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# Ensemble forecasting with a stochastic convective parametrization based on equilibrium statistics

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## Abstract

The stochastic Plant-Craig scheme for deep convection was implemented in the COSMO mesoscale model and used for ensemble forecasting. Ensembles consisting of 100 48 h forecasts at 7 km horizontal resolution were generated for a 2000 × 2000 km domain covering central Europe. Forecasts were made for seven case studies and characterized by different large-scale meteorological environments. Each 100 member ensemble consisted of 10 groups of 10 members, with each group driven by boundary and initial conditions from a selected member from the global ECMWF Ensemble Prediction System. The precipitation variability within and among these groups of members was computed, and it was found that the relative contribution to the ensemble variance introduced by the stochastic convection scheme was substantial, amounting to as much as 76 % of the total variance in the ensemble in one of the studied cases. The impact of the scheme was not confined to the grid scale, and typically contributed 25–50 % of the total variance even after the precipitation fields had been smoothed to a resolution of 35 km. The variability of precipitation introduced by the scheme was approximately proportional to the total amount of convection that occurred, while the variability due to large-scale conditions changed from case to case, being highest in cases exhibiting strong mid-tropospheric flow and pronounced meso- to synoptic scale vorticity extrema. The stochastic scheme was thus found to be an important source of variability in precipitation cases of weak large-scale flow lacking strong vorticity extrema, but high convective activity.

## 1 Introduction

A given state of the atmosphere cannot be represented perfectly in a numerical model for at least two reasons. The first reason is that for practical reasons the atmospheric state cannot be known with infinite accuracy at every thinkable location. The second reason is that a numerical model resolves the real state only up to a given level of

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detail, limited by the grid-spacing or spectral truncation of the model, and by the time step of the simulation (Palmer, 2001). Both of these imperfections lead to errors, some of which may grow quickly over time because of the chaotic nature of the atmosphere (Lorenz, 1963). In order to obtain information on the possible future states of the atmosphere, ensemble forecasting techniques are used: multiple integrations of the model that, by introducing small perturbations, try to account for the aforementioned imperfections.

First, uncertainties in the initial state of the model are accounted for by starting the model integrations with slightly modified initial conditions (Toth and Kalnay, 1993; Houtekamer and Derome, 1995; Molteni et al., 1996). Second, the problem of the error caused by the limited resolution can be addressed by using stochastic parametrizations. Parametrizations, in the context of numerical weather prediction (NWP), are algorithms that represent the effects of unresolved processes such as radiation, boundary-layer processes and convection. In contrast to traditional deterministic parametrizations, the fundamental idea of stochastic parametrizations is that the small-scale processes that they represent are not uniquely determined by the resolved flow, but are also affected by unresolved processes that are inherently unknown but can be modelled in a stochastic manner (Palmer, 2001).

Several approaches to stochastic parametrization have been taken. Buizza et al. (1999) introduced randomness by multiplying the effects of all parametrized processes by a factor that may be smaller or larger than unity. Shutts (2005) introduced stochastic perturbations based on backscatter of a portion of the kinetic energy that is normally dissipated by parametrized processes, and parametrizations based on this concept have been tested by Bowler et al. (2008), Berner et al. (2009) and Tennant et al. (2011). Many stochastic parametrizations have focussed on cumulus convection, which shows substantial variability on scales close to the truncation limit of current numerical models. Lin and Neelin (2003) have developed two stochastic schemes for deep convection, one by making the closure time-scale (the time in which destabilization is compensated by convective processes) stochastic, the other by adding

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stochastic perturbations to the vertical distribution of the temperature tendencies produced by the scheme. Bright and Mullen (2002) have developed a stochastic version of the Kain-Fritsch convective scheme by adding a stochastic component to its trigger function. In each of these studies, the spatial and/or temporal autocorrelation of the perturbations were controlled by parameters that could be adjusted to produce a desired increase in ensemble spread. In contrast, Berner et al. (2008) employed a cellular automaton to generate patterns of spatial variability, while Khouider et al. (2003) showed how a birth-death model of convective initiation could be used to formally derive a stochastic parametrization for larger scales. In the scheme developed by Plant and Craig (2008; hereafter PC08), used in this study, the convective variability is constrained by an underlying theory, which is based on equilibrium statistics (Craig and Cohen, 2006). In this study we report on the use of the PC08 scheme, previously developed and tested only in a single-column mode, with a limited area model.

If the goal of using a stochastic parametrization scheme, like the PC08 scheme, is to add additional variability to an ensemble, its effects need to be quantified so that a comparison can be made with other sources of variability, e.g. from perturbations in the initial conditions. If the stochastic scheme is to have a sizeable effect on the ensemble spread, the amount of introduced variability must not be negligible in comparison to those other sources. One may anticipate that the relative importance of the stochastic variability is dependent on the meteorological situation, because both the overall magnitude and the degree of randomness of the parametrization are likely to be weather dependent (Craig and Cohen, 2006).

The variability that a stochastic parametrization scheme introduces can be split into two parts: a direct and an indirect component. The direct component is the variability that develops instantaneously because of different stochastic microscopic realizations in the same resolved (macroscopic) flow. This component has the same spatial and temporal scales as the tendencies provided by the stochastic scheme. In contrast, the indirect component is variability of the resolved flow that develops because of upscale growth of the direct variability (Tan et al., 2004; Zhang et al., 2007). This difference

is of importance, because the direct component of variability and the corresponding probabilistic information may alternatively be arrived at by statistical post-processing of a deterministic forecast, as done by e.g. Applequist et al. (2002), Bremnes (2003) or Theis et al. (2005). In contrast, such post-processing cannot account for the impact of small-scale variability on the large-scale flow, so that the stochastic parametrization approach has the potential to be qualitatively superior to such techniques.

Based on the above considerations, our evaluation of the performance of the PC08 parametrization will be directed towards the following questions:

1. How large is the impact of the stochastic variability introduced by the convective scheme compared with that introduced by varying initial and boundary conditions?
2. How much of the variability can be considered a different realization of the same resolved flow, and how much is due to changes of the resolved flow due to upscale error growth?
3. How does the variability depend on the weather pattern?

The paper is structured as follows. Section 2 describes the implementation of the Plant-Craig scheme in the limited-area model. In Sect. 3, the set-up of the ensemble forecasting system is presented. The results are presented and discussed in Sect. 4, and we formulate our conclusions in Sect. 5.

## 2 Implementation of the Plant-Craig scheme in the COSMO model

For the current study, the PC-scheme (PC08) was integrated into the COSMO (Consortium for Small-scale Modelling) model (Schättler et al., 2007), Version 4.8. This model is developed and used by the Consortium for Small Scale Modelling (COSMO), and is both non-hydrostatic and fully compressible. It is used, for example, at the German Weather Service (Deutscher Wetterdienst, DWD) to support operational forecasting,

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and for mesoscale meteorological studies. The model uses a terrain-following coordinate system. Its computational grid is an Arakawa C-grid, with Lorenz grid staggering in the vertical.

The PC-scheme produces small-scale variability while maintaining quasi-equilibrium on a large scale. Large-scale fields are obtained by applying spatial or spatio-temporal averaging, and a CAPE-based closure is assumed. To obtain the small-scale variability, the scheme draws convective elements, or plumes, from a probability density function (Craig and Cohen, 2006), normalized with this closure. The feedback of each plume on the resolved flow is calculated with an adapted version of the Kain-Fritsch plume model (Kain and Fritsch, 1990). For a comprehensive description of the PC-scheme, the reader is referred to Plant and Craig (2008). In what follows, we will recall its main features and describe a number of modifications that were made upon its implementation in the COSMO model.

The PC-scheme is called from the model for each  $(x,y)$  grid cell every *convective time step*, to provide the convective feedback. In the current study the convective time step was set to 10 model time steps (5 min and 30 s, respectively).

Figure 1 summarizes the different steps carried out during a single call of the scheme. First, plumes that were activated in earlier call to the scheme and have exceeded their lifetime are removed (Fig. 1). As in PC08, the lifetime was set to 45 min regardless of plume properties. Next, the scheme evaluates whether any layers could act as source layers for new convective plumes, and calculates the closure mass flux (Fig. 1). To do so, the PC-scheme uses vertical profiles of temperature and humidity that represent an averaged atmospheric state. This averaging must be over a sufficient area (or time period) to contain a large number of clouds, to ensure that the near-equilibrium statistics on which the scheme is based are valid.

Ideally, as in PC08, the determination of the size of this area would consist of an iterative process, whereby (1) an arbitrary initial cloud spacing is chosen, (2) an averaging of the atmospheric state over an area containing many clouds is performed, and (3) a cloud density is computed by the scheme and used to give a better estimate of

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the cloud spacing for the next iteration. However, it is not evident that such a procedure would always converge, and it is computationally expensive. For these reasons, we have chosen to use a fixed averaging area of about 1200 km<sup>2</sup> or 25 grid points. Typically, about 10 to 100 clouds occur within an area of this size in regions of active convection.

Using the averaged profile, the scheme attempts to launch plumes from a series of layers (as described in PC08, their Sect. 3.2), evaluating whether a lifted parcel would be positively buoyant, thereby initiating a convective plume. In PC08 the temperature of each lifted parcel was initially increased by 0.2 K and, if it did not become buoyant, increased several times by 0.1 K. To reduce computational costs, we have instead applied a single 1.0 K perturbation. If a parcel with this perturbation would not become buoyant, the layer was discarded as a potential source for convection.

If a buoyant parcel is found (right panels of Fig. 1), a closure mass flux  $\langle M \rangle$  is calculated, that produces the stabilization required to offset 90 % of the CAPE with a fixed closure timescale  $\tau_c$ . For this calculation, the plume model of the Kain-Fritsch scheme (Kain and Fritsch, 1990; Kain 2004) is used. Using this value, a probability density function (PDF) is defined that expresses the chance that a cloud with a certain radius  $r$ , which is assumed to be related to the mass flux  $m$  according to  $m = (\langle m \rangle / \langle r^2 \rangle) r^2$ , is launched within the time interval  $\delta t$  between two calls of the convection scheme. Angle brackets denote an average over the theoretical ensemble of convective clouds. This PDF may be expressed as

$$p(r)dr = \frac{2r}{\langle r^2 \rangle} \exp\left(\frac{-r^2}{\langle r^2 \rangle}\right) dr \quad (1)$$

The scheme considers a range of  $r$  values from 0 to  $3\langle r^2 \rangle$  and for each radius determines, by evaluating a pseudo-random number against the value of

During test simulations, it was found that with the values of mass flux, mean cloud radius and closure timescale used in PC08, too little convective precipitation was produced in the simulations. The following adjustments enabled the scheme to

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produce amounts of convective precipitation comparable to the non-stochastic Kain-Fritsch (1990) and Tiedtke (1989) schemes, and are explained in detail below:

1. the root mean squared cloud radius  $\langle r^2 \rangle^{1/2}$  was increased from 450 m to 1200 m;
2. the closure time scale  $\tau_c$  was fixed and set to 600 s, or 10 min;
3. the mean mass flux per cloud,  $\langle m \rangle$ , was reduced from  $2 \times 10^7 \text{ kg s}^{-1}$  to  $1 \times 10^7 \text{ kg s}^{-1}$ .

The increase of the mean squared cloud radius increased the convective activity very strongly. This increase is reasonable because that PC08 calibrated their values to produce results similar to that of a cloud-resolving simulation over a tropical ocean, where it is known that the boundary layer is typically shallower than in mid-latitudes with which we are concerned here, leading to correspondingly narrower updraughts. Moreover, entrainment is probably stronger and more inhibiting for small convective plumes in the mid-latitude troposphere than it is in the tropics.

After changing the mean cloud radius, it was still found that a very large fraction of the rainfall produced in the simulations originated from the grid-scale rather than the PC convective scheme. It appeared that the parametrized convection was not able to reduce the CAPE rapidly enough to prevent grid-scale convection from developing. We hypothesize that this is the case because the gravity waves that communicate the stabilization in the real atmosphere (Bretherton and Smolarkiewicz, 1989) are strongly damped by numerical diffusion, so that temperature perturbations are overly confined to the grid cell where a plume occurs. A solution to this problem would be to parametrize the feedback of the scheme in such a way that the stabilization occurs not only in the grid cell where the convection occurs, but also in neighbouring grid cells. A quicker solution that we have chosen was to reduce the closure time-scale  $\tau_c$ , making convection more intense and more likely to set in before explicit convection sets in. The final adjustment of reducing  $\langle m \rangle$  by 50% also increased the tendency for the scheme to produce convection, since this favours larger numbers of plumes.

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After launching a new plume, the temperature and moisture tendencies produced by it are calculated. Finally, for all plumes, both newly launched and pre-existing, the sum of their effects on the vertical temperature and moisture profiles is computed and returned to the model.

### 3 Ensemble forecasting experiments

The ensemble experiment was structured as follows. We used the European Centre for Medium-Range Weather Forecasts (ECMWF) Ensemble Prediction System (EPS), consisting of 50 members per forecast. These forecasts were rerun from ECMWF operational analyses out to 48 h. 10 members of the ensemble forecast were selected using the RM (representative member) selection algorithm developed by Molteni et al. (2001). This algorithm involves a cluster analysis followed by the selection of a representative member from each of the clusters. These representative members were used as initial and boundary conditions for the simulations with the COSMO model. For each EPS member 10 COSMO simulations were carried out, using different random seeds for the stochastic parametrization, resulting in a 100 member ensemble of COSMO forecasts for each case.

The COSMO model was set up following the COSMO-EU configuration used by the German Weather Service to support operational weather forecasting (DWD, 2011), the only differences being the use of the PC-scheme for convection instead of the Tiedtke scheme, and the use of a different domain. The domain of the simulations for our study stretched across central Europe (Fig. 2) and had a size of approximately  $2100 \times 2100$  km. For one case (M3) the domain was shifted southwards to better capture the Mediterranean cyclone that was responsible for most of the precipitation. The grid-spacing was  $0.0625^\circ$  ( $\sim 7$  km) and the simulations were run out to 48 h.

Seven cases were selected for this study (see Table 1) in an attempt to represent situations with different amounts of large-scale forcing and convective activity. Moreover, five of the cases have been subject of prior scientific studies. As an indication of

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large-scale forcing the presence of a large-scale trough, characterized by a local maximum of vorticity at 500 hPa, was used. Each of the cases was subjectively assigned to one of three categories: W (weakly-forced), M (moderately-forced), or S (strongly-forced).

5 As an example of a strongly-forced case, Fig. 2 (left top) shows the relative vorticity and geopotential of case S1, which features a maximum of relative vorticity over the northwestern part of the domain which is embedded in a strong southwesterly-flow, indicative of strong advection of cyclonic vorticity. According to quasi-geostrophic theory, this implies forcing for upward vertical motion. Cases categorized as moderately-  
10 forced (M1, M2, and M3) feature local maxima of relative vorticity as well (for example, for case M1, a feature stretching over eastern France), but those are weaker and embedded within a weaker steering flow. It must be noted that strong small-scale maxima and minima of vorticity coinciding with convective activity can be seen in all but the S1 case. These, however, have been ignored for the categorization of the cases, as they  
15 are much smaller than the Rossby radius of deformation and hence have little meaning in the context of quasi-geostrophic dynamics. Finally, for cases categorized as weakly forced, large-scale vorticity maxima were absent (W2, W3) or very weak (W1).

## 4 Results and discussion

### 4.1 Structure of the PC-scheme precipitation field

20 The stochastic nature of the PC-scheme is reflected in the spatial distribution of precipitation that the scheme produces. Figure 3 shows snapshots of the precipitation rate that illustrate the differences between the Tiedtke (a), Plant-Craig (b), and Kain-Fritsch (c) convective schemes. Additionally, although validation of the stochastic Plant-Craig scheme with regard to observations is not part of this study, a radar-derived estimate  
25 of the precipitation rate is provided for reference (d).

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as conveyed by the ensemble mean mass flux  $\langle M \rangle$ , was much smaller in simulation (d) than in (a), (b) and (c), resulting in much less precipitation.

In contrast to the accumulations within the square, some evidence can be found that simulations driven by the same initial and boundary conditions can occasionally develop variability on scales of the size of a convective ensemble (35 km by 35 km) or larger. Within the circles in Fig. 4, one can see that simulations (a), (b), and (c) not only differ on scales much smaller than the circle (which has a radius of approximately 80 km): the circle simulation (a) contains more precipitation than simulations (b) and (c). Closer inspection reveals that it was the result of an area of non-convective precipitation being larger and more intense. This area of precipitation has a spatial extent comparable to the circle's radius, i.e. larger than a convective ensemble, indicating that the stochastic parametrization has had an upscale influence through interactions with the grid-scale cloud scheme

### 4.3 Relative impact of the stochastic perturbations

A primary objective of the current study is to compare the variability produced by the initial and boundary conditions with that produced by the stochastic convective parametrization. In order to do this, the variance among all members is calculated for a given quantity, and compared with the average variance among members driven by the same EPS member. The latter represents the variability owing to the stochastic scheme, whereas the total variance represents variability introduced by all sources. Formally this can be written down as follows.

For a domain with  $N$  gridpoints, we define  $r_{ij}(x, y)$  to denote the value of  $r$  (for example, the hourly rainfall accumulation) at a grid point  $(x, y)$  of stochastic realization  $i$  driven by EPS member  $j$ , where  $i$  and  $j$  each range from 1 to 10. Then the mean  $\bar{r}$  averaged over all 10 stochastic realizations of driving member  $j$  is given by

$$\bar{r}_j(x, y) = \frac{1}{10} \sum_{i=1}^{10} r_{ij}(x, y), \quad (2)$$

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and the mean  $r$  averaged over all simulations by

$$\bar{r}(x, y) = \frac{1}{100} \sum_{j=1}^{10} \sum_{i=1}^{10} r_{ij}(x, y) \quad (3)$$

The sample variance over all stochastic realizations of driving member  $j$  is then

$$s_j^2 = \frac{1}{10N} \sum_{i=1}^{10} \sum_{x,y} (r_{ij}(x, y) - \bar{r}_j(x, y))^2 \quad (4)$$

- 5 The variance due to the stochastic scheme, which we will call *internal variability*, can be expressed as

$$s_{\text{int}}^2 = \frac{1}{10N} \sum_{j=1}^{10} s_j^2 = \frac{1}{100N} \sum_{i=1}^{10} \sum_{j=1}^{10} \sum_{x,y} (r_{ij}(x, y) - \bar{r}_j(x, y))^2 \quad (5)$$

and the total as

$$s_{\text{tot}}^2 = \frac{1}{100N} \sum_{i=1}^{10} \sum_{j=1}^{10} \sum_{x,y} \left( r_{ij}(x, y) - \bar{r}(x, y) \right)^2 \quad (6)$$

- 10 Figure 5 shows an example of the total and internal variances, taking  $r$  to be 1-hourly rainfall accumulations, for one case (W1), with values shown for times at six hour intervals throughout the forecast. For this weakly forced case, the internal variability associated with the stochastic convection scheme accounts for the major part of the variance at all times. One-hour accumulated precipitation (convective and total) is also plotted in Fig. 5, and shows a clear diurnal cycle. The forecast hours 6, 24, 30, and 48, at which variability is greatest, correspond to times at which diurnally-driven convection is most intense, i.e. 18:00, 12:00, 18:00 and 12:00 UTC, respectively (12:00 UTC is just after local noon and 18:00 UTC is in the early evening). These times also show the
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greatest total and internal variance in the precipitation. The fraction of the total variance accounted for by the internal variance remains approximately uniform throughout the diurnal cycle.

The spotty nature of the precipitation fields produced by the PC-scheme (Fig. 3) suggests that much of the internal variance occurs on spatial scales close to the model grid length. This is confirmed in Fig. 6, which shows the total and internal variances computed from precipitation fields that have been filtered using the same 25-point (35 km × 35 km) smoothing kernel that was used to calculate the convective forcing within the PC-scheme. The total variance in the ensemble of smoothed fields is about an order of magnitude less than that of the unsmoothed fields (Fig. 5). It is significant however that even after smoothing, the internal variance is still about half as large as the total variance, showing that the PC-scheme is still a major source of ensemble spread, even on scales substantially larger than those directly forced by the stochastic variability. It is also apparent in Fig. 6 that the total and internal variances follow the diurnal cycle in precipitation, as was the case for the unsmoothed fields.

A relationship between the variance introduced by the stochastic convection and the amount of convective precipitation is expected from the design of the PC08-scheme. The equilibrium distribution function for convective mass flux corresponds to a marked Poisson process (Craig and Cohen, 2006), and has the property that the variance is proportional to the mean convective mass flux  $\langle M \rangle$ , i.e.  $\langle (M - \langle M \rangle)^2 \rangle = 2\langle M \rangle \langle m \rangle$  (Cohen, 2001). If we assume that precipitation  $r$  in a grid box is proportional to the convective mass flux  $M$ , then a similar proportionality will hold between  $r$  and its mean. To verify this, Fig. 7 shows the internal variability  $s_{\text{int}}^2$ , plotted as a function of 1-hourly convective precipitation at six hour intervals for all 7 cases. The relationship is indeed approximately linear, although with some scatter, which may reflect a different proportionality between mass flux and precipitation in different weather regimes.

The relationships between the total precipitation and total and internal variances are explored in Fig. 8. For clarity, the variances computed at 6-hourly intervals are averaged over the two day period of each forecast and plotted against the 48 h accumulated

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convective precipitation. For all case studies the internal variance (closed triangles) is roughly proportional to the amount of convective precipitation. The total variance however shows no such relationship.

Instead it would appear that the ratio of internal to total variance depends upon the meteorological environment (Fig. 9). The cases that were subjectively categorized as weakly forced (W1, W2, W3) have ratios of internal to total variance of about 0.5 (0.39, 0.42 and 0.55 respectively) after smoothing. Those that had moderate forcing (M1, M2, M3) have ratios much lower than that (0.24, 0.26, and 0.31 respectively). The strongly-forced winter storm case (S1) has a ratio of 0.02. These results indicate that the stochastic scheme has a relatively high impact when external forcing is weak, less impact when convection is more strongly constrained by the large-scale flow, and negligible impact for the winter storm case where precipitation was mainly non-convective.

## 5 Conclusions

The impact of a stochastic convective parametrization has been investigated by running a large 100 member ensemble consisting of 10 stochastic realizations of a simulation initiated with 10 members from the ECMWF EPS, for seven individual weather situations that differ in the amount of forcing and convective activity. Based on an evaluation of the precipitation fields produced by the simulations, we can answer the questions posed in the introduction.

First, regarding the relative impact of the stochastic scheme we can conclude that it is, compared with the effects of varying initial and boundary conditions, relatively strong when considering hourly precipitation accumulations at the model grid scale. The fraction of sample variance attributable to the stochastic scheme varies between 1.7% (case S1) and 76.3% (case W2) of the total variance depending on the weather pattern. The variability introduced by the stochastic scheme appears to be approximately proportional to the total amount of convective precipitation.

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Second, concerning the impacts of the stochastic scheme on the resolved flow, we find that smoothing the precipitation reduces the variability considerably, but a large impact (a fraction of one quarter to one half of sample variance) due to the stochastic scheme remains in all of the simulated weather patterns except for the winter storm (S1). This implies that at least some of the convective variability still has an effect on larger scales. Visual inspection of selected precipitation fields (e.g. Fig. 3), shows indications of such upscale error growth, but these signals are very subtle.

Last, regarding the dependency of the importance of stochastic perturbations on the weather type, we conclude that in weather patterns that are weakly-(strongly-)forced the relative impact of the stochastic scheme is high (low). This can be explained by the fact that the total variance in weakly-forced weather patterns tended to be smaller than in the strongly-forced patterns, while the variance contributed by the stochastic scheme is proportional to the amount of convective rainfall. The relative importance of the stochastic scheme, is thus larger in the weakly-forced cases.

The results of this first study show that a physically-based stochastic parametrization of convective variability can provide a significant source of variance for ensemble forecasting of convective precipitation. An important next step is to verify that this increased variance leads to better probabilistic forecasts when compared to observations (this work is in progress). Furthermore, the dependence of the convective variability on weather regime hints at a potential for developing flow-dependent algorithms to generate forecast products, or adaptive ensemble design where computational resources are more optimally assigned to simulations that will contribute most to ensemble spread. For example, our results suggest that in weakly-forced weather patterns with widespread convection, it would be wise to make sure many stochastic realizations are available. Conversely, in strongly-forced weather patterns with little convection, the use of the stochastic scheme should not be given top priority. An important pre-requisite for such developments is the identification of an appropriate quantitative measure of large-scale forcing, such as the quasi-geostrophic omega equation diagnostic of Deveson et al. (2002).

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Case	Initial date and time (yyyy mm dd hh)	Domain-averaged 48 h convective precipitation (mm)	Description
S1	2005 01 06 12	0.12	Winter Storm Erwin/Gudrun
W1	2006 07 11 12	1.84	PRINCE field campaign Groenemeijer et al. (2009)
M1	2007 07 19 12	1.16	COPS field campaign IOP 9c Corsmeier et al. (2011)
M2	2008 06 24 12	1.08	Strong squall line in central parts of Europe (Púik et al. (2011), Simon et al. (2011))
M3	2008 09 11 12	1.09	Mediterranean cyclone case Grams et al. (2011)
W2	2009 06 30 12	2.09	Diurnally-driven convection case
W3	2010 06 26 12	0.48	Summer day with little convective activity

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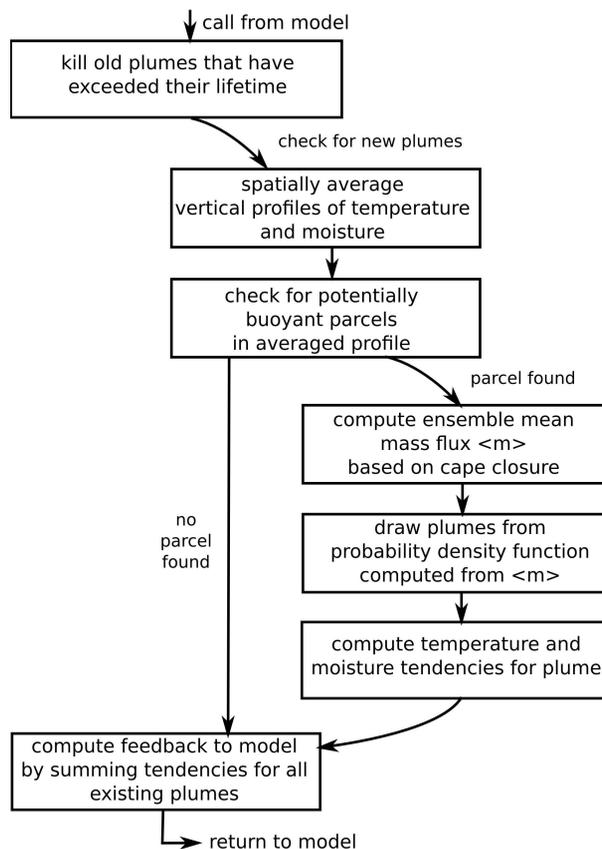
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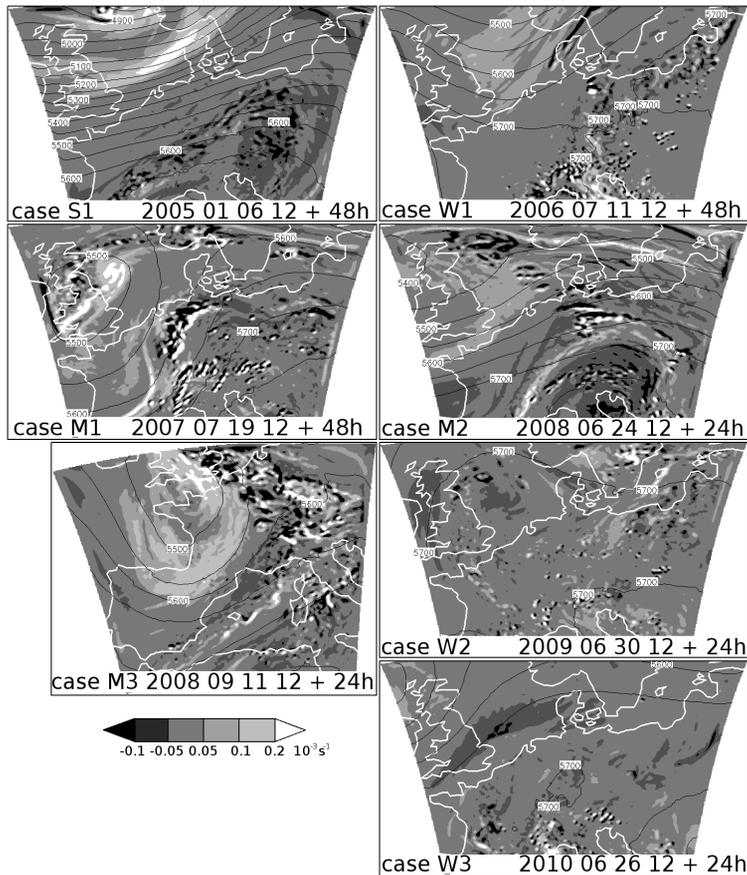
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**Fig. 1.** Flowchart displaying the tasks performed in the Plant-Craig convection scheme.

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**Fig. 2.** 500 hPa relative vorticity ( $\text{s}^{-1}$ , shaded), and geopotential height (m, in black contours) for selected cases.

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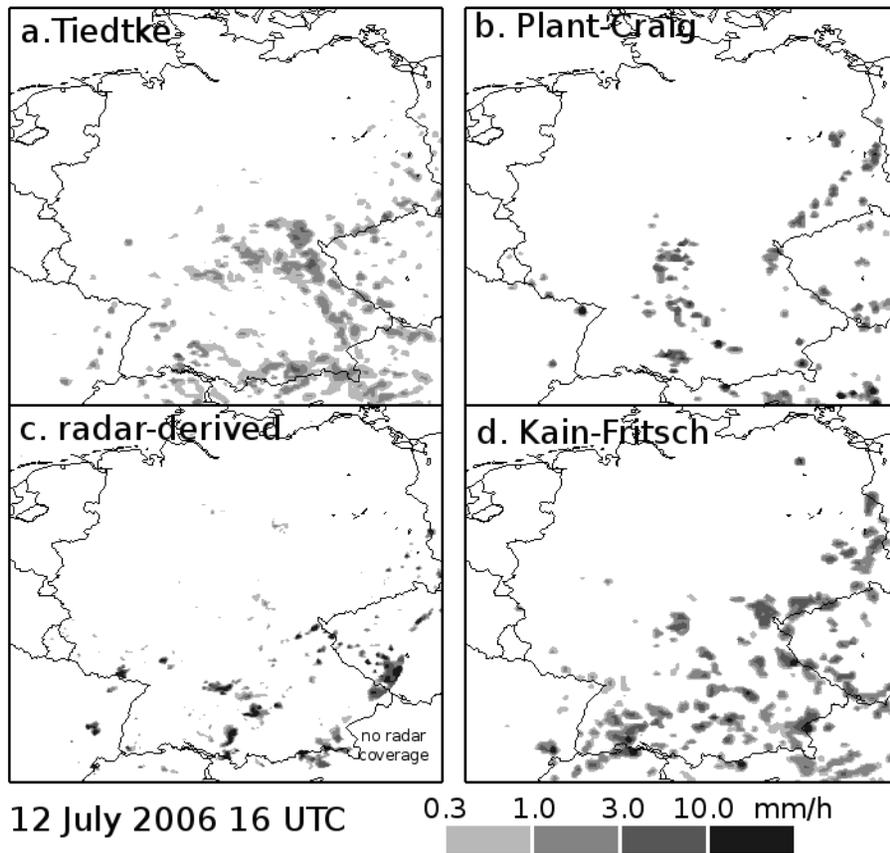
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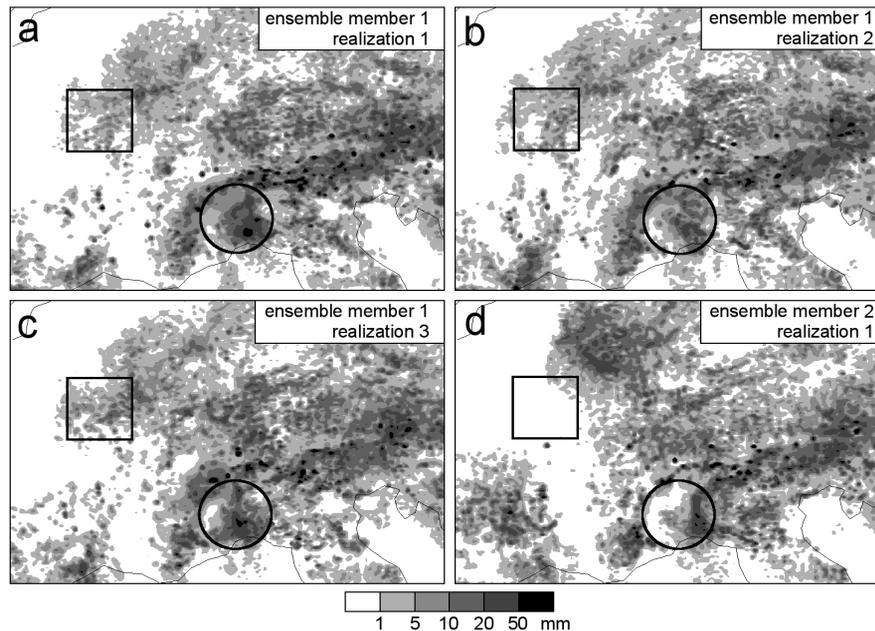




**Fig. 3.** Comparison of precipitation rates of Tiedtke **(a)**, Plant-Craig **(b)** and Kain-Fritsch **(d)** convective schemes, and the radar-derived rates **(c)**.

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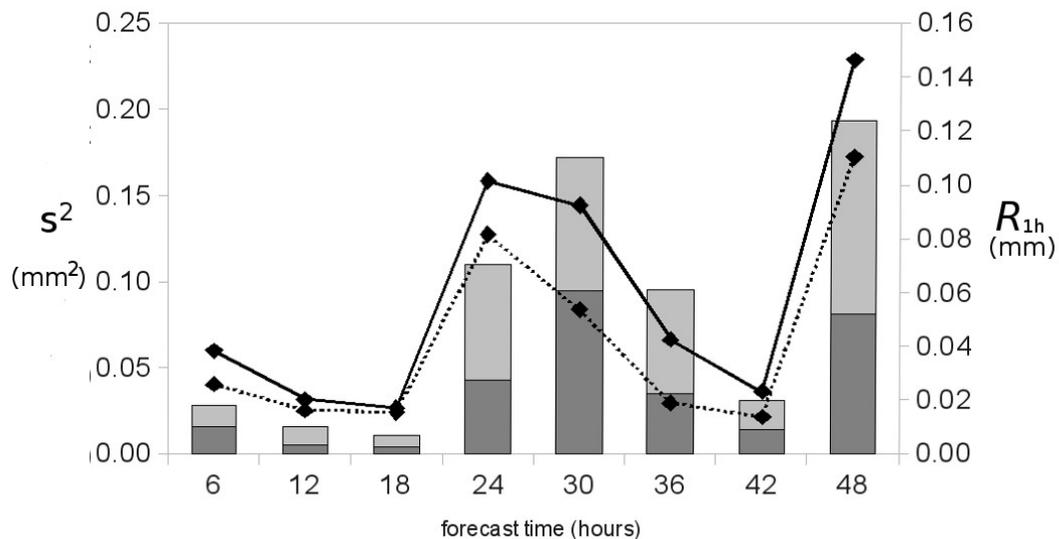
**Fig. 4.** 48 h accumulated rainfall of four realizations of the PC-scheme across part of the domain centered on the western Alps. Panels (a), (b) and (c) are simulations run with initial and boundary conditions provided by the same EPS ensemble member (1), panel (d) is a simulation driven by another member (2). The circle and the square denote regions discussed in the text.

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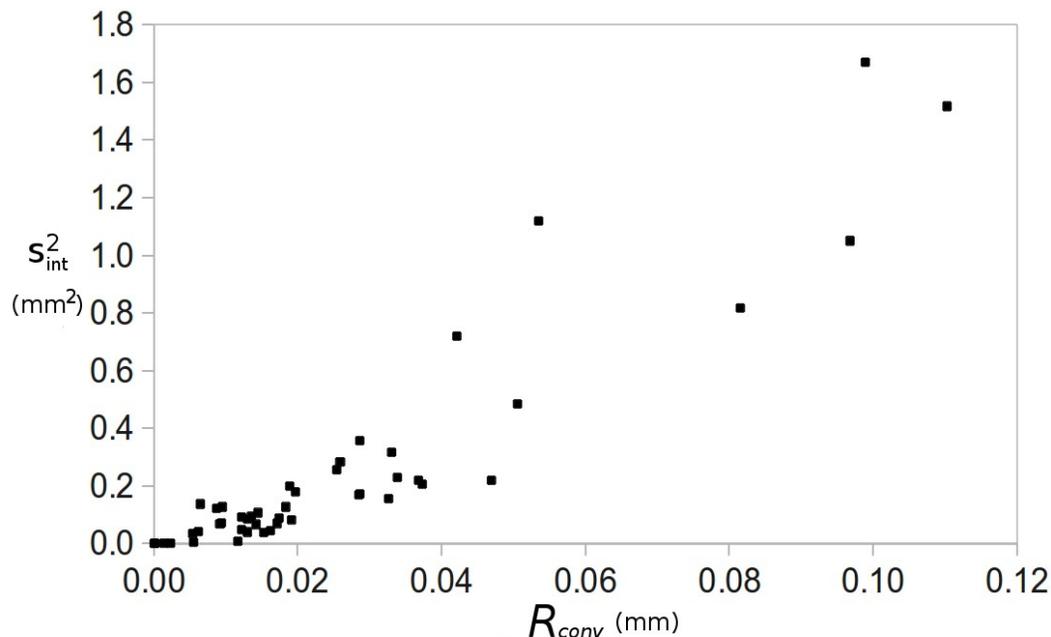


**Fig. 6.** As for Fig. 5 but after smoothing the precipitation field (see text).

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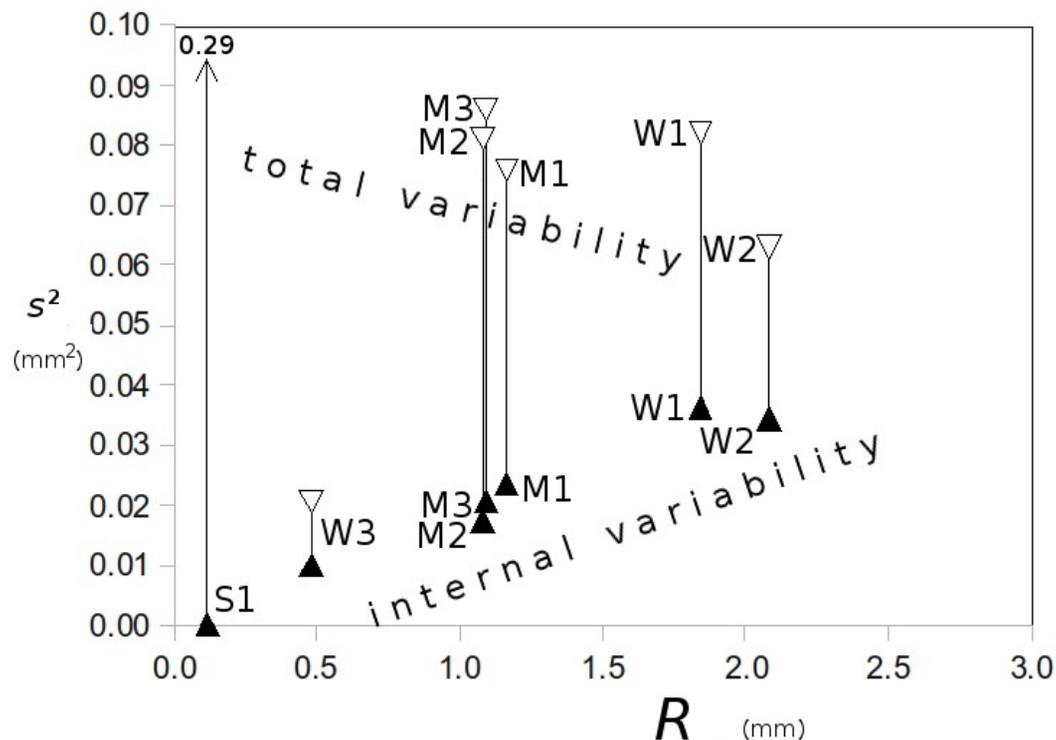


**Fig. 7.** The mean internal sample variance of the precipitation accumulation  $s_{int}^2$  as a function of the mean convective precipitation accumulation  $R_{conv}$ , over the hour preceding the 6, 12, 18, 24, 30, 36, 42 and 48 h forecast times for all cases listed in Table 1.

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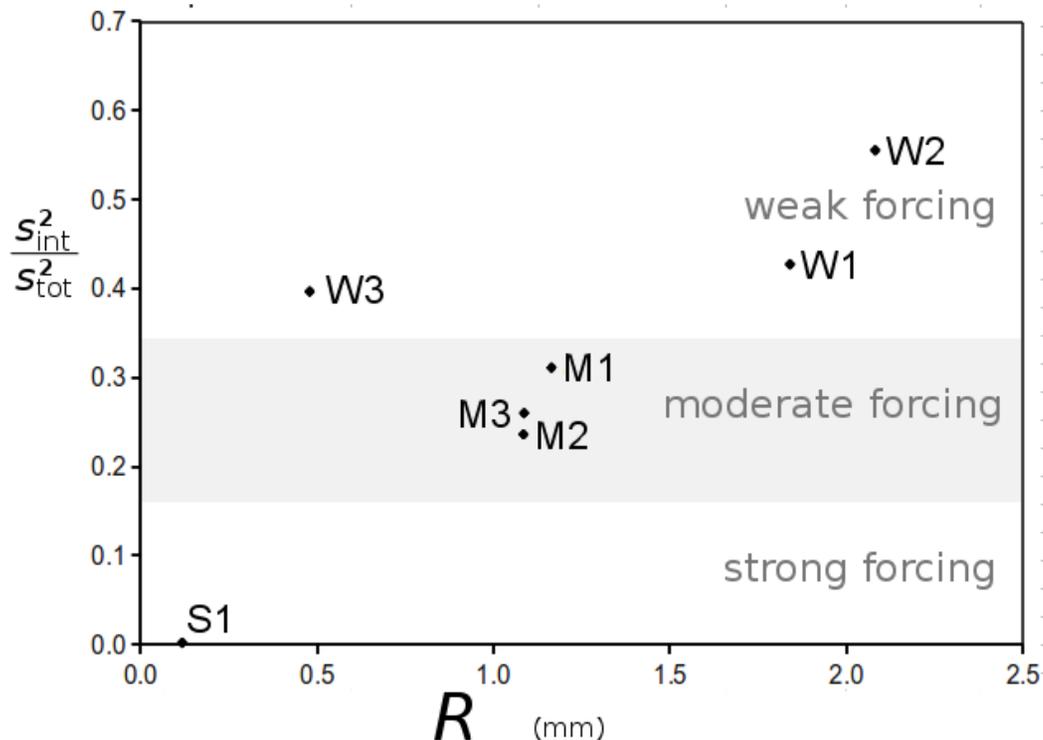
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**Fig. 8.** Total  $s_{\text{tot}}^2$  (open triangles), and internal  $s_{\text{int}}^2$  (closed triangles) sample variance of the smoothed precipitation accumulations over the hour preceding the 6, 12, 18, 24, 30, 36, 42, and 48 h forecast time, as a function of the ensemble average accumulated precipitation over the 48 h forecast period  $R$ .

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**Fig. 9.** Ratio of internal ( $s_{int}^2$ ) to total ( $s_{tot}^2$ ) sample variance of the smoothed precipitation accumulations over the hour preceding the 6, 12, 18, 24, 30, 36, 42, and 48 h forecast time as a function of the ensemble average accumulated precipitation over the 48 h forecast period  $R$ .

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