig. 9. (a): Radius-time plot of layer-averaged spin-up function, \bar{S} for the simulation 3D3k. Red contours denote positive values of \bar{S} , blue contours denote negative values. Thin contour interval $1 \times 10^{-5} \text{ s}^{-1}$ up to magnitude $4 \times 10^{-5} \text{ s}^{-1}$; thick contour interval $5 \times 10^{-5} \text{ s}^{-1}$. Zero contour is omitted. Yellow shading denotes regions where layer-averaged intensification rate for the gradient wind exceeds $\partial \bar{v}_g / \partial t > 0.5 \text{ m s}^{-1} \text{ h}^{-1}$; thick green curve denotes the radius of maximum \bar{v}_g . For reasons given in the text, the layer average used comprises a height spanning the bulk of the troposphere ($1.5 < z < 12 \text{ km}$), but purposefully omits the frictional boundary layer ($0 < z < 1.5 \text{ km}$) and outflow layer ($z > 12 \text{ km}$) of the developing storm where axisymmetric balance dynamics formally breaks down. **(b):** Time series of the volume-averaged spin-up function \hat{S} in units of $1 \times 10^{-5} \text{ (s}^{-1}\text{)}$ (blue) and volume-averaged gradient wind tendency (in units of $\text{m s}^{-1} \text{ h}^{-1}$) (red). The volume averaging is carried out from the axis of rotation to the radius of maximum layer-averaged gradient wind (thick green curve in **(a)**) and over the same height as employed in **(a)**. **(c)** and **(d)** are the corresponding plots for the axisymmetric simulation AX3k. The contour intervals are identical. All fields have a Gaussian time smoother applied prior to averaging.

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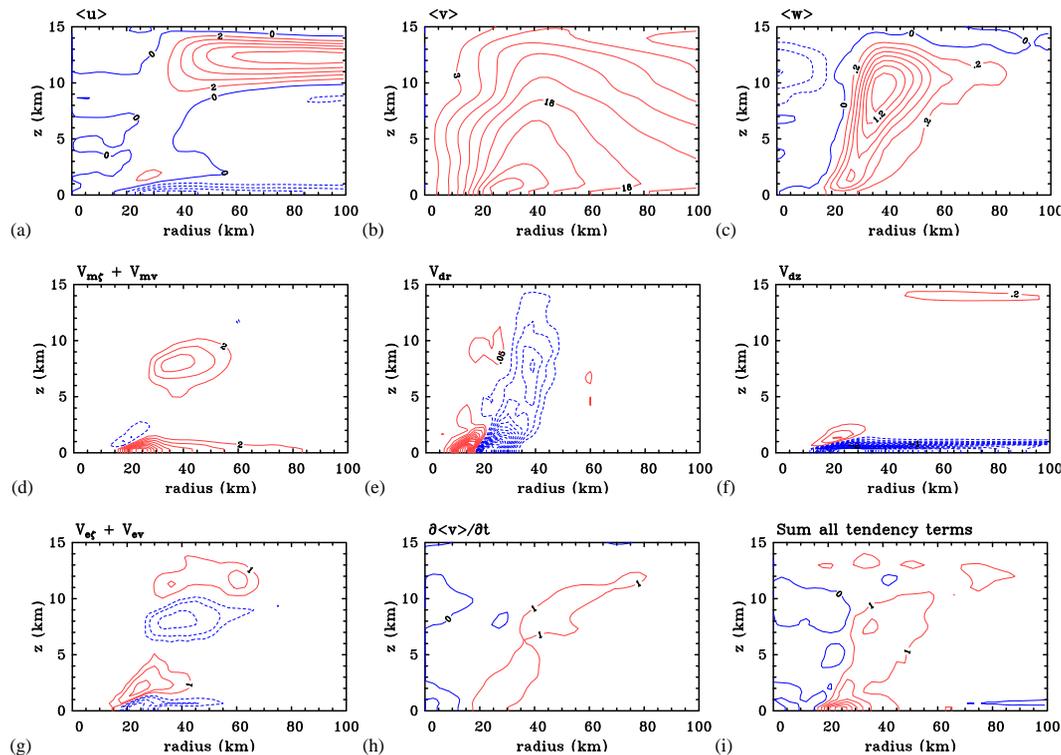


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Fig. 10. Terms of the tangential wind tendency equation for the simulation 3D3k, averaged during the period of rapid intensification (65–69 h). Red contours denote positive values; blue contours denote negative values. **(a)** Radial velocity $\langle u \rangle$ (Contour interval 2 m s^{-1}); **(b)** Tangential velocity $\langle v \rangle$ (Contour interval 3 m s^{-1}); **(c)** Vertical velocity $\langle w \rangle$ (Contour interval 0.2 m s^{-1} ; blue contours -0.1 , -0.05 , and 0 m s^{-1}); **(d)** Sum of mean vorticity influx and vertical advection $V_{m\zeta} + V_{mv}$ (Contour interval $2 \text{ m s}^{-1} \text{ h}^{-1}$); **(e)** Radial (subgrid-scale) diffusive tendency V_{dr} (Contour interval $0.05 \text{ m s}^{-1} \text{ h}^{-1}$); **(f)** Vertical (subgrid-scale) diffusive tendency V_{dz} (Contour interval $0.2 \text{ m s}^{-1} \text{ h}^{-1}$); **(g)** Combined eddy tendencies $V_{e\zeta} + V_{ev}$ (Thick contour interval is $2 \text{ m s}^{-1} \text{ h}^{-1}$, thin contours are $\pm 1 \text{ m s}^{-1}$); **(h)** Mean tangential wind tendency $\partial \langle v \rangle / \partial t$ (Contour interval $1.0 \text{ m s}^{-1} \text{ h}^{-1}$); **(i)** Sum of all tendency terms (Contour interval $1.0 \text{ m s}^{-1} \text{ h}^{-1}$).

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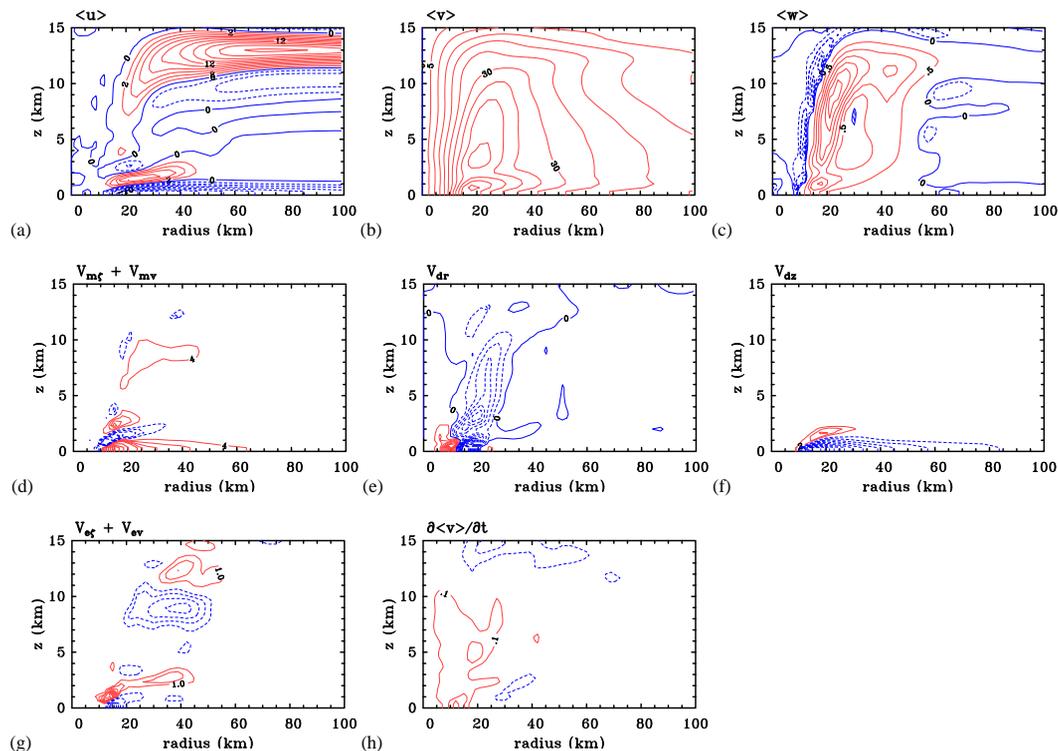


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Fig. 11. Terms of the tangential wind tendency equation for the simulation 3D3k, averaged during the mature stage (214–226 h). Red contours denote positive values; blue contours denote negative values. **(a)** Radial velocity $\langle u \rangle$ (Contour interval 2 ms^{-1}); **(b)** Tangential velocity $\langle v \rangle$ (Contour interval 5 ms^{-1}); **(c)** Vertical velocity $\langle w \rangle$ (Contour interval for positive 0.5 ms^{-1} ; negative contours $-0.05, -0.1, -0.15, -0.2 \text{ ms}^{-1}$); **(d)** Sum of mean vorticity influx and vertical advection $V_{m\zeta} + V_{mv}$ (Contour interval: thin contours $4 \text{ ms}^{-1} \text{ h}^{-1}$, thick contours $20 \text{ ms}^{-1} \text{ h}^{-1}$); **(e)** Radial (subgrid-scale) diffusive tendency V_{dr} (Contour interval $0.5 \text{ ms}^{-1} \text{ h}^{-1}$); **(f)** Vertical (subgrid-scale) diffusive tendency V_{dz} (Contour interval $2 \text{ ms}^{-1} \text{ h}^{-1}$); **(g)** Combined eddy tendencies $V_{e\zeta} + V_{ev}$ (Contour interval $2 \text{ ms}^{-1} \text{ h}^{-1}$); **(h)** Mean tangential wind tendency $\partial \langle v \rangle / \partial t$ (Contour interval $0.1 \text{ ms}^{-1} \text{ h}^{-1}$).

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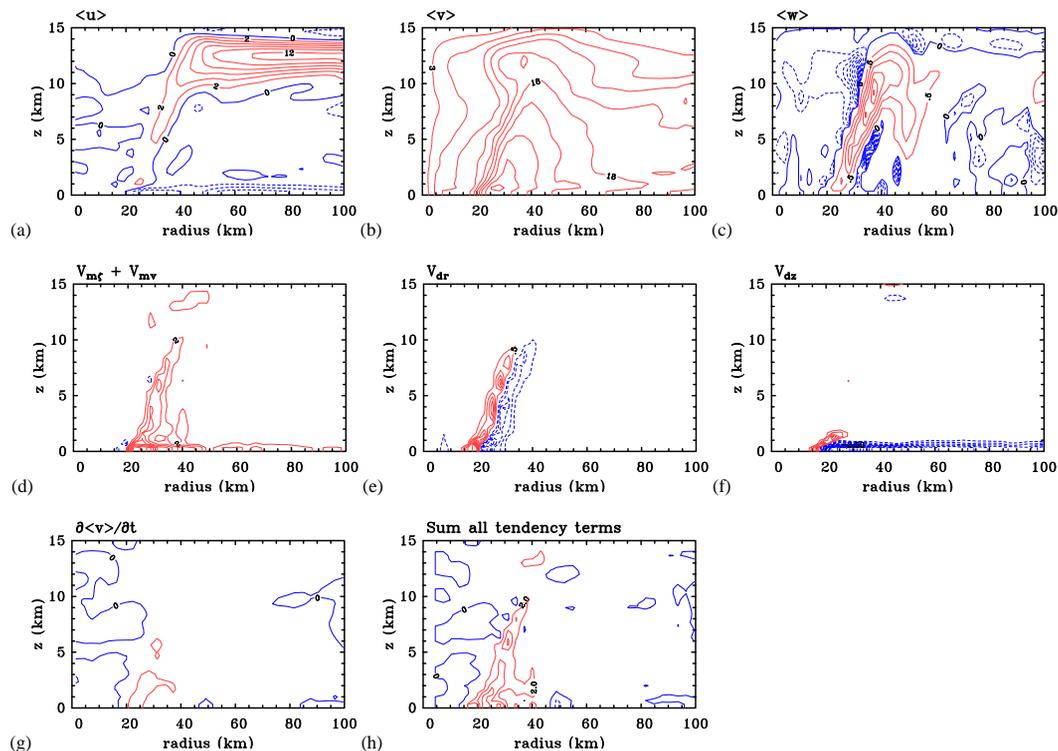


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Fig. 12. Terms of the tangential wind tendency equation for the simulation AX3k, averaged during the rapid intensification stage (77–83 h). Red color denotes positive values; blue color denotes negative values. **(a)** Radial velocity $\langle u \rangle$ (Contour interval 2 m s^{-1}); **(b)** Tangential velocity $\langle v \rangle$ (Contour interval 3 m s^{-1}); **(c)** Vertical velocity $\langle w \rangle$ (Contour interval for positive 0.5 m s^{-1} ; negative contours $-0.05, -0.1, -0.15, -0.2 \text{ m s}^{-1}$); **(d)** Sum of mean vorticity influx and vertical advection $V_{m\zeta} + V_{mv}$ (Contour interval: $2 \text{ m s}^{-1} \text{ h}^{-1}$); **(e)** Radial (subgrid-scale) diffusive tendency V_{dr} (Contour interval $0.5 \text{ m s}^{-1} \text{ h}^{-1}$); **(f)** Vertical (subgrid-scale) diffusive tendency V_{dz} (Contour interval $0.5 \text{ m s}^{-1} \text{ h}^{-1}$); **(g)** Mean tangential wind tendency $\partial \langle v \rangle / \partial t$ (Contour interval $2 \text{ m s}^{-1} \text{ h}^{-1}$); **(h)** Sum of all tendency terms (Contour interval $2 \text{ m s}^{-1} \text{ h}^{-1}$).

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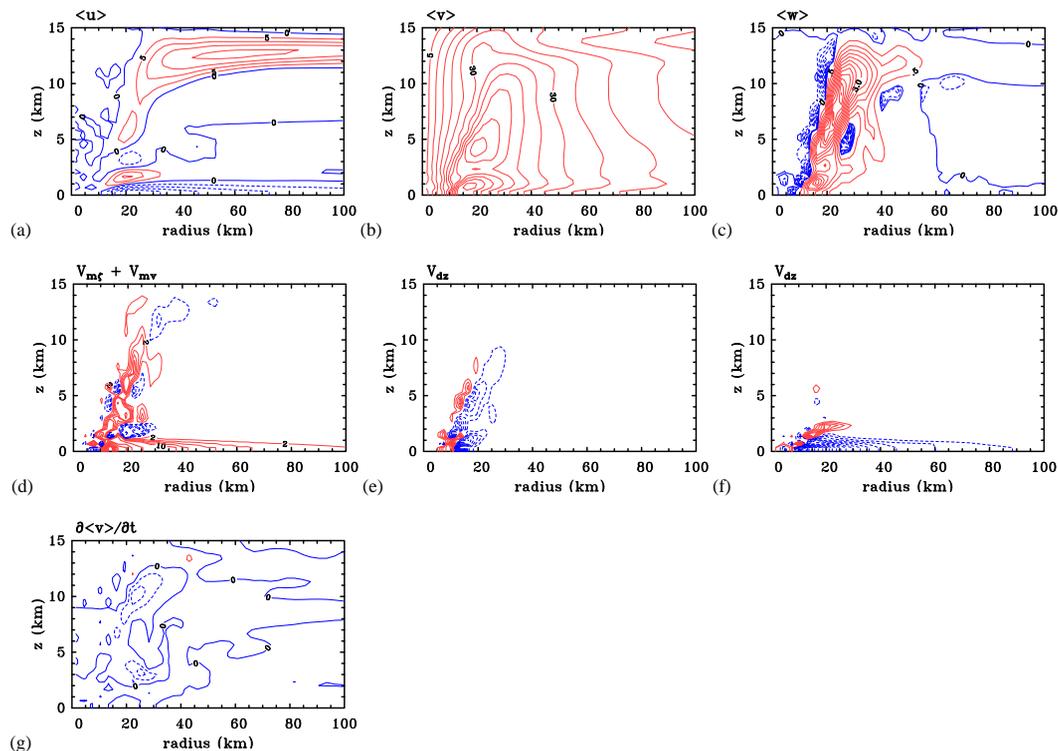


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Fig. 13. Terms of the tangential wind tendency equation for the simulation AX3k, averaged during the mature stage (176–200 h). Red color denotes positive values; blue color denotes negative values. **(a)** Radial velocity $\langle u \rangle$ (Contour interval 5 m s^{-1}); **(b)** Tangential velocity $\langle v \rangle$ (Contour interval 5 m s^{-1}); **(c)** Vertical velocity $\langle w \rangle$ (Contour interval for positive 0.5 m s^{-1} ; negative contours $-0.05, -0.1, -0.15, -0.2 \text{ m s}^{-1}$); **(d)** Sum of mean vorticity influx and vertical advection $V_{m\zeta} + V_{mv}$ (Contour interval: thin, $2 \text{ m s}^{-1} \text{ h}^{-1}$; thick, $10 \text{ m s}^{-1} \text{ h}^{-1}$); **(e)** Radial (subgrid-scale) diffusive tendency V_{dr} (Contour interval $2 \text{ m s}^{-1} \text{ h}^{-1}$); **(f)** Vertical (subgrid-scale) diffusive tendency V_{dz} (Contour interval $2 \text{ m s}^{-1} \text{ h}^{-1}$); **(g)** Mean tangential wind tendency $\partial \langle v \rangle / \partial t$ (Contour interval $0.2 \text{ m s}^{-1} \text{ h}^{-1}$).

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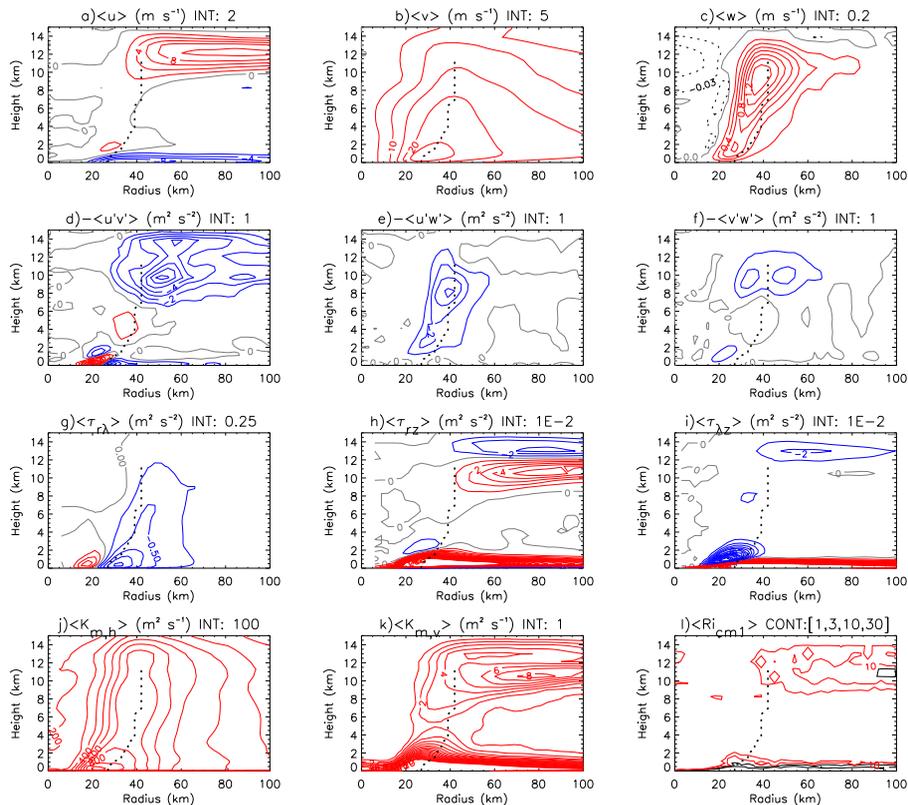


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Fig. 14. Radius-height contour plots of resolved and subgrid-scale eddy momentum fluxes and related quantities from the 3D3k simulation using data at a 2 min interval and averaged over the first intensification interval (65–69 h), which is the interval of maximum intensification rate. Except where otherwise noted, there are 20 positive red contours and 20 negative blue contours. **(a)**: $\langle u \rangle$ with contour interval 2 m s^{-1} ; **(b)**: $\langle v \rangle$ with contour interval 5 m s^{-1} ; **(c)**: $\langle w \rangle$ with contour interval 0.2 m s^{-1} ; **(d)**: resolved horizontal momentum flux $\langle -u'v' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(e)**: resolved vertical eddy flux of radial momentum $\langle -v'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(f)**: resolved vertical eddy flux of tangential momentum $\langle -v'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(g)**: subgrid momentum flux corresponding to **(d)**: $\langle \tau_{r\lambda} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(h)**: subgrid momentum flux corresponding to **(e)**: $\langle \tau_{rz} \rangle$ with contour interval $1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$; **(i)**: subgrid momentum flux corresponding to **(f)**: $\langle \tau_{\lambda z} \rangle$ with contour interval $1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$; **(j)**: horizontal diffusivity $\langle K_{m,h} \rangle$ with contour interval $100 \text{ m}^2 \text{ s}^{-1}$; **(k)**: vertical diffusivity $\langle K_{m,v} \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-1}$; **(l)**: time and axisymmetric average of the gradient Richardson number used in the CM1 model $\langle \text{Ri}_{\text{cm}1} \rangle$ with black contours 1 and 3 and red contours 10 and 30. The radius of maximum $\langle v \rangle$ at each height is shown with the black dashed curve (up to 11 km).

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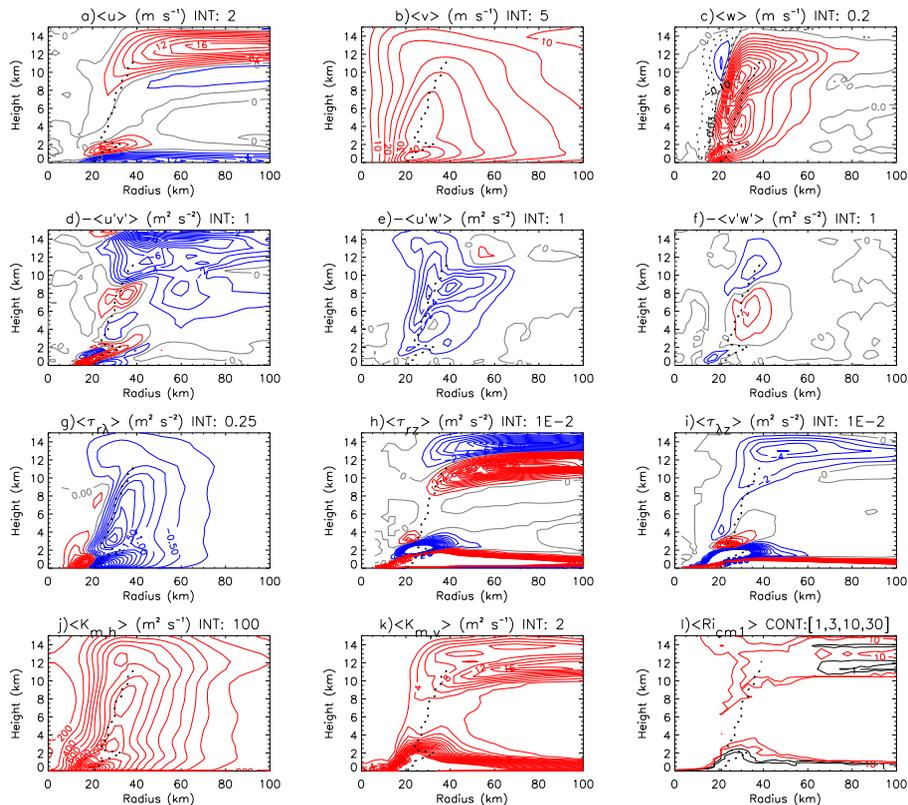


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Fig. 15. Radius-height contour plots of resolved and subgrid-scale eddy momentum fluxes and related quantities from the 3D3k simulation using data at a 2 min interval and averaged over the second intensification interval (144–148 h). Contour intervals are the same as in Fig. 14. Except where otherwise noted, there are 20 positive red contours and 20 negative blue contours. **(a):** $\langle u \rangle$ with contour interval 2 m s^{-1} ; **(b):** $\langle v \rangle$ with contour interval 5 m s^{-1} ; **(c):** $\langle w \rangle$ with contour interval 0.2 m s^{-1} ; **(d):** resolved horizontal momentum flux $\langle -u'v' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(e):** resolved vertical eddy flux of radial momentum $\langle -u'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(f):** resolved vertical eddy flux of tangential momentum $\langle -v'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(g):** subgrid momentum flux corresponding to **(d):** $\langle \tau_{r\lambda} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(h):** subgrid momentum flux corresponding to **(e):** $\langle \tau_{rz} \rangle$ with contour interval $1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$; **(i):** subgrid momentum flux corresponding to **(f):** $\langle \tau_{\lambda z} \rangle$ with contour interval $1 \times 10^{-2} \text{ m}^2 \text{ s}^{-2}$; **(j):** horizontal diffusivity $\langle K_{m,h} \rangle$ with contour interval $100 \text{ m}^2 \text{ s}^{-1}$; **(k):** vertical diffusivity $\langle K_{m,v} \rangle$ with contour interval $2 \text{ m}^2 \text{ s}^{-1}$; **(l):** time and axisymmetric average of the gradient Richardson number used in the CM1 model $\langle \text{Ri}_{\text{cm1}} \rangle$ with black contours 1 and 3 and red contours 10 and 30. The radius of maximum $\langle v \rangle$ at each height is shown with the black dashed curve (up to 11 km).

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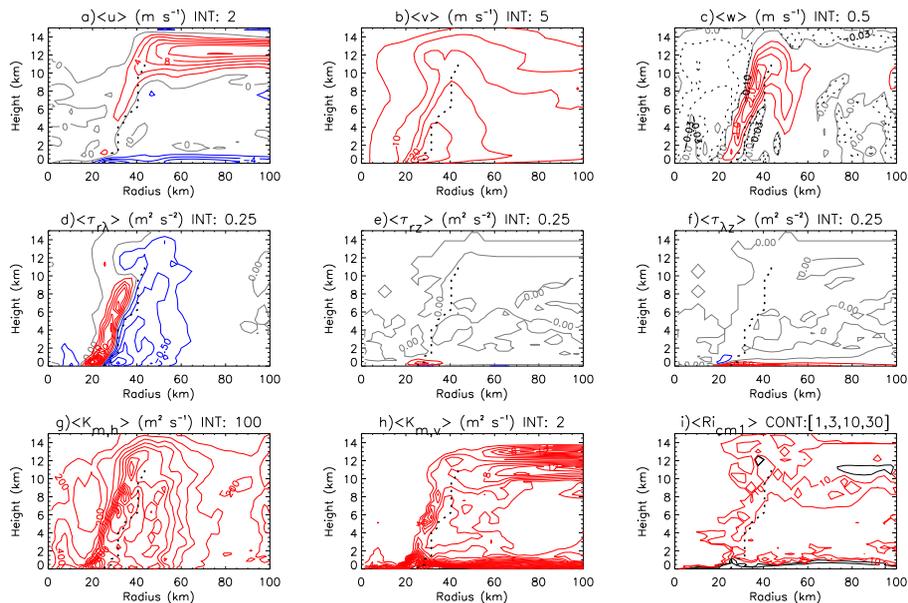


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Fig. 16. Radius-height contour plots of resolved and subgrid eddy momentum fluxes and related quantities from the AX3k simulation using data at a 2 min interval and averaged over the interval of maximum intensification rate (77–83 h). Except where otherwise noted, there is a maximum of 20 positive red contours and 20 negative blue contours. **(a):** $\langle u \rangle$ with contour interval 2 m s^{-1} ; **(b):** $\langle v \rangle$ with contour interval 5 m s^{-1} ; **(c):** $\langle w \rangle$ with contour interval 0.5 m s^{-1} ; **(d):** subgrid momentum flux corresponding to Fig. 14d $\langle \tau_{r\lambda} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(e):** subgrid momentum flux corresponding to Fig. 14e $\langle \tau_{rz} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(f):** subgrid momentum flux corresponding to Fig. 14f $\langle \tau_{\lambda z} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(g):** horizontal diffusivity $\langle K_{m,h} \rangle$ with contour interval $100 \text{ m}^2 \text{ s}^{-1}$; **(h):** vertical diffusivity $\langle K_{m,v} \rangle$ with contour interval $2 \text{ m}^2 \text{ s}^{-1}$; **(i):** time and axisymmetric average of the gradient Richardson number used in the CM1 model $\langle \text{Ri}_{\text{cm1}} \rangle$ with black contours 1 and 3 and red contours 10 and 30. The radius of maximum $\langle v \rangle$ at each height is shown with the black dashed curve (up to 11 km).

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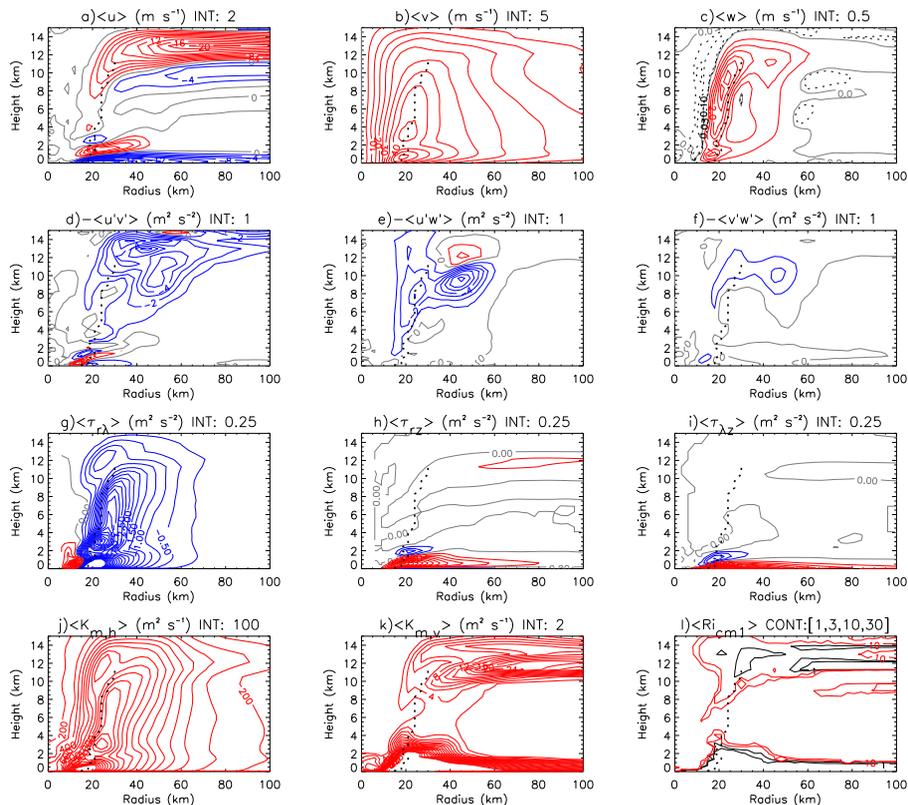


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Fig. 17. Radius-height contour plots of resolved and subgrid eddy momentum fluxes and related quantities from the 3D3k simulation using data at a 10 min interval and averaged over a mature period (214–226 h). Except where otherwise noted, there are 20 positive red contours and 20 negative blue contours. **(a)**: $\langle u \rangle$ with contour interval 2 m s^{-1} ; **(b)**: $\langle v \rangle$ with contour interval 5 m s^{-1} ; **(c)**: $\langle w \rangle$ with contour interval 0.5 m s^{-1} ; **(d)**: resolved horizontal momentum flux $\langle -u'v' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(e)**: resolved vertical eddy flux of radial momentum $\langle -u'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(f)**: resolved vertical eddy flux of tangential momentum $\langle -v'w' \rangle$ with contour interval $1 \text{ m}^2 \text{ s}^{-2}$; **(g)**: subgrid momentum flux corresponding to **(d)** $\langle \tau_{r\lambda} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(h)**: subgrid momentum flux corresponding to **(e)** $\langle \tau_{rz} \rangle$ with contour interval $10 \times 10^{-3} \text{ m}^2 \text{ s}^{-2}$; **(i)**: subgrid momentum flux corresponding to **(f)** $\langle \tau_{\lambda z} \rangle$ with contour interval $10 \times 10^{-3} \text{ m}^2 \text{ s}^{-2}$; **(j)**: horizontal diffusivity $\langle K_{m,h} \rangle$ with contour interval $200 \text{ m}^2 \text{ s}^{-1}$; **(k)**: vertical diffusivity $\langle K_{m,v} \rangle$ with contour interval $2 \text{ m}^2 \text{ s}^{-1}$; **(l)**: time and azimuthal average of the gradient Richardson number used in the CM1 model $\langle \text{Ri}_{\text{cm1}} \rangle$ with black contours 1 and 3 and red contours 10 and 30. The radius of maximum $\langle v \rangle$ at each height is shown with the black dashed curve (up to 11 km).

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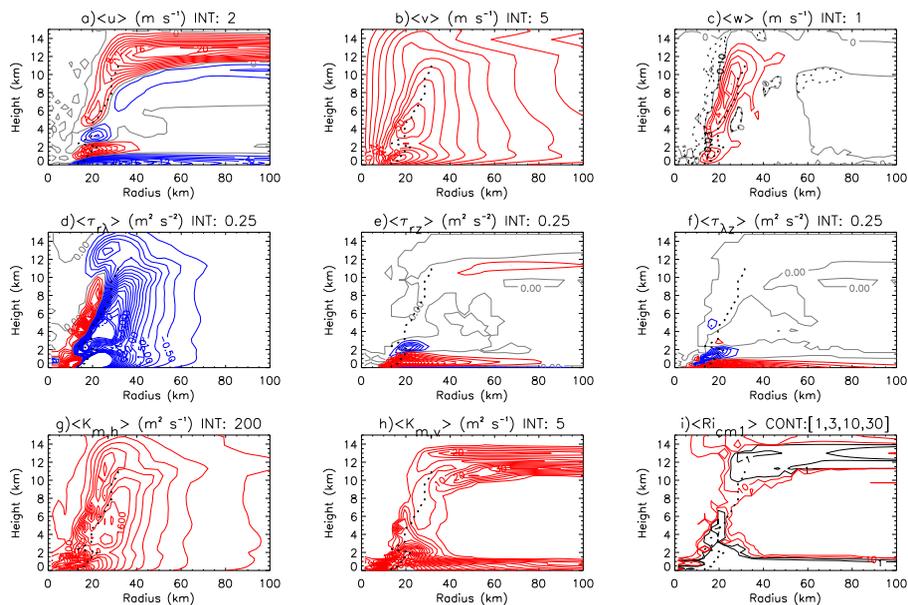


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Fig. 18. Radius-height contour plots of resolved and subgrid eddy momentum fluxes and related quantities from the AX3k simulation using data at a 2 min interval and averaged over a mature period (176–200 h). Except where otherwise noted, there are 20 positive red contours and 20 negative blue contours. **(a)**: $\langle u \rangle$ with contour interval 2 m s^{-1} ; **(b)**: $\langle v \rangle$ with contour interval 5 m s^{-1} ; **(c)**: $\langle w \rangle$ with contour interval 1 m s^{-1} ; **(d)**: subgrid momentum flux corresponding to Fig. 17d $\langle \tau_{r\lambda} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(e)**: subgrid momentum flux corresponding to Fig. 17e $\langle \tau_{rz} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(f)**: subgrid momentum flux corresponding to Fig. 17f $\langle \tau_{\lambda z} \rangle$ with contour interval $0.25 \text{ m}^2 \text{ s}^{-2}$; **(g)**: horizontal diffusivity $\langle K_{m,h} \rangle$ with contour interval $200 \text{ m}^2 \text{ s}^{-1}$; **(h)**: vertical diffusivity $\langle K_{m,v} \rangle$ with contour interval $5 \text{ m}^2 \text{ s}^{-1}$; **(i)**: time and azimuthal average of the gradient Richardson number used in the CM1 model $\langle \text{Ri}_{\text{cm1}} \rangle$ with black contours 1 and 3 and red contours 10 and 30. The radius of maximum $\langle v \rangle$ at each height is shown with the black dashed curve (up to 11 km).

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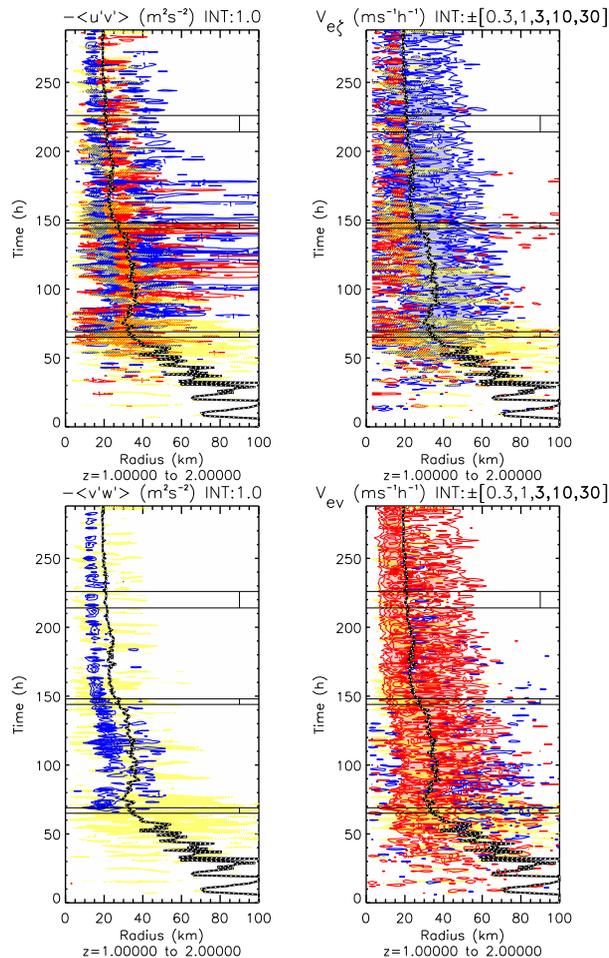


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Fig. 19. Radius-time (Hovmöller) plots of layer-averaged **(a)** horizontal eddy momentum flux ($-\langle u'v' \rangle$), **(b)** radial eddy vorticity flux ($V_{e\zeta}$), **(c)** vertical eddy tangential momentum flux ($-\langle w'v' \rangle$) and **(d)** vertical advection of eddy tangential momentum (V_{ev}), averaged between 1 and 2 km altitude from the 3D3k simulation. **(a)**: contour interval $\pm 1.0 \text{ m}^2 \text{ s}^{-2}$; **(b)**: contours, $\pm 0.3, 1, 3, 10$ and $30 \text{ m s}^{-1} \text{ h}^{-1}$; **(c)**: contour interval $\pm 1.0 \text{ m}^2 \text{ s}^{-2}$; **(d)**: contours $\pm 0.3, 1, 3, 10$ and $30 \text{ m s}^{-1} \text{ h}^{-1}$. Red contours denote positive values and blue contours denote negative values. Spotted black-curve denotes layer-averaged RMW. Yellow shaded area denotes regions where the layer-averaged tangential wind tendency is positive and exceeds $0.25 \text{ m s}^{-1} \text{ h}^{-1}$. Horizontal black lines denote the time intervals analyzed in detail in this paper.

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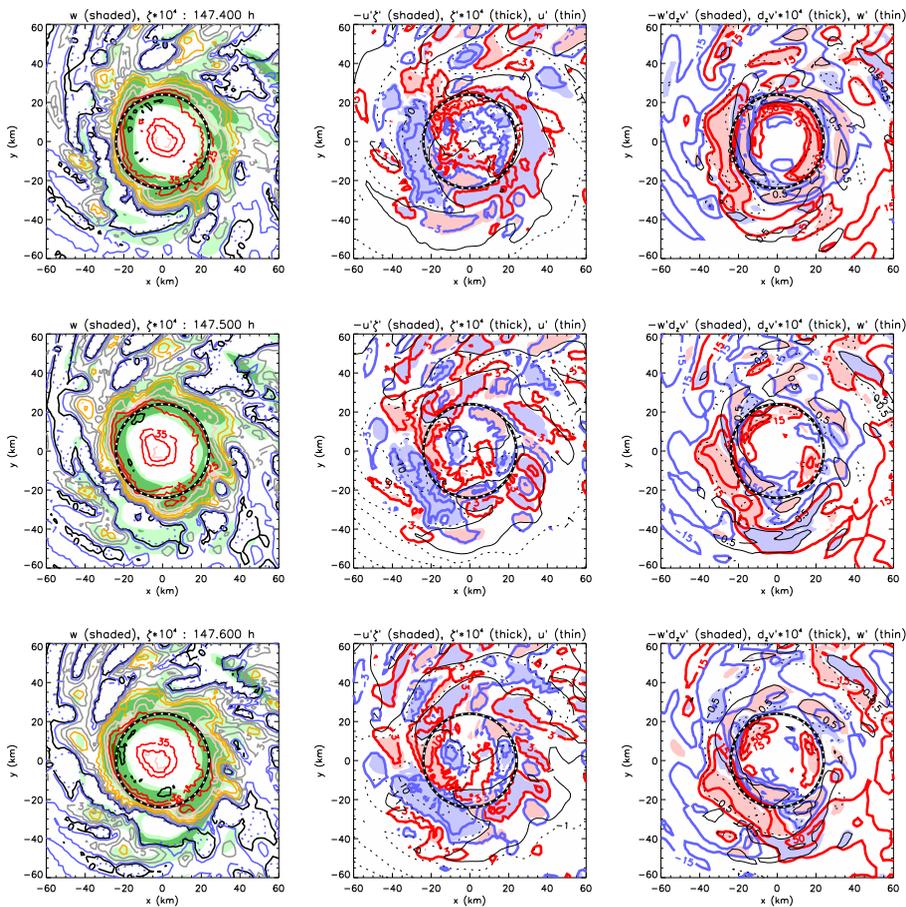


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Fig. 20. (Left) Vertical velocity w (shaded; levels 0.3, 1.0, 3.0 m s^{-1}) and relative vertical vorticity ζ times 10^4 (levels (s^{-1}): -1 blue dotted, 0 black, 1 blue, 3 and 5 gray, 7 and 10 orange, 15 and 20 pink, 25 and 35 red, 50 and 75 black) at a sequence of times at $z = 1.5$ km from the 3D3k simulation. (Center) Radial eddy contributions (shaded ($\text{m s}^{-1} \text{h}^{-1}$): blue $-u'\zeta' < -3$; pink $-u'\zeta' > 3$) to the azimuthally-averaged tangential wind tendency $\partial\langle v \rangle/\partial t$ at the same sequence of times at $z = 1.5$ km from the 3D3k simulation. The eddy vertical vorticity $\zeta' \times 10^4$ (thick blue contours $-30, -10, -3 \text{ s}^{-1}$; thick red contours 3, 10, 30 s^{-1}) and eddy radial velocity u' (dashed negative contours: $-10, -1 \text{ m s}^{-1}$; thin black contours: 1, 10 m s^{-1}) are superposed. (Right) Vertical eddy contributions (shaded ($\text{m s}^{-1} \text{h}^{-1}$): blue $-w'\partial v'/\partial z < -3$; pink $-w'\partial v'/\partial z > 3$) to $\partial\langle v \rangle/\partial t$ at the same sequence of times at $z = 1.5$ km from the 3D3k simulation. The vertical derivative of eddy tangential wind $\partial v'/\partial z \times 10^4$ (thick blue contours $-15, -5, -1.5 \text{ s}^{-1}$; thick red contours 1.5, 5, 15 s^{-1}) and eddy vertical velocity w' (dashed negative contours $-0.5, -5 \text{ m s}^{-1}$; thin black contours 0.5, 5 m s^{-1}). For reference, a spotted-black curve highlights the $r = 24$ km radius, the approximate low-level RMW during this analysis interval.

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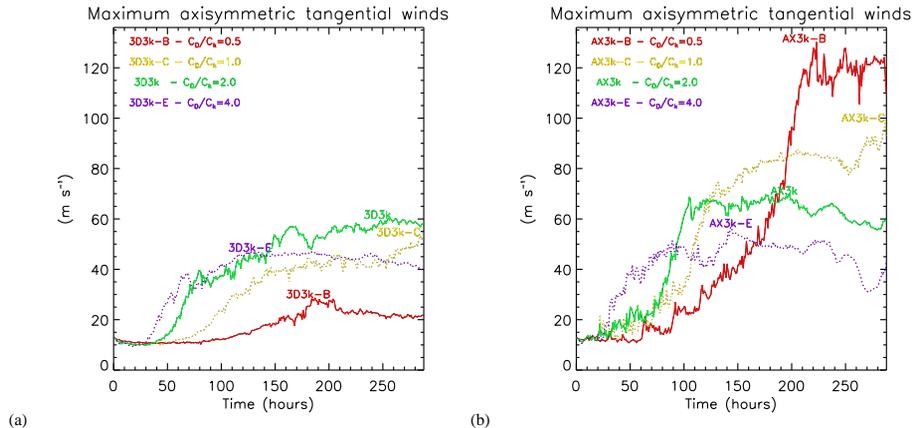


Fig. 21. Maximum tangential velocity as a function of time for a series of experiments in the CM1 model with increasing surface drag coefficient C_D : **(a)** four 3-D simulations (3D3k-B, solid red; 3D3k-C, dotted yellow; 3D3k, solid green; 3D3k-E, dotted-blue,) with 3D3k being the control; and **(b)** four AX simulations (Ax3k-B, solid red; Ax3k-C, dotted yellow; Ax3k, solid green; Ax3k-E, dotted blue), with Ax3k being the control. Experiments B have $C_D = 0.25 \times$ control C_D . Similarly, experiments (C, E) have $C_D = (0.5, 2.0) \times$ control C_D , respectively. See text for details.

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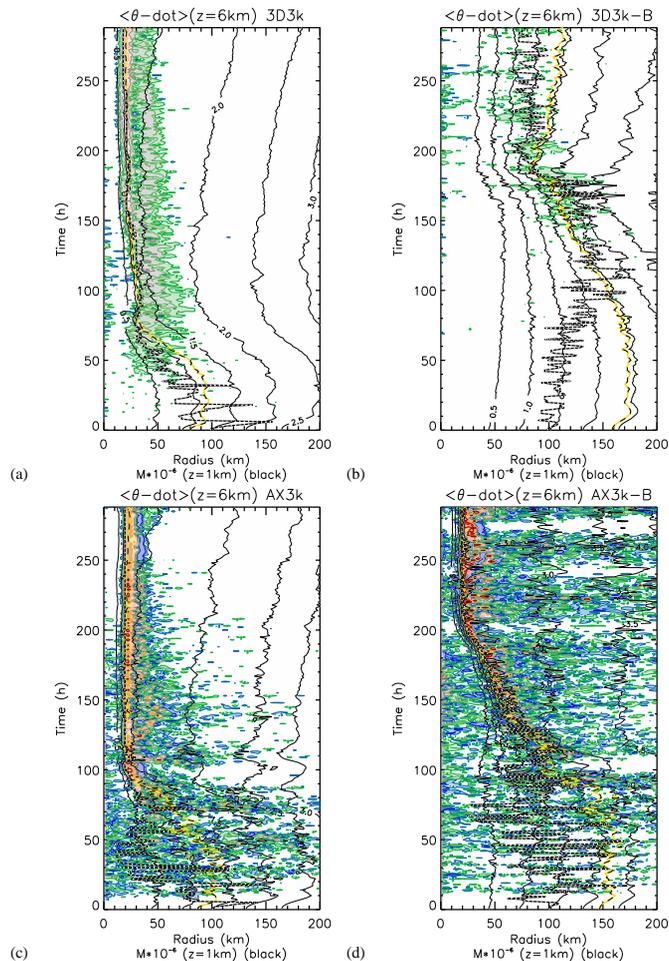


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Fig. 23. Axisymmetric mean heating rate ($\langle\dot{\theta}\rangle$, shaded) and axisymmetric mean absolute angular momentum ($\langle M\rangle$, black contours, interval $0.5 \times 10^6 \text{ m}^2 \text{ s}^{-1}$) from the **(a)** 3D3k, **(b)** 3D3k-B, **(c)** AX3k, and **(d)** AX3k-B simulations. Colored $\langle\dot{\theta}\rangle$ contours (K h^{-1}) are -10 (dark blue), -3 (blue), 3 (green), 10 (light green), 30 (gray), 50 (pink), 75 (orange), 100 (red), 150 (red), and 200 (black). The white-spotted black line is the RMW. The yellow-dashed black line is the value of $\langle M\rangle$ found at the RMW at times of mature intensity for each simulation.